

Question Number	Scheme	Marks
9		
(a)	$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$ $\cos 2\theta = \cos^2 \theta - (1 - \cos^2 \theta)$ $\cos^2 \theta = \frac{1}{2}(\cos 2\theta + 1) \quad (*)$	M1 A1 cso (2)
(b)	$f(\theta) = 8\left(\frac{1}{2}(\cos 2\theta + 1)\right)^2 + 4 \times \frac{1}{2}(\cos 2\theta + 1) - 5$ $= 2(\cos^2 2\theta + 2\cos 2\theta + 1) + 2\cos 2\theta + 2 - 5$ $= 2 \times \frac{1}{2}(\cos 4\theta + 1) + 4\cos 2\theta + 2\cos 2\theta - 1$ $= \cos 4\theta + 6\cos 2\theta \quad (*)$	M1 M1 M1 A1 cso (4)
(c)	$8\cos^4 x + 4\cos^2 x - 5 - 6\cos 2x = -0.5$ $\cos 4x + 6\cos 2x - 6\cos 2x = -0.5$ $\cos 4x = -0.5$ $4x = 120, 240, 480, 600$ $x = 30, 60, 120, 150$	M1 A1 M1 A1 (4)
(d)(i)	$\int f(\theta) d\theta = \int (\cos 4\theta + 6\cos 2\theta) d\theta$ $= \frac{1}{4}\sin 4\theta + 3\sin 2\theta (+c)$	M1 A1
(ii)	$\int_0^{\frac{\pi}{3}} f(\theta) d\theta = \frac{1}{4}\sin \frac{4\pi}{3} + 3\sin \frac{2\pi}{3}$ $-\frac{1}{4} \times \frac{\sqrt{3}}{2} + 3 \times \frac{\sqrt{3}}{2}, = \frac{11\sqrt{3}}{8}$	M1 A1,A1 (5)
		[15]