

Question number	Scheme	Marks
4	$(S_4 =) \frac{a(1-r^4)}{1-r} = 80 \quad \text{or} \quad (S_{\infty} =) \frac{a}{1-r} = 81 \quad \text{or} \quad a + ar + ar^2 + ar^3 = 80$ $\frac{81(1-r)(1-r^4)}{1-r} = 80 \Rightarrow (81(1-r^4) = 80)$ <p>or</p> $81(1-r) = \frac{80(1-r)}{1-r^4}$ $(\Rightarrow (81-81r)(1-r^4) = 80(1-r) \Rightarrow 81r^5 - 81r^4 - r + 1 = 0 \Rightarrow (81r^4 - 1)(r-1) = 0)$ <p>or</p> $81(1-r) + 81(1-r)r + 81(1-r)r^2 + 81(1-r)r^3 = 80$ $r^4 = \frac{1}{81}$ $r = \pm \frac{1}{3}$ $[a = 54]$ $S_7 = \frac{{}^{54}P_7 \left(1 - \left(\frac{1}{3} \right)^7 \right)}{1 - \frac{1}{3}} \text{ or } \frac{2186}{27} \text{ or } 81 \left(1 - \left(\frac{1}{3} \right)^7 \right)$ $81 - \frac{2186}{27} = \frac{1}{27} *$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>dM1 A1* cso (7)</p>
ALT	<p>FINAL THREE MARKS</p> $S_7 = \frac{{}^{54}P_7 \left(1 - \left(\frac{1}{3} \right)^7 \right)}{1 - \frac{1}{3}} \text{ or } \frac{2186}{27}$ $81 - \frac{1}{27} = \frac{2186}{27}$	<p>M1</p> <p>ddM1 A1</p>
Total 7 marks		

Marks	Notes
B1	For $\frac{a(1-r^4)}{1-r} = 80$ or $\frac{a}{1-r} = 81$ or $a + ar + ar^2 + ar^3 = 80$
M1	For substituting S_{∞} into S_4 and eliminating a Students may also rearrange to make a the subject of both and then substitute to eliminate a . Allow one error in manipulation. Must use a valid method to eliminate. Using their S_{∞} and S_4
M1	For reaching $r^4 = \dots$ or for reaching $81r^5 - 81r^4 - r + 1 = 0$
A1	For $r = \frac{1}{3}$ (accept \pm)
M1	Correct substitution into $\frac{a(1-r^7)}{1-r}$ or $a + ar + ar^2 + ar^3 + ar^4 + ar^5 + ar^6$ or $81(1-r^7)$ - using their a and their r . r must be positive. Or $\frac{2186}{27}$
dM1	For $81 - \frac{2186}{27}$ Dependant on previous method mark. Their r must be positive. If a and r are correct, the evaluation of each part of these calculations need not be shown (can be done on a calculator). If either a or r are incorrect, their $\frac{2186}{27}$ must have been evaluated and 81 used.
A1 cso*	Obtains the given answer. No incorrect work.
ALT	Final 3 marks
M1	Correct substitution into $\frac{a(1-r^7)}{1-r}$ or $a + ar + ar^2 + ar^3 + ar^4 + ar^5 + ar^6$ - using their a and their r . r must be positive.
dM1 A1	Must state $81 - \frac{1}{27} = \frac{2186}{27}$ (for this ALT, candidates must evaluate and get $\frac{2186}{27}$) It isn't possible to get dM1 A0 on the ALT Dependent on previous method mark.