

Question Number	Scheme	Marks
9(a)	$y = \frac{2+4x-x^2}{2x+1} \Rightarrow x^2 - 4x - 2 + 2yx + y (=0)$ $x^2 + (2y-4)x + (y-2) = 0$	M1A1A1 (3)
(b)	$(2y-4)^2 \geq 4(y-2)$ $4y^2 - 16y + 16 = 4y - 8 \Rightarrow 4y^2 - 20y + 24 = 0$ $y \leq 2 \text{ or } y \geq 3 \quad *$	M1 M1A1 A1cso (4)
(c)	$y = \frac{2+4x-x^2}{2x+1}$ $\frac{dy}{dx} = \frac{(4-2x)(2x+1) - 2(2+4x-x^2)}{(2x+1)^2} \quad \text{See notes for product rule method}$ $\frac{dy}{dx} = 0 \Rightarrow (4-2x)(2x+1) - 2(2+4x-x^2) = 0$ $2x(x+1) = 0 \Rightarrow x = 0, -1$ <p>stationary points are (0,2) (-1,3)</p>	M1A1A1
ALT	$x^2 + (2y-4)x + (y-2) = 0 \Rightarrow 2x + (2y-4) + 2\frac{dy}{dx}x + \frac{dy}{dx} = 0$ $\frac{dy}{dx} = 0 \Rightarrow x + y = 2$ <p>(using (b)) stationary points are (0,2) (-1,3)</p>	M1 A1 A1 (6) M1A1A1 M1 A1A1
(d)	<p>The graph shows a curve with a vertical asymptote at <math>x = -\frac{1}{2}</math>. The curve passes through the points <math>(-1, 3)</math> and <math>(0, 2)</math>. The x-axis is labeled with <math>2 - \sqrt{6}</math> (or <math>-0.45</math>) and <math>2 + \sqrt{6}</math> (or <math>4.45</math>). The origin is labeled <math>O</math>.</p>	<p>B1 curve (i) M1A1 (M1 finding coords, A1 correct (oe or min 2dp) and on diagram</p> <p>(ii) B1 (iii) B1ft (5) [18]</p>

<b>(a)M1</b>	Re-write the equation of $C$ without fractions and rearrange to the required form.
<b>A1</b>	Correct value for $a$ and either $b$ or $c$ . These values need not be stated explicitly.
<b>A1</b>	Fully correct equation. Values of $a$ , $b$ and $c$ need not be stated explicitly. Condone missing brackets round " $y - 2$ ". Award this mark when the equation is reached – isw any listing of values with incorrect signs.
<b>(b)</b>	
<b>M1</b>	Use " $b^2 \geq 4ac$ " for their equation
<b>M1</b>	Re-arrange their inequality to a 3TQ in $y$ . Allow an equation here.
<b>A1</b>	Correct 3TQ, as shown or any equivalent
<b>A1cso</b>	Deduce the CVs (need not be shown explicitly) and state the (given) inequalities. There must be no errors in the working but the equation, if correct, can be solved easily so no working need be shown. Condone use of "and" instead of "or".
<b>(c)</b>	
<b>M1</b>	Differentiate the equation of $C$ using the quotient rule. The denominator must be correct and the numerator must consist of the difference of 2 terms of the type shown. The product rule can be used.
<b>A1</b>	Either numerator term correct
<b>A1</b>	Fully correct numerator
<b>ALT:</b>	<b>Product Rule</b> $y = (2 + 4x - x^2)(2x + 1)^{-1}$
<b>M1A1</b>	$\frac{dy}{dx} = (4 - 2x)(2x + 1)^{-1} - 2(2 + 4x - x^2)(2x + 1)^{-2}$
<b>A1</b>	M1: rewrite without denominator and attempt product rule. Difference of 2 terms of the form shown needed (Difference because of the negative power)
	A1 Either term correct A1 Second term correct
<b>M1</b>	Equate the numerator of their derivative to 0 and solve to $x = \dots$ (any valid method of solving a quadratic with 2 or 3 terms) If product rule used must multiply through by $(2x + 1)^2$
<b>A1</b>	Both $x$ values correct
<b>A1</b>	Both stationary points correct
<b>ALT</b>	
<b>M1</b>	Use implicit differentiation on the re-arranged equation
<b>A1</b>	Correct derivative of $(2y - 4)x$ (inc use of product rule)
<b>A1</b>	Fully correct derivative
<b>M1</b>	Set $\frac{dy}{dx} = 0$ and use the result from (b) to obtain solutions
<b>A1</b>	One correct stationary point
<b>A1</b>	Both correct stationary points
<b>(d)</b>	
<b>B1</b>	Shape: Two parts, one above $y = 3$ and the other below $y = 2$
<b>(i)M1</b>	Attempt to find the $x$ coordinates of the crossing points
<b>A1</b>	Correct coordinates shown on their sketch, 2 crossing points only. $y = 0$ need not be seen. There must be a curve through these points.
<b>(ii)B1</b>	The asymptote must be drawn and labelled (by its equation or by showing the $x$ coordinate of the point where it crosses the $x$ -axis). There must be at least one part of the curve which is asymptotic to the line $x = -\frac{1}{2}$ . No part of the curve should touch/cross the asymptote or curve dramatically away from the line.
<b>(iii)B1ft</b>	Label the stationary points with their coords. Follow through provided the result is sensible.