

| Question number | Scheme | Marks |
|-----------------|--|-------------------------------------|
| 4 (a) | $2 = 4 \sin 2t \Rightarrow \sin 2t = 0.5 \Rightarrow 2t = \frac{\pi}{6} \Rightarrow t = \frac{\pi}{12} \quad [\approx 0.26179\dots]$ | M1A1 (2) |
| (b) | $a = \frac{dv}{dt} = 8 \cos 2t \Rightarrow a = 8 \cos \left(2 \times \frac{\pi}{12} \right) = 4\sqrt{3} \quad (6.928\dots) \text{ (m/s}^2\text{)}$ | M1dM1 A1cao (3) |
| (c) | $s = \int 4 \sin 2t \, dt = -2 \cos 2t \quad (+c)$ $t = \frac{\pi}{4} \Rightarrow 3 = -2 \cos \frac{\pi}{2} + c \Rightarrow c = 3$ $s = 3 - 2 \cos 0 \Rightarrow s = 3 - 2 = 1 \text{ (m)}$ | M1A1 dM1 A1cao (4) [9] |
| (a) | | |
| M1 | Equate v to 2 and solve the equation by any valid method to obtain at least one value of t (not nec the least, but must be radians) Allow degrees only if then changed to radians. | |
| A1 | Correct, least value. Can be exact or decimal – 3 sf minimum | |
| (b) | | |
| M1 | Differentiate v . $4 \sin 2t \rightarrow k \cos 2t$, $k = \pm 8$ or ± 4 | |
| dM1 | Substitute their answer from (a) and obtain a positive value for a . Depends on the previous M mark OR: use $\cos 2x = \sqrt{1 - \sin^2 2x}$ with their value for $\sin 2x$ from (a) | |
| A1cao | $4\sqrt{3}$ or 6.928... 6.93 (3 sf minimum) Allow all marks here if their answer from (a) is in degrees | |
| (c) | | |
| M1 | Integrate v . $4 \sin 2t \rightarrow k \cos 2t$, $k = \pm 2, \pm 4$. If definite integration ignore limits here. | |
| A1 | Correct integration, constant (or limits) not needed | |
| dM1 | Substitute $t = \frac{\pi}{4}$ and $s = 3$ to obtain the value of c Definite integration: Substitute correct limits $t = 0, \frac{\pi}{4}$ and $s = 3$ Depends on the previous M mark. | |
| A1cao | $s = 1 \text{ (m)}$ | |