

Question	Scheme	Marks
<b>3(a)</b>	$\left( y = \int (mx^2 - 10x - 37) dx = \frac{mx^3}{3} - \frac{10x^2}{2} - 37x (+c) \right)$ $\left[ \text{At } (1, 20) \right]$ $20 = \frac{m \times 1^3}{3} - \frac{10 \times 1^2}{2} - 37 \times 1 + c \left( \Rightarrow 62 = \frac{m}{3} + c \right) \quad \text{oe}$ $\left[ \text{Factor of } (x - 5) \right]$ $0 = \frac{m \times 5^3}{3} - \frac{10 \times 5^2}{2} - 37 \times 5 + c \left( \Rightarrow 310 = \frac{125m}{3} + c \right) \Rightarrow m = 6 \quad c = 60$ $\Rightarrow (g(x) =) 2x^3 - 5x^2 - 37x + 60 \quad *$	<p>M1</p> <p>dM1</p> <p>M1 M1</p> <p>A1cso [5]</p>
<b>ALT</b>	$3^{\text{rd}} \text{ and } 4^{\text{th}} \text{ method marks}$ $(x - 5) \left( \frac{m}{3} x^2 + bx + \frac{c}{5} \right) = \frac{m}{3} x^3 - 5x^2 - 37x \pm c \Rightarrow m = 6 \quad c = 60 \quad (b = 5)$	M1 M1
<b>Special case up to SC3 – mark as M1dM1M1 M0A0 in Epen</b>	<p>Differentiates the given expression for <math>g(x)</math> correctly to give <math>2(3x^2) - 5(2x) - 37 (= 6x^2 - 10x - 37)</math></p> <p>and concludes <math>m = 6</math></p> <p>Correctly substitutes <math>x = 5</math> into the given function and shows <math>g(x) = 0</math>  <math>(g(5) =) 2 \times 5^3 - 5 \times 5^2 - 37 \times 5 + 60 = 0</math></p> <p>Correctly substitutes <math>x = 1</math> into the given function and shows and <math>g(x) = 20</math>  <math>(g(1) =) 2 \times 1^3 - 5 \times 1^2 - 37 \times 1 + 60 = 20</math></p>	<p>SC1</p> <p>SC1</p> <p>SC1</p>
<b>(b)</b>	$\begin{array}{r} 2x^2 + 5x - 12 \\ x - 5 \overline{) 2x^3 - 5x^2 - 37x + 60} \end{array}$ $2x^2 + 5x - 12 = (2x - 3)(x + 4)$ $(g(x) = (x - 5)(2x - 3)(x + 4) = [0])$ $\Rightarrow x = 5, \quad \frac{3}{2}, \quad -4$	<p>M1</p> <p>M1</p> <p>A1 [3]</p>
<b>Total 8 marks</b>		

Part	Mark	Notes
(a)	M1	For a minimally acceptable attempt to integrate the given expression (see general guidance). No power of $x$ to decrease. +c is not required for this mark
	dM1	Correctly substitutes $x = 1$ and $y = 20$ to form an equation – simplification is not required Dependent on 1 <sup>st</sup> method mark. A fully correct equation with no incorrect working can imply this mark. We will be lenient on not seeing the substitution of $x = 1$ as this is trivial, so long as the resulting equation is correct from their $g(1) = 20$ . +c is not required for this mark
	M1	Uses the information correctly that $(x - 5)$ is a factor of $g(x)$ by correct substitution of $x = 5$ and $g(x) = 0$ into their $g(x)$ . Their $g(x)$ <b>must</b> be a 4 term cubic expression. A fully correct equation with no incorrect working can imply this mark – but if the equation is incorrect we must see substitution of $x = 5$ such that $g(5) = 0$ .
	M1	Uses a valid and complete method to solve their resulting simultaneous equations which must be in two variables. Allow up to 2 errors.
	A1 cso	For the correct function as shown or the correct expression. This is a show question. There must be no errors for the award of this mark.
	ALT	
(b)	3 <sup>rd</sup> M1	Uses the information correctly that $(x - 5)$ is a factor of $g(x)$ by writing a correct statement like the one shown for their $g(x)$ . Their $g(x)$ <b>must</b> be a 4 term cubic expression.
	4 <sup>th</sup> M1	Uses a valid and complete method to solve their resulting simultaneous equations in three variables. Allow up to 2 errors. It is not necessary to see the value for “ $b$ ”.
	M1	For an attempt at polynomial division or equate coefficients to reach a 3 term quotient. The minimally acceptable quotient is $2x^2 \pm 5x \pm k \quad k \neq 0$ where $k$ is a constant. In the absence of any other working, $2x^2 \pm 5x \pm k \quad k \neq 0$ may be accepted as evidence of working.
	M1	For attempting to factorise their quotient which must be of the form $2x^2 \pm 5x \pm k \quad k \neq 0$ - we must at least see a quadratic factor to factorise. See General Guidance for the definition of an attempt. It would also be possible to see a minimal attempt to use the quadratic formula or completing the square to solve (see general guidance) if their quadratic, of the form $2x^2 + 5x \pm k \quad k \neq 0$ does not factorise. If using the formula the substitution of their $a$ , $b$ and $c$ must be completely correct.
	A1	For the correct values of $x$
Candidates have clearly been directed to use algebra in the question and therefore 0 marks can be scored without seeing M1 M1		