

Question number	Scheme	Marks
7 (a)	$(V =) x^3 \quad \left(\frac{dV}{dx} =\right) 3x^2 \quad (\text{at } x = 2 \quad \frac{dV}{dx} = 12)$ $\frac{dx}{dt} = 0.1$ $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt} = "12" \times 0.1 \quad \text{oe}$ $1.2 \text{ m}^3/\text{s} \text{ cao oe}$	M1 B1 (A1 on ePen) M1 A1cao (4)
(b)	$(\text{Surface Area} =) 6x^2 \quad \left(\frac{dA}{dx} =\right) 12x \quad \text{at } x = 6$ $\frac{dA}{dx} = 72$ $\frac{dV}{dx} = 108 \quad \frac{dA}{dt} = 0.05$ $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dA} \times \frac{dA}{dt} = "108" \times " \frac{1}{72} " \times 0.05$ $0.075 \text{ m}^3/\text{s}$ <u>ALT</u> $A = 6x^2 \quad \text{leading to an expression in } A \text{ for } V \quad V = \left(\frac{A}{6}\right)^{\frac{3}{2}}$ $\frac{dV}{dA} = \frac{1}{4} \left(\frac{A}{6}\right)^{\frac{1}{2}} \text{ oe}$ $\frac{dV}{dA} = \frac{3}{2} \text{ and } \frac{dA}{dt} = 0.05 \text{ oe}$ $\frac{dV}{dt} = \frac{dV}{dA} \times \frac{dA}{dt} = " \frac{3}{2} " \times 0.05$ $1.2 \text{ m}^3/\text{s} \text{ cao oe}$	M1 A1 B1 M1 A1 (5) M1 A1 B1 M1 A1cao [5] [9]

Part	Mark	Additional Guidance
(a)	M1	Correct expression for Volume, attempt at differentiation to $ax^2$ , $a$ is an integer, $a > 1$ .
	B1	$\frac{dx}{dt} = 0.1$ , can be explicit or implicitly used in a chain rule.
	M1	For <b>any correct chain rule</b> , that would lead to a value for $\frac{dV}{dt}$ and substitution of 0.1 and their value for $\frac{dV}{dx}$ . They must show an attempt to find $\frac{dV}{dx}$ , need not be a correct attempt, this isn't a dependent mark.
	A1	cao oe
(b)	M1	Correct expression for Surface Area, attempt at differentiation to $bx$ , $b$ is an integer, $b > 1$ .
	A1	$\frac{dA}{dx} = 72$
	B1	$\frac{dV}{dx} = 108$ & $\frac{dA}{dt} = 0.05$ clearly stated, implicitly in chain rule or explicitly
	M1	For <b>any correct chain rule</b> , that would lead to a value for $\frac{dV}{dt}$ and substitution of 0.05 and their values for $\frac{dA}{dx}$ and $\frac{dV}{dx}$ . They must show an attempt to find $\frac{dV}{dx}$ , need not be a correct attempt, this isn't a dependent mark.
(b) ALT	A1	cao oe
	M1	Correct expression for area, attempt to rearrange, expression for $V$ in terms of $A$
	A1	oe
	B1	Both derivatives clearly stated, implicitly in a chain rule or explicitly
	M1	For <b>any correct chain rule</b> , that would lead to a value for $\frac{dV}{dt}$ and substitution of 0.05 and their value for $\frac{dV}{dA} \cdot \frac{dA}{dt}$ doesn't need to come from correct working, but there must have been some attempt to find an expression for $V$ in terms of $A$ and $\frac{dV}{dA}$ presented somewhere in the working.
(b) ALT	A1	cao oe