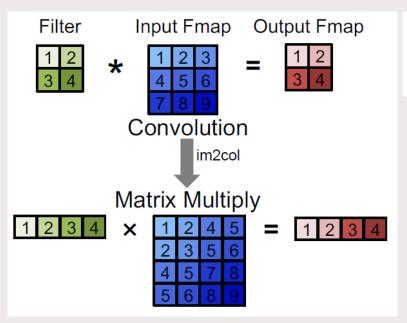
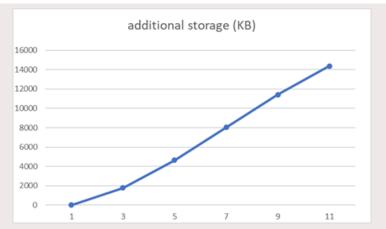




Part 1: Im2col



original memory =
$$H * W * M * N * \frac{4}{1024}$$
 (KB)
 $im2col\ memory = R * S * (H - R + 1) * (W - S + 1) * M * N * \frac{4}{1024}$ (KB)





2

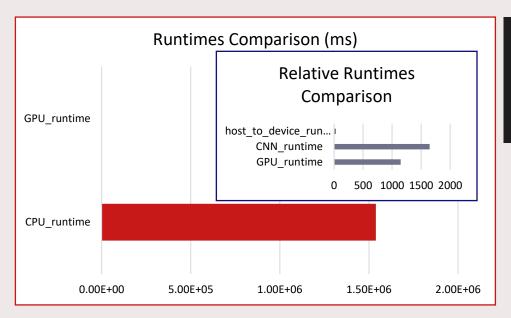
Part 2: GPU

```
_global__ void optimized_fpu_gemm(fpu_type* A, fpu_type* B, float* C, float* D, int gemmM, int gemmN ,int gemmK ,float alpha , float beta){
  // implement the optimized floating point unit kernel using shared memory and loop unrolling
  // some step hints for you. Feel free to follow different steps
  // step 1. creat shared memory buffer
  __shared__ fpu_type A_tile[M_tiles_CUDA][K_tiles_CUDA];
  __shared__ fpu_type B_tile[M_tiles_CUDA][K_tiles_CUDA];
  // shorten parameters for clean re-use
  int tx = threadIdx.x:
  int ty = threadIdx.y;
  fpu_type accu = 0.0;
  int row = blockIdx.y * blockDim.y + threadIdx.y;
  int col = blockIdx.x * blockDim.x + threadIdx.x;
  for (int tileIdx = 0; tileIdx < gemmK / K tiles CUDA; tileIdx++){</pre>
      // step 1: load data from global mem to shared mem
      if (tx + 1 <= K_tiles_CUDA && ty + 1 <= K_tiles_CUDA){</pre>
          A_tile[ty][tx] = A[row * gemmK + (tileIdx * K_tiles_CUDA + tx)];
          B_tile[ty][tx] = B[col * gemmK + (tileIdx * K_tiles_CUDA + ty)]; //Coalesced
      __syncthreads();
      // step 2: load data from shared mem to register
      for (int k = 0; k < K tiles CUDA; k++){
          accu = accu + A_tile[ty][k] * B_tile[k][tx]; //Coalesced
      __syncthreads();
  // step 3: addtional computations: adding matrix C
  accu = alpha * static_cast<float>(accu) + beta * C[row * gemmN + col];
  // step 4 store back the final results to globla memory
  D[row * gemmN + col] = accu;
```



Baseline CUDA core

CPU_runtime	GPU_runtime	CNN_runtime	host_to_device_runtime
1.54E+06	1147.35	1647	31



```
Matrix Size : MxNxK : 4096x4096x4096

Warm-up Rounds = 0

TEST_ROUNDS = 1

average time of CPU baseline = 1.53906e+06 ms

Runtime of memory copying from host to device = 31 ms
average time of kernel simple_fpu = 1147.35 ms

Total runtime of the CNN layer = 1647 ms
```

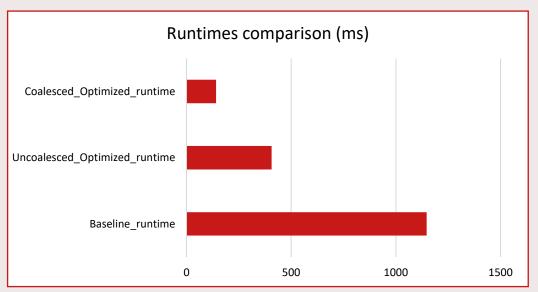
```
1540000 \div 1147.35 \approx 1342 \ times \ faster
```

$$1540000 \div 1647 \approx 935 \ times \ faster$$



Optimized CUDA core

Baseline_runtime	Uncoalesced_Optimized_runtime	Coalesced_Optimized_runtime	
1147.35	406.769	141.204	



Uncoalesced tiling

```
Matrix Size : MxNxK : 4096x4096x4096
numeric check passed
Tiling size = 32
average time of kernel optimized_fpu = 406.769 ms
```

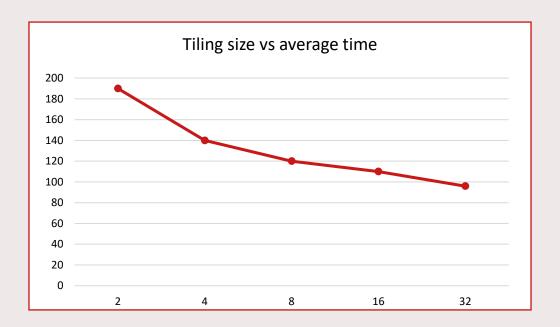
Coalesced tiling

```
1 Matrix Size : MxNxK : 4096x4096x4096
2 Runtime of matrix transpose = 376 ms
3 numeric check passed
4 Tiling size = 32
5 average time of kernel optimized_fpu = 141.204 ms
```

```
1147.35 \div 406.769 \approx 3 times faster 1147.35 \div 141.204 \approx 8 times faster
```



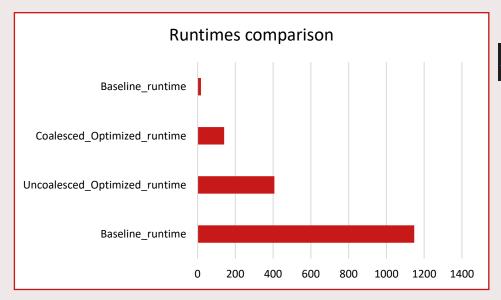
Tiling size vs Average time





Baseline Tensor core

CUDA			Tensor
Baseline_runtime	Uncoalesced_Optimized_runtime	Coalesced_Optimized_runtime	Baseline_runtime
1147.35	406.769	141.204	17.9



average time of kernel simple_wmma = 17.9091 ms
Total runtime of the CNN layer = 363 ms

 $1147.35 \div 17.9 \approx 64 \text{ times faster}$

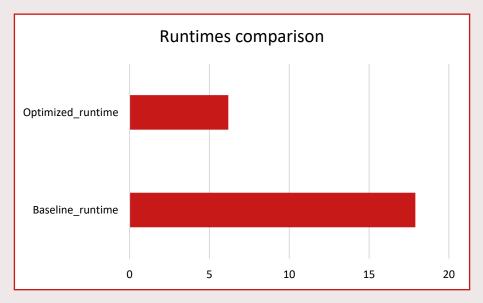
 $406.769 \div 17.9 \approx 23 \text{ times faster}$

 $141.204 \div 17.9 \approx 8 \ times \ faster$



Optimized Tensor core (shared memory only)

Tensor			
Baseline_runtime	Optimized_runtime		
17.9	6.18		



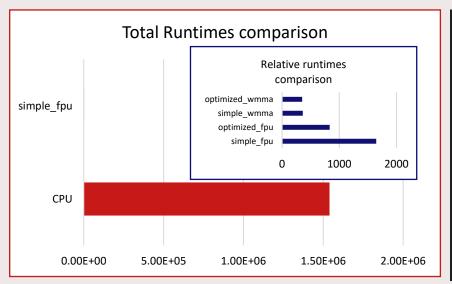
average time of kernel optimized_wmma = 6.18253 ms Total runtime of the CNN layer = 352 ms

 $17.9 \div 6.18 \approx 3 \text{ times faster}$



Comparison of total run time

Total Runtime						
CPU	simple_fpu	optimized_fpu	simple_wmma	optimized_wmma		
1.54E+06	1647	833	363	352		
Kernel Runtime						
1.54E+06	1147.35	111.72	17.9	6.18		



```
Matrix Size : MxNxK : 4096x4096x4096
Warm-up Rounds = 0
TEST ROUNDS = 1
average time of CPU baseline = 1.53906e+06 ms
Runtime of memory copying from host to device = 31 ms
average time of kernel simple_fpu = 1147.35 ms
Total runtime of the CNN layer = 1647 ms
average time of kernel simple wmma = 17.9091 ms
Total runtime of the CNN layer = 363 ms
Runtime of matrix transpose = 376 ms
Tiling size = 32
average time of kernel optimized fpu = 111.721 ms
Total runtime of the CNN layer = 833 ms
average time of kernel optimized wmma = 6.18253 ms
Total runtime of the CNN layer = 352 ms
```

