

Question Number	Scheme	Marks
<b>5(a)</b>	$V = x \times 4x \times h = 772$ $h = \frac{193}{x^2} = \frac{772}{4x^2}$ $A = 2 \times 4x^2 + 2xh + 2 \times 4xh = 8x^2 + 10xh$ $A = 8x^2 + 10x \times \frac{193}{x^2} = 8x^2 + \frac{1930}{x} \quad *$	<b>B1</b>  <b>M1A1cso (3)</b>
<b>(b)</b>	$(A =) 8x^2 + 1930x^{-1}$ $\left(\frac{dA}{dx} =\right) 16x - 1930x^{-2}$ $\left(\frac{dA}{dx} = 0 \Rightarrow\right) 16x = \frac{1930}{x^2}$ $x^3 = \frac{1930}{16} \quad x = 4.9409... = 4.94$ $\left(\frac{d^2A}{dx^2} =\right) 16 + 3860x^{-3}$ $x = 4.94 \Rightarrow \frac{d^2A}{dx^2} > 0 \quad \therefore \text{minimum}$	<b>M1</b>  <b>dM1</b>  <b>A1</b>  <b>M1</b>  <b>A1ft (5)</b>
<b>(c)</b>	$A_{\min} = 8 \times 4.940...^2 + \frac{1930}{4.940...} = 585.9..., = 586$	<b>M1,A1cao (2)</b>  <b>[10]</b>
<b>(a)B1</b> <b>M1</b> <b>A1cso</b> <b>(b)</b> <b>M1</b> <b>dM1</b> <b>A1</b> <b>M1</b> <b>A1ft</b>  <b>ALTs</b>  <b>(c)</b> <b>M1</b> <b>A1cao</b>	$h = \frac{193}{x^2}$ or $\frac{772}{4x^2}$ or $xh = \frac{193}{x}$ oe Seen explicitly or used in the expression for A Form an expression for A in terms of x and h which must be dimensionally correct and replace h with a function of x Obtain the given expression for A. No errors seen. Must start A = ... or area = ... Differentiate the GIVEN expression for A Equate their derivative to 0. Dependent on the previous M mark. $x = 4.94$ Must be 3 sf <b>Special Case:</b> 4.94 with no working (calculator solution) scores M1M1A1 Attempt the second derivative - must have 2 terms. Deduce that their value of x gives a minimum, follow through their x. No need to evaluate the derivative provided the value of x is positive and the derivative is algebraically correct. Must have a conclusion. For last 2 marks: Look at signs of $\frac{dA}{dx}$ either side of $x = 4.94$ <b>and</b> calculate the values of $\frac{dA}{dx}$ (M1) All correct with conclusion (A1) or refer to the graph - sketch must be shown. Use their value of x in the given expression for A and complete to A = ... 586 Must be 3sf unless rounding already penalised in (b)	