

Question number	Scheme	Marks
2	$4 - x^2 = x + 2 \Rightarrow x^2 + x - 2 = 0 \Rightarrow (x-1)(x+2) = 0 \Rightarrow x = 1, -2$ $V = \pi \int_{-2}^1 (4 - x^2)^2 dx - \pi \int_{-2}^1 (x+2)^2 dx$ $V = \pi \int_{-2}^1 x^4 - 9x^2 - 4x + 12 dx = \pi \left[ \frac{x^5}{5} - \frac{9x^3}{3} - 2x^2 + 12x \right]_{-2}^1$ $V = \pi \left\{ \left( \frac{1^5}{5} - 3 \times 1^3 - 2 \times 1^2 + 12 \times 1 \right) - \left( \frac{[-2]^5}{5} - 3 \times [-2]^3 - 2 \times [-2]^2 + 12 \times [-2] \right) \right\}$ $V = \frac{153\pi}{5} - 9\pi$ $V = \frac{108\pi}{5}$ <b>ALT</b> $V = \pi \int_{-2}^1 (4 - x^2)^2 dx - \frac{\pi}{3} \times 3^2 \times 3$ $V = \pi \int_{-2}^1 (16 - 8x^2 + x^4) dx - [9\pi] = \pi \left[ 16x - \frac{8x^3}{3} + \frac{x^5}{5} \right]_{-2}^1 - [9\pi]$ $V = \pi \left\{ \left( 16 \times 1 - \frac{8(1)^3}{3} + \frac{(1)^5}{5} \right) - \left( 16 \times (-2) - \frac{8(-2)^3}{3} + \frac{(-2)^5}{5} \right) \right\} - [9\pi]$ $V = \frac{153\pi}{5} - 9\pi$ $V = \frac{108\pi}{5}$	M1A1  M1  M1  M1  A1  [M1 M1 M1 A1]
<b>Total 6 marks</b>		

Mark	Notes
<b>M1</b>	For equating the equation of the curve and the straight line, form a 3TQ with an acceptable attempt to solve the equation to find the $x$ coordinates of the <b>two</b> points of intersection. [See General Guidance for the definition of an attempt] This mark is awarded for a complete method.
<b>A1</b>	For $x = 1$ and $-2$
<b>Method 1</b>	
<b>M1</b>	Uses the <b>correct</b> form for the volume of rotation. Ft their $x$ coordinates used correctly. Everything must be correct for this mark including $\pi$
<b>M1</b>	For an attempt to integrate their expression for the volume of rotation for either the curve or the line (or even a combined expression). Do not accept a mixture of integration and differentiation. [See general guidance for minimum requirements for integration]. Award even if their expression is not squared. Ignore the absence of $\pi$ or limits for this mark.
<b>M1</b>	For attempting to evaluate their integrated expression (which must be a changed expression) with their limits the correct way round. Substitution must be seen. Ignore the absence of $\pi$ and ft their values of $x$ for this mark
<b>A1</b>	For the correct exact value of $\frac{108\pi}{5}$ or exact equivalent.
<b>Method 2</b>	
<b>M1</b>	Uses the <b>correct</b> form for the volume of rotation of the curve minus the volume of the cone. The volume of the cone is: $\frac{1}{3} \times \pi \times (1+2)^2 \times (1-(-2))$ Ft their $x$ coordinates for the limits and for the dimensions of the cone. Everything must be correct for this mark including $\pi$
<b>M1</b>	For an attempt to integrate their expression for the curve. Do not accept a mixture of integration and differentiation. [See general guidance for minimum requirements for integration]. Award even if their expression is not squared, Ignore the absence of $\pi$ or limits for this mark.
<b>M1</b>	For attempting to evaluate their integrated expression (which must be a changed expression) with their limits the correct way round. Substitution must be seen. Ignore the absence of $\pi$ and ft their values of $x$ for this mark
<b>A1</b>	For the correct exact value of $\frac{108\pi}{5}$ or exact equivalent.