

Question	Scheme	Marks
10(a)	(i) $\vec{AB} = -\vec{OA} + \vec{OB} \Rightarrow \vec{AB} = -2\mathbf{a} + 4\mathbf{b}$	B1
	(ii) $\vec{MY} = \vec{MA} + \frac{3}{4}(\vec{AB}) = \mathbf{a} + \frac{3}{4}(-2\mathbf{a} + 4\mathbf{b}) = -\frac{\mathbf{a}}{2} + 3\mathbf{b}$	M1A1 [4]
(b)	$\vec{OX} = \mu \vec{OB} = \mu 4\mathbf{b}$	M1
	$\vec{OX} = \vec{OM} + \vec{MX} = \vec{OM} + \lambda \vec{MY} = \mathbf{a} + \lambda \left(-\frac{\mathbf{a}}{2} + 3\mathbf{b}\right) = \mathbf{a} \left(1 - \frac{\lambda}{2}\right) + 3\lambda \mathbf{b}$	M1
	$\Rightarrow \mu 4\mathbf{b} = \mathbf{a} \left(1 - \frac{\lambda}{2}\right) + 3\lambda \mathbf{b}$	dM1
	$\Rightarrow 1 - \frac{\lambda}{2} = 0 \Rightarrow \lambda = 2$	ddM1
	$\Rightarrow 4\mu = 3\lambda \Rightarrow \mu = \frac{6}{4} = \frac{3}{2}$	
	$OB : OX = 2 : 3$ oe	A1 [5]
	ALT – working with alternative vector within triangle OMX	
	$\vec{MX} = \vec{MO} + \vec{OB} + \mu \vec{OB} = -\mathbf{a} + 4\mathbf{b} + \mu 4\mathbf{b}$	[M1
	$\vec{MX} = \lambda \left(-\frac{\mathbf{a}}{2} + 3\mathbf{b}\right)$	M1
	$\Rightarrow -\mathbf{a} = -\frac{\lambda \mathbf{a}}{2} \Rightarrow \lambda = 2$	dM1
	$\Rightarrow 4\mathbf{b} + \mu 4\mathbf{b} = 3\lambda \mathbf{b} \Rightarrow \mu = \frac{1}{2}$	ddM1
	$OB : OX = 2 : 3$ oe	A1]
(c)	$\frac{\Delta YBX}{\Delta ABX} = \frac{1}{4}$	M1
	$\frac{\Delta ABX}{\Delta OAX} = \frac{1}{3}$	
	$\Rightarrow \frac{\Delta YBX}{\Delta OAX} = \frac{1}{4} \times \frac{1}{3} = \frac{1}{12} \Rightarrow \Delta YBX : \Delta OAX = 1 : 12$	M1A1 [3]
	ALT – working with relative areas of triangles	
	Area $\Delta YBX = a$	[M1
	Area $\Delta ABX = 4a$	
	Area $\Delta AYX = 3a$	
	Area $\Delta OYB = 2a$	
	Area $\Delta OAX = 12a$	M1
	$\Delta YBX : \Delta OAX = 1 : 12$	A1]
Total 11 marks		

Part	Mark	Notes
(a)	B1	For the correct simplified vector \vec{AB}
	M1	For the correct vector statement for \vec{MY}
	A1	For the correct simplified vector for \vec{MY}
(b)	M1	For the statement $\vec{OX} = \mu 4\mathbf{b}$ Note: this is a B mark on open.
	M1	For the correct vector for \vec{OX} (ft their \vec{MY})
	dM1	For equating both vectors for \vec{OX} and for comparing coefficients of \mathbf{a} and \mathbf{b} Dep on M1M1
	ddM1	For finding a value for their parameter for μ Note: there is no mark for only finding λ , they must find μ Dep on M1M1M1
	A1	For the correct ratio $OB : OX = 2 : 3$ Allow equivalent ratios e.g. $4 : 6$, $1 : 1.5$
	ALT – working with alternative vector within triangle OMX	
	M1	For a vector statement which includes $\mu 4\mathbf{b}$ (for OX or BX) (ft their \vec{MY}) Note: this is a B mark on open.
	M1	For a correct second vector equation for the same vector (ft their \vec{MY})
	dM1	For equating both vectors and comparing coefficients of \mathbf{a} and \mathbf{b} Dep on M1M1
	ddM1	For finding a value for their parameter for μ Note: there is no mark for only finding λ , they must find μ Dep on M1M1M1
	A1	For the correct ratio $OB : OX = 2 : 3$ Allow equivalent ratios e.g. $4 : 6$, $1 : 1.5$ Condone $OX : OB = 3 : 2$ if clearly stated, but not just $3 : 2$
	ALT – working with relative areas	
(c)	M1	For either the relationship between the of areas of triangles BYX and ABX or the relationship between the areas of triangles ABX and OAX
	M1	For finding the relationship between the of areas of triangles BYX and OAX
	A1	For the correct ratio $[1:12]$ Allow equivalent ratios. Note: do not penalise answer given as a fraction i.e. $\frac{1}{12}$ if already penalised in (b).
	ALT – working with relative areas	
	M1	For assigning a value to one triangle area and writing a second area in terms of this. Note: This could also follow from working with area of a triangle $= \frac{1}{2}ab \sin C$

		e.g. $\Delta YBX = \frac{1}{2}yz \sin B$ and $\Delta ABX = \frac{1}{2}y(4z) \sin B$
	M1	For finding the relationship between the of areas of triangles BYX and OAX Note: This could also follow from working with area of a triangle $= \frac{1}{2}ab \sin C$ e.g. $\Delta YBX = \frac{1}{2}yz \sin B$ and $\Delta ABX = \frac{1}{2}y(4z) \sin B$
	A1	For the correct ratio [1:12] Allow equivalent ratios. Note: do not penalise answer given as a fraction i.e. $\frac{1}{12}$ if already penalised in (b).

