

Question	Scheme	Marks
2(a)	$\frac{2}{\sqrt{1+3x}} = 2(1+3x)^{\left(-\frac{1}{2}\right)}$ $\{2\} \left(1 + \left(-\frac{1}{2}\right)(3x) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)(3x)^2}{2!} + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)(3x)^3}{3!} + \dots \right)$ $2 - 3x + \frac{27x^2}{4} - \frac{135x^3}{8} + \dots$	B1 M1A1 A1 [4]
(b)	$-\frac{1}{3} < x < \frac{1}{3} \quad \left(\text{Accept } x < \frac{1}{3}\right)$	B1 [1]
Total 5 marks		

Part	Mark	Notes
(a)	B1	Correct simplification of the given expression. This mark may be implied by a correct expansion.
	M1	Attempts at the binomial expansion $(1+3x)^{\pm\frac{1}{2}}$ or $2(1+3x)^{\pm\frac{1}{2}}$ For an attempt at the binomial expansion. <ul style="list-style-type: none"> The first term is 1 or 2 The powers of $3x$ are correct in all terms, e.g. $(3x)^2$ The correct denominators are used, $2!$ and $3!$ oe
	A1	Allow this mark for at least 1 correct algebraic term, correctly simplified, from $-3x + \frac{27x^2}{4} - \frac{135x^3}{8}$ or $-\frac{3}{2}x + \frac{27x^2}{8} - \frac{135x^3}{16}$
	A1	Correct simplified expansion in ascending order, coefficients must be in simplest fractions . (Ignore extra terms with powers > 3) Do not isw
(b)	B1	For the correct range of values of x . $-\frac{1}{3} < x < \frac{1}{3}$ or $ x < \frac{1}{3}$, do not accept $ 3x < 1$

ALT for (a) Uses **Maclaurin's expansion** (If seen send to review)

$$f(x) = f(0) + f'(0)x + \frac{f''(x)}{2!}x^2 + \frac{f'''(x)}{3!}x^3 + \dots$$

B1 Correct simplification of the given expression.

M1 Achieves $f'(x) = P(1+3x)^{-\frac{3}{2}}$, $f''(x) = Q(1+3x)^{-\frac{5}{2}}$, $f'''(x) = R(1+3x)^{-\frac{7}{2}}$, $P, Q, R \neq 0$ and attempts to find the values of $f'(0)$, $f''(0)$ and $f'''(0)$

A1 Correct unsimplified expansion OR at least 2 correct simplified terms

A1 Fully correct simplified expansion. (Ignore extra terms with powers higher than 3)

For reference, the correct derivatives are:

$$f'(x) = -3(1+3x)^{-\frac{3}{2}}, f''(x) = \frac{27}{2}(1+3x)^{-\frac{5}{2}}, f'''(x) = \frac{-405}{4}(1+3x)^{-\frac{7}{2}}$$