

Question number	Scheme	Marks
7 (a)	<p>Throughout this question condone missing degree signs</p> $\cos \theta^\circ = \frac{6^2 + 8^2 - k^2}{2 \times 6 \times 8} = \frac{100 - k^2}{96} *$	M1A1cso [2]
(b)	$\sqrt{455} = \frac{1}{2} \times 6 \times 8 \times \sin \theta^\circ$ $\Rightarrow \sin \theta^\circ = \frac{\sqrt{455}}{24} \Rightarrow \left(\sin^2 \theta^\circ = \frac{455}{576} \right)$ $\cos^2 \theta^\circ = 1 - \sin^2 \theta^\circ \Rightarrow \cos^2 \theta^\circ = 1 - \frac{455}{576} = \frac{121}{576}$ $\Rightarrow \cos \theta^\circ = \pm \frac{11}{24} \quad \text{both values required}$ $\cos \theta^\circ = \frac{11}{24} = \frac{100 - k^2}{96} \Rightarrow k^2 = 56 \Rightarrow k = \sqrt{56} = (2\sqrt{14})$ $\cos \theta^\circ = -\frac{11}{24} = \frac{100 - k^2}{96} \Rightarrow k^2 = 144 \Rightarrow k = 12$ <p>ALT</p> $\sqrt{455} = \frac{1}{2} \times 6 \times 8 \times \sin \theta^\circ$ $\Rightarrow \sin \theta^\circ = \frac{\sqrt{455}}{24}$ $\theta^\circ = \sin^{-1} \left(\frac{\sqrt{455}}{24} \right) (= 62.72 \dots^\circ)$ $\theta^\circ = 62.72 \dots, 117.27 \dots \quad \text{both values required}$ $\cos \theta^\circ = \frac{100 - k^2}{96} \Rightarrow k^2 = 100 - 96 \cos \theta^\circ$ $\Rightarrow k^2 = 100 - 96 \cos 62.72 \dots \Rightarrow k^2 = 56 \Rightarrow k = \sqrt{56}$ $\cos \theta^\circ = \frac{100 - k^2}{96} \Rightarrow k^2 = 100 - 96 \cos \theta^\circ$ $\Rightarrow k^2 = 100 - 96 \cos 117.27 \dots \Rightarrow k^2 = 144 \Rightarrow k = 12$	M1 A1 M1 A1 M1A1 A1 [7] [M1 A1 M1 A1 M1A1 A1] Total 9 marks

Part	Mark	Notes
(a)	M1	For correct substitution into the cosine rule and attempt to rearrange to find an expression for $\cos \theta^\circ$
	A1 cso	For obtaining the given expression for $\cos \theta$ $\cos \theta^\circ = \frac{100 - k^2}{96}$ <p>Note: This is a show question. There must be no errors seen.</p>

(b)	M1	For using the correct formula for area of a triangle and substitution of the given values to obtain $\sqrt{455} = \frac{1}{2} \times 6 \times 8 \times \sin \theta^\circ$ and attempt to rearrange to obtain $\sin \theta^\circ = \dots$
	A1	$\sin \theta^\circ = \frac{\sqrt{455}}{24}$ Allow for $\sin \theta = \frac{\sqrt{455}}{0.5 \times 8 \times 6}$
	M1	For use of $\sin^2 \theta + \cos^2 \theta = 1$ to obtain a value for $\cos \theta^\circ$. $\cos^2 \theta^\circ = 1 - \frac{'455'}{576} \Rightarrow \cos \theta^\circ = \pm \sqrt{1 - \frac{'455'}{576}}$ Allow use of their $\sin \theta^\circ$ provided $-1 \leq \sin \theta^\circ \leq 1$ Allow if only one value of $\cos \theta^\circ$ obtained.
	A1	$\cos \theta^\circ = \pm \frac{11}{24}$
	M1	For forming an equation for k using their $\cos \theta^\circ$ and attempt to solve for k . $\cos \theta^\circ = \frac{'11'}{24} = \frac{100-k^2}{96} \Rightarrow k^2 = 56 \Rightarrow k = \sqrt{56}$ $\cos \theta^\circ = -\frac{11'}{24} = \frac{100-k^2}{96} \Rightarrow k^2 = 144 \Rightarrow k = 12$
	A1	For one correct value of k $\sqrt{56}$ or awrt 7.48 or awrt 12
	A1	For both correct values of k $\sqrt{56}$ or awrt 7.48 and awrt 12
ALT – working with angles		
	M1	For using the correct formula for area of a triangle and substitution of the given values to obtain $\sqrt{455} = \frac{1}{2} \times 6 \times 8 \times \sin \theta^\circ$ and attempt to rearrange to obtain $\sin \theta^\circ = \dots$
	A1	$\sin \theta^\circ = \frac{\sqrt{455}}{24}$ Allow for $\sin \theta = \frac{\sqrt{455}}{0.5 \times 8 \times 6}$
	M1	For use of the inverse trigonometric function to obtain a value for θ° $\theta^\circ = 62.72 \dots, 117.27 \dots$ If working not shown then award for angle correct to a minimum of 1 d.p. Allow if only one value of θ° found. Condone working in radians awrt 1.09, awrt 2.05
	A1	$\theta^\circ = 62.72 \dots, 117.27 \dots$ Allow awrt 62.7° , 117.3° Both angles found. Condone working in radians awrt 1.09, awrt 2.05
	M1	For forming an equation in k using their θ and an attempt to solve for k . $\cos \theta^\circ = \frac{100-k^2}{96} \Rightarrow k^2 = 100 - 96 \cos \theta^\circ$ $\Rightarrow k^2 = 100 - 96 \cos 62.72 \dots \Rightarrow k^2 = 56 \Rightarrow k = \sqrt{56}$ $\cos \theta^\circ = \frac{100-k^2}{96} \Rightarrow k^2 = 100 - 96 \cos \theta^\circ$ $\Rightarrow k^2 = 100 - 96 \cos 117.27 \dots \Rightarrow k^2 = 144 \Rightarrow k = 12$
	A1	For one correct value of k $\sqrt{56}$ or awrt 7.48 or awrt 12
	A1	For both correct values of k and no others. $\sqrt{56}$ or awrt 7.48 and awrt 12