1. Solve each of the following nots of simultaneous congruenas @x = 1 (mod 3), x = 2 (mod 5), x = 2 (mod 5), x = 3 (mod 7)

Solo Product of all moduli, M= 3×5×7 = 105 We can compute partial moduli, dividing M by each modulus:

 $M_1 = \frac{105}{3} = 35$ ,  $M_2 = \frac{105}{5} = 21$ ,  $M_3 = \frac{105}{7} = 15$ 

Inverse at Mg mod mi; where my are 3,5,7.

1. 35 mod 3 = 2 inversed 35 mod 3 = 2

2.21 mod 5 = 1 Priverse of 21 mod 5 = 1

3.15 mod 7 = 1 inverse of 15 mod 7 = 1

total weighted som = 1.35.2 + 2.21.1 + 3.15.1

= 70+42+45

- 157

X=157 mod 105 > X=52 (or 1 remainder 52)

:. x = 52/mod 105)

(b) x = 5 (mod (1)), n = 14 (mod 29), n = 15 (mod 31)

products of all moduli, m = 11.29.31

= 9889

GOOD LUCK

partial moduli:

$$M_1 = \frac{9889}{11} = 899$$
  $M_2 = \frac{7889}{29}$ 

$$m_2 - \frac{9889}{29} = 341$$

$$M_3 = \frac{9889}{31} = 319$$

modular inverses of Mi mod mi or yi :

we know, Miy; - 1 (mod mi)

1. Mi mod m; = 899 mod 11 - 8

2.341 mod 29 = 22

3.319 mod 31 = 9 9
$$y_3 = 1 \text{ mod } (31) \times 9 \times 7 - 63 = 19$$
  
 $y_3 = 7$ 

18 +0 11 - m ilvbory (lasto duborg

c) 2=5 mod 6, x=4 mod 11, x=3 mod 17.

sol: Products of the moduli, M = my x mx x mz

= 6.11.17 = 1122

Partial moduli: My = 1122 - 187

m= 1122/1 = 102

Mg = 1122/17 = 66

modular Inverse: M; J; = 1 mod mi

1. My mod m; = 187 mod 6 = 1

1×1=1>1/2=1

2. 102 mod 11 = 3 3x4=12=1> 12=4

3.66 mod 17=15 15×8=120 =1 > y3=8

total sum = 5.257.1 + 4.102.4 + 3.66.8

= 4151

x = 4151 mod 1122 > x = 785 or (3 remainder 785)

Spring special town on abelian group.

2 = 785 mod 1122