

| Question | Scheme | Marks |
|-----------------------|---|-------------------------------------|
| 7(a) | $v = t^2 - 10t + 28 = 19$ [m/s] | B1 [1] |
| (b) | $s = \int (t^2 - 10t + 28) dt = \frac{t^3}{3} - \frac{10t^2}{2} + 28t (+c)$ $24 = \frac{3^3}{3} - \frac{10 \times 3^2}{2} + 28 \times 3 + c \Rightarrow c = -24 \Rightarrow \left[s = \frac{t^3}{3} - \frac{10t^2}{2} + 28t - 24 \right]$ $t = 5, \quad s = \frac{5^3}{3} - \frac{10 \times 5^2}{2} + 28 \times 5 - 24 = \frac{98}{3} \text{ [m]}$ | M1 M1A1 M1A1 [5] |
| (c) | $\frac{dv}{dt} = 2t - 10$ when $t = 9$, acceleration = 8 [m/s ²] | M1 A1 [2] |
| (d) | (i) $v = (t - 5)^2 + 3$ Irrespective of the value of t $v \geq 3$ so the particle never comes to rest. ALT $b^2 - 4ac < 0 \Rightarrow (-10)^2 - 4 \times 1 \times 28 = -12$ No real solutions so the particle never comes to rest. (ii) Least value of v is 3 [m/s] | M1 A1 [M1 A1] B1 [3] |
| Total 11 marks | | |

| Question | Notes | Marks |
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| 7(a) | $v = t^2 - 10t + 28$ $v = 1^2 - 10 \times 1 + 28 = 19$ [m/s] | B1 [1] |
| (b) | For an attempt to integrate the given expression for v [See general guidance for the definition of an attempt] $s = \int (t^2 - 10t + 28) dt = \frac{t^3}{3} - \frac{10t^2}{2} + 28t (+c)$ | M1 |
| | For finding the value of c . They cannot score this mark without $+c$ $24 = \frac{3^3}{3} - \frac{10 \times 3^2}{2} + 28 \times 3 + c \Rightarrow c = \dots$ | M1 |
| | For the correct expression for s . This need not be explicitly stated. $s = \frac{t^3}{3} - \frac{10t^2}{2} + 28t - 24$ | A1 |

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| | Award for the correct value of c seen -24 [m] | |
| | For using their integrated expression for s to find a value of the displacement when $t = 5$ $s = \frac{5^3}{3} - \frac{10 \times 5^2}{2} + 28 \times 5 - 24 = \dots$ | M1 |
| | For the correct value of $s = \frac{98}{3}$ [m] Accept $s = 32.7$ [or better] | A1 [5] |
| (c) | For an attempt to differentiate the given v and substituting $t = 9$ into their differentiated expression. $\frac{dv}{dt} = 2t - 10 \Rightarrow \frac{dv}{dt} = 2 \times 9 - 10 = \dots$ | M1 |
| | For acceleration $= 8$ [m/s ²] | A1 [2] |
| (d)(i) | Method A Completes the square to give $v = (t - 5)^2 + 3$ | M1 |
| | Concludes that at the minimum velocity [3 m/s] $t = 5$ so P never comes to rest | A1 |
| | Method B Finds the value of the discriminant $b^2 - 4ac < 0 \Rightarrow (-10)^2 - 4 \times 1 \times 28 = -12$ | M1 |
| | Concludes that as there are no real solutions, so P does not come to rest. | A1 |
| | Method C Solves the 3TQ to give the following two [non-real] values of t : $5 + \sqrt{3}i$ and $5 - \sqrt{3}i$ or $(t - [5 + \sqrt{3}i])(t - [5 - \sqrt{3}i]) = 0$ | M1 |
| | Concludes that as there are no real solutions, so P does not come to rest. | A1 |
| | Method D Uses their result from (c) $\frac{dv}{dt} = 2t - 10 = 0 \Rightarrow t = 5$ | M1 |
| | Concludes that at the minimum velocity [3 m/s] $t = 5$ so P never comes to rest | A1 |
| (ii) | For the correct value of $v = 3$ [m/s] | B1 [3] |
| Total 11 marks | | |