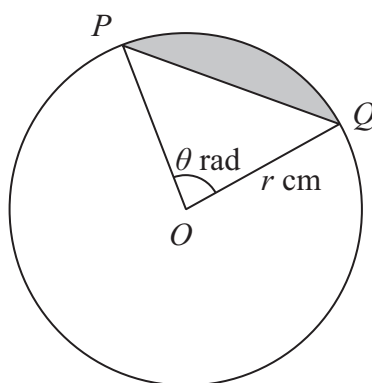


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### Figure 1

The points  $P$  and  $Q$  lie on the circumference of a circle with centre  $O$  and radius  $r$  cm. Angle  $POQ = \theta$  radians. The segment shaded in Figure 1 has area  $A$  cm<sup>2</sup>.

- (a) Show that  $A = \frac{1}{2} r^2 (\theta - \sin \theta)$  (3)

When angle  $POQ$  is increased to  $(\theta + \delta\theta)$  radians, where  $\delta\theta$  is small, the area of the shaded segment is increased to  $(A + \delta A)$  cm<sup>2</sup>, where  $\delta A$  is small.

- (b) Show that  $\delta A \approx \frac{1}{2} r^2 (1 - \cos \theta) \delta \theta$

For a circle of radius 4 cm, the area of the shaded segment is increased by  $0.05 \text{ cm}^2$  when angle  $POQ$  increases by 0.02 radians.

- (c) Find, to 1 decimal place, an estimate for  $\theta$  (4)







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