| <b>Question Number</b> | Scheme   | Marks         |
|------------------------|--|---------------|
| 10(a)                  | $\frac{y4}{-4 - 1} = \frac{x6}{-6 - 4} \Rightarrow y + 4 = \frac{1}{2}(x + 6)  \text{oe eg } y = \frac{1}{2}x - 1$ | M1A1 (2)      |
| (b)                    | $\left(\frac{3\times4+2\times-6}{5},\frac{3\times1+2\times-4}{5}\right) \Rightarrow (0,-1)$                        | M1A1 (2)      |
| (c)                    | Gradient of perpendicular = $-2$<br>Allow all following work if $x$ , $y$ used instead of $m$ , $n$                | B1            |
|                        | $-2 = \frac{n-1}{m-0}  (\Rightarrow -2m = n+1)$  | B1ft          |
|                        | $(3\sqrt{5})^2 = (m-0)^2 + (n-1)^2 \Rightarrow 45 = m^2 + (n+1)^2$   |               |
|                        | $45 = m^2 + 4m^2 \Rightarrow 45 = 5m^2 \Rightarrow m = \pm 3$ negative required $m = -3$                           | M1A1          |
|                        | $\Rightarrow n = -2m - 1 \Rightarrow n = -2 \times -3 - 1 = 5  \text{coordinates are } (-3, 5)$                    | A1 (5)        |
| (d)(i)                 | $RQ = \sqrt{(-13 - 3)^2 + (0 - 5)^2} = 5\sqrt{5}$ $AB = \sqrt{(4 - 6)^2 + (1 - 4)^2} = 5\sqrt{5}$                  | M1            |
|                        | $AB = \sqrt{(46)^2 + (14)^2} = 5\sqrt{5}$ With conclusion  | Alcso         |
| (ii)                   | Gradient of $AB = \frac{1}{2}$ Gradient of $RQ = \frac{5-0}{-3-13} = \frac{1}{2}$                                  | M1            |
|                        | With conclusion *  | A1cso (4)     |
| ALT                    | By vectors – combines both parts:  |               |
|                        | $\overrightarrow{AB} = 10\mathbf{i} + 5\mathbf{j}$ or equivalent column vector                                     | M1            |
|                        | $\overrightarrow{RQ} = 10\mathbf{i} + 5\mathbf{j}$ or equivalent column vector                                     | M1            |
|                        | So same length and parallel (provided both vectors are correct)  | A1A1          |
| (e)                    | Area is base × height $A = 3\sqrt{5} \times 5\sqrt{5} = 75$ (units) <sup>2</sup>                                   | M1A1 (2) [15] |
| ALT:                   | $A = \frac{1}{2} \begin{vmatrix} -3 & 4 & -6 & -13 & -3 \\ 5 & 1 & -4 & 0 & 5 \end{vmatrix} $ M1                   |               |
|                        | $= \frac{1}{2} \left[ (-3 - 20) + (-16 + 6) + (0 - 52) - (65 - 0) \right] = -75 \Rightarrow 75$ A1                 |               |
|                        |  |               |
|                        |  |               |

| <b>Question</b><br><b>Number</b>         | Scheme  | Marks          |
|--|---|----------------|
| (a)<br>M1<br>A1<br>(b)                   | Any complete method for obtaining an equation of $l$ Correct equation in any form inc unsimplified  |                |
| M1<br>A1                                 | Obtaining at least one of the coords of <i>P</i> . Must be correct. Can be by formula or diagram. Both coords correct.  NB: If both coords are just written down, award M1A1 if both correct; M0A0 otherwise                                |                |
| (c)<br>B1<br>B1ft                        | Correct gradient of the perpendicular Correct equation connecting $m$ and $n$ from equating their gradient to -2 Can be unsimplified. Follow through their gradient of the perpendicular but must be negative reciprocal of gradient of $l$ |                |
| M1                                       | Use Pythagoras (with + sign as shown oe)to find the length of $PQ$ , equate this to 3 solve to $m =$  | $\sqrt{5}$ and |
| A1<br>A1                                 | Correct value for $m \pm 3$ allowed here<br>Correct value for $n$ Values do not have to be written in coordinate brackets. Only of answer or this mark is lost.   | one final      |
| (d)<br>(i)M1<br>A1cso<br>(ii)M1<br>A1cso | Use Pythagoras to find the length of $RQ$ or $AB$<br>Lengths of both lines correct with working for each and a conclusion shown<br>Find the gradient of $RQ$ Must show working<br>Correct gradient of both lines and a conclusion shown     |                |
| ALT                                      | M1M1 one M mark for each vector correct or working shown but slip made A1A1 one A mark for each conclusion <b>provided</b> the vectors are correct.   |                |
| (e)<br>M1<br>A1                          | Obtaining the area of $ABPQ$ by using the formula for the area of a parallelogram Correct area  |                |
| ALT:                                     | Use the "determinant" method.   |                |
| M1                                       | Formula must be correct ie $\frac{1}{2}$ needed, 5 pairs of coordinates with first and last the   | same,          |
| A1                                       | coordinates to be in order round the quadrilateral (clockwise or anticlockwise). An evaluate also needed.  Correct area - must be positive.   | attempt to     |

| <b>Question Number</b> | Scheme  | Marks           |
|------------------------|---|-----------------|
| 11(a)                  | $AC = \sqrt{12^2 + 8^2}$ $\left(=\sqrt{208} = 4\sqrt{13}\right)$ or $AO$ or $OC = \sqrt{6^2 + 4^2}$ $\left(=2\sqrt{13}\right)$                    | M1              |
|                        | $h = \sqrt{10^2 - 52} = \sqrt{48} = 4\sqrt{3} $ *   | M1A1cso (3)     |
| <b>(b)</b>             | $\angle OCE = \cos^{-1}\left(\frac{2\sqrt{13}}{10}\right) = 43.8537 \approx 43.9^{\circ}$   | M1A1 (2)        |
|                        | or $\sin^{-1}\left(\frac{4\sqrt{3}}{10}\right)$ or $\tan^{-1}\left(\frac{4\sqrt{3}}{2\sqrt{13}}\right)$   | M1A1 (2)        |
| (c)                    | Let $M$ be the midpoint of $BC$ .   |                 |
|                        | $EM = \sqrt{10^2 - 4^2} = 2\sqrt{21}$   | M1              |
|                        | $\cos\theta^{\circ} = \frac{4\sqrt{3}}{2\sqrt{21}} = \frac{2\sqrt{7}}{7} \qquad *$  | M1A1cso         |
|                        | or cosine rule $\cos \theta^{\circ} = \frac{(4\sqrt{3})^2 + (2\sqrt{21})^2 - 6^2}{2 \times 4\sqrt{3} \times 2\sqrt{21}} = \frac{2\sqrt{7}}{7}$    | (3)             |
| ( <b>d</b> )           | Let $N$ be the midpoint of $EM$   |                 |
|                        | $\sqrt{21} \qquad 40.9^{\circ}$ $\sqrt{21}$   |                 |
|                        | $M \stackrel{\frown}{=} 0$  |                 |
|                        | $NO = \sqrt{\left(\sqrt{21}\right)^2 + \left(4\sqrt{3}\right)^2 - 2 \times \sqrt{21} \times 4\sqrt{3} \times \frac{2\sqrt{7}}{7}} = \sqrt{21}$    | M1A1ftA1        |
|                        | hence triangle <i>NEO</i> is isoceles, so required angle ( $\angle ENO$ )<br>$\angle ENO = 180 - 2 \times 40.8933 = 98.2134 \approx 98.2^{\circ}$ | B1 (4)          |
| ALT                    | Based on symmetry:  | [12]            |
|                        | $\tan\frac{\theta}{2} = \frac{\left(\frac{h}{2}\right)}{3} = \frac{2\sqrt{3}}{3}$   | M1A1            |
|                        | $\frac{\theta}{2} = 49.1066$  | A1              |
|                        | $\theta = 98.2^{\circ}$   | A1(B1 on e-PEN) |

| Question<br>Number       | Scheme   | Marks     |
|--------------------------|--|-----------|
| (a)<br>M1<br>M1<br>A1cso | Use Pythagoras with a + sign to find $AC$ or $AO$ or |           |
| (b)<br>M1<br>A1<br>(c)   | Use any trig function to obtain angle <i>OCE</i> Correct size of angle <i>OCE</i> Must be 1 dp   |           |
| M1<br>M1                 | Use Pythagoras with a – sign to obtain the length of <i>EM</i> (need not be correct) $\cos \theta^{\circ} = \frac{4\sqrt{3}}{EM} \text{ with their } EM \text{ or cosine rule as shown. Must reach } \cos \theta = \dots \text{ if other form used}$   |           |
| A1cso<br>(d)             | at start. (NB not dependent)  Correct completion to the <b>given</b> answer  |           |
| M1<br>A1ft<br>A1         | Use of cosine rule in $\triangle EON$ to obtain $ON$<br>Correct numbers follow through their $EM$<br>Correct length $ON$ , exact or awrt 4.58<br><b>Correct</b> size of angle, must be 1 dp unless already penalised in (b). (Can be obtained  | ed by the |
| B1                       | isos triangle as shown or by cosine or sine rule in $\Delta EON$ )  NB: No A1ft in alt method as h is given in (a)   | ed by the |
|                          | 1,2. 1.0 1111 in all method as n is given in (a)   |           |