2024 1st Half Chonnam Nat'l Univ PIMM Algorithm Party

Solutions Commentary Editorial

	Problem	Difficulty	Author
A	Clock Tower	Bronze	Mingyu Kojjkmk1013
В	Guessing the Song using the Intro	Bronze	Yoonsu Leelys9546
С	Rotating Sequence and Query	Silver	Jeonghwan Choijh01533
D	Escaping Hexagontiles	Silver	Yoonsu Leelys9546
Е	Retiring from Retirement	Gold	Jonghyeon Parkbelline0124
F	Mighty Fine Morning	Gold	Geunseong Kimonsbtyd
G	Move or Block!	Gold	Jeonghwan Choijh01533
Н	Guardians of the Forest	Gold	Yeongdo Jeong
	Three Number XOR and Query	Platinum	Jeonghwan Choijh01533

A. Clock Tower

#implementation

Difficulty — Easy

- Author: Mingyu Kojjkmk1013
- 219 Submitted, 180 Passed
 AC Ratio: 82.648%
- First Solver: ychangseok, +1min

A. Clock Tower

- ✓ You can solve it by dividing the equation by 30 minutes of the changed clock tower, where the speed of the minute hand changes.
- \checkmark For the correct time minutes f(x), the minute the minute the changed clock tower points to x is as below.

$$f(x) = \begin{cases} \frac{1}{2}x & (x \le 30) \\ \frac{3}{2}x + 15(x > 30) \end{cases}$$

✓ Simulations of calculating the actual time are also possible, adding 0 minutes to 1 for the time of the changed clock tower.

B. Guessing the Song using the Intro

#implementation, #brute_force

Difficulty — Bronze

Author: Yoonsu Leelys9546

192 Submitted, 158 Passed
 AC Ratio: 83.333%

First Solver: nflight11, +2min

B. Guessing the Song using the Intro

- ✓ You can solve the equation by dividing it based on the 30-minute point of the changed clock tower, where the speed of the minute hand changes.
- \checkmark For the correct minute f(x), if you set up the equation with the minute x that the minute hand of the changed clock tower points to, it is as follows.

$$f(x) = \begin{cases} \frac{1}{2}x & (x \le 30) \\ \frac{3}{2}x + 15(x > 30) \end{cases}$$

✓ You can also simulate calculating the actual time by adding 1 from 0 minutes for the time of the changed clock tower.

#prefix_sum, #implementation

Difficulty — Silver

- Author: Jeonghwan Choijh01533
- 288 Submitted, 74 Passed
 AC Ratio: 29.514%
- First Solver: mj1000j, +3min

- \checkmark Let's think about how to rotating the sequence to the right by k.
- ✓ If we simply use the deque to remove the last element and put it in the front by repeating the task k times, the time complexity will be O(NQ), and the time will exceed.
- Is there a way to achieve the same effect as rotating without actually rotating it?

- ✓ Let's think of the sequence as a raw sequence. When the raw sequence is rotated, the distance moved by all elements is the same and the left-right relationship between elements is always constant.
- ✓ In other words, if we only know the unrotated sequence and the distance moved by one element, we can know the current sequence.
- \checkmark Let's say the moved distance is D. (Initially, D=0)
- \checkmark When query 1 comes in, it rotates to the right by k, so it's the same as doing D+=k.
- \checkmark When query 2 comes in, it rotates to the left by k, so it's the same as doing D-=k.

- ✓ Let's process query 3 using the above information.
- \checkmark Recalculate input a, b using D. For convenience, we use 0-based (indexing from 0).
- $x = (a 1 D) \mod N$ (mod is remainder operation, be careful to handle negative mod)
- $\checkmark y = (b-1-D) \mod N$

(It would be good to draw the original sequence yourself and see how it works.)

- In this case, the problem is to find the sum from the x index to the y index in the unrotated sequence, and this can be found using the cumulative sum technique.
- ✓ Note that if y < x, we need to process it as (interval sum from x to (N-1)) + (interval sum from 0 to y).
- \checkmark The total time complexity is O(N+Q).

D. Escaping Hexagontiles

#graph, #bfs

Difficulty — Silver

Author: Yoonsu Leelys9546

88 Submitted, 60 Passed
 AC Ratio: 69.318%

First Solver: kyo20111, +11min

D. Escaping Hexagontiles

- You can model a graph by treating the odd and even rows of adjacent hexagonal tiles differently.
- ✓ Then, you can find the shortest path tiles from the starting point (0,0) to (N-1,M-1) through BFS.

E. Retiring from Retirement

#dp, #knapsack

Difficulty — Gold

- Author: Jonghyeon Parkbelline0124
- 66 Submitted, 25 Passed

AC Ratio: 37.879%

• First Solver: dabbler1, +25min

E. Retiring from Retirement

- All three queries given bring relatively forward a retirement of Yeongdo.
- Since this problem asks about the relative difference in retirement dates between Jonghyeon and Yeongdo, the three queries can be processed as if they bring forward a retirement of Yeongdo.

- \checkmark Early retirement: Bring forward a retirement of Yeongdo by D.
- \checkmark Military training unit: Bring forward a retirement of Yeongdo by D.
- \checkmark Temporary non-commissioned officer: Bring forward a retirement of Yeongdo by $M\times30$.

E. Retiring from Retirement

- ✓ If you unify the target of the queries to one person, this problem can be solved with 0-1 knapsack.
- ✓ Since the relative difference in retirement dates between the two must be processed, it can be processed as if Jonghyeon's retirement is delayed.

#floyd_warshall, #dijkstra

Difficulty — Gold

- Author: Geunseong Kimonsbtyd
- 75 Submitted, 22 Passed

AC Ratio: 29.333%

• First Solver: kyo20111, +21min

- \checkmark The summary of this problem is "Find the minimum cost of going from node S to node E without going through node K times Q."
- Representative algorithms for finding this shortest path include Bellman-Ford, Floyd-Warshall, and Dijkstra.

✓ Bellman-Ford

It computes with a time complexity of $O(N^3M)$. It will time out approximately 10 billion in the given constraint.

✓ Floyd-Warshall

It computes with a time complexity of $O(N^4)$. It will pass within the given constraint with approximately 1 billion in the given constraint.

Heap Dijkstra

It computes with a time complexity of $O(N^2(N+M)\log N)$. It will time out approximately 7 billion in the given constraint.

\checkmark N^2 Dijkstra

It computes with a time complexity of $O(N^4)$. Given the constraint, it passes within the time limit of approximately 1 billion.

✓ The Solution is to run $O(N^2)$ Dijkstra N^2 times, or $O(N^3)$ Floyd Warshall N times.

Dijkstra

Declare an array in the form D[N][N][N].

If you start at node i and do not visit node j, run Dijkstra N^2 times in advance, filling in D[j][i][1~N].

✓ Floyd Warshall:

Declare an $N \times N$ array with N layers in the form D[N][N][N].

It uses the fact that the outermost k loop of the Floyd Warshall loop connects the path entering the kth node and the path leaving the kth node.

D[1~k-1][1~N][1~N], D[k+1 ~ N][1~N][1~N], that is, it updates the rest except for the kth layer.

You can calculate the above process and answer each query. The total time complexity is $O(N^4+Q)$.

- Key
 - 1. 1 billion operations can be completed within 1 second.
 - 2. Heap Dijkstra is slower than N^2 Dijkstra in a complete graph.
 - 3. Floyd's outermost k loop connects the incoming and outgoing paths.

#game_theory

Difficulty — Gold

- Author: Jeonghwan Choijh01533
- 74 Submitted, 9 Passed
 AC Ratio: 12.162%
- First Solver: fermion5, +49min

- ✓ For convenience, we will express the action of moving as a move, building a wall as a block, and assume that there is a wall outside the game board.
- ✓ Let's handle the trivial case first.
- ~~x0x~~ Second turn win (not given as input)
- ✓ ~~X0.~~, ~~.0X~~ First turn win
- The following explanation does not consider the above cases.

To solve this problem, we need to combine several observations.

- 1. Except in cases where it is possible to end the game or it is unavoidable, you should not block adjacent squares or move to a place that is a wall.
 - This is a move that leads directly to defeat.
 - Other observations are established under the assumption that this rule is followed.

- 2. It is best for a player with a sure-win strategy to block every turn.
 - ✓ Let's assume that only move is the best.

If the next person does move back to the original position, the pattern repeats and the game never ends. In other words, you can't win.

✓ Therefore, if you have a surefire strategy, you can see that block every turn is the best.

- 3. When the words are blocked with ~~x.0.x~~
 - ✓ If the number of remaining . is odd, the first turn wins, and if it is even, the second turn wins.
- 4. If the game ends, you must go through the case of statement 3.
 - It is always established by statement 1.
- 5. If it is not the current case of 3., you can make the number of .s as biased as you want after your turn ends while satisfying 1.
 - ✓ If you want to maintain the current bias, you can block it if it is not a move.
 - Players win by making the case of statement 3. and making the number of .s even.

- ✓ When making statement 3., you must block, so to win, the number of . must be odd on your turn.
- However, if it is not statement 3. at the current point, based on statement
 5.,

you can always hand over a situation where the number of . is even to the opponent.

According to statement 4., this means you can make it so that the opponent can never win.

In other words, if you fail to make statement 3. on the first turn of the game, you will always end up in a draw. Therefore, we can divide the whole thing into 5 cases.

- ~~x0x~~: After-turn win (does not need to be processed because it is not given as input.)
- ✓ ~~X0.~~, ~~.0X~~: First-turn win
- ~~X.0.X~~: If the number of . is odd, the first turn wins, if it is even, the second turn wins
- ~~X.0..~~, ~~..0.X~~: If the number of . is odd, first turn wins, if it is even, then a draw
- ~ ~~..0..~~: Draw

#tree, #graph_theory, #graph_traversal, #greedy

Difficulty — Gold

- Author: Yeongdo Jeong
- 16 Submitted, 4 Passed
 AC Ratio: 25%
- First Solver: dabbler1, +117min

The output of this problem is the maximum number of times you can use replication.

- ✓ You can see that replication is most efficient when it is executed at every vertex you pass, and it is also most efficient when you do not use wait.
- In other words, it can be simplified to "How many vertices are visited when the path passes through as many vertices as possible?"

O(N) solution

- ✓ It is inefficient to use one edge more than 3 times.
- ✓ It is an unnecessary back—and—forth between two vertices.
- ✓ In other words, all edges should be used less than 2 times.

- ✓ The number of visited vertices increases by one every time the number of edges used 2 times increases by one.
- ✓ Similarly, the number of visited vertices also increases by one when the number of edges used 1 times increases by one.
- ✓ The optimal solution is guaranteed when the sum of the edges used 2 times and the edges used 1 times is the maximum.
- \checkmark Assuming that a random path is created for the root to move, the number of edges used 1 times is the same as the number of edges between the b vertex and the destination vertex of the path.

- \checkmark We can deduce deductively that "the optimal solution is guaranteed when the root moves as much as possible in the direction of the a vertex."
- ✓ There is more than one optimal path.
- \checkmark Let's assume that the arbitrary vertex on the tree that becomes the destination of the optimal path is the c vertex.

- \checkmark When the a vertex is set as the root node of the tree, if the c vertex is a descendant node of the b vertex,
- \checkmark It is guaranteed that the root moves as much as possible in the direction of the fire and then moves to the c vertex is one of the optimal paths.
- ✓ This is because the number of edges used 1 times remains unchanged, and the number of edges used 2 times is maximized.

- \checkmark When vertex a is set as the root node of the tree, if vertex c is not a descendant of vertex b,
- ✓ In order to reach vertex c from vertex b, the root must move in the direction of vertex a.
- \checkmark If the descendant node of the vertex where the root is located has moved until it becomes vertex c,
- \checkmark It is guaranteed that the root moves in the direction of the maximum fire and then moves to vertex c is one of the optimal paths.

A solution that operates in time complexity O(N) can be derived.

- 1. Find the midpoint between vertex a and vertex b.
- \checkmark This midpoint is the last vertex where the root can stand when moving from vertex b to vertex a as much as possible.
- \checkmark Let's assume this vertex is vertex d.
- 2. After selecting a random vertex on the tree, assume this vertex is the c vertex.
- 3. Find the optimal path when the c vertex is the destination and the number of vertices passed on the optimal path.
- [(the number of vertices between the b vertex and the d vertex) + the number of vertices between the d vertex and the c vertex) (the number of vertices in

the overlapping part of the previous two paths)] = the number of vertices passed

- 4. Repeat steps $2. \sim 3$. for all vertices. The maximum number of vertices from step 3. for all vertices is the answer to the problem.
- \checkmark The values required to perform step 3. can be calculated in advance in O(N) time before performing step 4..

#bitmask, #lazyprop

Difficulty — Platinum

- Author: Jeonghwan Choijh01533
- 16 Submitted, 1 Passed
 AC Ratio: 12.5%
- First Solver: kyo20111, +63min

- ✓ Let's process query 1 first.
- \checkmark Since A_i is small, we can preprocess all the three pairs that can make a number.
- ✓ The number of three pairs that can make x is 715, so if we only know the number of numbers in the interval [l, r], we can process query 1.
- ✓ We can find the number of numbers in the interval using a segment tree, but it seems difficult to return within $O(Q64 \log N + 715 Qc)$ time.

- \checkmark Let's take a closer look at 'The number of three pairs that can make x'.
- ✓ If 3 numbers are the same among the three pairs, it is in the form (x, x, x), and if 2 numbers are the same, it is in the form (y, y, x).
- \checkmark Does this mean that x exists in more than 3 cases? Which number exists more than 2 and x exists? It can be simplified to.
- Therefore, if we process the form separately, we only need to find the set of numbers, not the number of numbers, and this can be quickly found using a segment tree using a bit set.

- ✓ Based on the above information, let's construct a segment tree using a bit set.
- \checkmark Using the unsigned long long (or bitset) data type, we store whether the number i exists in the current section in the ith bit.
- ✓ The operation to merge nodes can be quickly calculated using the OR operation of two nodes.
- ✓ In this way, we quickly found the set of numbers in the section in $O(\log N)$.

- \checkmark The method for processing the (x,x,x) and (y,y,x) forms will be described later, and we need to check 651 cases excluding these.
- Even though the amount of operations seems large, since the set of numbers in the interval is bits, one case can be processed with a simple & operation, so it can be processed quickly.
- ✓ If you do not check all 651 cases, but only check the numbers included in the set, the number of operations is reduced by more than 2 times due to the characteristics of XOR.

Let's process query 2.

- ✓ It can be processed with a slowly updated segment tree. This can also be accelerated with bit operations.
- ✓ Doing $+x \mod 64$ on a node is the same as rotating the bits x spaces to the right.
- ✓ node = ((node << (64-x)) | (node >> x)) & (1<<64-1 | If you use a 64-bit data type, it is okay to omit it, be careful of overflow)

- \checkmark 'Are there 3 or more x? There are several ways to process 'Which number exists more than 2 and x exists'.
- ✓ Add a set of numbers that exist more than 2 and a set of numbers that exist more than 3 to the node. This can also be easily processed with bit operations.
- ✓ The set of numbers that exist more than 3 can be processed using the pigeonhole principle without inserting them.

- ✓ The overall time complexity is $O(N \log N + Q \log N + 651Q)$.
- ✓ The 651Q part may look large, but as described above, it is a simple operation that can be processed with a single & operation, and if you only search the numbers in the interval, the amount of operation is reduced by half according to the characteristics of XOR. It can be processed in about 0.1 seconds without any special optimization.