

Question	Scheme	Marks
7	$x = 0, y = 0^2 + 2 = 2$ $[y = x^2 + 2 \Rightarrow x^2 = y - 2]$ $V = \pi \int_2^a x^2 \, dy \Rightarrow 18\pi = \pi \int_2^a (y - 2) \, dy, = \pi \left[\frac{y^2}{2} - 2y \right]_2^a$ $18\pi = \pi \left[\left(\frac{a^2}{2} - 2a \right) - \left(\frac{2^2}{2} - 2 \times 2 \right) \right]$ $0 = a^2 - 4a - 32$ $a^2 - 4a - 32 = (a + 4)(a - 8) = 0 \Rightarrow a = 8$	B1 M1,M1 M1 M1A1 M1A1 [8]
	ALT $x = 0, y = 0^2 + 2 = 2$ $[y = x^2 + 2 \Rightarrow x^2 = y - 2]$ $18\pi = \pi \int_2^a (y - 2) \, dy, \quad 18\pi = \pi \left[\frac{(y - 2)^2}{2} \right]_2^a$ $18\pi = \pi \left[\left(\frac{a - 2}{2} \right)^2 - \left(\frac{2 - 2}{2} \right)^2 \right]$ $18 = \left(\frac{a - 2}{2} \right)^2 \Rightarrow 36 = (a - 2)^2$ $a = 2 \pm \sqrt{36} \Rightarrow a = 8$	[B1 M1,M1 M1 M1A1 M1A1]
Total 8 marks		

Question	Notes	Marks
7	The intersection of S with the y -axis is at the point with coordinates $(0, 2)$. May be given as when $x = 0, y = 2$	B1
	For a correct statement for the volume, condone missing or incorrect limits and missing π $[y = x^2 + 2 \Rightarrow x^2 = y - 2]$ $V = \pi \int_2^a x^2 \, dy \Rightarrow 18\pi = \pi \int_2^a (y - 2) \, dy$	M1
	METHOD A For an attempt to integrate the expression which must be in the minimally acceptable form $y \pm 2$ $18\pi = \pi \left[\frac{y^2}{2} - 2y \right]_2^a$ [Ignore limits and π for this mark]	M1
	For substituting the limits into their integrated expression to form an equation in a . No simplification is required for this mark. $18\pi = \pi \left[\left(\frac{a^2}{2} - 2a \right) - \left(\frac{2^2}{2} - 2 \times 2 \right) \right]$	M1
	For forming a 3TQ in terms of a $0 = a^2 - 4a - 32$	M1
	For the correct 3TQ $0 = a^2 - 4a - 32$	A1
	For an attempt to solve their 3TQ $a^2 - 4a - 32 = (a + 4)(a - 8) = 0 \Rightarrow a = \dots$	M1
	For the correct value of $a = 8$ If $a = -4$ is also stated then it must be rejected.	A1 [8]
	METHOD B For an attempt to integrate the expression which must be in the minimally acceptable form $y \pm 2$ $18\pi = \pi \left[\frac{(y-2)^2}{2} \right]_2^a$ [Ignore limits and π for this mark]	M1
	For substituting the limits into their integrated expression to form an equation in a . No simplification is required for this mark. $18\pi = \pi \left[\left(\frac{a-2}{2} \right)^2 - \left(\frac{2-2}{2} \right)^2 \right]$	M1
	For forming an equation in a $18 = \left(\frac{a-2}{2} \right)^2 \Rightarrow 36 = (a-2)^2$	M1A1
	For an attempt to solve their equation. $a = 2 \pm \sqrt{36} \Rightarrow a = 8$	M1A1

Total 8 marks
