

Question	Scheme	Marks
<b>2(a)</b>	$(1 + Ax)^n = 1 + n(Ax) + \frac{n(n-1)(Ax)^2}{2} + \dots$ $\Rightarrow nA = -\frac{1}{3} \quad \frac{n(n-1)A^2}{2} = \frac{5}{36}$ $\Rightarrow A = -\frac{1}{3n}$ $\Rightarrow \frac{n(n-1)\left(-\frac{1}{3n}\right)^2}{2} = \frac{5}{36} \Rightarrow n = -\frac{2}{3} \Rightarrow A = \frac{1}{2}$ <b>ALT 1</b> $\Rightarrow nA = -\frac{1}{3} \quad \frac{n(n-1)A^2}{2} = \frac{5}{36}$ $\Rightarrow n = -\frac{1}{3A}$ $\Rightarrow \frac{-\frac{1}{3A}\left(-\frac{1}{3A}-1\right)(A)^2}{2} = \frac{5}{36} \Rightarrow A = \frac{1}{2} \Rightarrow n = -\frac{2}{3}$ <b>ALT 2</b> $\Rightarrow nA = -\frac{1}{3} \Rightarrow \left[(nA)^2 = \frac{1}{9}\right]$ $\frac{n(n-1)A^2}{2!} = \frac{5}{36} \Rightarrow \left[\frac{(nA)^2 - A(An)}{2!} = \frac{5}{36}\right]$ $\Rightarrow \frac{\frac{1}{9} - A\left(-\frac{1}{3}\right)}{2} = \frac{5}{36} \Rightarrow A = \frac{1}{2} \Rightarrow n = -\frac{2}{3}$	<p>B1</p> <p>M1</p> <p>M1dM1A1A1 [6]</p> <p>[M1</p> <p>M1dM1A1A1]</p> <p>[M1</p> <p>M1dM1A1A1]</p>
<b>(b)</b>	$\text{Coefficient of } x^3 \Rightarrow \frac{\left(-\frac{2}{3}\right)\left(-\frac{5}{3}\right)\left(-\frac{8}{3}\right)\left(\frac{1}{2}\right)^3}{3!} = -\frac{5}{81}$	<p>M1A1 [2]</p>
<b>Total 8 marks</b>		

Part	Mark	Notes
(a)	B1	For the correct expansion of $(1 + Ax)^n$ This can be implied by correct work in the term in $x$ and $x^2$
	M1	Equates their second term to $-\frac{1}{3}$ and their third term to $\frac{5}{36}$ Allow presence of $x$ and $x^2$ , provided it is on <b>BOTH</b> sides. eg Allow $nAx = -\frac{1}{3}x$ and $\left[\frac{n(n-1)A^2}{2}\right]x^2 = \frac{5}{36}x^2$
	M1	Substitutes $A$ into $n$ to form an equation in $n$
	dM1	For solving <b>their</b> equation in $n$ If they make errors in simplification to this step e.g., $\left(-\frac{1}{3n}\right)^2 \Rightarrow \left(\frac{1}{9n}\right)$ or $\left(-\frac{1}{3n}\right)^2 \Rightarrow -\left(\frac{1}{9n^2}\right)$ then this is M0 Their equation must be either a quadratic or linear if they cancel an $n$ This is dependent on the previous M mark only.
	A1	For the correct value of $n$ <b>or</b> $A$ $n = -\frac{2}{3}, A = \frac{1}{2}$ isw $n = 0$ seen. This is equivalent to cancelling $n$ 's
	A1	For the correct value of $n$ <b>and</b> $A$
	<b>ALT 1 First two marks same as main method</b>	
	M1	Substitutes $n$ in terms of $A$ into an equation in $A$ $\frac{\left(-\frac{1}{3A}\right)^2 - \left(-\frac{1}{3A}\right)(A)^2}{2} = \frac{5}{36}$ <b>Do not</b> allow a substitution of $n = -\frac{1}{3}$ for this mark
	dM1	For solving <b>their</b> equation in $A$ to find a value for $A$ Their equation must be either a quadratic or linear if they cancel an $A$ This is dependent on the previous M mark only.
	A1	For the correct value of $n$ <b>or</b> $A$ $n = -\frac{2}{3}, A = \frac{1}{2}$
	A1	For the correct value of $n$ <b>and</b> $A$
	<b>ALT 2 First two marks same as main method</b>	
	M1	Substitutes $nA$ into $\frac{(nA)^2 - A(An)}{2!} = \frac{5}{36}$
	dM1	Solves their equation to find a value for $A$ provided no errors introduced. This is dependent on the previous M mark only.
	A1	For the correct value of $n$ <b>or</b> $A$ $n = -\frac{2}{3}, A = \frac{1}{2}$
	A1	For the correct value of $n$ <b>and</b> $A$

(b)	M1	Uses the <b>correct form</b> for the fourth term of a binomial expansion with their $A$ and their $n$ . You may see this in terms of $A$ and $n$ in part (a)  Accept as a minimum, the correct power of $\left(\frac{1}{2}\right)^3$ with the correct denominator i.e. $3!$ Allow the presence of $x^3$ for this mark.
	A1	For the correct value of $-\frac{5}{81}$  If you see the correct value following the correct values of $A$ and $n$ with no working, award M1A1