Accept any fraction that simplifies to $\frac{1}{48}$. You will see $\frac{12}{576}$ which is completely acceptable.

| Question | Scheme | Marks |
|---------------|--|-------------|
| 7(a) | $S = 5x^3 + (3x - 4)^2$ | M1 |
| | $\Rightarrow S = 5x^3 + 9x^2 - 24x + 16*$ | A1 |
| | | cso |
| | | [2] |
| (b) | $\frac{dS}{dx} = 15x^2 + 18x - 24 = 0$ | M1 |
| | $\Rightarrow (5x-4)(x+2) = 0 \Rightarrow x = \frac{4}{5}, -2$ | M1A1 |
| | $\frac{d^2S}{dx^2} = 30x + 18 = 30\left(\frac{4}{5}\right) + 18 \Rightarrow +\text{ve hence minimum}$ | M1A1 [5] |
| (c) | $S = 5\left(\frac{4}{5}\right)^3 + 9\left(\frac{4}{5}\right)^2 - 24\left(\frac{4}{5}\right) + 16 = \frac{128}{25}$ or 5.12 | M1A1 [2] |
| Total 9 marks | | l 9 marks |

| Part | Mark | Notes |
|------|------|--|
| (a) | | |
| | | Substituting <i>x</i> will not yield the required expression. |
| | A1 | For obtaining the given expression with no errors. |
| | cso | You must check every line of their working. |
| (b) | M1 | For an attempt to differentiate the given expression for S wrt x , |
| | | Accept at least two terms fully correct with no power of x to increase. |
| | M1 | Sets their differentiated expression = 0 and attempts to solve, provided it is a |
| | | quadratic. See General Guidance for the definition of an attempt to solve a QE |
| | A1 | For the correct two values of <i>x</i> . |
| | M1 | Attempts to differentiate again. |
| | | Minimally acceptable attempt is $\left(\frac{d^2S}{dx^2}\right) = Ax + B$ |
| | A1 | Conclusion: |
| | | Concludes that the positive value of $x\left(\frac{4}{5}\right)$ will give a positive $\frac{d^2S}{dx^2}$ hence will |
| | | be a minimum. For example, positive + positive = positive hence minimum. OR |
| | | Substitutes either value of x , with the appropriate conclusion and correctly |
| | | concludes that $x = \frac{4}{5}$ gives a minimum. |