

Question number	Scheme	Marks
7(a)	$\frac{27^{(x+2)} - 3^{(3x+5)}}{3^x \times 9^{(x+2)}} = \frac{3^{3(x+2)} - 3^{(3x+5)}}{3^x \times 3^{2(x+2)}}$ $= \frac{3^{(3x+6)} - 3^{(3x+5)}}{3^x \times 3^{(2x+4)}} = \frac{3^{3x} \times 3^6 - 3^{3x} \times 3^5}{3^{3x} \times 3^4}, = \frac{3^{3x}(3^6 - 3^5)}{3^{3x} \times 3^4}, \left(= \frac{486}{81} \right) = 6$ <p>ALTs for last 3 marks</p> $= \frac{3^{(3x+6)} - 3^{(3x+5)}}{3^x \times 3^{(2x+4)}} = \frac{3^{3x} \times 3^6 - 3^{3x} \times 3^5}{3^{3x} \times 3^4}, = \frac{3^{3x}(3^6 - 3^5)}{3^{3x} \times 3^4} = \frac{3^5(3-1)}{3^4}, = 6$	M1A1 dM1,ddM1,A1 (5)
ALT 1		
(b)	$\log_y 2 = \frac{\log_2 2}{\log_2 y} = \frac{1}{\log_2 y} \quad \text{or} \quad \log_2 y = \frac{\log_y y}{\log_y 2} = \frac{1}{\log_y 2}$ <p>Forming 3TQ:</p> $2 \log_2 y + \frac{3}{\log_2 y} = 7 \Rightarrow 2(\log_2 y)^2 + 3 = 7 \log_2 y$ $2(\log_2 y)^2 - 7 \log_2 y + 3 = 0 \quad \text{OR} \quad 2 - 7 \log_y 2 + 3(\log_y 2)^2 = 0$ <p>(Let $A = \log_2 y$)</p> $2A^2 - 7A + 3 = 0 \Rightarrow (2A-1)(A-3) = 0 \Rightarrow A = \frac{1}{2}, 3$ $\log_2 y = \frac{1}{2} \Rightarrow y = 2^{\frac{1}{2}} (= \sqrt{2}) \quad \log_2 y = 3 \Rightarrow y = 2^3 = 8$	M1 dM1 ddM1A1 A1A1 (6) [11]

(a)**M1** Attempt to change power of 9 or 27 to a power of 3**A1** Correct unsimplified expression with powers of 3 alone**dM1** Expand brackets in the powers and write with all powers as single terms, depends on first M mark**ddM1** Remove common factor in numerator, depends on both previous M marks**A1** Correct value of k obtained (need not be written explicitly as $k = 6$)**(b)****M1** Change base. Can change to base 2 or base y or both terms to any other (same) base**dM1** Obtain a 3TQ Depends on the first M mark. Term can be in any order but must be 3 separate terms.**ddM1** Solve their 3TQ. Substitution shown not needed. Depends on both previous M marks.**A1** Correct values for $\log_2 y$ or A OR $\log_y 2$ **A1** One correct value for y **A1** Second correct value for y