


Please check the examination details below before entering your candidate information

Candidate surname					Other names									
Pearson Edexcel International GCSE					Centre Number					Candidate Number				
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Time 2 hours					Paper reference 4PM1/02									
Further Pure Mathematics PAPER 2														
Calculators may be used.										Total Marks				

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

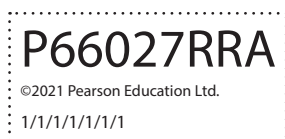
Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.
- Good luck with your examination.

Turn over ►



International GCSE in Further Pure Mathematics Formulae sheet

Mensuration**Surface area of sphere** $= 4\pi r^2$ **Curved surface area of cone** $= \pi r \times \text{slant height}$ **Volume of sphere** $= \frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to n terms, $S_n = \frac{n}{2} [2a + (n - 1)d]$ **Geometric series**Sum to n terms, $S_n = \frac{a(1 - r^n)}{(1 - r)}$ Sum to infinity, $S_\infty = \frac{a}{1 - r} \quad |r| < 1$ **Binomial series** $(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Question 1 continued

(Total for Question 1 is 5 marks)



Use algebraic integration to find the exact volume of the solid formed.

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Question 2 continued

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(Total for Question 2 is 6 marks)



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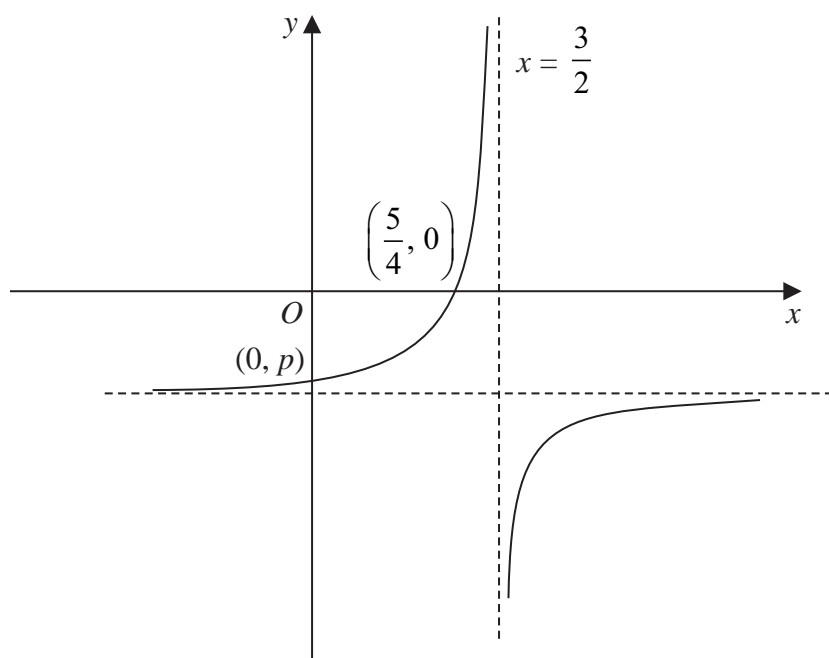


Figure 1

Figure 1 shows a sketch of the curve with equation

$$y = \frac{a - bx}{cx - d} \quad x \neq \frac{d}{c}$$

where a , c and d are prime numbers and b is an integer.

The asymptote to the curve that is parallel to the y -axis has equation $x = \frac{3}{2}$

(a) Write down the value of c and the value of d

(2)

The curve crosses the x -axis at the point $\left(\frac{5}{4}, 0\right)$

(b) Find the value of a and the value of b

(2)

The curve crosses the y -axis at the point $(0, p)$ where p is a rational number.

(c) Find the value of p

(2)

(d) Find an equation of the asymptote to the curve that is parallel to the x -axis.

(1)



Question 3 continued

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Question 3 continued

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(Total for Question 3 is 7 marks)



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- (1)

- (6)

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Question 4 continued

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(Total for Question 4 is 11 marks)



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Question 5 continued

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(Total for Question 5 is 6 marks)



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(3)

Question 6 continued

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(Total for Question 6 is 8 marks)



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7 A geometric series G has first term a and common ratio r

The sum of the first three terms of G is $\frac{61}{6}$

The sum to infinity of G is $\frac{125}{6}$

(a) (i) Show that $r = \frac{4}{5}$

(ii) Find the value of a

(6)

The sum of the first n terms of G is S_n

Given that $S_n > 19.8$

(b) show that $n \lg\left(\frac{4}{5}\right) < \lg\left(\frac{31}{625}\right)$

(2)

(c) Hence find the least value of n

(2)

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 10 marks)



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- 8** (a) Complete the table of values for $y = 2x + \frac{3}{x^2} - 3$ giving your answers to 2 decimal places where appropriate.

x	0.5	0.75	1	1.5	2	3	4	5
y	10		2				5.19	7.12

(2)

- (b) On the grid opposite, draw the graph of $y = 2x + \frac{3}{x^2} - 3$ for $0.5 \leq x \leq 5$

(2)

- (c) By drawing a suitable straight line on the grid, obtain estimates, to one decimal place, of the roots of the equation $4x^3 - 10x^2 + 3 = 0$ for $0.5 \leq x \leq 5$

(5)

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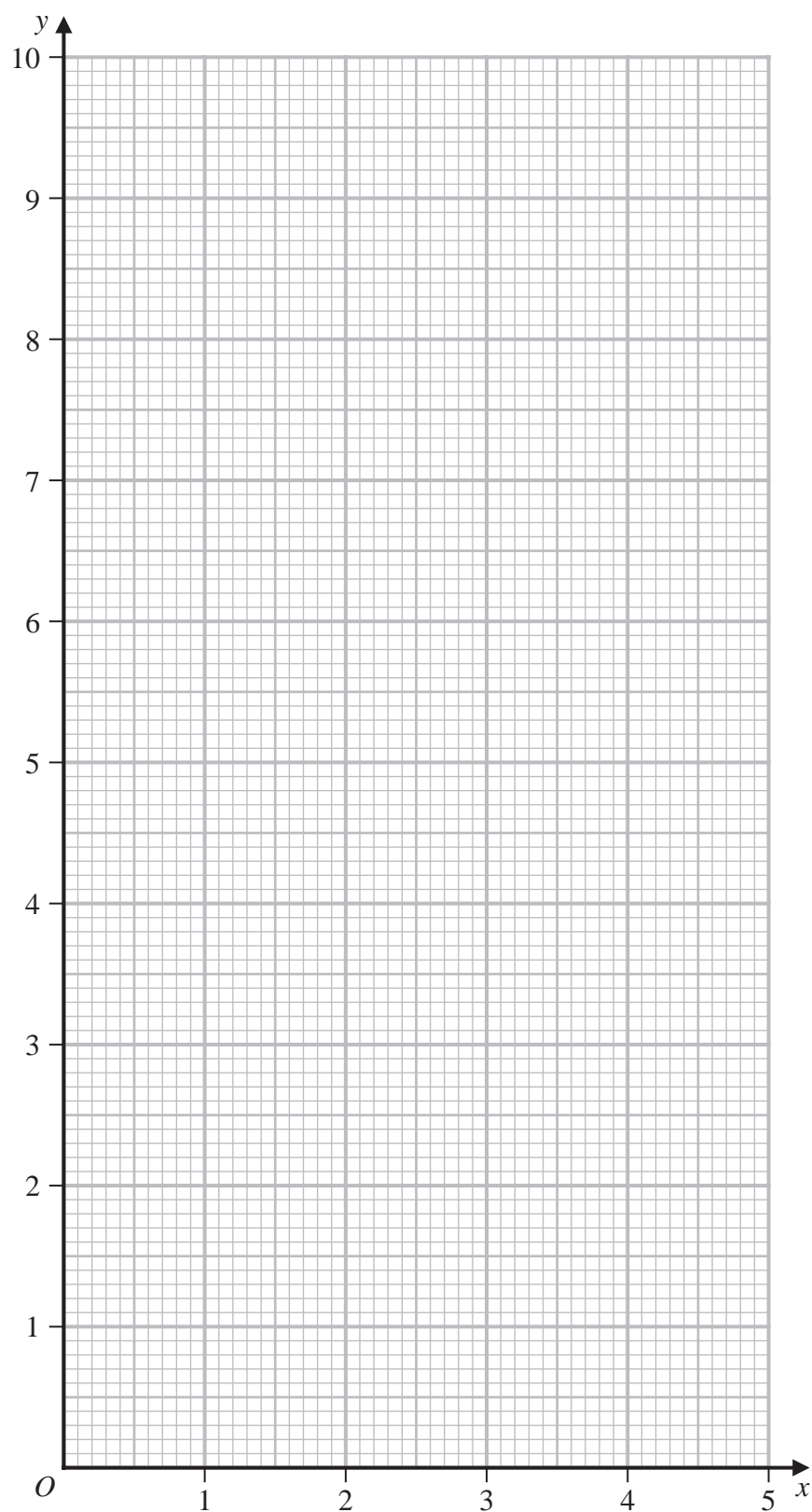
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Question 8 continued



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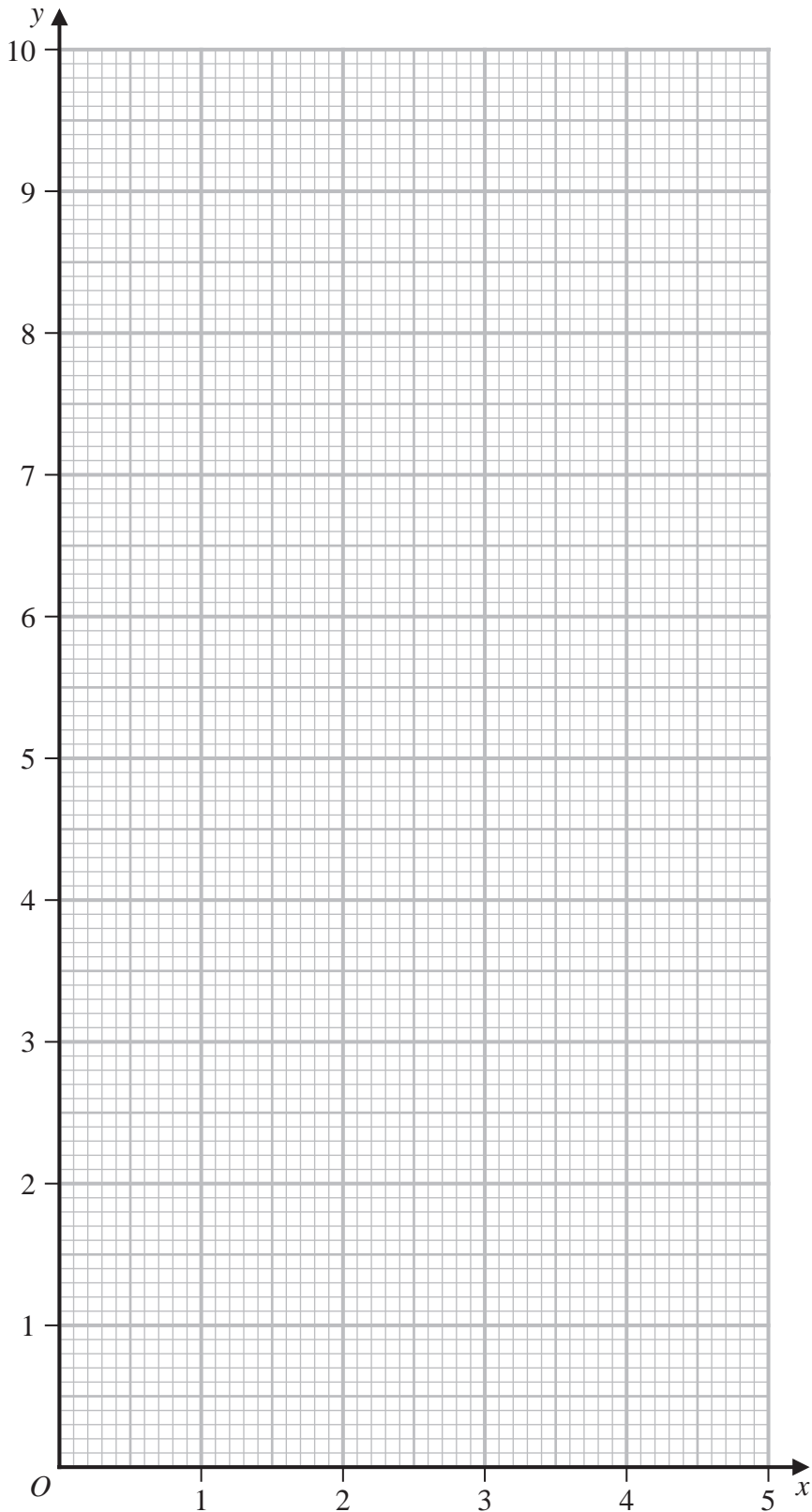
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Question 8 continued

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(Total for Question 8 is 9 marks)



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9

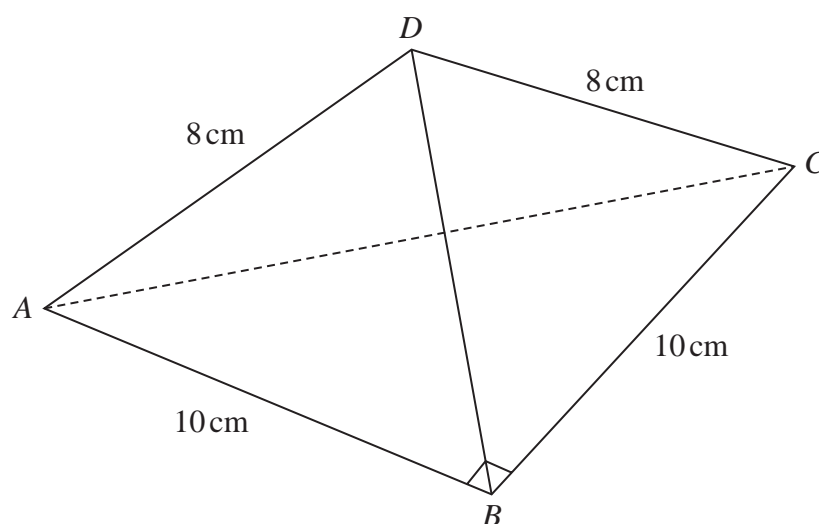
Diagram **NOT**
accurately drawn**Figure 2**

Figure 2 shows a triangular pyramid $ABCD$ with base ABC

$$AB = BC = 10 \text{ cm} \quad AD = CD = 8 \text{ cm} \quad \angle ABC = 90^\circ$$

- (a) Find the exact length of AC

Give your answer in the form $p\sqrt{q}$ cm where p is an integer and q is a prime number.

(2)

The point M is the midpoint of AC

- (b) Find the exact length of BM

Give your answer in the form $m\sqrt{n}$ cm where both m and n are prime numbers.

(2)

Given that $BD = 6$ cm,

- (c) find, in degrees to one decimal place, the size of the acute angle between the plane ACD and the plane ABC

(4)

The base ABC of the pyramid is placed on a horizontal plane.

- (d) Find, in cm to 3 significant figures, the vertical height of D above the base.

(2)

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 10 marks)



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10 (a) Show that $\frac{3}{\sqrt{9-3x}} = \left(1 - \frac{x}{3}\right)^{-\frac{1}{2}}$ (2)

(b) Hence expand $\frac{3}{\sqrt{9-3x}}$ in ascending powers of x up to and including the term in x^3 expressing each coefficient as an exact fraction in its lowest terms.

$$f(x) = \frac{1 + 2x}{\sqrt{9 - 3x}}$$

(c) Find the expansion of $3f(x)$ in ascending powers of x up to and including the term in x^3 expressing each coefficient as an exact fraction in its lowest terms.

(d) Hence, using algebraic integration, obtain an approximation to 6 significant figures for

$$\int_{0.1}^{0.2} \frac{1+2x}{\sqrt{9-3x}} \, dx \quad (4)$$

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Question 10 continued

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(Total for Question 10 is 13 marks)



11 The points A and B have coordinates $(-3, -5)$ and $(7, 5)$ respectively.

- (a) Find an equation for the line AB (2)

The point C has coordinates $(p, 1)$ where $p < 0$

Given that AC and BC are perpendicular,

- (b) prove that $p = -5$ (7)

The point D , where BCD is a straight line, is such that C divides BD in the ratio $4:3$

- (c) Find the coordinates of D (2)

- (d) (i) Find the exact length of AC
(ii) Hence, or otherwise, find the area of triangle ABD (4)

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Question 11 continued

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TOTAL FOR PAPER IS 100 MARKS