

Question	Scheme	Marks
8(a)	$a + ar = 360 \quad \text{oe e.g. } \frac{a(1-r^2)}{1-r} = 360$ $ar + ar^2 = 288 \quad \text{oe}$ $r = \left\{ \frac{a(1+r)}{ar(1+r)} \right\} \frac{288}{360} = \frac{4}{5}$ $a = \frac{360}{1 + \frac{4}{5}} = 200$ $U_n = 200 \left(\frac{4}{5} \right)^{n-1} \quad *$	M1M1 (B1B1 on ePen dM1A1 M1A1 A1cso(B1 on ePen) [7]
8(a) ALT	$a + ar = 360 \quad \text{oe e.g. } \frac{a(1-r^2)}{1-r} = 360$ $ar + ar^2 = 288 \quad \text{oe}$ $a \left(\frac{360}{a} - 1 \right) + a \left(\frac{360}{a} - 1 \right)^2 = 288$ $\Rightarrow a = 200$ $r = \frac{360}{200} - 1 = \frac{4}{5}$ $U_n = 200 \left(\frac{4}{5} \right)^{n-1} \quad *$	M1M1 (B1B1 on ePen) dM1A1 M1A1 A1cso(B1 on ePen) [7]
(b)	$\{S \text{ is convergent because}\} \left \frac{4}{5} \right < 1$	B1 [1]
(c)	$S_\infty = \frac{200r}{1-r\left(\frac{4}{5}\right)} = 1000$	M1A1cao [2]
(d)	$\frac{200 \left(1 - \left(\frac{4}{5} \right)^n \right)}{1 - \left(\frac{4}{5} \right)} > 978$ $\left(\frac{4}{5} \right)^n < \frac{11}{500}$ $n \log \left(\frac{4}{5} \right) < \log \left(\frac{11}{500} \right)$ $\Rightarrow n > 17.104 \dots$ $n = 18$	M1 dM1 ddM1 A1 [4]
Total 14 marks		

Part	Mark	Notes
(a)	M1	For either correct equation. Allow use of U_1 as the first term instead of a
	M1	For both correct equations. Allow use of U_1 as the first term instead of a
	dM1	For eliminating a from their equations, reaches $r = \dots$ (Depends on previous mark)
	A1	For the correct value of r
	M1	Uses their value of r to find a value for a
	A1	For $a = 200$
	A1 cso	For the correct required expression of $U_n = 200 \left(\frac{4}{5}\right)^{n-1}$ (must have U_n)
(a)ALT	M1	For either correct equation.
	M1	For both correct equations
	dM1	For eliminating r from their equations, reaches $a = \dots$ (Depends on previous mark)
	A1	For the correct value of a
	M1	Uses their value of a to find a value for r
	A1	For the correct value of r
	A1 cso	For the correct required expression of $U_n = 200 \left(\frac{4}{5}\right)^{n-1}$ (must have U_n)
(b)	B1	For stating the correct reason, $ r < 1$ or $-1 < r < 1$ or " 0.8 " < 1 or " $\frac{4}{5}$ " < 1 Do not accept just $r < 1$ without a correct reason
(c)	M1	For using their value of A/a /first term of their geometric sequence and their r (provided their $ r < 1$) in a correct formula for the sum to infinity. $S_\infty = \frac{\text{their } A}{1 - (\text{their } r)}$
	A1cao	For the correct value of 1000
(d)	M1	Uses their a and r (their r can be $ r < 1$ or $ r > 1$) to set the correct formula for the sum of a geometric series > 978 or $= 978$ or ≥ 978 (> 978 or $= 978$ or ≥ 978 may be implied by later work.)
	dM1	Attempts to rearrange and achieves ($\text{their } r$) $^n < k$ (k is non zero positive constant) Allow strict or non-strict inequalities or equation: $<, >, \geq, \leq$ or $=$
	ddM1	For correctly takes logs (any base)/ln, and achieves a positive value for n , it maybe implied by 17.1...but not 18 ALT: trial and error to find a value of n (at least tries $n=17$ and $n=18$)
	A1	For $n = 18$ Must come from correct working, achieves $n=18$ with no incorrect inequalities in their working.

If a candidate does not score the dM1 mark but arrives at an answer of 17.1... this scores a maximum of M1 as clear use of calculator is not condoned.