

| Question Number | Scheme  | Marks |
|-----------------|---|-------|
| 8(a)            | $\mathbf{r} = (13\mathbf{i} + 5\mathbf{j}) + t(3\mathbf{i} - 10\mathbf{j})$   | M1 A1 |
|                 |   | (2)   |
| 8(b)            | $\mathbf{s} = (3\mathbf{i} - 5\mathbf{j}) + t(15\mathbf{i} + 14\mathbf{j})$   | M1 A1 |
|                 | $\overrightarrow{AB} = \mathbf{s} - \mathbf{r}$   | M1    |
|                 | =   |       |
|                 | $\overrightarrow{AB} = (12t - 10)\mathbf{i} + (24t - 10)\mathbf{j} \text{ km}^*$  | A1 *  |
|                 |   | (4)   |
| 8(c)            | $AB^2 = (12t - 10)^2 + (24t - 10)^2 \quad (720t^2 - 720t + 200)$  | M1    |
|                 | Differentiate and equate to 0 <b>OR</b> Complete square <b>OR</b> use $t = \frac{-b}{2a}$   | M1    |
|                 | $1440t - 720 = 0$ oe $720(t - \frac{1}{2})^2 + 20$  | A1    |
|                 | Solve for $t$ Use $(t - \frac{1}{2})^2 \geq 0$ $t = \frac{720}{2 \times 720}$   | DM1   |
|                 | Substitute their value of $t$ into their $AB$ expression  | M1    |
|                 | $\sqrt{20}$ oe (km) 4.5 or better   | A1    |
|                 |   |       |
|                 | <b>OR for last 5 marks:</b>   |       |
|                 | Complete method   | M1    |
|                 | $720t^2 - 720t + 200 = D^2$ i.e. $720t^2 - 720t + 200 - D^2 = 0$  | A1    |
|                 | (For real $t$ , $720^2 \geq 4 \times 720(200 - D^2)$ )  | DM1   |
|                 | Solve for $D$ , ( $D \geq \sqrt{20}$ )  | M1    |
|                 | $\sqrt{20}$ oe (km) 4.5 or better   | A1    |
|                 |   | (6)   |
| 8(d)            | Use $\overrightarrow{AB} = -4\mathbf{i} + 2\mathbf{j}$ at $t = \frac{1}{2}$ to obtain a relevant angle e.g. $26.56^\circ$ ..<br>Allow e.g. $\tan \alpha = \frac{1}{2}$ or $\tan^{-1} \frac{1}{2}$ | M1    |
|                 | Bearing is $297^\circ$ or better  | A1    |
|                 |   | (2)   |
|                 |   | (14)  |
|                 | <b>Notes for question 8</b>   |       |
|                 | Accept column vectors through out apart from the answer for (b)   |       |
| 8(a)            | M1 Expression with correct structure  |       |
|                 | A1 cao  |       |
| 8(b)            | M1 Expression with correct structure  |       |
|                 | A1 cao  |       |
|                 | M1 Allow difference in either order   |       |
|                 | A1* Correct given expression correctly obtained<br><b>N.B.</b> $\overrightarrow{AB} = (-10 + 12t)\mathbf{i} + (-10 + 24t)\mathbf{j}$ is A0  |       |
| 8(c)            | M1 Correct expression (with or without square root)   |       |
|                 | M1 Attempt to differentiate (at least one power decreasing by 1) or to complete the square  |       |
|                 | A1 Correct equation or expression   |       |
|                 | DM1 Dependent on previous M for finding the critical value for $t$<br><b>OR</b> For the completing the square method, for 'ignoring' the $(t - \frac{1}{2})^2$ term.                              |       |