

Question number	Scheme	Marks
10 (a)	$\sin x + 1 = \cos x + 1 \Rightarrow \tan x = 1$ $x = \frac{\pi}{4}, \frac{5\pi}{4}$	M1 A1 A1 (3)
(b)	Area R_1 : $\int_{\frac{\pi}{4}}^{\frac{5\pi}{4}} (\sin x + 1) - (\cos x + 1) dx = \int_{\frac{\pi}{4}}^{\frac{5\pi}{4}} (\sin x - \cos x) dx$ $\left[-\cos x - \sin x \right]_{\frac{\pi}{4}}^{\frac{5\pi}{4}}$ $\left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \right) - \left(-\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2} \right) = 2\sqrt{2}$ Area R_2 : $\int_{\pi}^{\frac{5\pi}{4}} (\cos x + 1) dx + \int_{\frac{5\pi}{4}}^{\frac{3\pi}{2}} (\sin x + 1) dx$ $\left[\sin x + x \right]_{\pi}^{\frac{5\pi}{4}} + \left[-\cos x + x \right]_{\frac{5\pi}{4}}^{\frac{3\pi}{2}}$ $\left[\left(-\frac{\sqrt{2}}{2} + \frac{5\pi}{4} \right) - \pi \right] + \left[\frac{3\pi}{2} - \left(\frac{\sqrt{2}}{2} + \frac{5\pi}{4} \right) \right] = -\sqrt{2} + \frac{1}{2}\pi$ area of R_1 : area of $R_2 = 2 : \left(\frac{\pi\sqrt{2}}{4} - 1 \right)$ oe	M1 M1 M1 A1 M1 A1 M1 A1 A1 (9)
Total 12 marks		

Part	Mark	Notes
(a)	M1	For $\tan x = 1$
	A1	For $x = \frac{\pi}{4}$ [Allow 45°]
	A1	For $x = \frac{5\pi}{4}$ [Allow 225°]
(b)	M1	For stating $A = \int_{\frac{\pi}{4}}^{\frac{5\pi}{4}} (\sin x + 1) - (\cos x + 1) dx$
	M1	For attempting to integrate their expression for the area. This must be correct for this mark. $\int (\sin x - \cos x) dx = -\cos x - \sin x$
	M1	For substitution of correct limits
	A1	For $2\sqrt{2}$
	M1	For attempting $\int f(x)dx + \int g(x)dx$ with the correct limits. $\int_{\pi}^{\frac{5\pi}{4}} (\cos x + 1) dx + \int_{\frac{5\pi}{4}}^{\frac{3\pi}{2}} (\sin x + 1) dx$
	M1	For attempting to integrate, which must be correct for this mark.
	M1	For substitution of their limits correctly.
	A1	For $-\sqrt{2} + \frac{1}{2}\pi$
	A1	For the simplified ratio $2 : \left(\frac{\pi\sqrt{2}}{4} - 1 \right)$