

Question number	Scheme	Marks
4 (a)	$\text{Gradient} = \frac{11+10}{3+4} = 3$ $y+10 = 3(x+4) \text{ or } y-11 = 3(x-3) \text{ oe}$	M1A1 (2)
(b)	e.g. $\left(\frac{4 \times -4 + 3 \times 3}{3+4}, \frac{4 \times -10 + 3 \times 11}{3+4} \right) = (-1, -1)$	M1 A1 (2)
ALT (b)	Using Vectors $\begin{pmatrix} -4 \\ -10 \end{pmatrix} + \frac{3}{7} \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix} \quad \text{or} \quad \begin{pmatrix} 3 \\ 11 \end{pmatrix} - \frac{4}{7} \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$	{M1} {A1}
(c)	$-\frac{1}{3} = \frac{n+1}{m+1} \Rightarrow -\frac{1}{3}(m+1) = n+1$ $(\sqrt{10})^2 = (m+1)^2 + (n+1)^2$ $10 = (m+1)^2 + \frac{1}{9}(m+1)^2$ $9 = (m+1)^2$ $m = -4 \quad n = 0$	M1 M1 M1 M1 A1 A1 (6)
ALT (c)	Using Vectors $\vec{AB} = \begin{pmatrix} 7 \\ 21 \end{pmatrix} \text{ so perpendicular to } \vec{AB} = \begin{pmatrix} 21 \\ -7 \end{pmatrix}$ $ \vec{AB} = 7\sqrt{10} \Rightarrow \vec{AP} = 3\sqrt{10}$ $\vec{PQ} = \frac{\sqrt{10}}{7\sqrt{10}} \times \begin{pmatrix} 21 \\ -7 \end{pmatrix} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$ So $Q = (-1-3, -1-1)$ $Q = (-4, 0)$	{M1} {M1, M1} {M1} {A1} {A1}
(d)(i)	$AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$	M1 A1
(d)(ii)	Gradient of $RQ = \frac{-21-0}{-11+4} = 3$ So Gradient of $AB (=3) = \text{Gradient of } RQ$	M1 A1 (4)

ALT (d)	Using Vectors $\vec{RQ} = \begin{pmatrix} -4 - (-11) \\ 0 - (-21) \end{pmatrix} = \begin{pmatrix} 7 \\ 21 \end{pmatrix}$ $\vec{AB} = \begin{pmatrix} 7 \\ 21 \end{pmatrix} = \vec{RQ}$ <p>Because the vectors are the same they must be parallel and the same length</p>	{M1} {A1}
(e)	Area = $7\sqrt{10} \times \sqrt{10} = 70$	{M1}
ALT (e)	Using Vectors $\begin{array}{c ccccc} 1 & 3 & -4 & -11 & -4 & 3 \\ \hline 2 & 11 & 10 & -21 & 0 & 11 \end{array}$ $= 70$	{M1} {A1}
Total is 16 marks		

Part	Mark	Guidance
(a)	M1	For a fully correct method of finding an equation of a straight line. $\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1} \Rightarrow \frac{y - (-10)}{11 - (-10)} = \frac{x - (-4)}{3 - (-4)}$ Or finds gradient $\frac{11+10}{3+4} = 3$ and uses $y + 10 = 3(x + 4)$ or $y - 11 = 3(x - 3)$ If $y = mx + c$ is used, they must find a complete equation for this mark. Allow one error only for the award of this mark.
	A1	For a correct line in any form. $y + 10 = 3(x + 4)$ or $y - 11 = 3(x - 3)$ or $y = 3x + 2$ or even $\frac{y+10}{21} = \frac{x+4}{7}$ but do not allow incomplete processing.
(b)	M1	For one correct from $x = -1$ or $y = -1$
	A1	For the correct coordinates of point P $(-1, -1)$ Accept $x = -1$ $y = -1$
(c)	M1	Uses the perpendicular gradient to set up an equation in m and n . $-\frac{1}{'3'} = \frac{n - '(-1)'}{m - '(-1)'} \Rightarrow -\frac{1}{'3'}(m + 1) = n + 1 \text{ or } n = -\frac{1}{3}m - \frac{4}{3}$ Ft their gradient in part (a) and their P from part (b) for this mark.
	M1	Uses Pythagoras theorem to set up an equation in m and n . $(\sqrt{10})^2 = (m - '(-1)')^2 + (n - '(-1)')^2$ Ft their coordinates of point P from part (b) for this mark.
	M1	Attempts to solve their two equations in n and m simultaneously and forms a quadratic equation in one variable only. $10 = (m + 1)^2 + \frac{1}{9}(m + 1)^2 \Rightarrow 9 = (m + 1)^2 \text{ or } 0 = m^2 + 2m - 8$ or $10 = 9(n + 1)^2 + (n + 1)^2 \Rightarrow 0 = 10n^2 + 20n$
	M1	For solving their either: $9 = (m + 1)^2 \Rightarrow m = \dots$ or $0 = 10n^2 + 20n \Rightarrow n = \dots$ which must be a quadratic equation.
	A1	For finding either $m = -4$ or $n = 0$ Condone the sight of $m = 2$ for this mark.
	A1	For finding both $m = -4$ and $n = 0 \Rightarrow (-4, 0)$ The final answer must be given as coordinates.
	ALT – using vectors – see main scheme.	
	(d)(i)	M1
		A1
(d)(ii)	M1	For finding either the length $AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ Or $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$
	A1	For finding both the length $AB = \sqrt{(3+4)^2 + (11+10)^2} = 7\sqrt{10}$ And $RQ = \sqrt{(-11+4)^2 + (-21)^2} = 7\sqrt{10}$ and states they are equal
(d)(ii)	M1	The gradient of $RQ = \frac{-21 - '0'}{-11 - '(-4)'} = '3'$ Ft their coordinates from part (c)

	A1	States that the gradient of $RQ = \text{gradient of } AB$ [from (a)]
	ALT	Uses vectors, see main scheme. Ft their coordinates of $Q = (m, n)$
(e)	M1	For a correct expression for the area using their length of AB and the given length of PQ ($\sqrt{10}$) Area = ' $7\sqrt{10}$ ' $\times \sqrt{10} = \dots$
	A1	For the area = 70 [square units]
	ALT	Uses the discriminant
	M1	For a correct expression of the area in sequential order using their coordinates for Q Area = $\frac{1}{2} \begin{vmatrix} 3 & -4 & -11 & '-4' & 3 \\ 11 & 10 & -21 & '0' & 11 \end{vmatrix}$
	A1	Area = 70 [square units]

Useful sketch

