

Question	Working	Answer	Mark	Notes
1(a)		56170	1	B1
(b)	$1.368 \times 10^9 - 2.144 \times 10^7$ or 1346560000			M1 for evidence of the correct subtraction (so M0 for $2.144 \times 10^7 - 1.368 \times 10^9$ unless recovered later) or for a correct answer (to at least 3 significant figures) in non-standard form (e.g., 1346560000, $13.4656 \times 10^8$ , 1350000000, etc.). The correct answer implies this mark
		$1.34656 \times 10^9$	2	A1 allow answers which round to (awrt) $1.35 \times 10^9$
(c)	$\frac{5.617 \times 10^4}{2.166 \times 10^6}$ or 0.02593...			M1 for evidence of division of the correct two values (condone for M1 $\frac{2.166 \times 10^6}{5.617 \times 10^4}$ ) or a correct answer (to at least 3 significant figures) in non-standard form (e.g., 0.0259, $0.259 \times 10^{-1}$ , 0.0259326, etc.) or for $2.59 \times 10^{-n}$ where $n$ is a positive integer
		$2.59 \times 10^{-2}$	2	A1 for awrt $2.59 \times 10^{-2}$ (e.g., $2.593259464 \times 10^{-2}$ scores both marks, but M1A0 for $2.6 \times 10^{-2}$ if more accurate answer not seen)
<b>Total 5 marks</b>				

<b>2</b>	$\frac{dy}{dx} = 3x^2 + 2ax + b$			M1 differentiating with at least 1 non-zero term correct.
	$3 \times (2)^2 + 2a \times (2) + b = 9.8$ or $4a + b = -2.2$ oe			M1 dep on 1 <sup>st</sup> M mark substitute in $x = 2$ into their $\frac{dy}{dx}$ and equating to 9.8 (allow any equivalent, e.g., $12 + 4a + b = 9.8$ )
	$6 = 8 + 4a + 2b + 8$ or $2a + b = -5$ oe			M1 substitute in $x = 2$ and $y = 6$ into $y = x^3 + ax^2 + bx + 8$
	$2a = 5 - 2.2$ or $b = -10 + 2.2$			M1 dep on 2nd and 3rd M marks. Correct method (but allow one sign slip) for eliminating $a$ or $b$ from their simultaneous equations  <u>Elimination method</u> (oe with coefficients of either $a$ or $b$ the same) e.g. $\begin{aligned} 2a + b &= -5 \\ 4a + b &= -2.2 \end{aligned} \Rightarrow (4a + b) - (2a + b) = -2.2 - (-5)$ (so for this set of equations the candidate must be subtracting the two equations) or e.g. $\begin{aligned} 4a + 2b &= -10 \\ 4a + b &= -2.2 \end{aligned} \Rightarrow (4a + 2b) - (4a + b) = -10 - (-2.2)$ <u>Substitution method</u> e.g. $b = -5 - 2a \Rightarrow 4a + (-5 - 2a) = -2.2$ or e.g. $a = \frac{1}{2}(-5 - b) \Rightarrow 4\left(\frac{-5 - b}{2}\right) + b = -2.2$ (or equivalent) This mark can be implied by either a correct value for $a$ or for $b$ . Allow by use of matrices.
		$a = 1.4$ $b = -7.8$	5	A1(oe e.g. $a = \frac{7}{5}, b = -\frac{39}{5}$ ) dependent on all four M marks <b>Correct answers with no working scores no marks</b>
				<b>Total 5 marks</b>

<b>3 (a)</b> <b>(i)</b>	$4x^2 + 18x + 24 = 160$ oe		<p>M1 adding <b>all</b> the subsets together and equating to 160. Need not be simplified (but if all 7 terms not shown explicitly then need to see at least <math>4x^2 + 18x + 24 = 160</math>).</p> <p>Must see the 160 e.g. <math>4x^2 + 18x + 24 - 160 = 0</math></p> <p>For reference (if fully un-simplified):</p> $8x + \left(\frac{5}{2}x + 7\right) + (x^2 + 9) + (4x - 1) + \left(\frac{3}{2}x + 8\right) + (2x^2 + 4) \\ + (x^2 + 2x - 3) = 160$
		$2x^2 + 9x - 68 = 0$	<p>A1 simplifying to the <b>given</b> 3 term quadratic (at least one intermediate line from initial line of working to given answer) – must include <math>= 0</math> (allow <math>0 = 2x^2 + 9x - 68</math>) so all terms on one side equal to zero</p>
<b>(ii)</b>			<p>M1 correct method for solving the <b>given</b> 3 term quadratic – either by formula, completing the square or factorising.</p>
			<p>By factorising: brackets must expand to give 2 out of 3 correct terms</p>
			<p>By formula: correct substitution into fully correct formula (allow 1 sign error)</p>
			<p>By completing the square: must see <math>2\left(x + \frac{9}{4}\right)^2 \pm ... = 0</math></p>
			<p>Either correct value of <math>x</math> (<math>x = -\frac{17}{2}</math> or <math>x = 4</math>) can imply this mark</p>
			<p><b>NB anything appearing in square brackets [..] is not required</b></p>
		$x = 4$	<p>A1 (A0 if <math>x = -\frac{17}{2}</math> given as a final answer too)</p>
<b>(b)</b>	$\frac{\frac{3 \times "4"}{2} + 8}{3 \times "4"{}^2 + 7.5 \times "4"{} + 8} \text{ oe}$		<p>M1 for either <math>\frac{\frac{3}{2}x + 8}{(\frac{3}{2}x + 8) + (4x - 1) + (2x^2 + 4) + (x^2 + 2x - 3)}</math> oe or for an equivalent expression with their value of <math>x</math> (which must be a positive integer) – if value for <math>x</math> substituted then numerator must be less than 160</p>
		$\frac{7}{43}$	<p>A1 oe exact value (A0 if non-exact answer e.g., 0.163 given and exact answer not seen) – award M1A0 if <math>7/43</math> seen in working (but not given as final answer)</p>

**Total 6 marks**

<b>4(a)</b>		$-2\mathbf{a} + 5\mathbf{b}$	1	B1 oe (e.g., $5\mathbf{b} - 2\mathbf{a}$ ) allow vectors not underlined throughout the question
<b>(b) (i)</b>	$\overrightarrow{OC} = 5\mathbf{b} + 6\mathbf{a} + 5\mathbf{b}$ or $\overrightarrow{OC} = 6\mathbf{a} + 10\mathbf{b}$			M1 for finding either $\overrightarrow{OC}$ , possibly seen as part of another vector e.g., $\overrightarrow{OP}$ where for reference: $\overrightarrow{OP} = \frac{1}{5}(5\mathbf{b} + 6\mathbf{a} + 5\mathbf{b})$ or for $\overrightarrow{AC} = -2\mathbf{a} + 5\mathbf{b} + 6\mathbf{a} + 5\mathbf{b} (= 4\mathbf{a} + 10\mathbf{b})$
	$\overrightarrow{AP} = -2\mathbf{a} + \frac{1}{5}("6\mathbf{a} + 10\mathbf{b}")$ or $\overrightarrow{PB} = -\frac{1}{5}("6\mathbf{a} + 10\mathbf{b}") + 5\mathbf{b}$ oe			M1 for finding either $\overrightarrow{AP}$ or $\overrightarrow{PB}$ (need not be simplified) oe (e.g., $\overrightarrow{PA}$ or $\overrightarrow{BP}$ ) e.g., $\overrightarrow{AP} = \overrightarrow{AC} + \overrightarrow{CP} = -2\mathbf{a} + 5\mathbf{b} + 6\mathbf{a} + 5\mathbf{b} - 4\left(\frac{6}{5}\mathbf{a} + 2\mathbf{b}\right) \left[= -\frac{4}{5}\mathbf{a} + 2\mathbf{b}\right]$ $\overrightarrow{PB} = \overrightarrow{PO} + \overrightarrow{OA} + \overrightarrow{AC} + \overrightarrow{CB} = -\left(\frac{6}{5}\mathbf{a} + 2\mathbf{b}\right) + 2\mathbf{a} + 4\mathbf{a} + 10\mathbf{b} - 6\mathbf{a} - 5\mathbf{b}$ $\left[= -\frac{6}{5}\mathbf{a} + 3\mathbf{b}\right]$ or for $\overrightarrow{AP} = \left(\frac{1}{5}\overrightarrow{AC} + \frac{4}{5}\overrightarrow{AO}\right) = \frac{1}{5}("4\mathbf{a} + 10\mathbf{b}") + \frac{4}{5}(-2\mathbf{a})$
	$\overrightarrow{AP} = -\frac{4}{5}\mathbf{a} + 2\mathbf{b} = \frac{2}{5}\overrightarrow{AB}$ or $\overrightarrow{PB} = -\frac{6}{5}\mathbf{a} + 3\mathbf{b} = \frac{3}{5}\overrightarrow{AB}$ or $\overrightarrow{AP} = -\frac{4}{5}\mathbf{a} + 2\mathbf{b} = \frac{2}{3}\overrightarrow{PB}$ oe			A1cso showing multiple using any two of $AP$ , $PB$ , $AB$ (or $PA$ , $PB$ , $BA$ or a mixture of the two e.g., $AP$ with $BA$ ) oe, e.g., $\overrightarrow{AB} = \frac{5}{2}\overrightarrow{AP}$ or $\overrightarrow{AP} = \frac{2}{3}\overrightarrow{PB}$ or $\overrightarrow{AB} = \frac{5}{3}\overrightarrow{PB}$ or $\overrightarrow{AB} = -\frac{5}{3}\overrightarrow{PB}$ or $\overrightarrow{AP} = -\frac{2}{3}\overrightarrow{BP}$ or $\overrightarrow{AB} = -\frac{5}{2}\overrightarrow{PA}$ etc.
		$AP$ and $AB$ are parallel with the point $A$ in common on each line $\therefore$ collinear		A1 for a comment that one is a multiple of the other (oe e.g. that they are parallel) and that there is a common point on each of the two lines (so if $\overrightarrow{AB}$ , $\overrightarrow{AP}$ used then must mention that $A$ is the common point, if $\overrightarrow{PB}$ , $\overrightarrow{AB}$ used then must mention that $B$ is the common point, etc.)
<b>(b) (ii)</b>		2 : 3	5	B1 oe Accept $m = 2$ and $n = 3$ oe (provided that $m$ and $n$ are in the ratio 2 : 3 e.g., 1 : 1.5, 4 : 6, or stating $m = 1$ $n = 1.5$ , etc.)
				<b>Total 6 marks</b>

<b>5</b>	$2x^2 = 11 - 3(4x - 5)^2$ or $2\left(\frac{5+y}{4}\right)^2 = 11 - 3y^2$			M1 for correct substitution of the linear equation $4x - y = 5$ into the quadratic equation $2x^2 = 11 - 3y^2$ to form an (unimplified) quadratic equation in either $x$ or $y$ . This mark can be implied by the second M mark.
	$2x^2 = 11 - 3(16x^2 - 40x + 25)$ or $2\left(\frac{25+10y+y^2}{16}\right) = 11 - 3y^2$			M1 for correct expansion of either their $(4x - 5)^2$ or $\left(\frac{5+y}{4}\right)^2$ in correct equation (not dependent on previous M mark)
	$25x^2 - 60x + 32 [= 0]$ or $25y^2 + 10y - 63 [= 0]$			A1 for a correct 3 term quadratic in either $x$ or $y$ dep on both previous M marks (oe e.g., $50x^2 - 120x + 64 [= 0]$ , $50y^2 + 20y - 126 [= 0]$ , etc. look out for all signs reversed)
	$(5x - 4)(5x - 8) [= 0]$ or $(5y - 7)(5y - 9) [= 0]$			M1 correct method for solving their 3-term quadratic – either by formula, completing the square or factorising. By factorising: brackets must expand to give 2 out of 3 correct terms By formula: correct substitution into fully correct formula (allow 1 sign error). By completing the square: must see e.g., $25\left(x - \frac{6}{5}\right)^2 \pm ... [= 0]$
	$4 \times "0.8" - y = 5$ or $4 \times 1.6 - y = 5$ or $4x - (-1.8) = 5$ or $4x - 1.4 = 5$ oe			M1 indep substituting their two $x$ values into either equation leading to values for $y$ or vice versa (not dependent on any previous M marks) – this mark can be implied by correct values (if no working seen). This mark can be implied by both correct pairs of values.
		(0.8, -1.8) (1.6, 1.4)	6	A1 for both correct pairs of $x$ and $y$ values (oe e.g., $x = \frac{4}{5}, y = -\frac{9}{5}$ and $x = \frac{8}{5}, y = \frac{7}{5}$ ) This mark is dependent on all previous marks. <b>Correct answer(s) with no working scores no marks</b>
				<b>Total 6 marks</b>

**Question 6**

For reference:  $y = x^2 + 2x + \frac{4}{x}$  and

$x$	-4	-2	-1	-0.5	0.5	1	2	4
$y$	7	-2	-5	-8.75	9.25	7	10	25

