

Question Number	Scheme	Marks
4	<p>Arithmetic series <math>S_3 = 6p</math></p> <p>Geometric series <math>p + pr + pr^2 = p(1 + r + r^2)</math></p> <p><math>6p = p(1 + r + r^2), \Rightarrow 6 = 1 + r + r^2, \Rightarrow r^2 + r - 5 = 0</math> 3TQ</p> <p><math>r = \frac{-1 \pm \sqrt{1^2 - 4 \times 1 \times -5}}{2 \times 1}, \Rightarrow r = \frac{-1 + \sqrt{21}}{2}</math> *</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1d,A1</p> <p>(5)</p>

**Notes**

- B1 for a correct  $S_3$  of  $6p$  or  $(p + 2p + 3p)$  for the arithmetic series
- B1 for a correct  $S_3$  for the geometric series
- M1 for equating the two series **AND** attempting to form a 3TQ in any order.
- M1d for using the formula or completing the square (see General Guidance for an acceptable attempt) to solve the 3TQ
- A1 for the given answer only

**Note:**  $r = \frac{-1 \pm \sqrt{21}}{2}$  is **A0**

**Note: this is a show question. Sufficient working must be seen to award marks.**

**ALT**

- B1 uses summation formula for arithmetic series  $S_3 = \frac{3}{2}(2p + (3-1)p)$
- B1 uses summation formula for geometric series  $S_3 = \frac{p(r^3 - 1)}{(r - 1)}$  or  $\frac{p(1 - r^3)}{(1 - r)}$

- M1 for equating the two series, and attempting to form a cubic in  $r$

$$\frac{3}{2}(2p + (3-1)p) = \frac{p(1 - r^3)}{(1 - r)} \Rightarrow r^3 - 6r + 5 = 0$$

- M1d for solving the cubic by;
- establishing that  $(r - 1)$  is a factor
  - dividing their cubic by  $(r - 1)$  to achieve  $r^2 + r - 5 = 0$
  - for using the formula or completing the square

- A1 for the given answer only

**Note:**  $r = \frac{-1 \pm \sqrt{21}}{2}$  is **A0**

**Note: this is a show question. Sufficient working must be seen to award marks.**