


Please check the examination details below before entering your candidate information			
Candidate surname		Other names	
<b>Pearson Edexcel</b> <b>International GCSE</b>	Centre Number		Candidate Number
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<div style="border: 1px solid black; padding: 5px; font-size: 1.5em; font-weight: bold;">Thursday 18 June 2020</div>			
Morning (Time: 2 hours)		Paper Reference <b>4PM1/02R</b>	
<div style="border: 1px solid black; padding: 5px;"> <b>Further Pure Mathematics</b>  <b>Paper 2R</b> </div>			
<div style="border: 1px solid black; padding: 5px;">Calculators may be used.</div>			<div style="border: 1px solid black; padding: 5px;">Total Marks</div>

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

### Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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**Pearson**

## International GCSE in Further Pure Mathematics Formulae sheet

**Mensuration****Surface area of sphere**  $= 4\pi r^2$ **Curved surface area of cone**  $= \pi r \times \text{slant height}$ **Volume of sphere**  $= \frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to  $n$  terms,  $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity,  $S_\infty = \frac{a}{1-r} \quad |r| < 1$ **Binomial series**

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

**Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

**Trigonometry****Cosine rule**In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$ 

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

**Logarithms**

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Answer all TEN questions.**

**Write your answers in the spaces provided.**

**You must write down all the stages in your working.**

**1** The  $n$ th term of an arithmetic series  $A$  is  $a_n$

The  $n$ th term of a geometric series  $G$  is  $t_n$

For these two series

$$a_1 = t_1 \quad a_{10} = t_3 = 48 \quad a_{10} = 4t_2$$

Find

(i) the common ratio of  $G$ ,

(ii) the common difference of  $A$ .

(6)

(Total for Question 1 is 6 marks)



P 6 2 2 8 4 A 0 3 3 2

2

$$f(x) = x^3 + px + q \quad \text{where } p \text{ and } q \text{ are constants.}$$

The remainder when  $f(x)$  is divided by  $(x - 1)$  is  $-12$

The remainder when  $f(x)$  is divided by  $(x - 4)$  is  $30$

(a) Find the value of  $p$  and the value of  $q$ . (6)

Using your values of  $p$  and  $q$

(b) show that  $f(3) = 0$  (1)

(c) Express  $f(x)$  as a product of linear factors. (3)

(d) Hence solve the equation  $f(x) = 0$  (1)

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**Question 2 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 2 is 11 marks)**



3

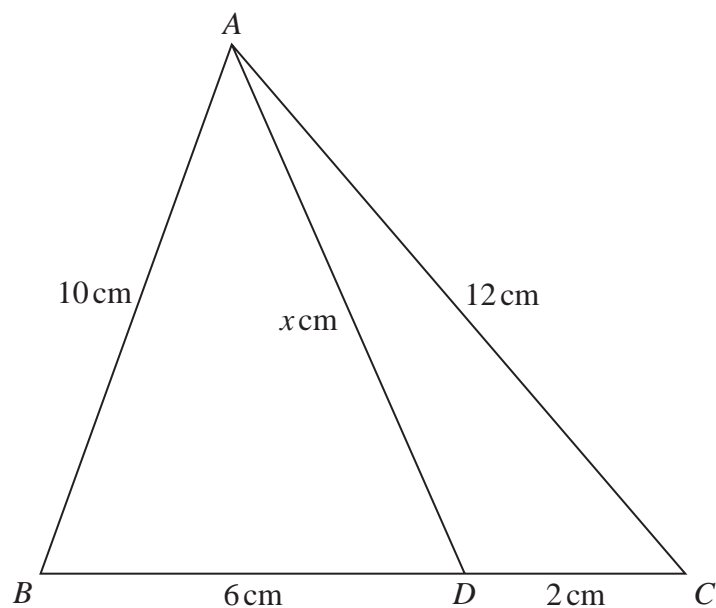
Diagram **NOT**  
accurately drawn**Figure 1**

Figure 1 shows the triangle  $ABC$  in which  $AB = 10\text{ cm}$  and  $AC = 12\text{ cm}$ .  
The point  $D$  lies on  $BC$  such that  $BD = 6\text{ cm}$ ,  $DC = 2\text{ cm}$  and  $AD = x\text{ cm}$ .

(a) Show that  $x = 11$

(4)

(b) Find the area, in  $\text{cm}^2$  to 3 significant figures, of triangle  $ADB$ .

(4)

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**Question 3 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 3 is 8 marks)**



- 4 (a) Complete the table of values for  $y = 2x + 1 + \frac{2}{x^2}$

Give your answers to 2 decimal places where appropriate.

$x$	0.5	1	1.5	2	2.5	3	3.5
$y$		5			6.32		8.16

(2)

- (b) On the grid opposite, draw the graph of  $y = 2x + 1 + \frac{2}{x^2}$  for  $0.5 \leq x \leq 3.5$

(2)

- (c) Use your graph to obtain estimates, to 1 decimal place, of the roots of the equation

$$2x + \frac{2}{x^2} = 7 \quad \text{in the interval } 0.5 \leq x \leq 3.5$$

(2)

- (d) By drawing a suitable straight line on the grid, obtain estimates, to 1 decimal place, of the roots of the equation

$$\frac{3x}{2} + \frac{2}{x^2} = 5 \quad \text{in the interval } 0.5 \leq x \leq 3.5$$

(5)

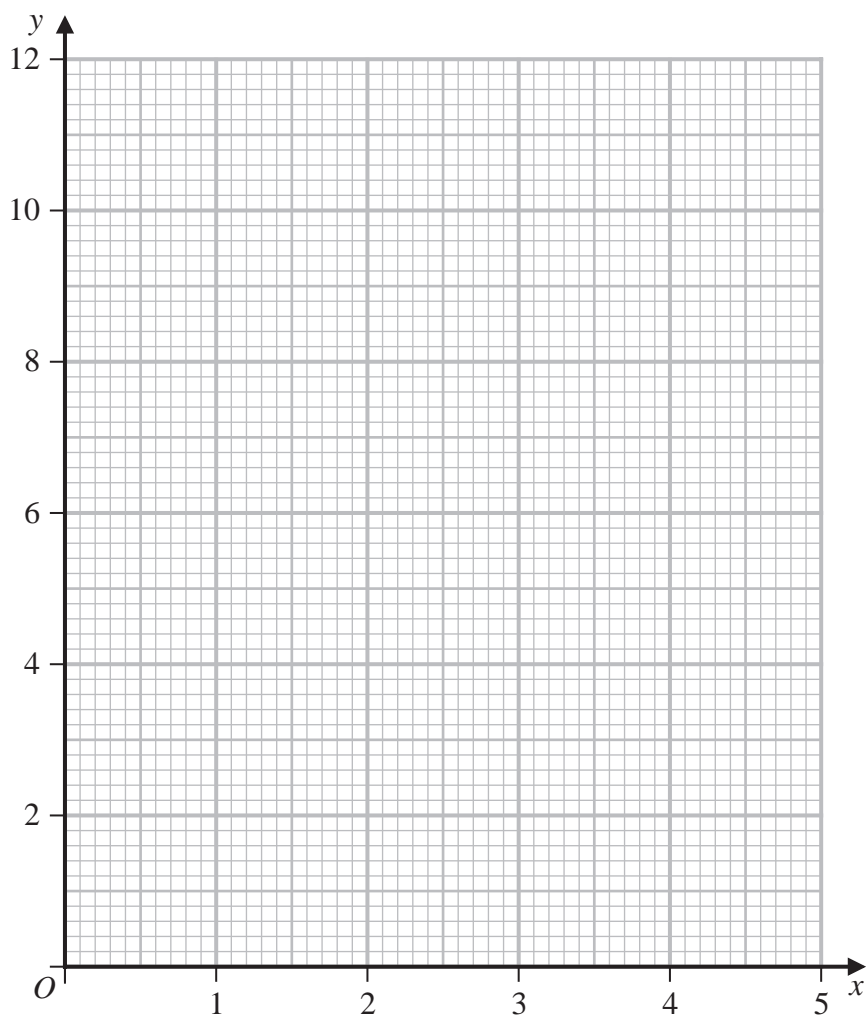
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**Question 4 continued**

Turn over for a spare grid if you need to redraw your graph.



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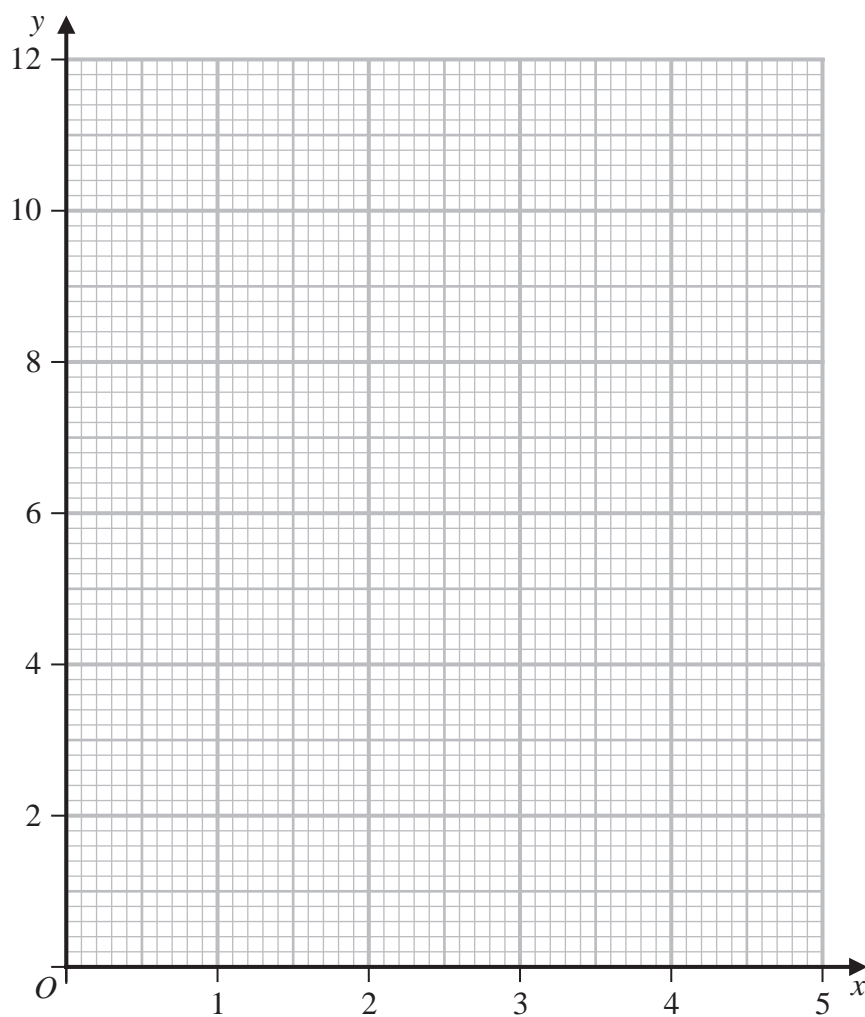
**Question 4 continued**

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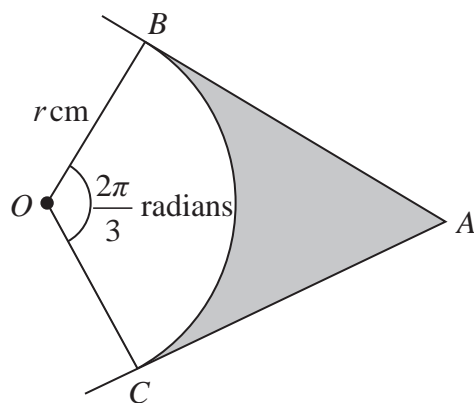
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**Question 4 continued****Only use this grid if you need to redraw your graph.****(Total for Question 4 is 11 marks)**

5

Diagram **NOT**  
accurately drawn**Figure 2**

In Figure 2,  $AB$  and  $AC$  are tangents to a circle with centre  $O$  and radius  $r$  cm.

The points  $B$  and  $C$  lie on the circle so that  $OBC$  is a sector of this circle and  $\angle BOC = \frac{2\pi}{3}$  radians.

Given that the area of the shaded region is  $10 \text{ cm}^2$ ,

find, to 3 significant figures, the value of  $r$ .

(8)

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**Question 5 continued**

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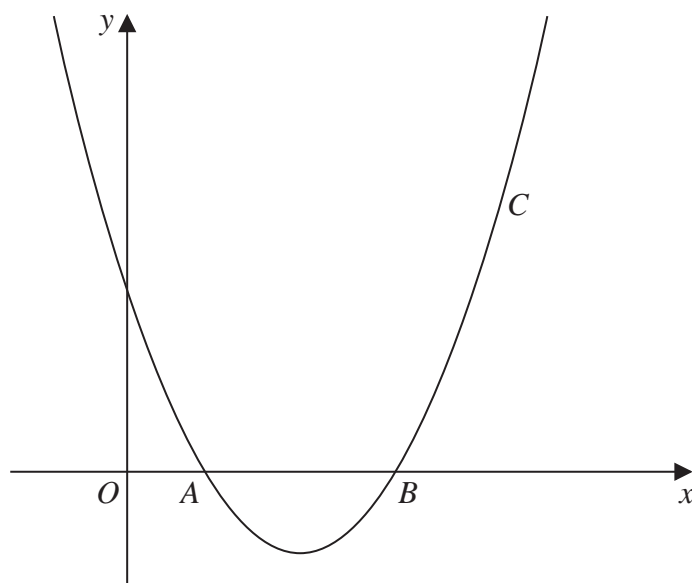
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**(Total for Question 5 is 8 marks)**

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6

Diagram **NOT**  
accurately drawn**Figure 3**

The curve  $C$  with equation  $y = x^2 - 5x + 4$  crosses the  $x$ -axis at the points  $A$  and  $B$ , as shown in Figure 3

- (a) Find the coordinates of  $A$  and the coordinates of  $B$ .

(3)

The tangent to  $C$  at  $A$  meets the tangent to  $C$  at  $B$  at the point  $T$ .

- (b) Find the coordinates of  $T$ .

(6)

The normal to  $C$  at  $A$  meets the normal to  $C$  at  $B$  at the point  $N$ .

- (c) Find the coordinates of  $N$ .

(3)

- (d) Find the area of the quadrilateral  $ATBN$ .

(3)

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**Question 6 continued**

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**Question 6 continued**

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**Question 6 continued**

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**(Total for Question 6 is 15 marks)**

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- 7 (a) Find the set of values of  $k$  for which the equation  $kx^2 - 4x + 2k = 7$  has real roots (4)

Given that the roots of the equation  $kx^2 - 4x + 2k = 7$  are  $\alpha$  and  $\beta$ ,

- (b) form a quadratic equation with roots  $\frac{\alpha + 1}{\alpha}$  and  $\frac{\beta + 1}{\beta}$

Give each coefficient in terms of  $k$ .

(8)

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**Question 7 continued**

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**Question 7 continued**

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**Question 7 continued**

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**(Total for Question 7 is 12 marks)**

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8 Solve the equation  $\log_3 x - 2\log_x 3 = 1$

(7)

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(Total for Question 6 is 7 marks)



9 Given that

$$x = e^{-t} \sin 2t$$

show that

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 5x = 0 \quad (8)$$

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**Question 9 continued**

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**Question 9 continued**

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**Question 9 continued**

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**(Total for Question 9 is 8 marks)**

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10

$$f(x) = 32x^3 - 33x + 1$$

(a) Show that  $f(1) = 0$  (1)

(b) Hence using an algebraic method solve  $f(x) = 0$  (4)

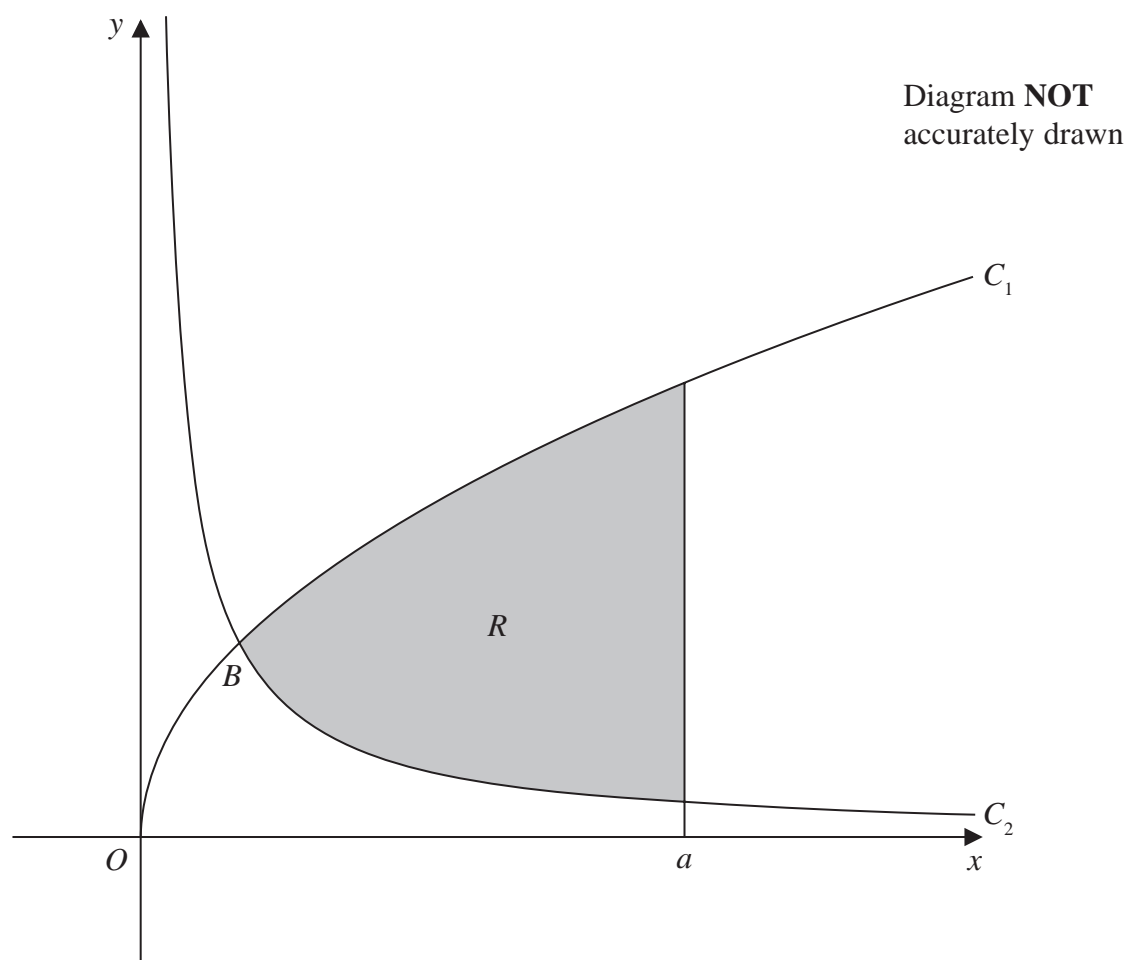


Figure 4

The region  $R$ , shown shaded in Figure 4, is bounded by the curve  $C_1$  with equation  $y = \sqrt{x}$ , by the curve  $C_2$  with equation  $y = \frac{1}{8x}$  and by the line with equation  $x = a$

The curves  $C_1$  and  $C_2$  intersect at the point  $B$ , with  $x$  coordinate  $p$ , where  $p < a$

(c) Find the value of  $p$ . (2)

The region  $R$  is rotated through  $360^\circ$  about the  $x$ -axis to generate a solid with volume  $\frac{27\pi}{64}$

(d) Use algebraic integration to find the value of  $a$ . (7)

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**Question 10 continued**



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**Question 10 continued**

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**(Total for Question 10 is 14 marks)****TOTAL FOR PAPER IS 100 MARKS**