

# **Linked Lists**

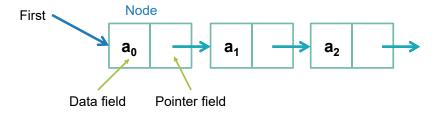
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### **Array**

- ■Store an ordered list
- Using sequential mapping
  - Element(node) a<sub>i</sub> is stored in the location L<sub>i</sub> of the array
  - Next node is at the location L<sub>i</sub>+1
- ■Pros:
  - Suitable for random access
  - Efficient to insert/delete from the end
  - Adequate for special data structures, Stack and Queue
- ■Con:
  - Difficult to insert/delete nodes at arbitrary location

### **Linked Lists**

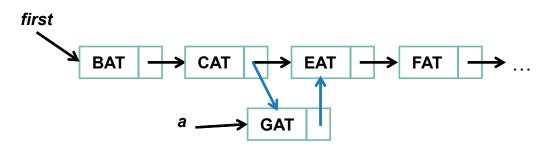
- ■Nodes are no longer continue in the memory
- ■Each node stores the address or location of the next one
- ■Singly Linked List (SLL)
  - Each node has exactly one pointer field



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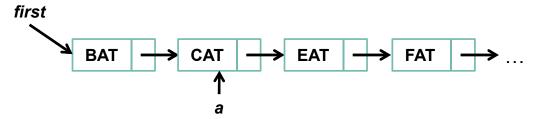
## **SLL Operation: Insert**



- Steps to insert a "GAT" in between "CAT" and "EAT" nodes
  - Create a new node "a" and set data field to "GAT"
  - Set the link field of "a" to "EAT" node
  - Set the link field of "CAT" node to "a"

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## **SLL Operation: Delete**



- ■Steps to delete a "EAT" node from the list
  - Locate the node "a" precedes the "EAT" node
  - Set the link field of "a" to node next to "EAT" node
  - Delete the "EAT" node

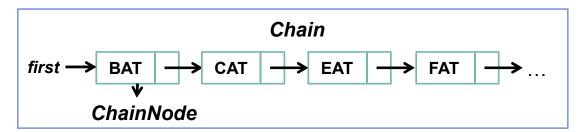
You do not need to move or shift any nodes!

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# **Conceptual Design**

- ■Defining a "ChainNode" class
  - Data field
  - Link field
- ■Designing a "Chain" class
  - Support various operation on ChainNodes



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### ChainNode & Chain Classes

### ■Composite class

```
class ChainNode
{
  friend class Chain;
  public:
    // Constructor
    ChainNode(int
    value=0, ChainNode*
    next=NULL) {
      data = value;
      link = next;

    private:
      int data;
      ChainNode *link;
};
```

```
class Chain
{
  public:
    // Create a chain with two nodes
    void Create2();

    // Insert a node with data=50
    void Insert50(ChainNode *x);

    // Delete a node
    void Delete(ChainNode *x, ChainNode *y);

private:
    ChainNode *first;
};
```

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### ChainNode & Chain Classes

#### ■Nested class

# **Review Pointer Manipulation**

#### Declaration

- NodeA \*a1=NULL, \*a2=NULL:
- **■**Allocate memory
  - a1 = new NodeA;
  - a2 = new NodeA[10];
- **■**Delete memory
  - delete a1; a1=NULL;
  - delete [] a2; a2=NULL;

#### Dereference

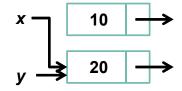
- NodeA &a1Ref = (\*a1);
- Access members
  - a1->memData;
  - a1->memFunc();
  - (\*a1).memData;
  - (\*a1).memFunc();

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# **Pointer Assignment**

- ■ChainNode \*x, \*y;
  - $x \longrightarrow 10 \longrightarrow y \longrightarrow 20 \longrightarrow$
- x = y;



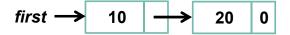
• 
$$*x = *y;$$

$$x \longrightarrow 20$$

$$y \longrightarrow 20$$

```
void Chain::Create2()
{
    // Create and set the fields of 2<sup>nd</sup> node
    ChainNode* second = new ChainNode(20,0);

    // Create and set the fields of 1<sup>st</sup> node
    first = new ChainNode(10, second);
}
```

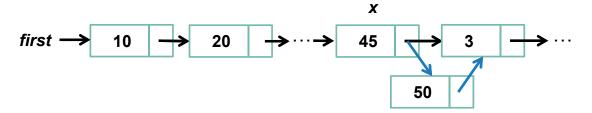


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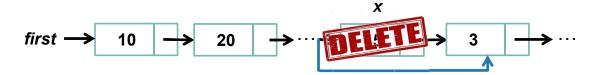
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## **Chain Operations**

```
void Chain::Insert50(ChainNode *x)
{
   if(first) // Insert after x
        x→link = new ChainNode(50, x->link);
   else // Insert into empty list
      first = new ChainNode(50);
}
```



```
void Chain::Delete(ChainNode *x, ChainNode *y)
{    // x is the node to be deleted and y is the node
    // preceding x
    if(x==first) first = first->link;
    else y->link = x->link;
    delete x;
    x=NULL;
}
```



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## **Template Chain Class**

```
Template < class T > class Chain; // Forward declaration
template < class T >
class ChainNode {
friend class Chain <T>;
private:
       T data;
       ChainNode<T>* link;
};
template <class T>
class Chain {
public:
       // Constructor
       Chain(void) {first = last = NULL;}
       // Chain operations...
private:
      ChainNode<T> *first;
      ChainNode<T> *last;
```

```
template < class T >
void Chain<T>::InsertBack(const T& e)
{
   if(first) {// Non-empty chain
      last->link = new ChainNode<T>(e);
      last = last->link;
   }
   else // Insert into an empty chain
      first = last = new ChainNode<T>(e);
}
```

```
template < class T >
void Chain<T>::Concatenate(Chain<T>& b)
{    // b is concatenated to the end of *this
    if ( first ) { last->link = b.first; last = b.last; }
    else { first = b.first; last = b.last; }
    b. first = b.last = 0;
}
```

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# **Chain Operations**

■ Reverse a chain, such that  $(a^1, a^2, \dots, a^n)$  turns into $(a^n, a^{n-1}, \dots, a^1)$ 

first 
$$\longrightarrow$$
 10  $\longrightarrow$  20  $\longrightarrow$  45  $\longrightarrow$  3 0

first

3

45

20

10

**0** → null

■ Reverse a chain, such that  $(a^1, a^2, \dots, a^n)$  turns into $(a^n, a^{n-1}, \dots, a^1)$ 





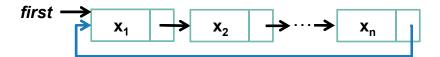
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## **Chain Operations**

### **Circular Lists**

- A singly-linked circular list
- ■The link field of the last node points to the first node



- ■Check for the last node
  - if(current->link == first)
- ■You could visit a node from any position

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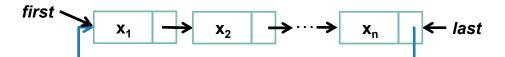
### Circular Lists: Insert

- ■Suppose we want to insert a new node at the front of list
- ■Set link field of new node to *first* and set *first* to new node
- ■Go to the last node and set the link field to new node



### **Circular Lists**

- Computation complexity for finding the last one?
  - O(N)
- Computation complexity for finding the first one?
  - We could away access the first node via [last->link]
  - O(1)
- It is more convenient to store the last node of a circular list



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### Circular Lists: Insert at Front

```
Template<class T>
void CircularList<T>::InsertFront(const T& e)
{
    ChainNode<T>* newNode = new ChainNode<T>(e);

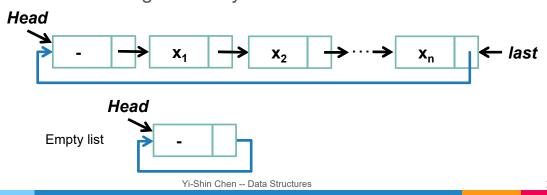
    if(last) { // nonempty list
        newNode->link = last->link;
        last->link = newNode;
    }
    else{ // empty list
        last = newNode;
        newNode->link = newNode;
    }
}
```

### **Circular Lists**

■How to represent an "empty" list?



■Introducing a dummy node "Header"



# **Sparse Matrix**

- A matrix has many zero elements
- Devise a sequential array
  - store non-zero elements
  - **row-major** order
- Access specific column is difficult
- Using circular lists representation

Α	row	col	value
smArray[0]	0	0	15
smArray[1]	0	3	22
smArray[2]	0	5	-15
smArray[3]	1	1	11
smArray[4]	1	2	3
smArray[5]	2	3	-6
smArray[6]	4	0	91
smArray[7]	5	2	28

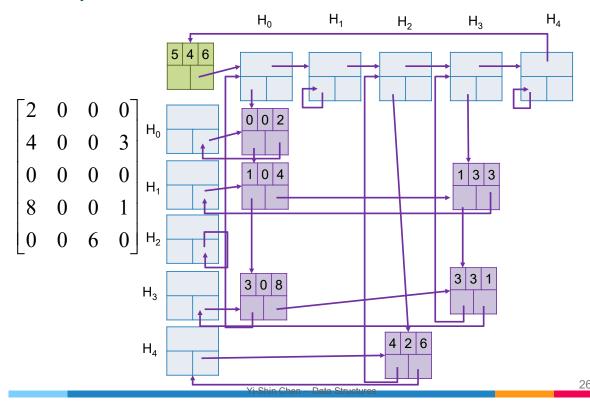
### **Linked Structure**

- ■Header node: for each row or column
  - **Down**: link to the 1<sup>st</sup> non-zero term in the column
  - **Right**: link to the 1<sup>st</sup> non-zero term in the row
  - Next: link to the next head node
  - The header node for row *i* is also the header node for column *i*
- ■Element node, each non-zero term that stores
  - Data of row, col, and value
  - A down field to link to the next non-zero term in the same column
  - A right field to link to the next non-zero term in the same row
- ■The header of header nodes (a circular list)
  - Store dimension of the matrix

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# Sparse Matrix in Linked Structure



### Create a Sparse Matrix

- ■Given a nxm sparse matrix with r non-zero terms
  - the total number of required nodes are max{n, m} + r + 1
- ■Input format
  - The 1st line gives the dimension of matric and # of non-zero terms
  - Each subsequent input line is a triple of the form (i, j, a<sub>ii</sub>)
    - Triples are ordered by rows and within rows by columns

Гэ	Λ	Λ	$^{-}$	IIIput
2	U	U	0	5,4,6;
4	0	0	3	0,0,2;
	0	0	Λ	1,0,4;
U	U	U	U	1,3,3;
8	0	0	1	3,0,8;
	•	_	_	3,3,1;
$\lfloor 0 \rfloor$	0	6	0_	4,2,6;

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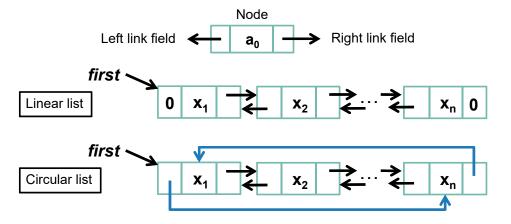
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## Create a Sparse Matrix

- ■Performance analysis
  - Set up header nodes, O(max{n,m})
  - Set up non-zero nodes, O(r)
  - Close column lists, O(max{n,m})
  - Link header nodes, O(max{n,m})
- ■Total complexity: O(max{n,m}+r) = O(n+m+r)

### **Double Linked Lists**

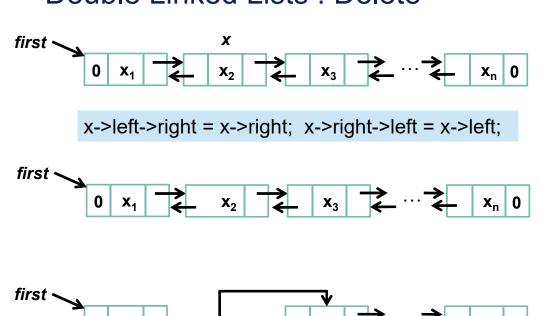
- ■Each node has two link fields
- ■Could move in two directions to visit nodes



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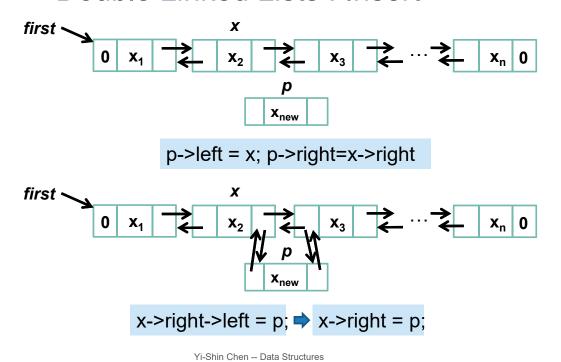
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### Double Linked Lists: Delete



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### **Double Linked Lists: Insert**



# **Self-Study Topics**

- ■Polynomial using linked lists
- ■Linked stacks and queues



### Visit Elements in a Container

- ■Suppose we have a chain C of datatype Chain<int>.
  - Output all integers in C
  - Obtain the maximum, minimum or mean of all integers in C
  - Obtain the sum, product, or sum of squares of all integers in C
- ■All operations require to visit every element in the chain C

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### How to Visit a Container?

```
For each item in C
{
    currentItem = current item in C;
    //do something with currentItem;
}
```

In an array representation

```
for (int i = 0; i < n; i++)
{
   int currentItem = a[i];
   // do something with currentItem;
}</pre>
```

### How to Visit a Container?

```
For each item in C
   currentItem = current item in C;
   // do something with currentItem;
```

■In a linked list representation

```
for (ChainNode<int> *ptr=first; ptr!=0; ptr=ptr->link)
   int currentItem = ptr->data;
   // do something with currentItem;
```

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# Visiting a Container using Iterator

- ■A powerful mechanism to visit a container with arbitrary data type
- Guarantee runtime range safety
- Applicable to all STL algorithms
- ■Suitable for team development
- Might scarify some amount of performance

```
// Possible implementation of STL copy algorithm
template < class Iterator >
void copy(Iterator start, Iterator end, Iterator to)
{ // copy from src[start, end) to dst[to, to+end-start)
   while (start != end)
   { *to = *start ; start++ ; to++; }
                      <del>Yi-Shin Chen -- Data Structure</del>:
```

### What is an Iterator?

```
void main()
{
   int x [3] = {0,1,2};
   for (int* y = x; y != x+3; y++)
      cout << *y << endl;
}</pre>
```

- ■An *iterator* is a pointer to an element in a container
- Using dereferencing operator (\*) to access an element
- ■Support pre- or post- increment operator (++)

```
void main()
{
   for (Iterator y = start; y != end; y++)
      cout << *y << endl;
}</pre>
```

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#### C++ Iterators

- ■Input iterator
  - Read access, pre- and post- "++" operators.
- **■Output** iterator
  - Write access, pre- and post- "++" operators.
- **■Forward** iterator
  - pre- and post- "++" operators.
- ■Bidirectional iterator
  - pre- and post- "++" and "--" operators.
- ■Random access iterator
  - Permit pointer jumps by arbitrary amounts.
- ■All iterators supports "==", "!=" and "\*" operators

### Forward Iterator for Chain

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### Forward Iterator for Chain

#### ■General usage

```
void main()
{
    Chain<int> myChain;
    // do operations on myChain here...

// print out every element in myChain
    Chain<int>::ChainIterator my_it;
    for (my_it = myChain.begin(); myChain!=myChain.end(); ++m_it)
        cout << *m_it << endl;

// Use STL algorithm to calculate the sum of myChain
    int sum = std::accumulate(myChain.begin(), myChain.end(),0);
}</pre>
```

```
Class ChainIterator{ // A nested class within Chain
public:
  // Constructor
  ChainIterator(ChainNode<T>* startNode = 0)
               {current = startNode;}
  // Dereferencing operator
  T& operator*() const {return current->data;}
  T* operator->() const {return &current->data;}
  // Increment operator
  ChainIterator& operator++() // pre-"++"
  { current = current->link ; return *this; }
  ChainIterator operator++(int)// post- "++"
    ChainIterator old = *this;
    current = current->link;
    return old;
  }
  // Equality operators
  bool operator!=(const ChainIterator right) const
  { return current != right.current; }
  bool operator==(const ChainIterator right) const
  { return current == right.current;}
private:
   ChainNode<T>* current;
};
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```