

Question	Scheme	Marks
<b>3(a)</b>	$\sin\left(\frac{\theta}{2}\right) = \frac{r}{2r} \Rightarrow \frac{\theta}{2} = \frac{\pi}{6}$ $\Rightarrow \theta = \frac{\pi}{3}$ <p><b>ALT works in degrees</b></p> $\sin\left(\frac{\theta}{2}\right) = \frac{r}{2r} \Rightarrow 30^\circ$ $\Rightarrow \theta = \frac{\pi}{3}$	<p>M1</p> <p>A1 [2]</p> <p>[M1</p> <p>A1]</p>
<b>(b)</b>	<p>Area of circle = <math>\pi r^2</math></p> <p>Area of sector = <math>\frac{\frac{\pi}{3}}{2\pi} \times (3r)^2 = \frac{3}{2} \pi r^2</math></p> <p>Shaded area: <math>8\pi = \frac{3}{2} \pi r^2 - \pi r^2 = \frac{\pi r^2}{2} \Rightarrow r^2 = 16 \Rightarrow r = 4 \text{ (cm)}</math></p> <p><b>ALT works in degrees</b></p> <p>Area of circle = <math>\pi r^2</math></p> <p>Area of sector = <math>\frac{60^\circ}{360^\circ} \times \pi \times (3r)^2 = \frac{3}{2} \pi r^2</math></p> <p>Shaded area: <math>8\pi = \frac{3}{2} \pi r^2 - \pi r^2 = \frac{\pi r^2}{2} \Rightarrow r^2 = 16 \Rightarrow r = 4 \text{ (cm)}</math></p>	<p>B1</p> <p>M1</p> <p>dM1A1 [4]</p> <p>[B1</p> <p>M1</p> <p>dM1A1]</p>
<b>Total 6 marks</b>		

Part	Mark	Notes
(a)	M1	For the correct use of sine with $r$ and $2r$ to obtain $\frac{\theta}{2} = \frac{\pi}{6}$  Allow working in degrees for the M mark only. i.e $\frac{\theta}{2} = 30^\circ$  <b>Any responses not based on trigonometry are M0A0</b> If you are not sure, please send to Review
	A1	For $\theta = \frac{\pi}{3}$ <b>ONLY</b>
(b)	B1	For the correct area of the circle seen anywhere in part (b)
	M1	For using the correct formula for the area of a sector with their $\theta$  <b>provided</b> $\theta$ is within the specified range. $\left[ 0 < \theta < \frac{\pi}{2}, \quad 0 < \theta < 1.57.. \right]$  Allow working in degrees for the sector provided it is correct. Do not allow use of the radian formula for a sector with degrees.
	dM1	For subtracting the area of the circle from the area of the sector and finding a value for $r$  $r = \sqrt{\frac{8\pi}{\left(\frac{1}{2} \times (3)^2 \times \frac{\pi}{3} - \pi\right)}}$  <b>This mark is dependent on the previous M mark</b>
	A1	For $r = 4$

USEFUL SKETCH

