

| Question | Working | Answer | Mark | Notes |
|----------------------|--|--|------|--|
| 3 (a) | $3a + 5a = 4 - 6$ oe | | | M1 |
| | | $-\frac{1}{4}$ | 2 | A1 |
| (b) | $-3p > 12$ or $-12 > 3p$ | | | M1 |
| | | $p < -4$ | 2 | A1 |
| (c) | | $w \leq 5$ | 1 | B1 allow use of $x \leq 5$ |
| (d) | | $x \geq -1$ or $x > -1$ and $y \geq 0$ or $y > 0$ | 1 | B1 allow $-1 < x < n$ where $n \geq 2$ allow $0 < y < m$ where $m \geq 6$ |
| | $y = -2x + \dots$ or $y = \dots x + 4$ | | | M1 |
| | | $y \leq -2x + 4$ or $y < -2x + 4$ oe | 2 | A1 |
| Total 8 marks | | | | |

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|----------------------|-----------------------|---|------|--|
| 4 (a) | | $x, 23-x, 31-x, 27-x$ $x-5, x-10, x-10$ 0 | 3 | B1 B1 B1 |
| (b) | $x + 56 = 75$ | | | M1ft |
| | | 19 | 2 | A1 |
| (c)(i) | 17 | | 1 | B1ft their "27" - "10" |
| (ii) | 44 | | 1 | B1ft $2x - "5" + "31" - "20$ |
| (d) | $\frac{"19" - 5}{49}$ | | | M1 denominator of 49, numerator < 49 |
| | | $\frac{14}{49}$ | 2 | A1ft oe (0.2857... allow 2dp truncated or rounded) |
| Total 9 marks | | | | |

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| 5 (a) | Factorising into 2 brackets | | | M1 When multiplied out it must give at least 2 of the 3 terms correct |
| | | $(x+6)(x-1)$ | 2 | A1 |
| (b) | $\frac{4(x+3)-5(2x-2)}{20}$ or $\frac{x+3}{5} - \frac{x-1}{2}$ | | | M1 |
| | $\frac{4x+12-10x+10}{20}$ or $\frac{2x+6-5x+5}{10}$ | | | M1 |
| | | $\frac{-3x+11}{10}$ | 3 | A1oe |
| Total 5 marks | | | | |

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|----------|--|------------|------|-------|
| | | | | |
| 6 (a) | | Triangle A | 1 | B1 |
| (b) | $\begin{pmatrix} -2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 1 & 3 & 4 \\ 1 & 1 & 3 \end{pmatrix}$ | | | M1 |
| | $\begin{pmatrix} -2 & -6 & -8 \\ 2 & 2 & 6 \end{pmatrix}$ | | | A1 |
| | | Triangle B | 3 | A1 |
| (c) | | Triangle C | 1 | B1 |

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| (d) | $\mathbf{N} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} -2 & 0 \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$ <p>Or</p> <p>$A \rightarrow C$ is an enlargement with centre O and scale factor -2 so that</p> $\begin{pmatrix} 1 \\ 0 \end{pmatrix} \mapsto \begin{pmatrix} -2 \\ 0 \end{pmatrix} \text{ and } \begin{pmatrix} 0 \\ 1 \end{pmatrix} \mapsto \begin{pmatrix} 0 \\ -2 \end{pmatrix}$ | | | M1 Allow M1 for $\begin{pmatrix} 0 & -2 \\ -2 & 0 \end{pmatrix}$ |
| | | $\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$ | 2 | A1 |
| (e) | Rotation 180° about any point | | | M1 |
| | | Triangle D | 2 | A1 |
| (f) | | Enlargement | 1 | B1 |
| | | SF $\frac{1}{2}$ | 1 | B1 |
| | | centre $(-2, -2)$ | 1 | B1 |
| Total 12 marks | | | | |

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| 7 (a) | | $5 < t \leq 8$ | 1 | B1 |
| (b) | $2.5 \times 10 + 6.5 \times 8 + 9 \times 5 + 12.5 \times 3 + 22.5 \times 2$ $(= 204.5)$ | | | M2 for at least 4 correct products added OR (M1 for use of a value within interval (incl. end points) for at least 4 products, which must be added). |
| | $\frac{"204.5"}{28}$ | | | M1(dep) on at least M1 |
| | | awrt 7.3 | 4 | A1 |
| (c) | | Bar drawn height 30 little squares | 1 | B1 |
| (d) | | $\frac{5}{35}$ oe | 1 | B1 (0.14(28571...) or 14(.28571)%) |
| Total 7 marks | | | | |

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| 8 | 5010, 4990, 10100, 9900, 33.5, 34.5, 68.5, 67.5 | | | M1 at least 1 from each row. |
| | Colin $\frac{10100}{67.5}$ or $\frac{10.1}{67.5}$ | | | A1 |
| | Jenny $\frac{4990}{34.5}$ or $\frac{4.99}{34.5}$ | | | A1 |
| | $\frac{\left(\frac{10100}{67.5} - \frac{4990}{34.5}\right) \times 60}{1000}$ | | | M1 |
| | | 0.2995 (km/h) | 5 | A1 |
| Total 5 marks | | | | |

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| 9 (a) | $8y^2 - \dots = 400$ or ... $-2x^2 = 400$ or $2y(4y - x) + \dots = 400$ or ... $+ x(2y - x) = 400$ | | | M1 |
| | $4y^2 - x^2 = 200$ | | | A1cso |
| | $10y + 2x + 5 = 2y$ therefore $2y = 2x + 5$ | | 3 | B1cso |
| (b) | $(2x+5)^2 - x^2 = 200$ | $4y^2 - \left(\frac{2y-5}{2}\right) = 200$ | | M1 |
| | $3x^2 + 20x - 175 = 0$ | $12y^2 + 20y - 825 = 0$ | | M1 Rearranging correctly to get a 3 term quadratic |
| | $(3x+35)(x-5)=0$ $\underline{-20 \pm \sqrt{20^2 - 4 \times 3 \times -175}}$ 2×3 | $(2y-15)(6y+55)=0$ $\underline{-20 \pm \sqrt{20^2 - 4 \times 12 \times -825}}$ 2×12 | | M1 dep on M1 for solving their quadratic equation using any correct method - if factorising, allow brackets which expanded give 2 out of 3 terms correct (if using formula or completing the square allow one sign error and some simplification – allow as far as eg $\frac{-20 \pm \sqrt{400+2100}}{6}$ or eg $3\left(x+\frac{20}{6}\right)^2 - \frac{625}{3}$) |
| | $3[(x+\frac{20}{6})^2 - (\frac{20}{6})^2] - 175$ | $12[(y+\frac{20}{24})^2 - (\frac{20}{24})^2] - 825$ | | |

| | | | | | |
|----------------------|----------------------------------|------------------------------------|-----------------------|---|--|
| | $x = 5$ | $y = 7.5$ | | | A1 one correct result for x or for y (ignore negative value for this mark) |
| | $y = \frac{2 \times "5" + 5}{2}$ | $x = \frac{2 \times "7.5" - 5}{2}$ | | | M1 |
| | | | $x = 5$ and $y = 7.5$ | 5 | A1 dep on M2 (positive values only) |
| Total 8 marks | | | | | |

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| 10 (a) | $3 \times \left(\frac{1}{3}\right)^3 - 7 \times \left(\frac{1}{3}\right)^2 + 5 \times \frac{1}{3} - 1$ | | | M1 |
| | | $= 0, (3x - 1) \text{ is a factor}$ | 2 | A1 |
| (b) | $x^2 - 2x + 1$ | | | M1 |
| | $(x-1)(x-1)$ | | | M1 |
| | | $x = \frac{1}{3} \text{ or } 1$ | 3 | A1 |
| (c) | $\frac{dy}{dx} = 9x^2 - 14x + 5$ | | | M1 |
| | $(x-1)(9x-5) = 0$ | | | M1 |
| | | $1, \frac{5}{9}$ | | A1 |
| | Substituting x values into $y = 3x^3 - 7x^2 + 5x - 1$ | | | M1 |
| | | $(1, 0)$ $\left(\frac{5}{9}, \frac{32}{243}\right)$ | 5 | A1 |
| (d) (i) | | 5 | 1 | B1ft (ft $\frac{dy}{dx}$) |
| (ii) | $y = "5"x - 1$ | | | M1 |
| | | $y = 5x - 1$ | 2 | A1oe |
| Total 13 marks | | | | |

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| 11 (a) | SF $\frac{1}{5}$ | | | B1 use or statement of the correct SF |
| | $\frac{1}{3}(\pi) \times 30^2 \times 100 - \frac{1}{3}(\pi) \times "6"^2 \times 20 \text{ oe}$ | | | M1 |
| | | 29760 | 3 | A1 |
| (b) | | 40800π | 1 | B1 |
| (c) | $\frac{2}{3}\pi \times 30^3 + \dots$ | | | M1 |
| | $g = \text{height of small cone}$ $\frac{2}{3}\pi \times 30^3 +$ $\frac{1}{3}\pi \times 30^2 \times 108 - \frac{1}{3}\pi \times \left(\frac{30}{108}g\right)^2 \times g = "40800\pi"$ $0.02572g^3 = 9600$ | or | M1 Condone $30k^2$ A1 Correct equation | |
| | $g = 72$ | | | A1 |
| | $h = 30 + (108 - 72)$ | | | M1 |
| | | awrt 66 | 6 | A1 |
| Alternate method | | | | |
| | $V_{\text{hemisphere}} = \frac{2}{3}\pi \times 30^3 [= 18000\pi]$ | | | M1 |
| | $V_{\text{frustum}} = 40800\pi - 18000\pi [= 22800\pi]$ | | | |

| | | | | |
|-----------------------|--|---------|--|----|
| | $V_{\text{whole cone}} = \frac{1}{3}\pi \times 30^2 \times 108 [= 32400\pi]$ | | | |
| | $V_{\text{top cone}} 32400\pi - 22800\pi [= 9600\pi]$ | | | M1 |
| | $V_{\text{top cone}} : V_{\text{whole cone}} = 9600\pi : 32400\pi$ | | | A1 |
| | $= 8 : 27$ | | | |
| | $H_{\text{top cone}} : H_{\text{whole cone}} = 2 : 3$ | | | A1 |
| | $\frac{138-h}{108} = \frac{2}{3}$ | | | M1 |
| | | awrt 66 | | A1 |
| Total 10 marks | | | | |

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| 12 (a) | $\frac{1}{2} \mathbf{b} \pm \frac{1}{5} \mathbf{a}$ | | | M1 |
| | | $-\frac{1}{5} \mathbf{a} + \frac{1}{2} \mathbf{b}$ | 2 | A1 |
| (b) | $\overrightarrow{FC} = \frac{4}{5} \mathbf{a} + 2 \overrightarrow{AB}$ | | | M1 or $\overrightarrow{EC} = -\frac{1}{2} \mathbf{b} + \mathbf{a} + 2 \overrightarrow{AB}$ |
| | $\overrightarrow{FC} = \frac{4}{5} \mathbf{a} + 2(\mathbf{b} - \mathbf{a})$ | | | M1 or $\overrightarrow{EC} = -\frac{1}{2} \mathbf{b} + \mathbf{a} + 2(\mathbf{b} - \mathbf{a})$ |
| | $\overrightarrow{FC} = 2\mathbf{b} - \frac{6}{5} \mathbf{a}$ | | | A1 or $\overrightarrow{EC} = \frac{3}{2} \mathbf{b} - \mathbf{a}$ |
| | $2\mathbf{b} - \frac{6}{5} \mathbf{a}$ is not a multiple of $\frac{1}{2} \mathbf{b} - \frac{1}{5} \mathbf{a}$ therefore F, E and C are not collinear. | | 4 | A1 $\frac{5}{3} \mathbf{b} - \mathbf{a}$ is not a multiple of $\frac{1}{2} \mathbf{b} - \frac{1}{5} \mathbf{a}$ therefore F, E and C are not collinear. |
| (c) | $\overrightarrow{OG} = \mathbf{a} + m(\mathbf{b} - \mathbf{a})$ | | | M1 |
| | $\overrightarrow{OG} = \frac{1}{5} \mathbf{a} + n \left(-\frac{1}{5} \mathbf{a} + \frac{1}{2} \mathbf{b} \right)$ | | | M1 |
| | $\left(\frac{1}{5} - \frac{1}{5} n \right) = 1 - m$ or $m = \frac{1}{2} n$ | | | M1 |
| | $n = \frac{8}{3}$ or $m = \frac{4}{3}$ | | | A1 |