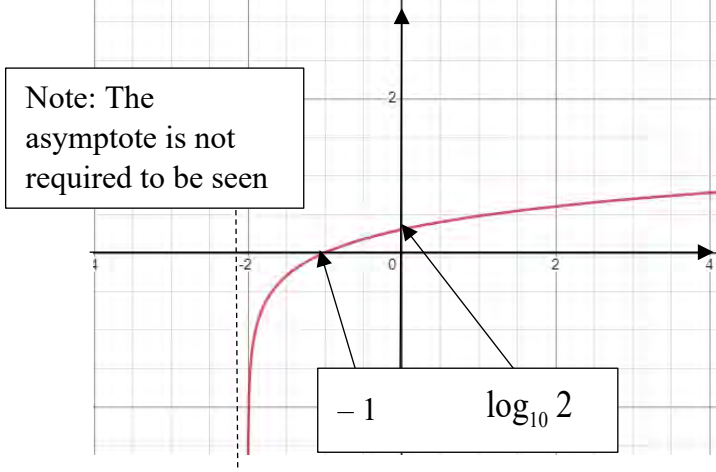


Question number	Scheme	Marks
7 (a)	<p>Shape of the curve, <b>crossing</b> negative <math>x</math>-axis and positive <math>y</math>-axis with the asymptotic nature of the curve shown.</p> <p>passes through <math>\log_{10} 2</math> (0.3(010.....)) <b>and</b> through <math>(-1, 0)</math> on <math>x</math>-axis</p>  <p>Note: The asymptote is not required to be seen</p>	<p>B1</p> <p>B1 [2]</p>
(b)	$(2\log_a 4 + 2\log_a 4^2)$ $2\log_a 4 + 4\log_a 4$ $\log_a 4 = \frac{1}{6}$ $a^{\frac{1}{6}} = 4$ $a = 4096$ <p><b>ALT</b></p> $(2)\log_a 64 = 1 \Rightarrow \log_a 64 = \frac{1}{2}$ $\Rightarrow a^{\frac{1}{2}} = 64$ $\Rightarrow a = 4096$ <p>or</p> $(2\log_a 2^2 + 2\log_a 2^4)$ $4\log_a 2 + 8\log_a 2$ $\log_a 2 = \frac{1}{12}$ $a^{\frac{1}{12}} = 2$ <p>oe</p>	<p>M1</p> <p>dM1</p> <p>A1</p> <p>[M1</p> <p>dM1 A1] [3]</p>
(c)	$\log_q 16 \rightarrow \frac{\log_2 16}{\log_2 q}$ $\left( 5 \frac{\log_2 16}{\log_2 q} + 4 \log_2 q = 24 \right)$ $20 + 4(\log_2 q)^2 = 24 \log_2 q$ $(\log_2 q - 5)(\log_2 q - 1) (= 0)$ $(\log_2 q = 5) \rightarrow q = 32$ $(\log_2 q = 1) \rightarrow q = 2$	$\log_2 q \rightarrow \frac{\log_q q}{\log_q 2} \text{ or } \frac{1}{\log_q 2}$ $\left( 5 \log_q 16 + 4 \frac{\log_q q}{\log_q 2} = 24 \right)$ $20(\log_q 2)^2 + 4 = 24 \log_q 2$ $(5 \log_q 2 - 1)(\log_q 2 - 1) (= 0)$ $\left( \log_q 2 = \frac{1}{5} \right) \rightarrow q = 32$ $(\log_q 2 = 1) \rightarrow q = 2$ <p>M1</p> <p>M1 A1</p> <p>dM1</p> <p>M1 A1 [6]</p>
Total 11 marks		

Part	Mark	Additional Guidance
(a)	B1	The curve must not bend back on itself and should cross both axes once on negative $x$ and once on positive $y$ . It needs to demonstrate an asymptotic nature. Accept an asymptote drawn correctly as well as their curve.
	B1	It is enough for $-1$ to be indicated on the $x$ -axis with the curve passing through this point and for $\log_{10} 2$ to be marked on the $y$ -axis (decimal 0.3..... allowed) There must be a curve drawn (even incorrectly) to achieve this mark. <b>Do not</b> accept intersections unless they are marked on the graph in the correct place.
(b)	M1	For the use of the power rule with logs to obtain $2\log_a 4$ from $\log_a 16$ OR $4\log_a 2$ from $\log_a 16$
	dM1	A <b>correct</b> rearrangement of their equation to obtain for example $a^{\frac{1}{6}} = 4$ or $a^{\frac{1}{12}} = 2$ or even of the type $a^1 = 64^2$ There are many ways of completing this. Look for a correct value for the corresponding correct power of $a$ . <b>This mark is dependent on the first M mark.</b> Look for correct log work for their values.
	A1	For $a = 4096$
	ALT	
ALT	M1	For use of the correct log rule to obtain $\log_a 64$
	dM1	A correct rearrangement of their equation to obtain $a^{\frac{1}{2}} = 64$ <b>This mark is dependent on the first M mark.</b> Look for correct log work for their values.
	A1	For $a = 4096$
	ALT	
(c)	M1	For a fully correct change of base of log to either base 2 or base $q$
	M1	For an attempt to rearrange and form a 3TQ quadratic. Allow one arithmetical slip only.
	A1	For the correct 3TQ.
	dM1	<b>Dependent on the second M mark</b> – an acceptable attempt to solve the quadratic equation – see general guidance.
	M1	For a correct application using either of their solutions moving from log form to exponential form. <b>Note this is an independent mark.</b>
	A1	<b>Both</b> correct solutions.