```
\sigma ::=
                                            Base type
          {\sf uint}
          bool
\psi \; ::= \;
                                            Source type
         \sigma
          \sigma[n]
c ::=
                                            Constant
                                            Source expression
e ::=
         e_1 + e_2
         \mathbf{cond}(e, e_1, e_2)
         e_1 > e_2
         [e_i]_n
         x[e]
         \mathbf{in}_{j}
                                            Source statement
     \psi x = e
         for x in n_1 \ldots n_2 do s
         x[e_1] := e_2
         if(e, s_1, s_2)
          \mathbf{out}\, e
         s_1; s_2
```

Figure 1: Source language

Figure 2: Source runtime

$$\rho \vdash e \Downarrow v$$

Figure 3: Source expression evaluation

$$\begin{array}{c} \rho \vdash e \Downarrow v \\ \hline \rho \vdash e \Downarrow v \\ \hline \rho \vdash \psi \ x = e \Downarrow \rho[x \mapsto v]; \end{array} \quad \text{SC_DECL} \\ \hline \rho \vdash e \Downarrow v \\ \hline \rho \vdash x := e \Downarrow \rho[x \mapsto v]; \end{array} \quad \text{SC_ASSGN} \\ \hline \frac{\rho[x \mapsto n_1] \vdash \textbf{loop} \ x \ \textbf{until} \ n_2 \ \textbf{do} \ s \Downarrow \rho_1; O}{\rho \vdash \textbf{for} \ x \ \textbf{in} \ n_1 \dots n_2 \ \textbf{do} \ s \Downarrow \rho_1; O} \quad \text{SC_FORT} \\ \hline \frac{\rho(x) > n_2}{\rho \vdash \textbf{loop} \ x \ \textbf{until} \ n_2 \ \textbf{do} \ s \Downarrow \rho_2; O} \quad \text{SC_LOOPT} \\ \hline \frac{\rho(x) \leq n_2}{\rho \vdash s \Downarrow \rho_1; O_1} \quad \text{SC_LOOPT} \\ \hline \frac{\rho(p_1|dom(\rho))[x \mapsto \rho(x) + 1] \vdash \textbf{loop} \ x \ \textbf{until} \ n_2 \ \textbf{do} \ s \Downarrow \rho_2; O_2}{\rho \vdash \textbf{loop} \ x \ \textbf{until} \ n_2 \ \textbf{do} \ s \Downarrow \rho_2; O_1, O_2} \quad \text{SC_LOOPI} \\ \hline \frac{\rho \vdash s \Downarrow \psi \ n}{\rho \vdash e_1 \Downarrow n} \quad \rho \vdash e_2 \Downarrow c \quad n < n' \\ \hline \rho \vdash x[e_1] := e_2 \Downarrow \rho[x \mapsto [c_i]_{n'}[n \mapsto c]]; \quad \text{SC_AWRITE} \\ \hline \frac{\rho \vdash e \Downarrow c}{\rho \vdash s_1 \Downarrow \rho'; O} \quad \text{SC_LIF} \\ \hline \frac{\rho \vdash e \Downarrow c}{\rho \vdash \textbf{out} \ e \Downarrow \rho'; O} \quad \text{SC_LIF} \\ \hline \frac{\rho \vdash e \Downarrow c}{\rho \vdash \textbf{out} \ e \Downarrow \rho_2; O_2} \\ \hline \rho \vdash s_1 \Downarrow \rho_1; O_1 \quad \rho_1 \vdash s_2 \Downarrow \rho_2; O_2 \\ \hline \rho \vdash s_1; s_2 \Downarrow \rho_2; O_2 \quad \text{SC_SEQ} \\ \hline \end{array}$$

Figure 4: Source command evaluation

 $v:\psi$

$$\frac{\overline{c: \mathsf{typeof}(c)}}{ V_{CONS}} \\ \frac{\forall i \in \{0, n-1\}. \ c_i : \sigma}{[c_i]_n : \sigma[n]} \quad V_{ARR}$$

Figure 5: Value typing

```
m ::=
                                                                                                           Secret label
        | A
| B
\ell ::=
                                                                                                           Label
                                                                                                           Type
\tau ::=
        \mid \quad \sigma^{\ell}
          \sigma^{\ell}[n]
\widetilde{e} ::=
                                                                                                           Target expression
                 \widetilde{e}_1 +_{\ell} \widetilde{e}_2
                  \operatorname{\mathbf{cond}}_{\ell}(\widetilde{e},\widetilde{e}_1,\widetilde{e}_2)
                  \widetilde{e}_1 >_{\ell} \widetilde{e}_2
                  [\widetilde{e}_i]_n
                  x[\widetilde{e}]
\mathbf{in}_{j}^{m}
\widetilde{e} \rhd m
\widetilde{s} ::=
                                                                                                           Target statement
                  \tau\,x=\widetilde{e}
                   x := \tilde{e}
                   for(x := n_1; x \le n_2; x := x + 1) \tilde{s}
                   x[\widetilde{e}_1] := \widetilde{e}_2
                  \mathbf{if}(\widetilde{e},\widetilde{s}_1,\widetilde{s}_2)
                   \mathbf{out}\,\widetilde{e}
                   \widetilde{s}_1; \widetilde{s}_2
\Gamma ::=
                                                                                                           Type environment
           \Gamma, x : \tau
```

Figure 6: Target language

$$\boxed{\Gamma \vdash e : \tau \leadsto \widetilde{e}}$$

$$\begin{array}{c} \Gamma \vdash c : \mathsf{typeof}(c)^{\mathcal{P}} \leadsto c \\ \hline \Gamma(x) = \tau \\ \hline \Gamma \vdash x : \tau \leadsto x \\ \hline S _{VAR} \\ \\ \forall i \in \{1,2\}. \ \Gamma \vdash e_i : \mathsf{uint}^{\ell} \leadsto \widetilde{e}_i \\ \ell = \mathcal{P} \lor \ell = \mathcal{A} \\ \hline \Gamma \vdash e_1 + e_2 : \mathsf{uint}^{\ell} \leadsto \widetilde{e}_1 +_{\ell} \widetilde{e}_2 \\ \hline \Gamma \vdash e : \mathsf{bool}^{\ell} \leadsto \widetilde{e} \\ \forall i \in \{1,2\}. \ \Gamma \vdash e_i : \sigma^{\ell'} \leadsto \widetilde{e}_i \\ \ell = \mathcal{P} \lor (\ell = \mathcal{B} \land \ell' = \mathcal{B}) \\ \hline \Gamma \vdash \mathbf{cond}(e, e_1, e_2) : \sigma^{\ell'} \leadsto \mathbf{cond}_{\ell}(\widetilde{e}, \widetilde{e}_1, \widetilde{e}_2) \\ \hline \hline \Gamma \vdash e : \mathcal{P} \lor \ell = \mathcal{B} \\ \hline \hline \Gamma \vdash e_1 > e_2 : \mathsf{bool}^{\ell} \leadsto \widetilde{e}_1 >_{\ell} \widetilde{e}_2 \\ \hline \hline \Gamma \vdash e : \mathsf{uint}^{\mathcal{P}} \leadsto \widetilde{e} \\ \hline \Gamma \vdash e : \mathsf{uint}^{\mathcal{P}} \leadsto \widetilde{e} \\ \hline \Gamma \vdash x[e] : \sigma^{\ell} \leadsto x[\widetilde{e}] \\ \hline \hline \Gamma \vdash \mathbf{in}_j : \sigma^m \leadsto \mathbf{in}_j^m \\ \hline \hline \Gamma \vdash e : \sigma^\ell \leadsto \widetilde{e} \\ \hline \Gamma \vdash e : \sigma^m \leadsto \widetilde{e} \rhd m \\ \hline \hline \Gamma \vdash e : \sigma^m \leadsto \widetilde{e} \rhd m \\ \hline \hline \Gamma \vdash e : \sigma^m \leadsto \widetilde{e} \rhd m \\ \hline \hline \end{array} \quad \mathbf{S}_{SUB}$$

Figure 7: Expression compilation

$$\begin{array}{c} \varphi = \sigma \Rightarrow \tau = \sigma^{\ell} \\ \psi = \sigma[n] \Rightarrow \tau = \sigma^{\ell}[n] \\ \Gamma \vdash e : \tau \rightsquigarrow \widetilde{e} \\ \hline \Gamma \vdash \psi x = e \rightsquigarrow \tau x = \widetilde{e} \mid \Gamma, x : \tau \\ \hline \Gamma(x) = \sigma^{\ell} \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \rightsquigarrow x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid \Gamma \\ \hline \Gamma \vdash x := e \mapsto x := \widetilde{e} \mid$$

Figure 8: Command compilation

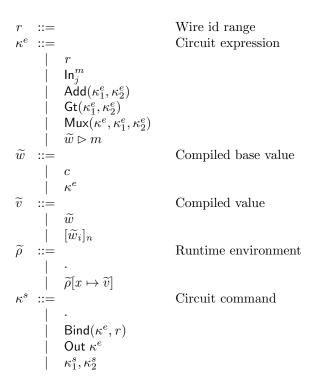


Figure 9: Target runtime

$$\widetilde{\rho} \vdash \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{v}$$

Figure 10: Target expression evaluation

$$\begin{array}{c} \widetilde{\rho} \vdash \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho'}; \kappa^s \\ \\ \dfrac{\widetilde{\rho} \vdash \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{v} \\ \widetilde{v} = c \lor \widetilde{v} \ \widetilde{v} = [c_i]_n \\ \widetilde{\rho} \vdash \tau x = \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{\rho}[x \mapsto \widetilde{v}]; . \end{array} \quad \text{EC_DECL} \\ \\ \dfrac{\widetilde{\rho} \vdash \widetilde{v} \ \widetilde{\Downarrow} \kappa^e \\ r = \text{next.range}()}{\widetilde{\rho} \vdash \tau x = \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{\rho}[x \mapsto r]; \text{Bind}(\kappa^e, r)} \quad \text{EC_DECLCKT} \\ \\ \dfrac{\widetilde{\rho} \vdash \widetilde{e} \ \widetilde{\Downarrow} \ [\kappa_i^s]_n \\ \forall i \in \{0, n-1\}. \ r_i = \text{next.range}() \\ \widetilde{\rho} \vdash \tau x = \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{\rho}[x \mapsto [r_i]_n]; \text{Bind}(\kappa_i^e, r_i)} \quad \text{EC_DECLCKTARR} \\ \\ \dfrac{\widetilde{\rho}[x \mapsto n_1] \vdash \mathbf{loop} \ x \ \mathbf{until} \ n_2 \ \mathbf{do} \ \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho}_1 \setminus \kappa^s \\ \widetilde{\rho} \vdash \mathbf{for}(x := n_1; x \leq n_2; x := x+1) \ \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho}_1 \setminus \kappa^s \\ \\ \dfrac{\widetilde{\rho}(x) > n_2}{\widetilde{\rho} \vdash \mathbf{loop} \ x \ \mathbf{until} \ n_2 \ \mathbf{do} \ \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho}_1 \setminus \kappa^s \\ \underbrace{\widetilde{\rho}[n_1]_{\mathrm{dom}(\widehat{\rho})}[x \mapsto \widetilde{\rho}(x) + 1] \vdash \mathbf{loop} \ x \ \mathbf{until} \ n_2 \ \mathbf{do} \ \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa_2^s \\ \widetilde{\rho} \vdash \mathbf{loop} \ x \ \mathbf{until} \ n_2 \ \mathbf{do} \ \widetilde{s} \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa_2^s \\ \underbrace{\widetilde{\rho} \vdash \kappa \widetilde{\Downarrow} \ \widetilde{\Downarrow} \ \widetilde{m}}_{p_1 \mapsto \widetilde{e} 2 \ \widetilde{\Downarrow} \ \widetilde{w} \\ n < n' \\ \widetilde{\rho} \vdash \kappa \widetilde{e} 1 \ \widetilde{\Downarrow} n \\ \widetilde{\rho} \vdash \kappa \widetilde{e} 1 \ \widetilde{\Downarrow} \ \widetilde{\rho}; \kappa^s \\ \overline{\widetilde{\rho}} \vdash \mathbf{if}(\widetilde{e}, \widetilde{s}_1, \widetilde{s}_2) \ \widetilde{\Downarrow} \ \widetilde{\rho}; \kappa^s \\ \underbrace{\widetilde{\rho} \vdash \mathbf{if}(\widetilde{e}, \widetilde{s}_1, \widetilde{s}_2) \ \widetilde{\Downarrow} \ \widetilde{\rho}_1; \kappa^s \\ \widetilde{\rho} \vdash \mathbf{out} \ \widetilde{e} \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \underbrace{\widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \underbrace{\widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \underbrace{\widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ \underbrace{\widetilde{\rho} \vdash \kappa^s_1; \widetilde{\aleph}_2 \ \widetilde{\Downarrow} \ \widetilde{\rho}_2; \kappa^s_1, \kappa^s_2 \\ } \underbrace{\mathsf{EC_SEQ}} \\ \end{aligned}$$

Figure 11: Target command evaluation

$$\begin{array}{ll} b & ::= & \text{Share (byte string)} \\ \widehat{\rho} & ::= & \text{Circuit environment} \\ & | & \widehat{\rho}[r \mapsto b] \end{array}$$

Figure 12: Circuit runtime

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa^{e} \Downarrow b_{1}, b_{2}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash r \Downarrow \widehat{\rho_{1}}[r], \widehat{\rho_{2}}[r] \qquad \text{CKTE_R}$$

$$\frac{(b_{1}, b_{2}) = \mathcal{E}_{m}(c)}{\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \ln_{j}^{m} \Downarrow b_{1}, b_{2}} \qquad \text{CKTE_IN}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{1}^{e} \Downarrow b_{11}, b_{21}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{2}^{e} \Downarrow b_{12}, b_{22}$$

$$n_{1} = \mathcal{D}_{\mathcal{A}}(b_{11}, b_{21})$$

$$n_{2} = \mathcal{D}_{\mathcal{A}}(b_{11}, b_{21})$$

$$n_{2} = \mathcal{D}_{\mathcal{A}}(b_{12}, b_{22})$$

$$(b_{1}, b_{2}) = \mathcal{E}_{\mathcal{A}}(n_{1} + n_{2})$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{1}^{e} \Downarrow b_{11}, b_{21}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{2}^{e} \Downarrow b_{12}, b_{22}$$

$$n_{1} = \mathcal{D}_{\mathcal{B}}(b_{11}, b_{21})$$

$$n_{2} = \mathcal{D}_{\mathcal{B}}(b_{12}, b_{22})$$

$$(b_{1}, b_{2}) = \mathcal{E}_{\mathcal{B}}(n_{1} > n_{2})$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{1}^{e} \Downarrow b_{11}, b_{21}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{1}^{e} \Downarrow b_{11}, b_{21}$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa_{2}^{e} \Downarrow b_{12}, b_{22}$$

$$c = \mathcal{D}_{\mathcal{B}}(b_{11}, b_{21})$$

$$c_{2} = \mathcal{D}_{\mathcal{B}}(b_{12}, b_{22})$$

$$c = \top \Rightarrow (b'_{1}, b'_{2}) = \mathcal{E}_{\mathcal{B}}(c_{1})$$

$$c = \bot \Rightarrow (b'_{1}, b'_{2}) = \mathcal{E}_{\mathcal{B}}(c_{2})$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa \text{m} \Downarrow b_{1}, b_{2}$$

$$(b_{1}, b_{2}) = \mathcal{E}_{m}(c)$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa \text{e} \Downarrow b_{1}, b_{2}$$

$$c = \mathcal{D}_{m_{1}}(b_{1}, b_{2})$$

$$(b'_{1}, b'_{2}) = \mathcal{E}_{m}(c)$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa \text{e} \Downarrow b_{1}, b_{2}$$

$$c = \mathcal{D}_{m_{1}}(b_{1}, b_{2})$$

$$(b'_{1}, b'_{2}) = \mathcal{E}_{m}(c)$$

$$\widehat{\rho_{1}}, \widehat{\rho_{2}} \vdash \kappa \text{e} \gg m \Downarrow b'_{1}, b'_{2}$$

$$CKTE_COERCER$$

Figure 13: Circuit expression evaluation

$$\widehat{\rho}_1, \widehat{\rho}_2 \vdash \kappa^s \Downarrow \widehat{\rho}'_1, \widehat{\rho}'_2; O$$

$$\begin{array}{c} \overline{\rho_1,\widehat{\rho}_2 \vdash \cdot \Downarrow \widehat{\rho}_1,\widehat{\rho}_2;} \cdot \text{CKTC_EMP} \\ \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \kappa^e \Downarrow b_1,b_2} \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \mathsf{Bind}(\kappa^e,r) \Downarrow \widehat{\rho}_1[r \mapsto b_1],\widehat{\rho}_2[r \mapsto b_1];} \cdot \\ \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \mathsf{Bind}(\kappa^e,r) \Downarrow \widehat{\rho}_1[r \mapsto b_1],\widehat{\rho}_2[r \mapsto b_1];} \cdot \\ \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \kappa^e \Downarrow b_1,b_2} \\ \underline{c = \mathcal{D}_m(b_1,b_2)} \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \mathsf{Out}} \; \kappa^e \Downarrow \widehat{\rho}_1,\widehat{\rho}_2;c,\cdot \\ \\ \overline{\rho_1,\widehat{\rho}_2 \vdash \kappa^s_1 \Downarrow \widehat{\rho}_1',\widehat{\rho}_2';O_1} \\ \underline{\rho_1',\widehat{\rho}_2' \vdash \kappa^s_2 \Downarrow \widehat{\rho}_1'',\widehat{\rho}_2'';O_2} \\ \overline{\rho_1',\widehat{\rho}_2 \vdash \kappa^s_1,\kappa^s_2 \Downarrow \widehat{\rho}_1'',\widehat{\rho}_2'';O_1,O_2} \quad \text{CKTC_SEQ} \end{array}$$

Figure 14: Circuit command evaluation

$$\psi \sim \tau$$

$$rac{\overline{\sigma \sim \sigma^\ell}}{\sigma[n] \sim \sigma^\ell[n]}$$
 ST_ARR

Figure 15: Source type and target type consistency

$$\begin{array}{c} \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \\ \hline \Gamma \vdash \cdots \hookrightarrow \vdots \cdots \vdots \cdots \\ \hline \Gamma(x) = \sigma^{\mathcal{P}} \\ \hline c : \sigma \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}[x \mapsto c]; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}[x \mapsto c]; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}[x \mapsto r]; \widehat{\rho}_{1}[r \mapsto b_{1}], \widehat{\rho}_{2}[r \mapsto b_{2}] \\ \hline \Gamma(x) = \sigma^{\mathcal{P}}[n] \\ \forall i \in \{0, n - 1\}. \ c_{i} : \sigma \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \sigma \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \hookrightarrow \widetilde{\rho}; \widehat{\rho}_{1}, \widehat{\rho}_{2} \\ \hline \Gamma \vdash \rho \vdash \rho \vdash [c_{i}]_{n}] \hookrightarrow \widetilde{\rho}[x \mapsto [r_{i}]_{n}]; \widehat{\rho}_{1}[r_{i} \mapsto b_{1i}], \widehat{\rho}_{2}[r_{i} \mapsto b_{2i}] \\ \hline \end{array} \quad \text{EN-SARR}$$

Figure 16: Source environment to target environment compilation