

# Assignment # 3

## Question (2)

Inputs:  $w$

Outputs:  $z$

States:  $Q_1, \bar{Q}_2$

FF on the top:  $D_1$

FF on the bottom:  $D_2$

Inputs to FF

$$\begin{aligned} \textcircled{1} D_1 &= w \cdot (\bar{Q}_1 + Q_2) \quad \textcircled{2} D_2 = Q_2 \oplus (\bar{w} \cdot Q_2 + w \cdot \bar{Q}_2 \cdot Q_1) \\ &= \bar{Q}_2 (\bar{w} \cdot Q_2 + w \cdot \bar{Q}_2 \cdot Q_1) + (\bar{w} \cdot Q_2 + w \cdot \bar{Q}_2 \cdot Q_1) \cdot Q_2 \\ &= \bar{Q}_2 \bar{Q}_2 \bar{w} + \bar{Q}_2 \bar{Q}_2 \cdot w \cdot Q_1 + (\bar{Q}_2 \bar{w}) \cdot Q_2 \\ &\quad + (\bar{Q}_2 w Q_1) \cdot Q_2 \\ D_2 &= w \cdot Q_1 \cdot \bar{Q}_2 + w \cdot Q_2 + w \cdot Q_2 \cdot \bar{Q}_1 \end{aligned}$$

Final Output

$$z = Q_1 \cdot Q_2$$

$$\hat{Q}_1 = w \cdot (\bar{Q}_1 + Q_2)$$

$$\hat{Q}_2 = w \cdot Q_1 \cdot \bar{Q}_2 + w \cdot Q_2 + w \cdot Q_2 \cdot \bar{Q}_1$$

State transition table.

	Clk'	Pr'	w	$Q_1$	$Q_2$	$\hat{Q}_1$	$\hat{Q}_2$	z
①	0	1	0	0	0	0	0	0
②	1	1	0	0	1	0	0	0 <del>1</del>
③	1	1	0	1	0	0	0	0 <del>1</del>
④	1	1	0	1	1	0	0	1
⑤	1	1	1	0	0	1	0	0
⑥	1	1	1	0	1	1	1	0
⑦	1	1	1	1	0	0	1	0
⑧	1	1	1	1	1	1	1	1

### Question 1

(1a) Done on logic works.

$$\begin{aligned} b) \quad T_{pd} &= 1 \quad T_{su} = 1 \quad T_{cl} = T_{mux} + T_{dff} \\ &= 4 + 1 \\ T_{cl} &= 5 \end{aligned}$$

$$\begin{aligned} f_{max} &= \frac{1}{T_{pd} + T_{su} + T_{cl}} \\ &= \frac{1}{1 + 1 + 5} \\ &= \frac{1}{7ns} \end{aligned}$$

$$f_{max} = 142.86 \text{ MHz}$$

c) First time analysis ran at max frequency.  
Second time analysis ran at shorter time,  $\therefore$  at a frequency higher than max frequency.  
There is a big difference in the two diagrams, which show that for a bigger frequency, the circuit fails.