Write your name here Surname	Other name	es
Pearson Edexcel International GCSE	Centre Number	Candidate Number
Further Pu Level 2 Paper 1	ure Mathe	ematics
Sample assessment material for first <b>Time: 2 hours</b>	teaching September 2017	Paper Reference 4PM1/01
Calculators may be used.		Total Marks

# **Instructions**

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You must NOT write anything on the formulae page.
   Anything you write on the formulae page will gain NO credit.

# Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

# **Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶

**PEARSON** 

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# **International GCSE in Further Pure Mathematics Formulae sheet**

### Mensuration

Surface area of sphere =  $4\pi r^2$ 

**Curved surface area of cone** =  $\pi r \times \text{slant height}$ 

**Volume of sphere** = 
$$\frac{4}{3}\pi r^3$$

# **Series**

## **Arithmetic series**

Sum to *n* terms, 
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

## Geometric series

Sum to *n* terms, 
$$S_n = \frac{a(1-r^n)}{(1-r)}$$

Sum to infinity, 
$$S_{\infty} = \frac{a}{1-r} |r| < 1$$

## **Binomial series**

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$$
 for  $|x| < 1, n \in \mathbb{Q}$ 

#### Calculus

## **Quotient rule (diferentiation)**

$$\frac{\mathrm{d}}{\mathrm{d}x} \left( \frac{\mathrm{f}(x)}{\mathrm{g}(x)} \right) = \frac{\mathrm{f}'(x)\mathrm{g}(x) - \mathrm{f}(x)\mathrm{g}'(x)}{\left[\mathrm{g}(x)\right]^2}$$

# **Trigonometry**

## Cosine rule

In triangle *ABC*:  $a^2 = b^2 + c^2 - 2bc \cos A$ 

$$\tan\theta = \frac{\sin\theta}{\cos\theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

# Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

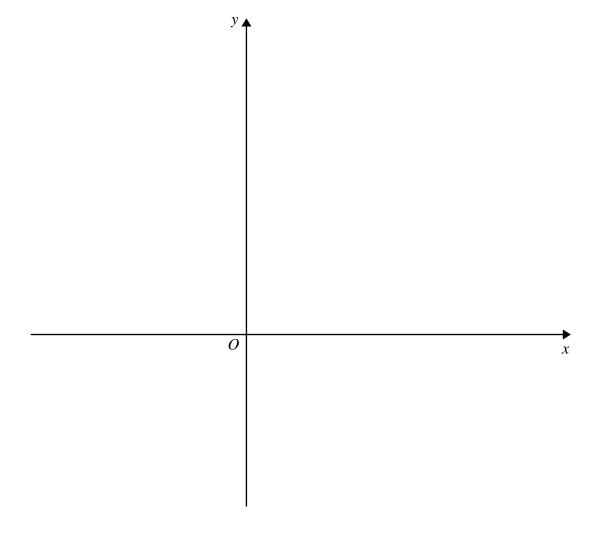
# Answer all ELEVEN questions.

# Write your answers in the spaces provided.

# You must write down all the stages in your working.

- 1 (a) On the axes below, sketch the lines with equations 2x + 3y = 8 and 2y = 4x + 1On your sketch, show the coordinates of the points where the lines cross the coordinate axes.
  - (b) Show, by shading on your sketch, the region R defined by the inequalities

$$2x + 3y \leqslant 8 \qquad 2y \leqslant 4x + 1 \qquad y \geqslant 0 \qquad x \leqslant 2 \tag{2}$$



(Total for Question 1 is 4 marks)

Diagram **NOT** accurately drawn

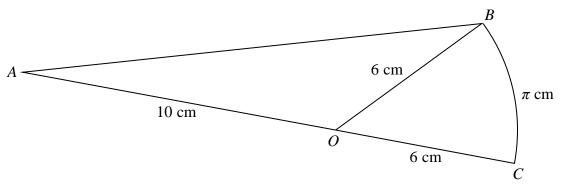


Figure 1

Figure 1 shows a shape ABC in which AOB is a triangle, AOC is a straight line and OBC is a sector of a circle with centre O.

AO = 10 cm, OC = OB = 6 cm and the length of arc  $BC = \pi$  cm.

Find, to 3 significant figures,

(a) the length of AB,

(3)

(b) the area o	the shape A.	BC.
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(3)

3	3 Solve, in degrees to 1 decimal place, for $0 \le \theta < 180$				
		$2\cos(2\theta + 30)^{\circ} + \tan(2\theta + 30)^{\circ} = 0$			
			(6)		

4	A particle <i>P</i> is moving along the <i>x</i> -axis.	
	At time t seconds ( $t \ge 0$ ) the velocity, $v$ m/s, of P is given by $v = 4t^2 - 19t + 12$	
	(a) Find the values of t for which P is instantaneously at rest.	
		(2)
	When $t = 0$ , the displacement of P from the origin is $-4$ m.	
	(b) Find the displacement of $P$ from the origin when $t = 6$	
		(4)
	At time $t$ seconds the acceleration of $P$ is $a$ m/s <sup>2</sup> .	
	(c) Find the value of $t$ when $a = 0$	(2)
		(3)

5	Two numbers $x$ and $y$ are such that $2x + y = 13$	
	The sum of the squares of $2x$ and $y$ is $S$ .	
	(a) Show that $S = 8x^2 - 52x + 169$	(3)
	Using calculus,	
	(b) find the value of x for which S is a minimum, justifying that this value of x gives a minimum value for S.	(4)
	(c) find the minimum value of <i>S</i> .	( - )
	(c) find the minimum value of 5.	(2)

Show that $y - 2\frac{\mathrm{d}y}{\mathrm{d}x} + \frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = 2\mathrm{e}^x$ (8)	
$dx + dx^2 $ (8)	

7 (a) Complete the table of values for

$$y = 2^{\left(\frac{x}{2} + 1\right)} + 1$$

giving your answers to 2 decimal places where appropriate.

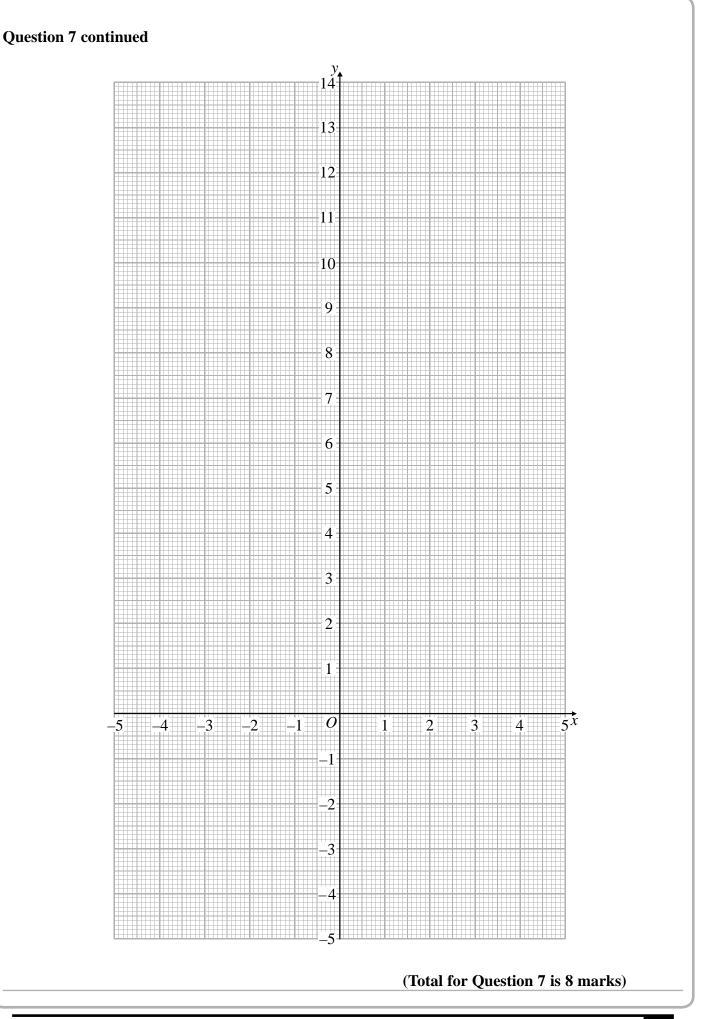
(2)

x	0	1	2	3	4	5
у	3				9	12.31

(b) On the grid opposite, draw the graph of  $y = 2^{\left(\frac{x}{2}+1\right)} + 1$  for  $0 \le x \le 5$ 

(2)

(c) By drawing a suitable straight line on the grid, obtain an estimate, to 1 decimal place, of the root of the equation  $\log_2(4x-6)^2 - x = 2$  in the interval  $0 \le x \le 5$ 

8 The sum $S_n$ of the first <i>n</i> terms of an arithmetic series is given by $S_n = 2n(n+3)$			
	(a) Find the first term of the series.		
		(1)	
	(b) Find the common difference of the series.	(2)	
	The <i>n</i> th term of the series is $T_n$		
	Given that $6S_{(n-4)} = 7T_{(n+3)}$		
	(c) find the value of <i>n</i> .		
		(6)	

- **9** The roots of a quadratic equation are  $\alpha$  and  $\beta$  where  $\alpha + \beta = -\frac{7}{3}$  and  $\alpha\beta = -2$ 
  - (a) Find a quadratic equation, with integer coefficients, which has roots  $\alpha$  and  $\beta$

(4)

Given that  $\alpha > \beta$  and without solving the equation,

(b) show that  $\alpha - \beta = \frac{11}{3}$ 

(2)

(c) form a quadratic equation, with integer coefficients, which has roots

$$\frac{\alpha+\beta}{\alpha}$$
 and  $\frac{\alpha-\beta}{\beta}$ 

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**10** 

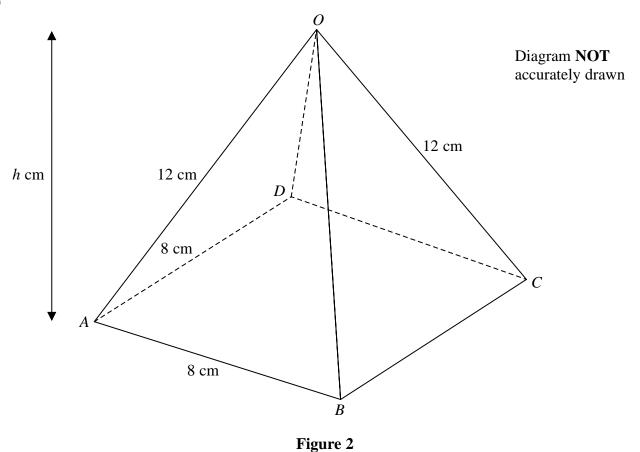


Figure 2 shows a right pyramid ABCDO with a horizontal square base of side 8 cm. The vertical height of the pyramid is h cm and OA = OB = OC = OD = 12 cm.

(a) Find the exact value of h.

(3)

(b) Find, to 1 decimal place, the size of the angle between *OA* and the plane *ABCD*.

(2)

(c) Find, to 1 decimal place, the size of the angle between the plane AOB and the plane ABCD.

**(2)** 

The midpoint of OA is P and Q is the point on BC such that BQ : QC = 3:1

(d) Show that  $PQ = 4\sqrt{5}$  cm.

(4)

(e) Find, to 1 decimal place, the size of angle *PQA*.

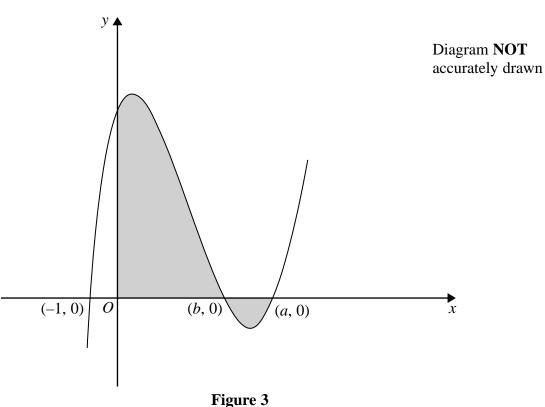
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Question 10 continued

11



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Figure 3 shows a sketch of the curve with equation y = f(x), which passes through the points with coordinates (-1, 0), (b, 0) and (a, 0) where 0 < b < a.

Given that  $f'(x) = 6x^2 - 26x + 12$ 

- (a) find,
  - (i) the value of a,
  - (ii) the value of b.

(8)

(b) Use algebraic integration to determine the exact value of the total area of the shaded regions shown in Figure 3.

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