

| Question | Scheme | Marks |
|-----------------------|---|-------------------------------|
| 9(a) | $AC = \sqrt{12^2 + 12^2} = \sqrt{288} = 12\sqrt{2}$ | M1A1 [2] |
| (b) | $x = \frac{12\sqrt{2}}{\cos 30^\circ} = \sqrt{96} = (4\sqrt{6})^*$ | M1A1 cso [2] |
| (c) | $\cos \angle AOB = \frac{96 + 96 - 12^2}{2 \times \sqrt{96} \times \sqrt{96}} \Rightarrow \angle AOB = 75.522\dots^\circ$ $\text{Area } \triangle OAB = \frac{1}{2} \times \sqrt{96} \times \sqrt{96} \times \sin 75.522^\circ = (46.4758\dots)$ $4 \times 46.4758 + 12^2 = 329.90\dots \Rightarrow \text{Area} = 330 \text{ [m}^2\text{]}$ | M1A1 M1 M1A1 [5] |
| (d) | $\left[\angle OBC = \frac{180 - 75.522}{2} = 52.239^\circ \right]$ Let Y on OB be the foot of the perpendicular from A to OB $AY = 12 \sin 52.239^\circ = (9.4868\dots)$ $\cos \angle AYC = \frac{9.4868^2 + 9.4868^2 - 288}{2 \times 9.4868 \times 9.4868} \Rightarrow \angle AYC = 126.87\dots \approx 127^{[o]}$ | M1 A1 M1A1 [4] |
| Total 13 marks | | |

| Question | Notes | Marks |
|----------|---|-----------|
| 9(a) | For using Pythagoras theorem on triangle ABC or triangle ADC $AC = \sqrt{12^2 + 12^2} = \dots$ | M1 |
| | For the correct value of AC $AC = \sqrt{288} = 12\sqrt{2}$ | A1 [2] |
| (b) | Let the intersection of AC and BD be X Uses any appropriate trigonometry on triangle OAX $\frac{12\sqrt{2}}{\cos 30^\circ}$ For example; $x = \frac{12\sqrt{2}}{\cos 30^\circ} = \dots$ OR $\frac{\sin 120^\circ}{12\sqrt{2}} = \frac{\sin 30^\circ}{OA} \Rightarrow OA = \dots$ OR $(12\sqrt{2})^2 = x^2 + x^2 - 2 \times x \times x \cos 120 \Rightarrow x = \dots$ | M1 |
| | For the correct value of x | A1 cso |

| | | |
|-----|---|----------------|
| | $x = \sqrt{96} = (4\sqrt{6})^*$ | [2] |
| (c) | For using trigonometry to find angle $\angle AOB$ $\cos \angle AOB = \frac{96+96-12^2}{2 \times \sqrt{96} \times \sqrt{96}} = \dots$ | M1 |
| | $\angle AOB = 75.522\dots^\circ$ | A1 |
| | Area of triangle OAB $\text{Area} = \frac{1}{2} \times \sqrt{96} \times \sqrt{96} \times \sin 75.522^\circ = (46.4758\dots)$ | M1 |
| | Total area of the pyramid = $4 \times 46.4758 + 12^2 = (329.90\dots)$ | M1 |
| | For the correct final area = awrt 330 (cm ²) | A1 [5] |
| | ALT | |
| | Height of the triangle of one of the triangular faces: $h = \sqrt{(4\sqrt{6})^2 - 6^2} = \dots$ | M1 |
| | $h = 2\sqrt{15}$ | A1 |
| | Area of triangle $OAB = \frac{1}{2} \times 2\sqrt{15} \times 12 = 12\sqrt{15} = (46.4758\dots)$ | M1 |
| | Total area of the pyramid = $4 \times 12\sqrt{15} + 144 = (329.903\dots)$ | M1 |
| | For the correct final area = awrt 330 (cm ²) Allow an exact answer of $48\sqrt{15} + 144$ (cm) ² oe | A1 |
| (d) | $\cos \angle AOB = \frac{96+96-12^2}{2 \times \sqrt{96} \times \sqrt{96}} = 75.522^\circ$ or $\angle OBC = \frac{180^\circ - 75.522^\circ}{2} = 52.239^\circ$ | |
| | Let Y on OB be the foot of the perpendicular from A to OB Length $AY = 12 \sin 52.239^\circ = (9.4868\dots)$ OR Length $AY = 4\sqrt{6} \sin 75.522^\circ = (9.4868\dots)$ | M1A1 [M1A1] |
| | For the appropriate trigonometry on triangle AYC to find angle AYC $\cos \angle AYC = \frac{9.4868^2 + 9.4868^2 - 288}{2 \times 9.4868 \times 9.4868} \Rightarrow (\angle AYC = 126.87)$ | M1 |
| | Angle between plane AOB and plane OBC = awrt 127[°] | A1 [4] |
| | Total 13 marks | |