

Question number	Scheme	Marks
3	<p>Let l be the length. $\frac{dl}{dt} = 0.005$</p> <p>$l = 10x \Rightarrow \frac{dl}{dx} = 10$ or $\frac{dl}{dt} = 10 \frac{dx}{dt} = 0.005 \Rightarrow \frac{dx}{dt} = 0.0005$</p> <p>$r = \frac{x}{2}, \quad V = \pi \left(\frac{x}{2} \right)^2 \times 10x \Rightarrow V = \frac{5\pi x^3}{2}$</p> <p>$\frac{dV}{dx} = \frac{15\pi x^2}{2}$</p> <p>$\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt} \times \frac{dl}{dt}$ or $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt}$</p> <p>$\frac{dV}{dt} = \frac{15\pi \times 3^2}{2} \times \frac{1}{10} \times 0.005$ or $\frac{dV}{dt} = \frac{15\pi \times 3^2}{2} \times 0.0005$</p> <p>$= 0.106028\dots$</p> <p>$\frac{dV}{dt} \approx 0.11 \text{ (cm}^3/\text{s)}$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>dM1</p> <p>A1 [6]</p>
Alternative		
	<p>$x = \frac{l}{10}$ or $r = \frac{l}{20}$ stated or used</p> <p>$V = \pi \left(\frac{l}{20} \right)^2 \times l = \frac{\pi l^3}{400}$</p> <p>$\frac{dV}{dl} = \frac{3\pi l^2}{400}$</p> <p>$\frac{dV}{dt} = \frac{dV}{dl} \times \frac{dl}{dt}$</p> <p>$\frac{dV}{dt} = \frac{3\pi \times 30^2}{400} \times 0.005 = 0.106028\dots$</p> <p>$\frac{dV}{dt} \approx 0.11 \text{ (cm}^3/\text{s)}$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>dM1</p> <p>A1 [6]</p>
Total 6 marks		

<p>Apart from x, which is defined in the question, different variables may be used providing that they are consistent throughout the working.</p> <p>Score the best mark using either alternative but not a mixture of both.</p>		
	B1	$\frac{dl}{dx} = 10$ or $\frac{dx}{dt} = 0.0005$
	B1	<p>Correct expression for the volume of the cylinder. Simplification not needed.</p> <p>Brackets for $\left(\frac{x}{2}\right)^2$ are required unless implied by subsequent working.</p>
	M1	<p>Attempt to differentiate to find $\frac{dV}{dx}$. You need to see a multiple of x^2 from differentiating x^3. ft their V if it is a multiple of x^3.</p> <p>Mark the differentiation and ignore any error in the label, $\frac{dV}{dx}$, for this mark only.</p>
	M1	State, or use correctly, the chain rule $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dl} \times \frac{dl}{dt}$ or $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt}$
	dM1	<p>Substitute to find a numerical expression for $\frac{dV}{dt}$ dep on both M marks.</p> <p>ft their $\frac{dV}{dx}, \frac{dl}{dx}, \frac{dx}{dt}$ if clearly stated.</p>
	A1	$\frac{dV}{dt} \approx 0.11$ given to 2SF

Alternative		
	B1	$x = \frac{l}{10}$ or $r = \frac{l}{20}$ stated or used
	B1	<p>Correct expression for the volume of the cylinder. Simplification not needed.</p> <p>Brackets for $\left(\frac{l}{20}\right)^2$ are required unless implied by subsequent working.</p>
	M1	<p>Attempt to differentiate to find $\frac{dV}{dl}$. You need to see a multiple of l^2 from differentiating l^3. ft their V if it is a multiple of l^3.</p> <p>Mark the differentiation and ignore any error in the label, $\frac{dV}{dl}$, for this mark only.</p>
	M1	State, or use correctly, the chain rule $\frac{dV}{dt} = \frac{dV}{dl} \times \frac{dl}{dt}$
	dM1	<p>Substitute to find a numerical expression for $\frac{dV}{dt}$ dep on both M marks.</p> <p>ft their $\frac{dV}{dl}$ if clearly stated.</p>
	A1	$\frac{dV}{dt} \approx 0.11$ given to 2SF