

Question Number	Scheme	Marks
8.	<p>(a) Gradient of <math>l_1</math> is <math>-\frac{2}{3}</math></p> <p>(b) Gradient of <math>l_2</math> is <math>-\frac{1}{-\frac{2}{3}} = \frac{3}{2}</math></p> <p>Equation of <math>l_2</math> is <math>y - 2 = \frac{3}{2}(x - 7)</math>      <math>[2y = 3x - 17]</math></p> <p>(c) <math>2x + 3y = -6 \Rightarrow 6x + 9y = -18</math>  <math>3x - 2y = 17 \Rightarrow 6x - 4y = 34</math>  <math>13y = -52</math>  <math>y = -4</math>  <math>2x - 12 = -6 \Rightarrow x = 3</math>      <math>[Q(3, -4)]</math></p> <p>(d) Equation of <math>l_3</math> is <math>y - 2 = -\frac{2}{3}(x - 7)</math>      <math>[3y + 2x = 20]</math>  or <math>2x + 3y + k = 0</math> so at <math>P(7, 2)</math>, <math>14 + 6 + k = 0</math>      M1  <math>k = -20 \Rightarrow 2x + 3y - 20 = 0</math>      A1</p> <p>(e) at <math>R</math>, <math>y = 0</math> so <math>2x + 6 = 0 \Rightarrow x = -3</math>      B1  <math>QR^2 = (3 + 3)^2 + (-4 - 0)^2</math> and <math>PQ^2 = (7 - 3)^2 + (2 + 4)^2</math>      M1  <math>\Rightarrow QR = \sqrt{36 + 16} = \sqrt{52}</math> and <math>PQ = \sqrt{4^2 + 6^2} = \sqrt{52}</math> or <math>QR^2 = PQ^2 = 52</math>      A1</p> <p>(f) <math>PQRS</math> is a square      B1  so area = <math>PQ \times QR = \sqrt{52} \times \sqrt{52}</math>      M1  <math>= 52</math>      A1      (15)</p>	

## Notes for Question 8

(a)

B1 for  $-\frac{2}{3}$  (or - 0.6 rec. or - 0.667, seen occasionally). Must be shown explicitly (re-arranging the equation to  $y = -\frac{2}{3}x - 2$  is not sufficient).

(b)

M1 for finding the gradient of  $l_2$  as  $-\frac{1}{\text{their gradient of } l_1}$

M1 for any complete method for finding the equation of  $l_2$ . Award M0 if gradient of  $l_1$  is used. Use of  $y = mx + c$  needs a value for  $c$  to be found.

A1cso for  $y - 2 = \frac{3}{2}(x - 7)$  oe. No need to simplify so ignore any simplification shown.

(c)

M1 for attempting the solution of the pair of simultaneous equations

A1 for  $x = 3$  or  $y = -4$

A1 for the second value correct. No need to write in coordinate brackets

(d)

M1 for attempting the equation of  $l_3$  - any complete valid method.

A1 for  $y - 2 = -\frac{2}{3}(x - 7)$  oe (Ignore any simplification shown)

(e)

B1 for  $x = -3$  No working need be shown.

M1 for attempting to obtain the length of either  $PQ$  or  $QR$  or  $PQ^2$  or  $QR^2$  using **their** coordinates of  $Q$ .

A1cao for both lengths or squares of lengths correct.

(f)

B1 state that or use the fact that  $PQRS$  is a square

M1 for Area =  $PQ \times QR = \dots$  using their values

A1cso for 52

## Notes for Question 8 Continued

*Alternatives:*

1. "Determinant" method:

B1 for  $S$  is (1, 6) seen explicitly or usedM1 for using **their** coordinates for  $P$ ,  $Q$ ,  $R$  and  $S$  in the "determinant"

- must have the points in order, clockwise or anticlockwise
- must have a closed shape, ie first and last in the determinant are the same
- must use  $\frac{1}{2}$ , either now or to complete the work

Example "determinant"  $\frac{1}{2} \begin{vmatrix} 7 & 3 & -3 & 1 & 7 \\ 2 & -4 & 0 & 6 & 2 \end{vmatrix}$

A1 for 52 (must be positive)

2. Drawing a square around  $PQRS$ , finding area of this square and subtracting the triangular corners.B1 for  $S$  is (1, 6) seen explicitly or usedM1 for a complete method, ie find **all** required areas and attempt the subtractions needed

A1 for 52