

Question Number	Scheme	Marks
8	$y = e^{3x} \sin 2x \quad \frac{dy}{dx} = 2e^{3x} \cos 2x + 3e^{3x} \sin 2x$ $\frac{d^2y}{dx^2} = (-4e^{3x} \sin 2x + 6e^{3x} \cos 2x) + (6e^{3x} \cos 2x + 9e^{3x} \sin 2x)$ $= 12e^{3x} \cos 2x + 5e^{3x} \sin 2x$ $\frac{d^2y}{dx^2} - 6\frac{dy}{dx} + 13y$ $= 12e^{3x} \cos 2x + 5e^{3x} \sin 2x - 6(2e^{3x} \cos 2x + 3e^{3x} \sin 2x) + 13e^{3x} \sin 2x$ $= 12e^{3x} \cos 2x + 5e^{3x} \sin 2x - 12e^{3x} \cos 2x - 18e^{3x} \sin 2x + 13e^{3x} \sin 2x$ $= 0$ *	M1A1 M1A1A1 dM1 ddM1 A1cso <b>[8]</b>
ALT	$\frac{dy}{dx} = 2e^{3x} \cos 2x + 3e^{3x} \sin 2x$ $\frac{dy}{dx} = 2e^{3x} \cos 2x + 3y$ $\frac{d^2y}{dx^2} = (-4e^{3x} \sin 2x + 6e^{3x} \cos 2x) + 3\frac{dy}{dx}$ $\frac{d^2y}{dx^2} - 6\frac{dy}{dx} + 13y = (-4e^{3x} \sin 2x + 6e^{3x} \cos 2x + 3\frac{dy}{dx}) - 6\frac{dy}{dx} + 13y$ $= -13y + 6e^{3x} \cos 2x + 9e^{3x} \sin 2x - 3\frac{dy}{dx} + 13y$ $= -13y + 3\frac{dy}{dx} - 3\frac{dy}{dx} + 13y = 0$ *	M1A1 M1A1A1 dM1 ddM1A1cso <b>[8]</b>
M1 A1 M1 A1 A1 dM1 ddM1 A1cso	<p>Attempt the product rule. 2 terms of the form <math>\pm ke^{3x} \cos 2x</math> and <math>\pm le^{3x} \sin 2x</math> with <math>k = 1</math> or <math>2</math> and <math>l = 1</math> or <math>3</math></p> <p>Fully correct first derivative</p> <p>Attempt the second derivative using the product rule <i>correctly</i> on either term. Must have at least one of the terms in the first derivative fully correct.</p> <p>A1 for each fully correct bracket</p> <p>Substitute their derivatives and y in <math>\frac{d^2y}{dx^2} - 6\frac{dy}{dx} + 13y</math> Depends on both previous M marks</p> <p>This and the following M mark may be awarded together.</p> <p>Remove the brackets</p> <p>Reach "0" from fully correct work.</p>	
ALT M1A1 M1 A1A1 dM1 ddM1 A1cso	<p>As above</p> <p>Replace sin term with a y term and attempt the second derivative using the product rule on first term.</p> <p>A1 Correct bracket A1 Correct second term</p> <p>As above</p> <p>Obtain an expression which is either all derivatives plus y terms or all trig terms</p> <p>Reach "0" from fully correct work</p>	