

## Assignment6

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```
getwd()  
## [1] "C:/Users/shari/OneDrive/Desktop/Business Analytics/QMM/Assignment6"  
setwd("C:/Users/shari/OneDrive/Desktop/Business Analytics/QMM/Assignment6")
```

### Question 2 - Research and Development Division of Emax Corporation

Based on the problem statement, the goal is to:

Maximize  $Z = P - 6C - 3D$

P = total (discounted) profit over the life of the new products, C = change (in either direction) in the current level of employment, D = decrease (if any) in next year's earnings from the current year's level.

Subject to:

Total Profit: Maximize  $P = 20X_1 + 15X_2 + 25X_3$

Employment Level:  $6X_1 + 4X_2 + 5X_3 = 50$

Earnings Next Year:  $8X_1 + 7X_2 + 5X_3 \geq 75$

As a result, the auxiliary variables become:

$Y_1 = 6X_1 + 4X_2 + 5X_3 - 50$   $Y_2 = 8X_1 + 7X_2 + 5X_3 - 75$

Which becomes:

$(Y_1P - Y_1M) = 6X_1 + 4X_2 + 5X_3 - 50$   $(Y_2P - Y_2M) = 8X_1 + 7X_2 + 5X_3 - 75$

Therefore, the final setup of the problem statement is:

Maximize  $Z = 20X_1 + 15X_2 + 25X_3 - 6Y_1P - 6Y_1M - 3Y_2M$

Subject to:

$6X_1 + 4X_2 + 5X_3 - (Y_1P - Y_1M) = 50$   $8X_1 + 7X_2 + 5X_3 - (Y_2P - Y_2M) = 75$

And:

$X_1, X_2, X_3 \geq 0$   $Y_1P, Y_1M, Y_2P, Y_2M \geq 0$

Lastly, we will run this problem in R as a linear programming model and discuss the results.

```
# This problem will require the "lpSolveAPI" library
require(lpSolveAPI)

## Loading required package: lpSolveAPI

## Warning: package 'lpSolveAPI' was built under R version 4.1.3

# Import the .lp file for this problem
lpm <- read.lp(filename="emax.lp",type = "lp")
# Return the linear programming model
lpm

## Model name:
##           X1      X2      X3      Y1P      Y1M      Y2M      Y2P
## Maximize   20      15      25      -6      -6      -3       0
## R1         6       4       5      -1       1       0       0 = 50
## R2         8       7       5       0       0       1      -1 = 75
## Kind       Std     Std     Std     Std     Std     Std     Std
## Type       Real    Real    Real    Real    Real    Real    Real
## Upper      Inf     Inf     Inf     Inf     Inf     Inf     Inf
## Lower      0       0       0       0       0       0       0

# Solve the linear programming model
solve(lpm)

## [1] 0

get.objective(lpm)

## [1] 225

get.variables(lpm)

## [1] 0 0 15 25 0 0 0
```

Based on the output of the linear programming model, we can conclude several things.

$X1 = 0$   $X2 = 0$   $X3 = 15$   $Y1P = 25$   $Y1M = 0$   $Y2M = 0$   $Y2P = 0$

Therefore, we can infer that only product 3 should be included in the product mix. This combination would result in an object value of 225 units. The employment level goal will be exceeded by 25 units, or 2,500 employees, which will result in a 150 unit penalty for the objective function and a full achievement of the earnings goal for the upcoming year.