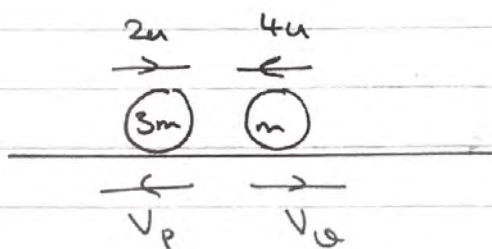


M1 June 2018 (MA)

Q1a)



C.L.M :  $3m(2u) - 4mu = mV_q - 3mV_p$

$$2u = V_q - 3V_p \quad \text{--- (1)}$$

$$I = m(v - u)$$

for P  $\rightarrow \frac{21mu}{4} = 3m(V_p - -2u)$

$$\Rightarrow \frac{21mu}{4} = 3mV_p + 6mu$$

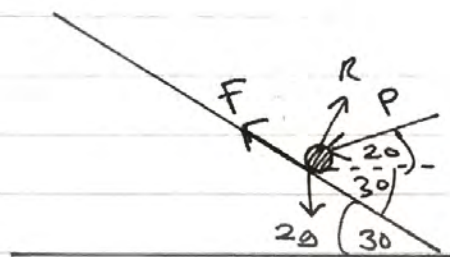
$$\Rightarrow -\frac{3u}{4} = 3V_p \quad \therefore V_p = -\frac{u}{4}$$

so speed =  $\boxed{\frac{u}{4}}$

b) (i):  $V_q = 2u + 3V_p = 2u + 3\left(-\frac{u}{4}\right)$

$$\therefore \boxed{V_q = \frac{5u}{4} = \text{speed}}$$

Q2)



note that we want the least possible value of  $P$ . This least value occurs when friction acts up the plane.

$R$  (Parallel to plane) :  $P \cos 50 + F = 2g \sin 30$  — (1)

$R$  (Perp. to plane) :  $R = 2g \cos 30 + P \sin 50$

$$F = \frac{1}{4} R$$

(1) :  $P \cos 50 + \frac{1}{4} R = 2g \sin 30$

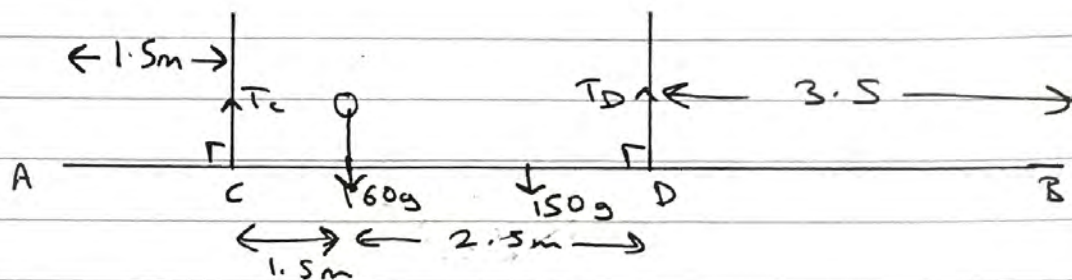
$\times 4$  :  $4P \cos 50 + (R) = 4g$

sub (2) :  $4P \cos 50 + (2g \cos 30) + (P \sin 50) = 4g$

$$P(4 \cos 50 + \sin 50) = 4g - 2g \cos 30$$

$$P = \frac{4g - 2g \cos 30}{4 \cos 50 + \sin 50} = \boxed{6.66 \text{ N}}$$

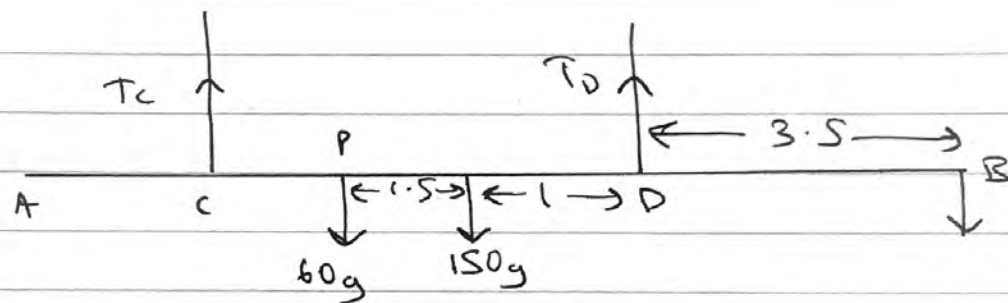
(Q3a)



$$\underline{M(C)} : T_c (4) = 150g(1) + 60g(2.5)$$

$$T_c = \frac{150g + 60g(2.5)}{4} = 75g = \boxed{735N}$$

b)



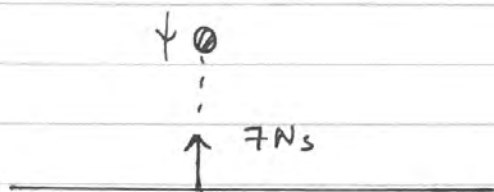
mass of gymnast at B is largest possible for beam to remain horizontal  $\rightarrow T_c = 0$

$$\underline{M(B)} : 150g(4.5) + 60g(6) = T_d(3.5)$$

$$\therefore T_d = \frac{150g(4.5) + 60g(6)}{3.5}$$

$$= \boxed{2900N}$$

Q4g)



$$\left. \begin{array}{l} s = 2.5 \\ u = u \\ v = v_1 \\ a = g \\ t = \end{array} \right\} \begin{array}{l} v_1^2 = u^2 + 2as \\ v_1^2 = u^2 + 5g \\ v_1 = \sqrt{u^2 + 5g} \end{array}$$

$$I = m(v - u)$$

$$7 = 0.2(v - -v_1)$$

$$7 = 0.2(10 + \sqrt{u^2 + 5g})$$

$$35 = 10 + \sqrt{u^2 + 5g}$$

$$25 = \sqrt{u^2 + 5g}$$

$$u^2 + 5g = 625$$

$$u^2 = 576 \quad \therefore \boxed{u = 24}$$

b)

$$\left. \begin{array}{l} s = 1 \\ u = 10 \\ v = \\ a = -g \\ t = t \end{array} \right\}$$

$$s = ut + \frac{1}{2}at^2$$

$$1 = 10t - 4.9t^2$$

$$4.9t^2 - 10t + 1 = 0$$

By Quadratic Formula :

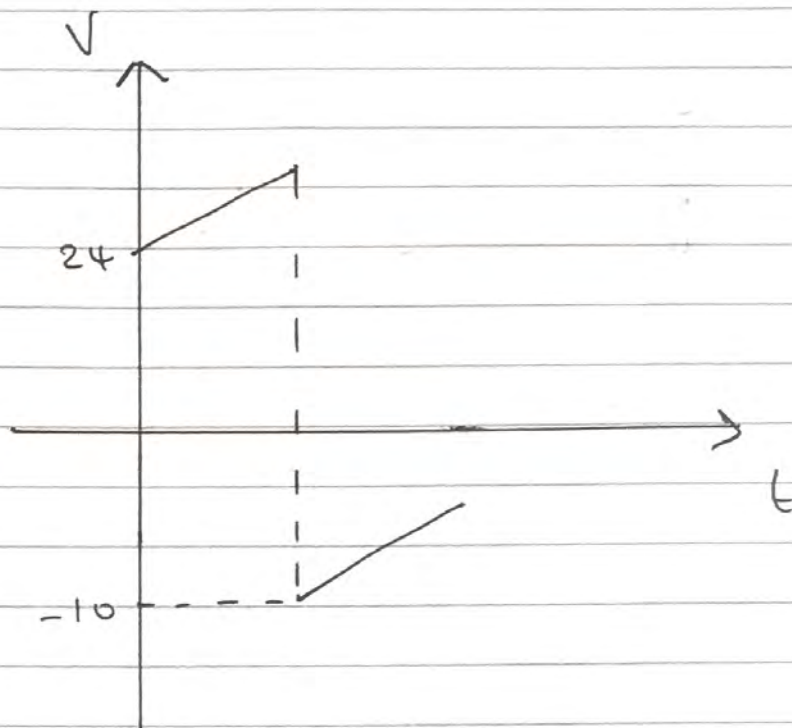
$$t = 1.94, \quad \boxed{0.105}$$

↑  
reject!

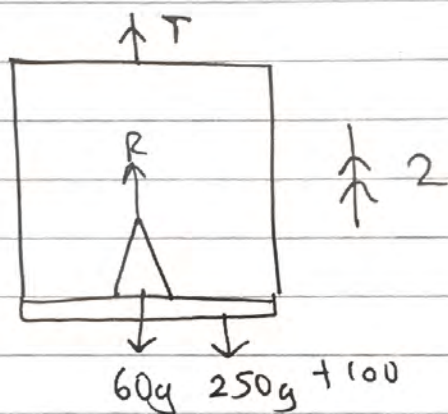
$$\underline{t = 0.11s}$$



c)



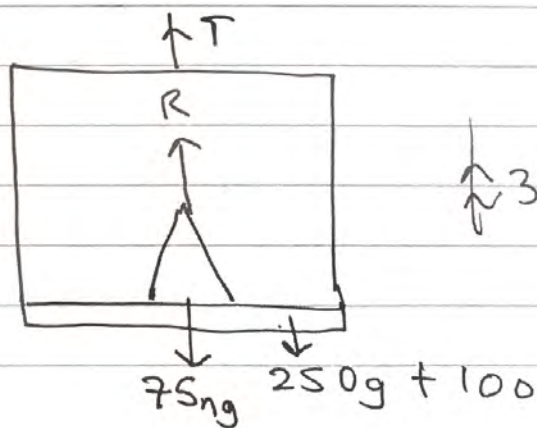
Q5a)



$$\text{N2L} \uparrow^+ (\text{woman}) : R - 60g = 60(2)$$

$$R = 60g + 120 = \boxed{708\text{N}}$$

b)



$$\uparrow^+ \quad \text{N2L(system)} : T - 250g - 100 = 7Sng = (250 + 75n)c$$

$T = 10000$  for max no. of occupants to be carried...

$$10000 - 250g - 100 = 7Sng + 250(3) + 75n(3)$$

$$6700 = n(75g + 3(75))$$

$$n = \frac{6700}{75g + 3(75)} = 6.979..$$

this isn't quite 7!

so max  $\boxed{n = 6}$

$$(Q6a) \quad F_1 + F_2 = R = \begin{pmatrix} 4 \\ -6 \end{pmatrix} + \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} p+4 \\ q-6 \end{pmatrix}$$

We are told  $R$  acts in the direction  $-2\mathbf{i} - \mathbf{j}$

$$\text{so} \dots \quad 2(q-6) = p+4$$

$\mathbf{i}$  component  $\Rightarrow 2q - 12 = p + 4$   
is double the  $\mathbf{j}$ .

$$\Rightarrow p - 2q = -16$$

b)  $q = 3 : p = 2q - 16 = 2(3) - 16 = -10 //$

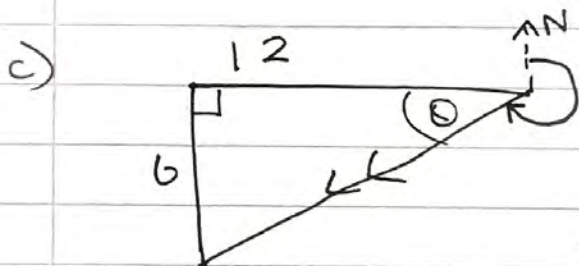
so  $R = \begin{pmatrix} -6 \\ -3 \end{pmatrix} = \Sigma F //$

$$\sum F = ma$$

$$|R| = \sqrt{6^2 + 3^2} = 3\sqrt{5}$$

$$R = ma ; \quad 3\sqrt{5} = 0.5a$$

$$\therefore a = 6\sqrt{5} = \boxed{13.4 \text{ ms}^{-2}}$$



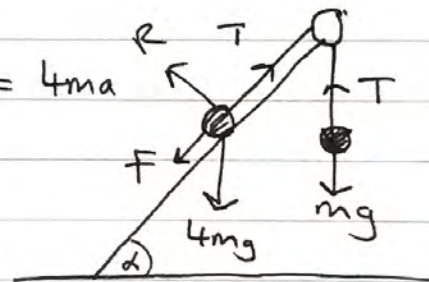
$$\tan \theta = \frac{6}{12} = \frac{1}{2}$$

$$\theta = \tan^{-1}\left(\frac{1}{2}\right) = 26.6^\circ$$

$$\text{Bearing: } 270 - 26.6 = \boxed{243^\circ}$$

(Q7a) Inextensible string

b) N2L(P)  $\downarrow$  :  $4mg \sin \alpha - T - F = 4ma$  (1)



N2L(Q)  $\uparrow$  :  $T - mg = ma$  (2)

c) (1) + (2) :  $4mg \sin \alpha - T + T - F - mg = 5ma$

$$\sin \alpha = \frac{3}{5} \quad \therefore \frac{12mg}{5} - F - mg = 5ma$$

$$F = \frac{1}{4}R, \quad R = 4mg \cos \alpha //$$

$$\therefore \frac{7}{5}mg - \frac{1}{4}(4mg)\left(\frac{4}{5}\right) = 5ma$$

$$\frac{3}{5}g = 5a \quad \therefore a = \boxed{\frac{3g}{25}} \text{ ms}^{-2}$$

d)  $\left. \begin{array}{l} S = h \\ u = 0 \\ v = v \\ a = \frac{3g}{25} \\ t = \end{array} \right\} \begin{array}{l} v^2 = u^2 + 2aS \\ v^2 = 0^2 + \frac{6gh}{25} \quad // \end{array}$

(For Q)  $\left. \begin{array}{l} S = s \\ u = \sqrt{\frac{6gh}{25}} \\ v = 0 \\ a = -g \\ t = \end{array} \right\} \begin{array}{l} v^2 = u^2 + 2aS \\ 0^2 = \frac{6gh}{25} - 2gs \end{array}$

(Q is under influence of g only)  $s = \frac{3h}{25} //$   
once P hits the ground.

so after P hits the ground (and string is not taut), Q travels an extra distance of  $\frac{3h}{25}$ .

Q does not reach the pulley so  $d >$  total distance travelled

$$\therefore d > \frac{3h}{25} + h$$

$$\boxed{d > \frac{28h}{25}}$$