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1. Back Savers is a company that produces backpacks primarily for students. They are considering offering some combination of two different models—the Collegiate and the Mini. Both are made from the same rip-resistant nylon fabric. Back Savers has a long-term contract with a supplier of the nylon and receives a 5000 square-foot shipment of the material each week. Each Collegiate requires 3 square feet while each Mini requires 2 square feet. The sales forecasts indicate that at most 1000 Collegiates and 1200 Minis can be sold per week. Each Collegiate requires 45 minutes of labor to produce and generates a unit profit of \$32. Each Mini requires 40 minutes of labor and generates a unit profit of \$24. Back Savers has 35 laborers that each provides 40 hours of labor per week. Management wishes to know what quantity of each type of backpack to produce per week.

a. Clearly define the decision variables

X and Y are the decision variables - A represents collegiate and B is Mini

b. What is the objective function?

The main objective function is to maximize the profit of the company,

$$\text{Profit } P = 32A + 24B$$

c. What are the constraints?

Back Saver sells Collegiate and Mini. Let's say Collegiate is A and Mini is B.

Each Collegiate requires 3 square feet and Mini required 2 square feet and Back Savers receives 5000 square feet material each week.

$$3A + 2B \leq 5000$$

Collegiate produces 32\$ profit and required 45 minutes labor.

Mini produces 24\$ profit and required 40 minutes labor

$$\text{Profit } P = 32X + 24Y$$

Total labor required is $(45A + 40B)$ minutes

Available labor is $35 \times 40 = 1400$ hours

$$= 84000 \text{ minutes}$$

$$45A + 40B \leq 84000 \text{ minutes per week.}$$

Sales forecasts indicate that at most 1000 Collegiates and 1200 Minis can be sold per week

$$A \leq 1000$$

$$B \leq 1200$$

And Variables must be greater than 0,

$$A, B \geq 0$$

d. Write down the full mathematical formulation for this LP problem.

$$P = 32A + 24B$$

$$3A + 2B \leq 5000$$

$$45A + 40B \leq 84000 \text{ minutes per week}$$

$$A \leq 1000$$

$$B \leq 1200$$

2. The Weigelt Corporation has three branch plants with excess production capacity. Fortunately, the corporation has a new product ready to begin production, and all three plants have this capability, so some of the excess capacity can be used in this way. This product can be made in three sizes--large, medium, and small--that yield a net unit profit of \$420, \$360, and \$300, respectively. Plants 1, 2, and 3 have the excess capacity to produce 750, 900, and 450 units per day of this product, respectively, regardless of the size or combination of sizes involved. The amount of available in-process storage space also imposes a limitation on the production rates of the new product. Plants 1, 2, and 3 have 13,000, 12,000, and 5,000 square feet, respectively, of in-process storage space available for a day's production of this product. Each unit of the large, medium, and small sizes produced per day requires 20, 15, and 12 square feet, respectively. Sales forecasts indicate that if available, 900, 1,200, and 750 units of the large, medium, and small sizes, respectively, would be sold per day. At each plant, some employees will need to be laid off unless most of the plant's excess production capacity can be used to produce the new product. To avoid layoffs if possible, management has decided that the plants should use the same percentage of their excess capacity to produce the new product. Management wishes to know how much of each of the sizes should be produced by each of the plants to maximize profit.

a. Clearly define the decision variables

Decision variables:

Let's say Y_{ij} , where i represents plants 1,2,3 and j represents size l, m, s.

Y_{1l} , Y_{1m} , Y_{1s} variables for plant 1

Y_{2l} , Y_{2m} , Y_{2s} variables for plant 2

Y3l, Y3m, Y3s variables for plant 3

b. Formulate the linear programming model for this problem.

Zmax is the maximum profit

Net unit profit of \$420, \$360, and \$300

$$Z_{\max} = 420(Y_{1l} + Y_{2l} + Y_{3l}) + 360(Y_{1m} + Y_{2m} + Y_{3m}) + 300(Y_{1s} + Y_{2s} + Y_{3s})$$

Since, plants 1, 2, and 3 have the excess capacity to produce 750, 900, and 450

Constraints for Max capacity:

$$Y_{1l} + Y_{1m} + Y_{1s} \leq 750$$

$$Y_{2l} + Y_{2m} + Y_{2s} \leq 900$$

$$Y_{3l} + Y_{3m} + Y_{3s} \leq 450$$

Plants 1, 2, and 3 have 13,000, 12,000, and 5,000 square feet, respectively, of in-process storage space available for days production:

Storage space:

$$20*Y_{1l} + 15*Y_{1m} + 12*Y_{1s} \leq 13000$$

$$20*Y_{2l} + 15*Y_{2m} + 12*Y_{2s} \leq 12000$$

$$20*Y_{3l} + 15*Y_{3m} + 12*Y_{3s} \leq 5000$$

900, 1,200, and 750 units of the large, medium, and small sizes, respectively, would be sold per day

$$900*(Y_{1l} + Y_{1m} + Y_{1s}) - 750*(Y_{2l} + Y_{2m} + Y_{2s}) = 0$$

$$450*(Y_{2l} + Y_{2m} + Y_{2s}) - 900*(Y_{3l} + Y_{3m} + Y_{3s}) = 0$$

$$450*(Y_{1l} + Y_{1m} + Y_{1s}) - 750*(Y_{3l} + Y_{3m} + Y_{3s}) = 0$$

$$Y_{1l} + Y_{2l} + Y_{3l} \leq 900$$

$$Y_{1m} + Y_{2m} + Y_{3m} \leq 1200$$

$$Y_{1s} + Y_{2s} + Y_{3s} \leq 750$$

$$Y_{ij} \geq 0 \text{ where } i = 1, 2, 3 \text{ and } j = l, m, s$$

R Code for LP Model

Sbaig1_Assignment2

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```
library(lpSolveAPI)

## Warning: package 'lpSolveAPI' was built under R version 4.1.3

setwd("C:/Users/shari/OneDrive/Desktop/Business Analytics/QMM/Assignment2")

##a linear program with 9 decision variables and 0 constraints

lp <- make.lp(0,9, verbose = "neutral")
lp

## Model name:
## a linear program with 9 decision variables and 0 constraints

## Model name:
## a linear program with 9 decision variables and 0 constraints
## Add the constraints
add.constraint(lp, c(1,1,1,0,0,0,0,0,0), "<=", 750 )
add.constraint(lp, c(0,0,0,1,1,1,0,0,0), "<=", 900)
add.constraint(lp, c(0,0,0,0,0,0,1,1,1), "<=", 450)
add.constraint(lp, c(20,15,12,0,0,0,0,0,0), "<=", 13000)
add.constraint(lp, c(0,0,0,20,15,12,0,0,0), "<=", 12000)
add.constraint(lp, c(0,0,0,0,0,0,20,15,12), "<=", 5000)
add.constraint(lp, c(1,1,1,0,0,0,0,0,0), "<=", 900)
add.constraint(lp, c(0,0,0,1,1,1,0,0,0), "<=", 1200)
add.constraint(lp, c(0,0,0,0,0,0,1,1,1), "<=", 750)
add.constraint(lp, c(6, 6, 6, -5, -5, -5, 0, 0, 0), "=", 0)
add.constraint(lp, c( 3, 3, 3, 0, 0, 0, -5, -5, -5), "=", 0)

## Create objective function. We need maximum profit so change sense to max
set.objfn(lp, c(420,360,300,420,360,300,420,360,300))
lp.control(lp, sense='max')

## $anti.degen
## [1] "none"
##
## $basis.crash
## [1] "none"
##
```

```

## $bb.depthlimit
## [1] -50
##
## $bb.floorfirst
## [1] "automatic"
##
## $bb.rule
## [1] "pseudononint" "greedy"          "dynamic"          "rcostfixing"
##
## $break.at.first
## [1] FALSE
##
## $break.at.value
## [1] 1e+30
##
## $epsilon
##      epsb      epsd      epsel      epsint  epsperturb  epspivot
##      1e-10      1e-09      1e-12      1e-07      1e-05      2e-07
##
## $improve
## [1] "dualfeas" "thetagap"
##
## $infinite
## [1] 1e+30
##
## $maxpivot
## [1] 250
##
## $mip.gap
## absolute relative
##      1e-11      1e-11
##
## $negrange
## [1] -1e+06
##
## $obj.in.basis
## [1] TRUE
##
## $pivoting
## [1] "devex"      "adaptive"
##
## $presolve
## [1] "none"
##
## $scalelimit
## [1] 5
##
## $scaling
## [1] "geometric"  "equilibrate" "integers"
##

```

```
## $sense
## [1] "maximize"
##
## $simplextype
## [1] "dual" "primal"
##
## $timeout
## [1] 0
##
## $verbose
## [1] "neutral"
```

To identify the variables and constraints, Set the variable names and the constraints

```
## set.bounds(lp, lower = c(0, 0, 0, 0, 0, 0, 0, 0, 0), columns = c(1,2,3,4,5,6,7,8,9))
RowNames <- c("Con1", "Con2", "Con3", "storage1", "Storage2", "Storage33", "Sale1", "Sale2", "Sale3", "%C1", "%C2")
ColNames <- c("Large1", "Medium1", "Small1", "Large2", "Medium2", "Small2", "Large3", "Medium3", "Small3")
dimnames(lp) <- list(RowNames, ColNames)
lp

## Model name:
## a linear program with 9 decision variables and 11 constraints

## Model name:
## a linear program with 9 decision variables and 11 constraints
write.lp(lp, filename = "QMMAssignment2.lp", type = "lp")
solve(lp)

## [1] 0

## [1] 0
get.objective(lp)

## [1] 696000

## [1] 696000
get.variables(lp)

## [1] 516.6667 177.7778 0.0000 0.0000 666.6667 166.6667 0.0000 0.0000 0
## [9] 416.6667

## [1] 516.6667 177.7778 0.0000 0.0000 666.6667 166.6667 0.0000 0.0000 0
## [9] 416.6667
```