

Question number	Scheme	Marks
10 (a)	$6x - x^2 = -(x^2 - 6x)$ $-(x^2 - 6x) = -\{(x-3)^2 - 9\} \Rightarrow f(x) = -(x-3)^2 + 9$ $D = -1, E = -3 \text{ and } F = 9$	M1A1A1 [3]
(b)	(i) $f(x)_{\max} = 9$ (ii) $x = 3$	B1ft B1ft [2]
(c)	$6x - x^2 = x^2 - 4x + 8 \Rightarrow 2x^2 - 10x + 8 = 0$ $2x^2 - 10x + 8 = (2x-2)(x-4) \Rightarrow x = 1, x = 4$ $y = 5, y = 8$ Coordinates are (1, 5) and (4, 8)	M1 M1A1 A1 [4]
(d)	$\text{Area} = \int_1^4 (6x - x^2) dx - \int_1^4 (x^2 - 4x + 8) dx = \int_1^4 [-2x^2 + 10x - 8] dx$ $= \left[\frac{-2x^3}{3} + \frac{10x^2}{2} - 8x \right]_1^4$ $= \left(\frac{-2 \times 4^3}{3} + \frac{10 \times 4^2}{2} - 8 \times 4 \right) - \left(\frac{-2 \times 1^3}{3} + \frac{10 \times 1^2}{2} - 8 \times 1 \right) = 9 \text{ (units}^2\text{)}$	M1 M1 M1A1 [4]
Total 13 marks		
(a) M1 A1 A1 (b) B1 ft B1 ft (c) M1 M1 A1 A1 (d) M1 M1 M1 A1	An attempt to factorise to make x^2 positive e.g. $-(x \pm a)^2 \pm b$ Complete the square to obtain an expression in the form $-(x \pm 3)^2 \pm q$ NB Any expression in this form will score M1A1 $D = -1, E = -3 \text{ and } F = 9$ $(f(x)_{\max} = 9)$ or follow through their value for F . $(x = 3)$ or follow through their value for E . Equating the two curves and simplifying to a 3 term quadratic Solve their 3 term quadratic $x = 1, x = 4$ (1, 5) and (4, 8) Use of $\int_a^b (f(x) - g(x)) dx$ or $\int_a^b f(x) dx - \int_a^b g(x) dx$ Ignore limits ($f(x)$ and $g(x)$ can be either way round) Attempt the integration. Limits not needed. Substitute the correct limits. 9 (units ²) NB A correct answer with no working will score 4 out of 4	