| Question | Scheme | Marks | | | |
|-----------|--|-------------|--|--|--|
| 9 (a) | $\left(1 - 2x\right)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-2x\right)^{2} + \left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\left(-2x\right)^{3}$ | | | | |
| | $(1-2x)^2 = 1 + \left(-\frac{1}{2}x - 2x\right) + \frac{1}{2!} + \frac{1}{3!}$ | M1 | | | |
| | Scheme $(1-2x)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2} \times -2x\right) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-2x\right)^{2}}{2!} + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\left(-2x\right)^{3}}{3!} + \dots$ $(1-2x)^{-\frac{1}{2}} = 1 + x + \frac{3}{2}x^{2} + \frac{5}{2}x^{3} + \dots$ | A1A1 [3] | | | |
| <u> </u> | | | | | |
| (b) | $\frac{1}{\sqrt{0.96}} = \frac{1}{\sqrt{\frac{96}{100}}} = \frac{10}{4\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \dots$ | M1 | | | |
| | ¥ 100 | A1 | | | |
| | $\frac{10\sqrt{6}}{4\times 6} = \frac{5\sqrt{6}}{12} *$ | cso | | | |
| | $\frac{1}{4\times 6} = \frac{1}{12}$ | [2] | | | |
| ALT – cor | ALT – confirming given result | | | | |
| | $\frac{1}{\sqrt{0.96}} = \frac{5\sqrt{6}}{12} \Rightarrow 12 = \sqrt{0.96} \times 5\sqrt{6}$ | [M1 | | | |
| | V0.70 12 | A1cso] | | | |
| | $12^2 = 0.96 \left(5\sqrt{6}\right)^2 = 0.96 \times 5^2 \times 6 *$ | 111688] | | | |
| (c) | $\frac{1}{\left(5\sqrt{6}-12\right)} \times \frac{\left(5\sqrt{6}+12\right)}{\left(5\sqrt{6}+12\right)}$ | | | | |
| | $\left(5\sqrt{6}-12\right)^{2}\left(5\sqrt{6}+12\right)$ | M1 | | | |
| | $=\frac{5\sqrt{6}+12}{150-12^2}=\frac{5\sqrt{6}+12}{6}=\frac{5\sqrt{6}}{6}+2$ | A1 | | | |
| | $=\frac{150-12^2}{6}=\frac{6}{6}=\frac{6}{6}+2$ | [2] | | | |
| (d) | $1 - 2x = 0.96 \Rightarrow 2x = 0.04 \Rightarrow x = 0.02$ | B1 | | | |
| | $\frac{9}{5\sqrt{6}-12} = 9\left(2 \times \left[\frac{5\sqrt{6}}{12}\right] + 2\right) =: 9 \times \left[2\left(1 + 0.02 + \frac{3}{2} \times 0.02^2 + \frac{5}{2} \times 0.02^3\right) + 2\right] = \dots$ | M1:M1 | | | |
| | 36.37116 | A1 [4] | | | |
| | 30.5/110 | [+] | | | |
| | Total 11 marks | | | | |

| Part | Mark | Notes |
|------|-----------|---|
| (a) | M1 | For an attempt to use the Binomial Expansion |
| | | The minimally acceptable attempt is as follows; |
| | | • The power of x must be correct in each term. $[x, x^2 \text{ and } x^3]$ |
| | | • The first term is 1 |
| | | The denominators are correct |
| | | • –2x correct in each term |
| | | $(1-2x)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2} \times -2x\right) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-2x\right)^2}{2!} + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\left(-2x\right)^3}{3!} + \dots$ |
| | | |
| | A1 | The first term and one algebraic term correct and simplified |

| | | $\left(1-2x\right)^{-\frac{1}{2}} = 1 + x + \frac{3}{2}x^2 + \frac{5}{2}x^3 + \dots$ | | |
|-------------------------------|------------|---|--|--|
| | A1 | Fully correct simplified expansion as shown above. | | |
| (b) | M1 | For changing 0.96 to $\frac{96}{100}$ or equivalent fraction and attempting to multiply numerator | | |
| | | and denominator by either $\sqrt{6}$ (or $\sqrt{96}$) | | |
| | | $\frac{1}{\sqrt{0.96}} = \frac{1}{\sqrt{\frac{96}{100}}} = \frac{10}{4\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \dots$ | | |
| | A1 cso | For the correct answer as shown with no errors $\frac{10\sqrt{6}}{4\times6} = \frac{5\sqrt{6}}{12}$ * | | |
| ALT – confirming given result | | | | |
| | M1 | For rearranging and squaring OR for squaring on both sides | | |
| | A1 cso | For showing that the two sides of the result are equal | | |
| | | $12^2 = 0.96 \left(5\sqrt{6}\right)^2 = 0.96 \times 5^2 \times 6 = 144$ | | |
| (c) | M1 | For myltinking nymouster and denominator by 5 /6 + 12 | | |
| (c) | IVII | For multiplying numerator and denominator by $5\sqrt{6} + 12$ | | |
| | | $\frac{1}{\left(5\sqrt{6}-12\right)} \times \frac{\left(5\sqrt{6}+12\right)}{\left(5\sqrt{6}+12\right)}$ [Can be implied by $\frac{\left(5\sqrt{6}+12\right)}{\left(150-12^2\right)}$ seen] | | |
| | A1 | For a correct expansion of brackets throughout. | | |
| | | $\frac{1}{(5\sqrt{6}-12)} \times \frac{(5\sqrt{6}+12)}{(5\sqrt{6}+12)} \left[= \frac{5\sqrt{6}+12}{150-12^2} = \right] \frac{5\sqrt{6}+12}{6} = \frac{5\sqrt{6}}{6} + 2$ | | |
| (d) | B 1 | For finding the required value of <i>x</i> | | |
| | 3.54 | $1 - 2x = 0.96 \Rightarrow 2x = 0.04 \Rightarrow x = 0.02$ | | |
| | M1 | For substituting their value of x provided it is $-\frac{1}{2} < x < \frac{1}{2}$ into the expansion as follows: | | |
| | | $\frac{9}{5\sqrt{6}-12} = 9\left(2 \times \left[\frac{5\sqrt{6}}{12}\right] + 2\right) =$ | | |
| | | Note: Must show substitution if <i>x</i> is incorrect. | | |
| | M 1 | For substituting their expansion for $\frac{5\sqrt{6}}{12}$ | | |
| | | $9 \times \left[2\left(1 + 0.02 + \frac{3}{2} \times 0.02^2 + \frac{5}{2} \times 0.02^3\right) + 2\right] = \cdots$ | | |
| | A1 | For the value of 36.37116 [The calculator value is 36.37117] | | |