

Question Number	Scheme	Marks
8(a)	$2xy + 5y = e^x \quad y = \frac{e^x}{(2x+5)}$ $\frac{dy}{dx} = \frac{e^x(2x+5) - 2e^x}{(2x+5)^2}$ $\frac{dy}{dx} = \frac{e^x}{(2x+5)} \times \frac{(2x+5-2)}{(2x+5)} = \frac{y(2x+3)}{(2x+5)} *$	M1A1A1
(b)	$x=0 \Rightarrow \frac{dy}{dx} = \frac{5-2}{5^2} = \frac{3}{25}$	M1A1 (2)
ALT	$x=0 \Rightarrow y = \frac{1}{5}, \quad \frac{dy}{dx} = \frac{1}{5} \times \frac{3}{5} = \frac{3}{25}$	
(c)	$x=0 \Rightarrow y = \frac{e^0}{(2 \times 0 + 5)} = \frac{1}{5}$ $y - \frac{1}{5} = -\frac{25}{3}x$ $125x + 15y - 3 = 0$	M1(Award if seen in (b) and used in (c)) M1 A1 (3)
		[10]

Part	Mark	Notes
(a)	$2xy + 5y = e^x \Rightarrow y = \frac{e^x}{(2x+5)}$	
	M1	For attempting Quotient Rule <ul style="list-style-type: none"> Both terms must be differentiated correctly $e^x \Rightarrow e^x \quad 2x+5 \Rightarrow 2$ There must be two terms subtracted in the numerator either way around The denominator must be the denominator squared. $\frac{dy}{dx} = \frac{e^x(2x+5) - 2e^x}{(2x+5)^2}$
	A1	For $e^x(2x+5)$ or $2e^x$
	A1	For a fully correct differentiated expression. $\frac{dy}{dx} = \frac{e^x(2x+5) - 2e^x}{(2x+5)^2}$

	M1	Subs in $y = \frac{e^x}{(2x+5)}$ as a common factor $\frac{dy}{dx} = \frac{e^x}{(2x+5)} \times \frac{(2x+5-2)}{(2x+5)} = \frac{y(2x+5-2)}{(2x+5)}$	Subs in $e^x = y(2x+5)$ and factorises $\frac{dy}{dx} = \frac{y(2x+5)(2x+5) - 2y(2x+5)}{(2x+5)^2}$	
	A1	For the correct answer with no errors. Note this is a given answer. $\frac{dy}{dx} = \frac{y(2x+3)}{(2x+5)}$		
	ALT – uses implicit differentiation on $2xy + 5y = e^x$			
	M1	$2\left(y + x \frac{dy}{dx}\right) + 5 \frac{dy}{dx} = e^x$		
	A1	Takes out $\frac{dy}{dx}$ as a common factor $\frac{dy}{dx}(2x+5) = e^x - 2y$		
	A1	For a fully correct differentiated expression as below. $\frac{dy}{dx} = \frac{e^x - 2y}{(2x+5)}$		
	M1	For separating the fraction, taking out y as a common factor and attempting to form a single fraction $\frac{dy}{dx} = \frac{e^x}{(2x+5)} - \frac{2y}{(2x+5)} = \frac{y(2x+5)}{(2x+5)} - \frac{2y}{(2x+5)} = \frac{y(2x+5-2)}{2x+5}$		
	A1	For the correct answer with no errors. $\frac{dy}{dx} = \frac{y(2x+3)}{(2x+5)}$		
(b)	M1	For substituting $x = 0$ into $\frac{dy}{dx} = \frac{e^x(2x+5) - 2e^x}{(2x+5)^2} = \frac{e^0(2 \times 0 + 5) - 2e^0}{(2 \times 0 + 5)^2} = \dots$		
	A1	For the correct value of $\frac{dy}{dx} = \frac{3}{25}$		
	ALT			
	M1	When $x = 0 \Rightarrow y = \frac{1}{5}$, $\frac{dy}{dx} = \frac{1}{5} \times \frac{3}{5} = \dots$		
	A1	For the correct value of $\frac{dy}{dx} = \frac{3}{25}$		
(c)	M1	$x = 0 \Rightarrow y = \frac{e^0}{(2 \times 0 + 5)} = \frac{1}{5}$ $x = 0 \Rightarrow y = \frac{1}{5}$ Award if seen in (b) and used in (c) This is a B mark in Epen.		
	M1	Inverts the gradient found in (b) and forms equation of the normal. ft their value of y $y - \frac{1}{5} = -\frac{25}{3}x$		
	A1	Equation of line is given in the required form. $125x + 15y - 3 = 0$		