

Question number	Scheme	Marks
8 (a)	$BN = 10 \cos 60^\circ$ $= 5 \text{ (cm)}^*$	M1 A1cso [2]
(b)	$FN^2 = 10^2 - 5^2 = 75$ or $FN = 10 \sin 60 = 5\sqrt{3}$ or $FN = 5 \tan 60$ $NE = \sqrt{12^2 + 75} = 14.7986... \approx 14.8 \text{ (cm)}$	M1 M1A1 [3]
(c)	Let $R$ be the midpoint of $FN$ and $P$ be the point on $AD$ that corresponds to point $N$ on $BC$ . $\angle RPN = \tan^{-1} \left( \frac{\frac{\sqrt{75}}{2}}{12} \right) = 19.84167...^\circ \approx 19.8^\circ$	M1A1 [2]
(d)	Let the perpendicular from $Y$ to line $BC$ meet $BC$ at $Z$ $AY = \sqrt{AZ^2 + ZY^2} = \sqrt{12^2 + 6.5^2 + \left( \frac{\sqrt{75}}{2} \right)^2} = \sqrt{205}$ $FC = \sqrt{FN^2 + NC^2} = \sqrt{75 + 3^2} = \sqrt{84} \Rightarrow FY = \sqrt{21}$ So $EY = \sqrt{12^2 + 21} = \sqrt{165}$ $\angle AYE = \cos^{-1} \left( \frac{205 + 165 - 100}{2 \times \sqrt{205} \times \sqrt{165}} \right) = 42.7745...^\circ \approx 42.8^\circ$	M1A1 M1 M1 M1A1 [6]
<b>Total 13 marks</b>		

(a)	M1	Use cosine or sine in triangle $BNF$ , or any complete method. $BN = 10 \cos 60^\circ$ or $\cos 60^\circ = \frac{BN}{10}$ or $\frac{BN}{\sin 30} = \frac{10}{\sin 90}$ or $BN = 10 \sin 30$ or $FN = 10 \sin 60 = 5\sqrt{3}$ and $BN^2 = 10^2 - (5\sqrt{3})^2$ (may use any single letter instead of $BN$ )
	A1 cso	$BN = 5 \text{ (cm)}$ Correct answer from correct working. (Answer given.) Must show a calculation in the form $BN = \dots$ e.g. $BN = 10 \cos 60$
(b)	M1	Use Pythag or trig to find a numerical expression for $FN$ or $FN^2$ eg $FN^2 = 10^2 - 5^2 (= 75)$ or $FN = 10 \sin 60 (= 5\sqrt{3} = 8.66...)$ or $FN = 5 \tan 60$
	M1	Use Pythag with their $FN$ to find a numerical expression for $NE$ , eg $NE = \sqrt{12^2 + (5\sqrt{3})^2} (= \sqrt{219})$
	A1	$NE = 14.8 \text{ (cm)}$ <b>given to 3SF.</b>
(c)	M1	Use tangent with their $FN$ , eg $\tan RPN = \left( \frac{\frac{1}{2}\sqrt{75}}{12} \right)$ or any complete method.
	A1	$19.8^\circ$ <b>given to 1DP.</b>

(d)	M1	Complete method to find $AY$ eg $AY = \sqrt{(12^2 + 6.5^2) + \left(\frac{\sqrt{75}}{2}\right)^2} (= \sqrt{205} = 14.31\dots)$ (allow their $FN$ )
	A1	$AY = \sqrt{205} (= 14.31\dots)$ (may be implied by subsequent working)
	M1	Complete method to find $FY$ eg $FC = \sqrt{75 + 3^2} (= \sqrt{84}) \Rightarrow FY = \frac{1}{2}\sqrt{84} (= \sqrt{21})$ (allow their $FN$ ) eg $FC = \sqrt{8^2 + 10^2 - 2 \times 8 \times 10 \cos 60} (= \sqrt{84}) \Rightarrow FY = \frac{1}{2}\sqrt{84} (= \sqrt{21} = 4.58\dots)$
	M1	Method to find $EY$ using their $FY$ (correct or from a correct method) eg $EY = \sqrt{12^2 + 21} (= \sqrt{165} = 12.84\dots)$
	M1	Substitute their values for $AY$ and $EY$ into the cosine rule used in triangle $AYE$ . $\cos AYE = \left( \frac{205 + 165 - 100}{2 \times \sqrt{205} \times \sqrt{165}} \right)$ oe
	A1	$\angle AYE = 42.8^\circ$ <b>given to 1DP</b> . Allow more than 1DP if 1DP was penalised in part (c).