

4

$$f(x) = 2x^3 + px^2 + qx + 12 \quad p, q \in \mathbb{Z}$$

Given that $(x + 3)$ is a factor of $f(x)$ and that when $f'(x)$ is divided by $(x + 3)$ the remainder is 37

(a) show that $p = 1$ and find the value of q (6)

(b) hence factorise $f(x)$ completely (2)

(c) show that the equation $f(x) = 0$ has only one real root. (2)

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Question 4 continued

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(Total for Question 4 is 10 marks)