

Qu numb	Scheme	Marks
5 (a)	<p>Applies Pythagoras Theorem  <math>5^2 + 15^2 = 250 \Rightarrow 5\sqrt{10} (= AC)</math>  <math>\Rightarrow \angle ABC = 90^\circ *</math></p> <p><b>ALT</b>  <math>\cos \angle ABC = \frac{15^2 + 5^2 - 250}{2 \times 15 \times 5} = 0</math>  <math>\Rightarrow \angle ABC = 90^\circ *</math></p>	<p>M1</p> <p>A1cso (2)</p>
(b)	<p><math>DC = \sqrt{5^2 + 10^2} (= 5\sqrt{5})</math> and <math>DA = \sqrt{15^2 + 10^2} (= 5\sqrt{13})</math></p> <p><math>\angle DAC = \cos^{-1} \left( \frac{(5\sqrt{13})^2 + (5\sqrt{10})^2 - (5\sqrt{5})^2}{2 \times 5\sqrt{13} \times 5\sqrt{10}} \right) = 37.874... \approx 37.9^\circ</math></p>	<p>B1B1</p> <p>M1A1cao (4)</p>
(c)	<p><math>\angle BCA = \tan^{-1} \left( \frac{15}{5} \right) = 71.5650...^\circ</math> or find <math>\angle BAC = \tan^{-1} \left( \frac{5}{15} \right) = 18.43^\circ</math>  <math>XB = 5 \sin 71.565 = 4.74341...</math> <math>XB = 5 \cos 18.43 = 4.743...</math>  Required angle <math>\angle DXB = \tan^{-1} \left( \frac{10}{4.74341} \right) = 64.6230...^\circ \approx 64.6^\circ</math></p>	<p>M1 dM1</p> <p>M1A1cao (4)</p>
ALT 1	<p><b>Alternatives:</b>  <math>\Delta s ABC</math> and <math>BCX</math> are similar <math>\Rightarrow \frac{BX}{5} = \frac{15}{5\sqrt{10}} \Rightarrow BX = \frac{15}{\sqrt{10}}</math> M2  (may not be stated, just used)  Find angle as main scheme M1A1</p>	
ALT 2	<p>Use area formula twice for triangle <math>ABC</math>  <math>\frac{1}{2} AC \times BX = \frac{1}{2} AB \times BC \Rightarrow BX = \frac{15}{\sqrt{10}}</math> M2  Find angle as main scheme M1A1</p>	
ALT 3	<p><math>DX</math> is perpendicular to <math>AX</math> (Stated or used. No explanation/proof needed)  <math>DX = AD \sin \angle DAC (= 5\sqrt{13} \sin 37.9...^\circ)</math> M2  <math>\sin \angle DXB = \frac{10}{DX} \Rightarrow \angle DXB = 64.6^\circ</math> M1A1</p>	
		[10]

(a)		
M1	Use Pythagoras with correct signs in $\triangle ABC$ or use cosine rule (formula correct) or any other complete method	
A1cso	Correct conclusion stated and no errors in their method	
(b)		
B1	Correct length of $DC$ or $DA$	
B1	Second length correct	
M1	Use cosine rule in either form, formula must be correct, and reach a value for the size of $\angle DAC$	
A1cao	$37.9^\circ$ (Must be 1 dp)	
(c)		
M1	Use any trig ratio to obtain a value for the size of $\angle BCA$ (not nec correct)	
dM1	Use their value for $\angle BCA$ to obtain the length of $XB$ Depends on the first M mark	
M1	Use $\tan DXB$ (or any other complete method) to obtain a value for the size of $\angle DXB$ (not nec correct)	
A1cao	$64.6^\circ$ Must be 1 dp unless rounding already penalised in (b)	
	For the alternatives:	
	Getting directly to $XB$ or $DX$ scores M2	
	Completion to the angle M1A1	