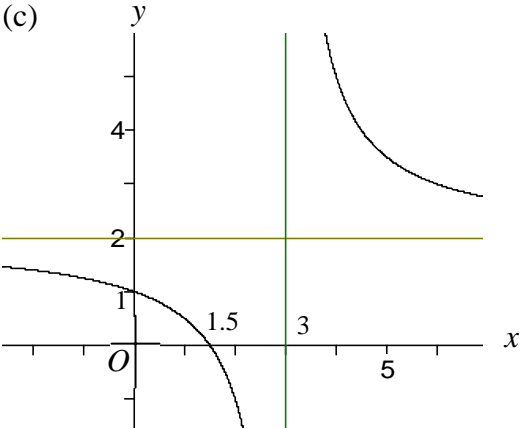


7	<p>(a) <math>A(1\frac{1}{2}, 0)</math>, <math>B(0, 1)</math></p> <p>(b) (i) <math>x = 3</math> (ii) <math>y = 2</math></p> <p>(c) </p> <p>(d) <math display="block">\frac{dy}{dx} = \frac{2(x-3) - (2x-3)}{(x-3)^2} = \frac{-3}{(x-3)^2}</math> At <math>B</math>, <math>x = 0</math> so <math>\frac{dy}{dx} = \frac{-3}{(-3)^2} = -\frac{1}{3}</math> Grad of normal <math>= -1/(-1/3) = 3</math> Normal <math>y = 3x + 1</math></p> <p>(e) At <math>D</math>, <math>3x + 1 = \frac{2x-3}{x-3}</math> <math>3x^2 - 8x - 3 = 2x - 3</math> <math>3x^2 - 10x = 0</math> <math>x(3x - 10) = 0</math> <math>x = 0</math> or <math>x = 10/3</math> At <math>D</math>, <math>x = 3\frac{1}{3}</math></p>	<p>B1, B1</p> <p>B1 B1</p> <p>B1 two branches in correct quadrants B1 asymptotes dep on some curve B1 intercepts</p> <p>M1 Quotient rule A1 Result (unsimplified)</p> <p>A1</p> <p>B1ft B1ft</p> <p>M1</p> <p>A1 M1</p> <p>A1 <b>16</b></p>
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10	<p>(a) (i) <math>\overrightarrow{BC} = -\frac{1}{2}\mathbf{c} - \mathbf{a} + \mathbf{c} = \frac{1}{2}\mathbf{c} - \mathbf{a}</math></p> <p>(ii) <math>\overrightarrow{PQ} = \frac{3}{4}\mathbf{a} + \frac{1}{2}\mathbf{c} + \frac{1}{3}(\frac{1}{2}\mathbf{c} - \mathbf{a}) = \frac{5}{12}\mathbf{a} + \frac{2}{3}\mathbf{c}</math>.</p> <p>(b) (i) <math>\overrightarrow{AT} = -\frac{3}{4}\mathbf{a} + \lambda(\frac{5}{12}\mathbf{a} + \frac{2}{3}\mathbf{c})</math></p> <p>(ii) <math>\overrightarrow{AT} = \mu(\mathbf{c} - \mathbf{a})</math></p> <p>(c) <math>-\frac{3}{4}\mathbf{a} + \lambda(\frac{5}{12}\mathbf{a} + \frac{2}{3}\mathbf{c}) = \mu(\mathbf{c} - \mathbf{a})</math>  <math>\Rightarrow -\frac{3}{4} + \frac{5}{12}\lambda = -\mu</math> and <math>\frac{2}{3}\lambda = \mu</math>  <math>\Rightarrow \frac{5}{12}\lambda = \frac{3}{4} - \frac{2}{3}\lambda</math>  <math>\Rightarrow 5\lambda = 9 - 8\lambda</math>  <math>\Rightarrow \lambda = \frac{9}{13}</math>  <math>\Rightarrow PT:TQ = 9:4</math></p>	<p>M1 A1</p> <p>M1 <math>\frac{3}{4}\mathbf{a} + \frac{1}{2}\mathbf{c} + \dots</math>  M1 <math>\frac{1}{3}(\frac{1}{2}\mathbf{c} - \mathbf{a})</math>  A1  B1ft</p> <p>B1</p> <p>M1  M1 A1ft  M1</p> <p>A1  A1ft</p> <p><b>13</b></p>
11	<p>(a)</p> $V = \pi \int_0^h x^2 dy = \pi \int_0^h (10y - y^2) dy$ $= \pi \left[ 5y^2 - \frac{1}{3}y^3 \right]_0^h$ $= \pi \left[ 5h^2 - \frac{1}{3}h^3 \right]$ $= \frac{1}{3}\pi h^2(15 - h)$ <p>(b) <math>V = \pi(5h^2 - \frac{1}{3}h^3) \Rightarrow \frac{dV}{dh} = \pi(10h - h^2)</math></p> <p>(c) <math>\frac{dV}{dt} = \pi(10h - h^2) \frac{dh}{dt}</math>  When <math>h=1.5</math>, <math>6 = \pi(15 - 2.25) \frac{dh}{dt}</math>  <math>\Rightarrow \frac{dh}{dt} = 6/(12.75\pi) = 0.150 \text{ cm/s (3sf)}</math></p> <p>(d) <math>W = \pi x^2 = \pi(10y - y^2)</math>  When depth is <math>h</math>, <math>W = \pi(10h - h^2)</math>  <math>\frac{dV}{dt} = \pi(10h - h^2) \frac{dh}{dt} = W \frac{dh}{dt}</math>  Since <math>\frac{dV}{dt} = 6</math>, <math>\frac{dh}{dt} = 6/W</math> so <math>k = 6</math></p>	<p>M1 use of <math>\int \pi x^2 dy</math></p> <p>M1 A1 integration</p> <p>M1 use of correct limits  A1 cso</p> <p>B1 oe</p> <p>M1 chain rule</p> <p>M1 A1 substitution  A1 cao</p> <p>B1</p> <p>M1  A1</p> <p><b>13</b></p>