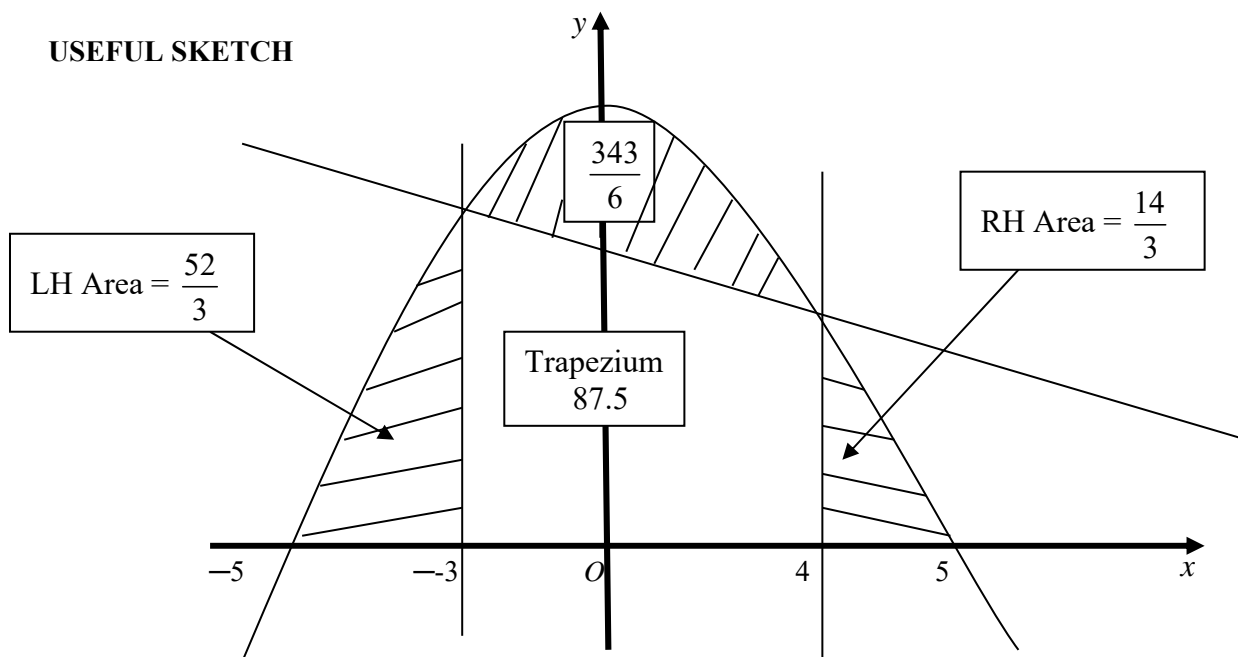


Question number	Scheme	Marks
5 (a)	$25 - x^2 = 13 - x$ $x^2 - x - 12 = 0$ $(x - 4)(x + 3) = 0$ $A = (-3, 16)$ $B = (4, 9)$	M1  M1 A1 A1 (4)
(b)	$\int_{-5}^5 (25 - x^2) dx - \left[ \int_{-3}^4 (25 - x^2) dx - \frac{1}{2}(16 + 9) \times 7 \right]$ $\left[ 25x - \frac{x^3}{3} \right]_{-5}^5 - \left\{ \left[ 25x - \frac{x^3}{3} \right]_{-3}^4 - 87.5 \right\}$ $\left( \frac{250}{3} + \frac{250}{3} \right) - \left[ \left( 100 - \frac{64}{3} \right) - (-75 + 9) - 87.5 \right]$ $\frac{219}{2} = (109.5)$  <b>Alternative (b)</b> $\int_{-5}^5 (25 - x^2) dx - \int_{-3}^4 (12 - x^2 + x) dx$ $\left[ 25x - \frac{x^3}{3} \right]_{-5}^5 - \left[ 12x - \frac{x^3}{3} + \frac{x^2}{2} \right]_{-3}^4$ $\left( \frac{250}{3} + \frac{250}{3} \right) - \left( \frac{104}{3} + \frac{45}{2} \right)$ $\frac{219}{2} = (109.5)$	M1 A1  M1 A1 B1  M1 A1 (7)  <b>[11]</b>  M1 A1  M1 A1 A1  M1 A1 (7)

## USEFUL SKETCH



Part	Mark	Additional Guidance
(a)	M1	For setting the given equation of the curve = given equation of the line $25 - x^2 = 13 - x$ and attempting to form a 3TQ $x^2 - x - k = 0$ ( $k$ is an integer) Ignore the absence of $= 0$ if further work shows that they are attempting to solve a 3TQ $= 0$
	M1	For attempting to solve their 3TQ See general guidance for the definition of an attempt.
	A1	For <b>either</b> $(-3, 16)$ or $(4, 9)$
	A1	For <b>both</b> $(-3, 16)$ and $(4, 9)$
(b)	There are two ways to calculate this area. In each case; The first M mark is for a correct strategy (allow ft from (a) in their limits) The first A mark (M mark in Epen) is a fully correct strategy with correct limits The second M mark is for an attempt to integrate The second A mark is for a fully correct integration – ignore limits for this mark. The B mark (and A mark in Epen) is for the area of the trapezium of 87.5 seen anywhere. The third M mark is for substituting in their limits The final A mark is the correct answer only.	
	<b>Method 1 – Trapezium + two sides</b>	
	M1	For an attempt at the correct strategy to find the area. Allow for this mark a correct statement with using their limits correctly. This may well be seen at the end when they combine individual areas. $(A =) \frac{1}{2} ('16' + '9') \times '7' + \int_{'4'}^{'5'} (25 - x^2) \, dx + \int_{'-5'}^{'-3'} (25 - x^2) \, dx$ OR $(A =) \int_{-3}^4 (13 - x) \, dx + \int_{'4'}^{'5'} (25 - x^2) \, dx + \int_{'-5'}^{'-3'} (25 - x^2) \, dx$
	A1	Fully correct expression with correct limits. $(A =) \frac{1}{2} (16 + 9) \times 7 + \int_4^5 (25 - x^2) \, dx + \int_{-5}^{-3} (25 - x^2) \, dx$ OR $(A =) \int_{-3}^4 (13 - x) \, dx + \int_{'4'}^{'5'} (25 - x^2) \, dx + \int_{'-5'}^{'-3'} (25 - x^2) \, dx$
	M1	For an attempt to integrate their expression for area. (Follow General Guidance for the definition of an attempt) Ignore limits for this mark
	A1	For a fully correct integrated expression for the Area with a correct expression for the trapezium ( <b>Ignore limits for this mark.</b> ) $\left[ 13x - \frac{x^2}{2} \right], \left[ 25x - \frac{x^3}{3} \right], \left[ 25x - \frac{x^3}{3} \right]$ OR $\frac{1}{2} (16 + 9) \times 7, \left[ 25x - \frac{x^3}{3} \right], \left[ 25x - \frac{x^3}{3} \right]$
	B1	For the correct area of the trapezium of 87.5. Award wherever seen. $\frac{343}{6}$ seen implies B1 If not seen explicitly, this can be implied from a correct final answer. <b>This is an A mark in Epen</b>

	M1	For an attempt to substitute <b>their</b> limits into <b>their integrated</b> expression.
	A1	For the correct final area of $A = \frac{219}{2}$ oe
	<b>Method 2 – Using the area under the whole curve between –5 and 5; minus the area of the curve between –4 and 3; plus the area of the trapezium</b>	
	M1	<p>For an attempt at the correct strategy to find the area  Allow for this mark, the correct strategy with <b>their</b> limits  This may well be seen at the end when they combine individual areas.</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (25 - x^2) dx + \frac{1}{2}('16' + '9') \times '7'$ <p>OR</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (25 - x^2) dx + \int_{-3}^{-4} (13 - x) dx$ <p>OR</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (12 + x - x^2) dx$
	A1	<p>For the correct expression with correct limits</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (25 - x^2) dx + \frac{1}{2}('16' + '9') \times '7'$ <p>OR</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (25 - x^2) dx + \int_{-3}^{-4} (13 - x) dx$ <p>OR</p> $(A =) \int_{-5}^5 (25 - x^2) dx - \int_{-3}^{-4} (12 + x - x^2) dx$
	M1	<p>For an attempt to integrate their expression for area.  (Follow General Guidance for the definition of an attempt)  Ignore limits for this mark</p>
	A1	<p>For a fully correct integrated expression for the Area with a correct expression for the trapezium. Accept this seen as individual parts  Ignore limits for this mark.</p> $\left[ 25x - \frac{x^3}{3} \right], \left[ 25x - \frac{x^3}{3} \right], \left[ 13x - \frac{x^2}{2} \right]$ <p>OR</p> $\left[ 25x - \frac{x^3}{3} \right], \left[ 25x - \frac{x^3}{3} \right], \frac{1}{2}(16+9) \times 7 \text{ OR } \left[ 25x - \frac{x^3}{3} \right], \left[ 12x + \frac{x^2}{2} - \frac{x^3}{3} \right]$
	B1	<p>For the correct area of the trapezium of 87.5  <math>\frac{343}{6}</math> seen implies B1  Award wherever seen.  If not seen explicitly, this can be implied from a correct final answer.  <b>This is an A mark in Epen</b></p>
	M1	For an attempt to substitute <b>their</b> limits into <b>their integrated</b> expression or individual parts..
	A1	For the correct final area of $A = \frac{219}{2}$ oe