

| Question              | Scheme   | Marks   |
|-----------------------|--|---|
| <b>5(a)</b>           | $y = Q(x-6)(x+2)$ where $Q$ is a constant<br>Using the coordinates $(4, -6)$<br>$-6 = Q(4-6)(4+2) \Rightarrow Q = \frac{-6}{-12} = \frac{1}{2}$<br>$y = \frac{1}{2}(x-6)(x+2) \Rightarrow y = \frac{x^2}{2} - 2x - 6$ *  | M1<br><br>M1<br><br>A1 cso<br>[3]                             |
| <b>(b)</b>            | $\frac{dy}{dx} = \frac{2x}{2} - 2$<br>$x = 4, \frac{dy}{dx} = 4 - 2 = 2$<br>Gradient of normal is $-\frac{1}{2}$<br>Equation of $l$ : $y - (-6) = -\frac{1}{2}(x - 4)$<br>$\Rightarrow y = -\frac{x}{2} - 4 \Rightarrow 2y + x + 8 = 0$ *  | M1<br><br>M1<br><br>B1ft<br><br>M1<br><br>A1<br>cso<br>[5]    |
| <b>(c)</b>            | $\frac{x^2}{2} - 2x - 6 = -\frac{x}{2} - 4 \Rightarrow \frac{x^2}{2} - \frac{3}{2}x - 2 = 0$<br>$\Rightarrow (x-4)(x+1) = 0 \Rightarrow x = -1, 4$<br>$\text{Area} = \int_{-1}^4 \left( \frac{x^2}{2} - 2x - 6 \right) dx - \int_{-1}^4 \left( -\frac{x}{2} - 4 \right) dx$<br>$= \left[ \frac{x^3}{6} - \frac{3}{4}x^2 - 2x \right]_{-1}^4$<br>$= \left( \frac{4^3}{6} - \frac{3}{4} \times 4^2 - 2 \times 4 \right) - \left( \frac{(-1)^3}{6} - \frac{3}{4} \times (-1)^2 - 2 \times (-1) \right)$<br>$= \left( \frac{4^3}{6} - \frac{3}{4} \times 4^2 - 2 \times 4 \right) - \left( \frac{(-1)^3}{6} - \frac{3}{4} \times (-1)^2 - 2 \times (-1) \right)$<br>$= -\frac{125}{12} \Rightarrow \text{Area} = \frac{125}{12} \text{ (units}^2\text{) oe}$ | M1<br>M1<br>A1<br><br>M1<br><br>M1<br><br>M1<br><br>A1<br>[7] |
| <b>Total 15 marks</b> |  |   |

| Part | Mark | Notes  |
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| (a)  | M1   | Uses the intersections with the $x$ -axes to form a quadratic equation of the form $y = Q(x \pm 6)(x \pm 2)$ |

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|-----|--|--|
|     | M1                                       | Uses their Quadratic with the coordinates $(4, -6)$ to find the value of $Q$<br>Allow just one processing error here.  |
|     | A1<br>cso                                | For the correct equation in the required form.<br>Note this equation is given to candidates.<br>Both above steps must be complete and correct for the award of this mark.  |
|     | <b>ALT – Uses simultaneous equations</b> |  |
|     | M1                                       | Sets up all three equations with the given coordinates. These must be correct.<br>$y = px^2 + qx + r$<br>$0 = 4p - 2q + r$ <b>1</b><br>$0 = 36p + 6q + r$ <b>2</b><br>$-6 = 16p + 4q + r$ <b>3</b>   |
|     | M1                                       | Attempts to solve their three simultaneous equations to find the values of $p$ , $q$ and $r$<br>At least one correct value is evidence of correct method.<br><b>2-1</b> $0 = 32p + 8q$ <b>4</b><br><b>3-2</b> $6 = 20p + 2q$ <b>5</b><br><b>5</b> $\times 4$ $24 = 80p + 8q$ <b>6</b><br><b>6-4</b> $24 = 48p \Rightarrow p = \frac{1}{2},$<br>$24 = 40 + 8q \Rightarrow q = -2$<br>$0 = 2 + 4 + r \Rightarrow r = -6$   |
|     | A1<br>cso                                | For the correct equation in the required form.<br>Note this equation is given to candidates.<br>All of the above steps must be complete and correct for the award of this mark.  |
| (b) | M1                                       | For differentiating the given expression.<br>This must be correct, simplified or unsimplified for this mark.   |
|     | M1                                       | For substituting $x = 4$ into their $\frac{dy}{dx}$ to find the gradient of the tangent.   |
|     | B1ft                                     | For finding the gradient of the normal.<br>Ft their gradient.  |
|     | M1                                       | For forming an equation for $l$ using the equation of the normal which must have come from use of calculus.<br>If they use $y = mx + c$ then they must find $c$ and form an equation for the award of this mark.<br>For example; $c = -4 \Rightarrow y = -\frac{x}{2} - 4$   |
|     | A1<br>cso                                | For the correct equation in the required form.<br>Accept the terms in any order.<br>For example: even $0 = -8 - x - 2y$  |
| (c) | M1                                       | For equating the equation of $S$ to their $l$ and forming a 3TQ  |
|     | M1                                       | For attempting to solve the 3TQ [see General Guidance for the definition of an attempt] to find two points of intersection.  |
|     | A1                                       | For <b>both</b> correct values of $x$  |
|     | M1                                       | For a correct statement for the area using <b>their two points of intersection</b> correctly.<br><b>Do not accept limits of <math>x = -2</math> and <math>4</math> or <math>6</math></b><br>They may complete these two areas separately and combine at the end. Check to the end of their work before you score this mark.<br>Accept either $\int_{-1}^{4'} \text{Curve} - \int_{-1}^{4'} \text{Line}$ or $\int_{-1}^{4'} \text{Line} - \int_{-1}^{4'} \text{Curve}$ for this mark. |
|     | M1                                       | For an attempt to integrate either the expression for the line or the curve.   |
|     |  |  |