

Question	Scheme	Marks
8(a)	$\int 17 + 2x - 3x^2 \, dx = 17x + \frac{2x^2}{2} - \frac{3x^3}{3} + k$ $0 = \left(17 \times (-1) + \frac{2 \times (-1)^2}{2} - \frac{3 \times (-1)^3}{3} \right) + k \Rightarrow k = 15$ $y = 15 + 17x + x^2 - x^3$	M1A1 M1 A1 [4]
(b)	$\frac{(15 + 17x + x^2 - x^3)}{(x+1)} = -x^2 + 2x + 15$ $-x^2 + 2x + 15 = (x+3)(5-x)$ $a = -3, [-1] \text{ and } b = 5$ <p>When $x = 0$ $y = 15$ so $c = 15$</p>	M1A1 M1A1 A1 B1 [6]
(c)	$\int_0^5 (15 + 17x + x^2 - x^3) \, dx - \frac{1}{2} \times 5 \times 15$ <p>OR</p> $\int_0^5 (15 + 17x + x^2 - x^3) \, dx - \int_0^5 (15 - 3x) \, dx$ $\int_0^5 (15 + 17x + x^2 - x^3) \, dx = \left[15x + \frac{17x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \right]_0^5$ $\left(15 \times 5 + \frac{17 \times 5^2}{2} + \frac{5^3}{3} - \frac{5^4}{4} \right) - (0) = \left(\frac{2075}{12} \right)$ <p>Area of triangle</p> $\text{Area} = \frac{1}{2} \times 5 \times 15 = 37.5$ <p>OR</p> $\text{Area} = \int_0^5 (15 - 3x) \, dx = \left[15x - \frac{3x^2}{2} \right]_0^5 = 37.5$ <p>For the correct area of $R = \frac{2075}{12} - 37 \frac{1}{2} = \frac{1625}{12} = 135 \frac{5}{12}$</p>	M1 M1 M1 B1 [B1] A1 [5]
Total 15 marks		

Question	Notes	Marks
8(a)	$f'(x) = 17 + 2x - 3x^2$	
	For an attempt to integrate $f'(x)$ $y = 17x + \frac{2x^2}{2} - \frac{3x^3}{3} + (k)$	M1
	For the correct integral including a constant of integration $y = 17x + \frac{2x^2}{2} - \frac{3x^3}{3} + k$	A1
	For substituting $(-1, 0)$ into their integrated expression, which must include a constant of integration. $0 = \left(17 \times (-1) + \frac{2 \times (-1)^2}{2} - \frac{3 \times (-1)^3}{3} \right) + k \Rightarrow (k = 15)$	M1
	For writing the equation in the required form $y = 15 + 17x + x^2 - x^3$ This is a given equation. Every step above must be seen for the award of full marks.	A1 cso [4]
(b)	Divides $(15 + 17x + x^2 - x^3)$ by $(x + 1)$ $\begin{array}{r} Q + 2x + x^2 \\ x+1 \overline{) 15 + 17x + x^2 - x^3} \end{array}$ OR Equates coefficients $(15 + 17x + x^2 - x^3) = (x + 1)(Ax^2 + Bx + c) \Rightarrow (x + 1)(-x^2 + 2x + Q)$ Where Q is a constant Minimal working here is sight of the quadratic factor.	M1
	For obtaining the correct 3TQ $-x^2 + 2x + 15$	A1
	For factorising their 3TQ [or otherwise solving] $-x^2 + 2x + 15 = (x + 3)(5 - x)$	M1A1
	For $a = -3$, $[-1]$ and $b = 5$ identified clearly.	A1
	SC No working seen [use of a root finder on a calculator]	
	For $(x + 1)(x - 5)(x + 3)$ seen leading to $a = -3$ and $b = 5$ with no working award: M0A0MA1A1	
	For $a = -3$ and $b = 5$ seen with no other working seen award: M0A0M0A0A1	
	For the value of $c = 15$	B1
(c)	For writing a correct expression for the area of R with the correct limits $\int_0^5 (15 + 17x + x^2 - x^3) \, dx - \frac{1}{2} \times 5 \times 15$ OR	M1

	$\int_0^5 (15 + 17x + x^2 - x^3) \, dx - \int_0^5 (15 - 3x) \, dx$	
	For an attempt to integrate the expression for the curve. [Ignore limits for this mark] $\text{Area} = \int_0^5 (15 + 17x + x^2 - x^3) \, dx = \left[15x + \frac{17x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \right]_0^5$	M1
	For evaluating their integral using their limits. $\text{Area} = \left(15 \times 5 + \frac{17 \times 5^2}{2} + \frac{5^3}{3} - \frac{5^4}{4} \right) - (0) = \left(\frac{2075}{12} \right)$	M1
	For the area of the triangle $\text{Area} = \frac{1}{2} \times 5 \times 15 = 37.5$ ALT Integrates the line $\text{Area} = \int_0^5 (15 - 3x) \, dx = \left[15x - \frac{3x^2}{2} \right]_0^5 = 37.5$	B1 [B1]
	For the correct area of R $\frac{2075}{12} - 37 \frac{1}{2} = \frac{1625}{12} = 135 \frac{5}{12}$	A1 [5]
	ALT	
	For writing an expression for the area of R with the correct limits. $\int_0^5 (15 + 17x + x^2 - x^3) \, dx - \int_0^5 (15 - 3x) \, dx = \left[\int_0^5 (20x + x^2 - x^3) \, dx \right]$	M1
	Award the B mark for a correct expression for the combined area.	B1
	For an attempt to integrate the expression for the combined area or just the curve. [Ignore limits for this mark] $\text{Area} = \int_0^5 (20x + x^2 - x^3) \, dx = \left[\frac{20x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \right]_0^5$	M1
	For evaluating their integral using their limits, but the lower limit must be 0. $\text{Area} = \left(\frac{20 \times 5^2}{2} + \frac{5^3}{3} - \frac{5^4}{4} \right) = \left(\frac{1625}{12} \right)$	M1
	For the correct final area.	A1 [5]
Total 15 marks		