| Question | Scheme | Marks |
|----------|--|---|
| 7(a) | (-3, 0) $(0, -1)$ $x = -4$ | B1 Shape and position B1 Intersection with x-axis B1 Intersection with y-axis B1 Asymptote [4] |
| (b) | $\log_{(x+4)} 256 - \log_4(x+4) = 0 \Rightarrow \frac{\log_4 256}{\log_4(x+4)} - \log_4(x+4) = 0$ $\Rightarrow 4 - (\log_4(x+4))^2 = 0 \Rightarrow (\log_4(x+4))^2 = 4$ $\Rightarrow \log_4(x+4) = \pm 2$ $x+4=4^2 \Rightarrow x=12$ $x+4=4^{-2} \Rightarrow x=-\frac{63}{16} \text{ or } -3.9375$ | M1 M1 M1 A1 A1 [5] |
| | | Total 9 marks |

| Part | Mark | Notes |
|------|----------|--|
| (a) | | For the correct shape in the correct position. |
| | | Ignore intersections and the asymptote for this mark. |
| | | Award as long as the curve is the correct way around in quadrants 2, 3 |
| | | and 4. |
| | | The ends must not turn back in themselves. |
| | | Do Not accept for example: |
| | | |
| | B1 | I^{ν} |
| | | |
| | | |
| | | |
| | | x x |
| | | If the are one true on many lines and condidates have not used along |
| | | If there are two or more lines, and candidates have not made clear |
| | | which ONE they want marked—award B0 |
| | B1 | For a line/curve passing through $(-3, 0)$ or accept $x = -3$ |
| | | Do not accept stopping at the axis. |
| | B1 | For a line/curve passing through $(0, -1)$ or accept $y = -1$ |
| | | Do not accept stopping at the axis. |
| | B1 | For the correct equation only of the asymptote. |
| (b) | Mothod | If they also give a horizontal asymptote then do not isw – it is B0 1 1 - Works in log base 4 |
| (0) | M1 | For changing the base of the log to base 4 |
| | 1711 | For forming a quadratic in terms of $(x + 4)$ |
| | M1 | Accept a substitution for the log |
| | | For taking the square root and undoing the log. |
| | M1 | Accept just the positive root for this mark. |
| | | 63 |
| | A1 | For either $x = 12$ or $-\frac{65}{16}$ |
| | | F 1 1 10 1 63 |
| | A1 | For both $x = 12$ and $$ |
| | M - 41 | 16 |
| | 1v1etno0 | 12 – Works in log base $(x + 4)$ |
| | | For changing the base of the log to base $(x + 4)$ |
| | M1 | $\log_{(x+4)} 256 - \frac{\log_{(x+4)} (x+4)}{\log_{(x+4)} 4} = 0 \Longrightarrow$ |
| | | $\log_{(x+4)} 4$ |
| | | Changes $\log_{(x+4)}(x+4) = 1$ and $\log_{(x+4)} 256 = 4\log_{(x+4)} 4$ |
| | M1 | And forming a quadratic equation with log base $(x + 4)$ |
| | M1 | $\left(\log_{(x+4)} 4\right)^2 = \frac{1}{4}$ Accept a substitution for the log |
| | | Takes the square root (accept just the positive root) and undoes the log |
| _ | M1 | $\log_{(x+4)} 4 = \pm \frac{1}{2} \Rightarrow 4 = (x+4)^{\frac{1}{2}} \text{ and } 4 = (x+4)^{-\frac{1}{2}}$ |
| | | 2 |
| | A1 | For either $x = 12$ or $-\frac{63}{16}$ |
| | | 10 |
| | A1 | For both $x = 12$ and $-\frac{63}{16}$ |
| | | 16 |

| Method 3 works in an unspecified base. If it is just log, assume base 10 | | |
|--|---|--|
| M1 | For changing the base $\frac{\log 256}{\log (x+4)} - \frac{\log (x+4)}{\log 4} = 0$ | |
| M1 | Forms a QE in terms of $(x + 4)$ $4(\log 4)^2 = (\log(x+4))^2$ oe | |
| M1 | Takes square root (accept just the positive root) and undoes the log $\pm 2 \log 4 = \log(x+4) \Rightarrow \log 4 = \pm \frac{1}{2} \log(x+4)$ $\Rightarrow \log 4 = \log(x+4)^{\pm \frac{1}{2}} \Rightarrow 4 = (x+4)^{\pm \frac{1}{2}}$ $\Rightarrow 16 = x+4, \frac{1}{16} = x+4$ | |
| A1 | For either $x = 12$ or $-\frac{63}{16}$ | |
| ,A1 | For both correct values $x = 12$ and $-\frac{63}{16}$ | |