

Question number	Scheme	Marks
9 (a)	$(2x+3)^{\frac{1}{2}} = \frac{x}{2} + \frac{3}{2} \Rightarrow 4(2x+3) = (x+3)^2, \Rightarrow 0 = x^2 - 2x - 3 \text{ oe}$ $x^2 - 2x - 3 = (x-3)(x+1) = 0 \Rightarrow x = 3, -1$ $y = 1, 3 \text{ so coordinates are } (-1, 1) \text{ and } (3, 3)$	M1, A1 M1 A1 A1 (5)
(b)	$\text{Vol} = \pi \int_{-1}^3 (2x+3) \, dx - \pi \int_{-1}^3 \left(\frac{x}{2} + \frac{3}{2} \right)^2 \, dx$ $\pi \int_{-1}^3 (2x+3) \, dx - \pi \int_{-1}^3 \left(\frac{x}{2} + \frac{3}{2} \right)^2 \, dx = \frac{\pi}{4} \int_{-1}^3 3 + 2x - x^2 \, dx = \frac{\pi}{4} \left[3x + x^2 - \frac{x^3}{3} \right]_{-1}^3$ $\Rightarrow \frac{\pi}{4} \left[(9+9-9) - \left(-3+1+\frac{1}{3} \right) \right] = \frac{8}{3}\pi$ <p>For separate integrals:</p> $\pi \int_{-1}^3 (2x+3) \, dx - \pi \int_{-1}^3 \left(\frac{x}{2} + \frac{3}{2} \right)^2 \, dx = \pi \left[x^2 + 3x \right]_{-1}^3 - \pi \left[\frac{x^3}{12} + \frac{3x^2}{4} + \frac{9x}{4} \right]_{-1}^3$ $= \dots$ <p>ALT:</p> $\text{Vol} = \pi \int_{-1}^3 (2x+3) \, dx - \text{vol of truncated cone}$ $\text{Vol} = \pi \left[x^2 + 3x \right]_{-1}^3 - \left(\frac{1}{3} \pi 3^2 \times 6 - \frac{1}{3} \pi 1^2 \times 2 \right)$ $= \pi (9+9-(1-3)) - \frac{52\pi}{3} = \frac{8}{3}\pi$	M1 M1 A1 dM1 A1 cao (5) [10]
(a)		
M1	Eliminate y and obtain a quadratic in x . Need not be simplified. Allow if $(x+3)^2 \rightarrow x^2 + 9$	
A1	Correct 3TQ, as shown or equivalent.	
M1	Solve their 3TQ by factorising, formula or completing the square (see general guidance)	
A1	Two correct values for x	
A1	Corresponding y coordinates. No need to write in coordinate brackets but pairing must be clear.	
	If one x and its corresponding y are correct, award A1A0, provided M mark has been gained	
ALT:	Elimination of x gives $y^2 = 2(2y-3)+3 \Rightarrow y^2 - 4y + 3 = 0 \Rightarrow (y-1)(y-3) = 0$ etc	

(b)	
M1	Correct expression for volume. If the integrals are evaluated separately or π omitted here award only when the correct difference has been obtained (and π included). Limits not needed.
M1	Attempt all the required integration (ie volume for the curve and volume for the line or a combination of these as on the mark scheme), π and limits not needed – ignore any shown
A1	Correct integration (can be one or 2 integrals); ignore limits, π may be missing
dM1	Substitute their x coordinates in their integrated expression(s). Depends on the second M mark. Substitution must be shown for both limits.
A1cao	Correct final answer. All 3 M marks needed
ALT	
M1	Correct expression for the volume including some attempt at the truncated cone. π needed for the cone but may appear later for the integral/
M1	Attempt the integration - π and limits not needed – ignore any shown – and attempt the vol of the truncated cone.
A1	Correct integration and correct difference of 2 cones
dM1	Substitute their x coordinates in their integrated expression. Depends on the second M mark. Substitution must be shown for both limits.
A1cao	Correct final answer. All 3 M marks needed