Write your name here		
Surname		Other names
Edexcel IGCSE	Centre Number	Candidate Number
Further Pu	ire Ma	thematics
Monday 13 June 2011 – Af Time: 2 hours	ternoon	Paper Reference 4PM0/01

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
 - there may be more space than you need.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.





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Answer all TEN questions

Write your answers in the spaces provided

You must write down all stages in your working

1	Solve	the	equations	
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$y = x^2 - 3x + 2$ $y - x = 7$	
y-x-t	(5)
 (Total for Question 1 is 5 mar	rks)



2	(a) Given that $\log_a x =$	$= \frac{\log_b x}{\log_b a} \text{ show that } \log_a b = \frac{1}{\log_b a}$	(2)
	(b) Hence solve the eq	uation	
		$\log_x 8 - 6\log_8 x = 1 \qquad x \in \mathbb{Z}^+$	(5)

Question 2 continued	
(Total for Question	on 2 is 7 marks)



3	Given that $y = e^{2x} \sin 3x$	
	(a) find $\frac{dy}{dx}$	
		(3)
	$d > 1$ $d^2 y = 2 dy$ $d^2 y = 2 dy$	
	(b) show that $\frac{d^2 y}{dx^2} = 2 \frac{dy}{dx} - 9y + 6e^{2x} \cos 3x$	(4)
		(4)

Question 3 continued	
(Tota	al for Question 3 is 7 marks)



4	$\sin(A+B) = \sin A \cos B + \cos A \sin B$ $\cos(A+B) = \cos A \cos B - \sin A \sin B$	
	(a) Write down an expression for $\sin 2A$ in terms of $\sin A$ and $\cos A$	(1)
	(b) Find an expression for $\cos 2A$ in terms of $\sin A$	(2)
	(c) Show that $\sin 3A + \sin A = 4\sin A - 4\sin^3 A$	(4)

Question 4 continued
(Total for Question 4 is 7 marks)



5

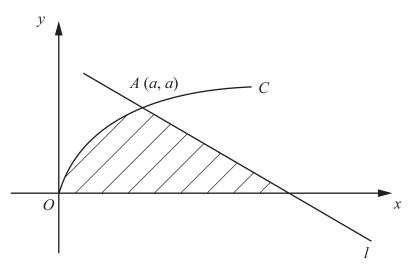


Figure 1

The curve C, with equation $y^2 = 5x$ and the line *l* intersect at the point A with coordinates (a, a), $a \ne 0$, as shown in **Figure 1**.

(a) Find the value of a.

(2)

The line *l* has gradient $-\frac{5}{7}$ and intersects the *x*-axis at the point *B*.

(b) Find the *x*-coordinate of *B*.

(3)

The shaded region is rotated through 360° about the *x*-axis.

(c) Find, in terms of π , the volume of the solid generated.

(5)

Question 5 continued	
	Total for Question 5 is 10 marks)



6	The third term of an arithmetic series is 70 and the sum of the first 10 terms of the series is 450	
	(a) Calculate the common difference of the series.	(4)
	The sum of the first n terms of the series is S_n	
	Given that $S_n \geqslant 350$	
	(b) find the set of possible values of n .	(6)
		(6)

Question 6 continued	
	Total for Question 6 is 10 marks)



7	(a) Solve	$5p^2 - 11p + 2 = 0$	
			(2)
	(b) Hence solve $5(3^{2x}) - 11(3^x) + 1$	-2 = 0 giving your answers to 3 significant figures.	(4)
	The curve with equation $y = 5(3^2 y) = 5(3$	$(2^{x}) - 6(3^{x})$ intersects the curve with equation	· /
		of these two points, giving your answers to 3 significant	nt
	and appropriate.		(4)

Question 7 continued	
	(Total for Question 7 is 10 marks)



8	The points A and B have coordinates $(1,5)$ and $(9,7)$ respectively.	
	(a) Find an equation of AB, giving your answer in the form $y = ax + b$, where a and b are rational numbers.	
		(3)
	The line l is the perpendicular bisector of AB .	
	(b) Find an equation of <i>l</i> .	(4)
	The point C has coordinates $(3,q)$. Given that C lies on l	
	(c) find the value of q .	
		(2)
	The line l meets the x -axis at the point D .	
	(d) Find the exact area of the kite <i>ACBD</i> .	(4)
		(4)

Question 8 continued



Question 8 continued



Question 8 continued	
(To	tal for Question 8 is 13 marks)



9	A curve has equation $y = \frac{2x^2 - 6}{3x - 6} \qquad x \neq 2$	
	(a) Write down an equation of the asymptote to the curve which is parallel to the <i>y</i> -axis.	(1)
	(b) Find the coordinates of the stationary points on the curve.	(7)
	The curve crosses the y -axis at the point A .	
	(c) Find an equation of the normal to the curve at A.	(3)
	The normal at A meets the curve again at B .	
	(d) Find the <i>x</i> -coordinate of <i>B</i> .	(4)



Question 9 continued	



Question 9 continued

Question 9 continued	
	Total for Question 9 is 15 marks)



10

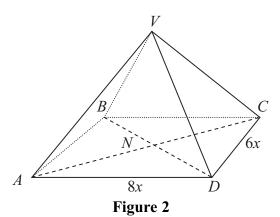


Figure 2 shows the pyramid VABCD. The base ABCD is a rectangle with CD = 6x cm and AD = 8x cm. The diagonals of the base intersect at the point N. The edges VA, VB, VC and VD are all of equal length. The angle between VA and the base ABCD is 60° .

Find, in terms of x,

(a) the height, VN, of the pyramid,

(4)

(b) the length of VA.

(3)

Find, in degrees to the nearest 0.1°,

(c) the size of the angle between the planes AVB and ABCD,

(3)

(d) the size of the angle between the planes BVD and AVC.

(3)

The volume of the pyramid is 1110 cm³.

(e) Find, to the nearest whole number, the value of x.

(3)

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Question 10 continued	



Question 10 continued	



Question 10 continued



Question 10 continued	
	(Total for Question 10 is 16 marks)
TOTAL FOR PAPER IS 100 MARKS	

