

Question Number	Scheme	Marks
<b>6</b>	<p>(a)</p> <p>At time <math>t</math>, <math>\text{vol} = \frac{1}{3}\pi(h \tan 30)^2 h, = \frac{1}{9}\pi h^3</math></p> <p><math>t = 0 \text{ vol} = \frac{1000\pi}{9}</math></p> <p><math>\frac{1000\pi}{9} - 2t = \frac{1}{9}\pi h^3</math></p> <p><math>h^3 = 1000 - \frac{18t}{\pi}</math></p> <p><math>h = \sqrt[3]{\left(1000 - \frac{18t}{\pi}\right)} \quad *</math></p> <p>(b)</p> <p><math>A = \pi r^2 = \pi(h \tan 30)^2 = \frac{\pi h^2}{3}</math></p> <p><math>\frac{dA}{dh} = \frac{2\pi h}{3}</math></p> <p><math>\frac{dA}{dt} = \frac{dA}{dh} \times \frac{dh}{dt} = \frac{2\pi h}{3} \times \frac{dh}{dt}</math></p> <p><math>h = \left(1000 - \frac{18t}{\pi}\right)^{\frac{1}{3}}</math></p> <p><math>\frac{dh}{dt} = \frac{1}{3} \left(1000 - \frac{18t}{\pi}\right)^{-\frac{2}{3}} \times -\frac{18}{\pi}</math></p> <p><math>\frac{dA}{dt} = -\frac{2\pi}{3} \times \left(1000 - \frac{18t}{\pi}\right)^{\frac{1}{3}} \times \frac{1}{3} \left(1000 - \frac{18t}{\pi}\right)^{-\frac{2}{3}} \times \left(-\frac{18}{\pi}\right)</math></p> <p><math>t = 15 \quad \frac{dA}{dt} = -\frac{2\pi}{3} \times \frac{1}{3} \times \frac{18}{\pi} \times \frac{1}{\left(1000 - \frac{18 \times 15}{\pi}\right)^{\frac{1}{3}}}</math></p> <p><math>= -0.412 \text{ cm}^2/\text{s}</math></p>	<p>M1,A1</p> <p>B1</p> <p>M1</p> <p>M1A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>

Question Number	Scheme	Marks
7	<p>(a)</p> $\text{Grad } AB = \frac{8-5}{7-3} = \frac{3}{4}$ $\text{Grad } AC = \frac{1-5}{6-3} = -\frac{4}{3}$ $\frac{3}{4} \times -\frac{4}{3} = -1$ $(\therefore AB \perp AC)$ <p>(b)</p> $\text{Eqn } AC: y - 5 = -\frac{4}{3}(x - 3)$ $3y + 4x - 27 = 0 \quad (\text{o.e. but must be integers})$ <p>(c) <math>D</math> is <math>(12, -7)</math></p> <p>(d)</p> $\text{Length } AD = \sqrt{((12-3)^2 + (-7-5)^2)}, \quad = 15$ $\text{Length } AB = \sqrt{((7-3)^2 + (8-5)^2)}, \quad = 5$ $\text{Area } \triangle ABD = \frac{1}{2} \times 15 \times 5 = 37\frac{1}{2} \text{ sq.units}$	<p>M1A1</p> <p>A1</p> <p>A1 cso</p> <p>M1A1ft</p> <p>A1</p> <p>B1B1</p> <p>M1,A1</p> <p>A1</p> <p>A1ft</p>