

Question Number	Scheme	Marks
	N.B. Answers to (a) and (b) should be in terms of \mathbf{i} and \mathbf{j} , but only penalise once. Column vectors can be used in working.	
7(a)	$\mathbf{v}_B = (20 \sin \alpha)\mathbf{i} + (20 \cos \alpha)\mathbf{j}$ oe e.g. use of Pythagoras but must get to an answer $= 16\mathbf{i} + 12\mathbf{j}$ (km h ⁻¹)	M1 A1 (2)
7(b)	$(\mathbf{s}) = (10\mathbf{i} + 5\mathbf{j}) + t(16\mathbf{i} + 12\mathbf{j})$ or $(10 + 16t)\mathbf{i} + (5 + 12t)\mathbf{j}$	M1 A1 ft (2)
7(c)	$\overrightarrow{AB} = \mathbf{s} - \mathbf{r} = (10\mathbf{i} + 5\mathbf{j}) + t(16\mathbf{i} + 12\mathbf{j}) - [20\mathbf{j} + 40t\mathbf{i}]$ $\overrightarrow{AB} = [(10 - 24t)\mathbf{i} + (12t - 15)\mathbf{j}]$ km *	M1 A1* (2)
7(d)	$10 - 24t = 0$ and $12t - 15 = 0$ OR $40t = 10 + 16t$ and $20 = 5 + 12t$	M1
	$t = \frac{5}{12}$ and $\frac{5}{4}$ or one correct t value which is then used in the other equation correctly to show that the equation is not true. Different t values oe so never collide*	A1 A1* (3)
	ALT 1: $(10 - 24t)^2 + (12t - 15)^2 = 0$ (i.e. $720t^2 - 840t + 325 = 0$)	M1
	$(-840)^2 - 4 \times 720 \times 325 = -230,400 < 0$ Or roots $\frac{7 \pm 4i}{12}$ (calculator)	A1
	No real roots oe so never collide* N.B. Must see justification for 'no real roots' to score either of the A marks.	A1*
	ALT 2: Finds minimum value of $720t^2 - 840t + 325$ or its square root using derivative or completing the square or calculator	M1
	80 or $\sqrt{80}$ or $\overrightarrow{AB} = -4\mathbf{i} - 8\mathbf{j}$ (at $t = \frac{7}{12}$)	A1
	so never collide*	A1*
7(e)	$10 - 24t = 12t - 15$ oe	M1
	$t = \frac{25}{36}$ or 0.69 or better	A1
	$\overrightarrow{AB} = \left[(10 - 24 \times \frac{25}{36})\mathbf{i} + (12 \times \frac{25}{36} - 15)\mathbf{j} \right]$ (km)	M1
	$AB = 20 \frac{\sqrt{2}}{3}$, 9.4 or better (km)	A1 (4)
		(13)