

UNIT 4 HOMEWORK

For some problems, you will need a normal probability calculator or chart. Here are some links:

Graphical standard normal calculator/chart:

<http://www.mathsisfun.com/data/standard-normal-distribution-table.html>

Simple standard normal calculator:

<http://stattrek.com/online-calculator/normal.aspx>

Question 1:

The following table shows a discrete probability distribution.

x	p(x)
0	0
1	.1
2	.2
3	.4
4	.1
5	.2

Find the expected value (mean) of this probability distribution. Please round to 1 decimal place.

Question 2:

The following table shows a discrete probability distribution.

x	p(x)
0	0
1	.1
2	.2
3	.4
4	.1
5	.2

Find the standard deviation. Please round to 2 decimal places.

Question 3:

If spine bone density is normally distributed in young women with a mean of 1.0 g/cm² and a standard deviation of .10 g/cm², then how many young women out of 100 would you expect to have bone densities less than .85 g/cm²?

Round to the nearest whole number.

Question 4:

If spine bone density is normally distributed in young women with a mean of 1.0 g/cm^2 and a standard deviation of $.10 \text{ g/cm}^2$, then how many young women out of 100 would you expect to have bone densities greater than 1.15 g/cm^2 ?

Round to the nearest whole number.

Question 5:

If the relative frequency of boys among newborn children in the USA is $.513$, what's the probability that exactly 4 of the next 5 births will be boys?

Answer as a percentage and round to the nearest tenth but do not include the % sign.

Question 6:

On a midterm exam, a particular class ended up with a mean raw score of 80 with a standard deviation of 10. The distribution of grades in the class was approximately normal. If the teacher wants to give A's to the top 25th percentile (top 25%) of the class, what is the lowest raw score you could get and still get an A on the exam? (Hint: go backwards from the probability to the Z score.)

Round your answer to the nearest hundredth.

Question 7:

A doctor performs 8 operations in a given day. Assume that the operations are independent, and each operation is a success with probability 0.95 . What's the probability that the doctor has exactly two failed operations on any given day? Calculate the exact binomial probability (do not use the normal approximation).

Please answer as a percentage and round your answer to the nearest tenth, but do not include the % sign.

Question 8:

A doctor performs 8 operations in a given day. Assume that the operations are independent, and each operation is a success with probability 0.95 . What's the probability that the doctor has two or more failed operations on any given day? Calculate the exact binomial probabilities (do not use the normal approximation).

Please answer as a percentage and round your answer to the nearest tenth (do not include the % sign).

Question 9:

You are playing a game that consists of rolling 4 dice at a time. You win the game if you roll at least 3 sixes. You have to pay \$50 to play each round, but you win \$1,000,000 if you win. TRUE or FALSE, the expected value of this game is negative.

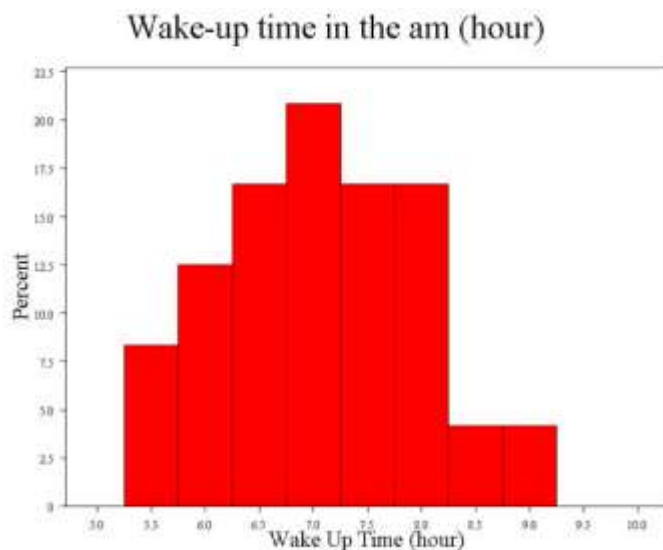
1. True
2. False

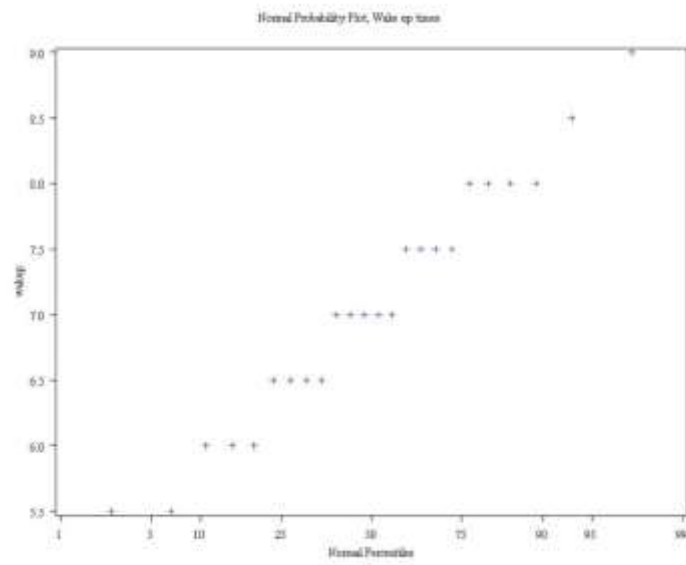
Question 10:

In a randomized trial, 200 subjects were to be randomly assigned either to the drug treatment group or to the placebo group. Researchers flipped a coin to decide each participant's treatment assignment. After randomization, 112 subjects were in the treatment group and 88 were in the control group. What's the probability that **112 or more** subjects could end up in the treatment group purely by chance? Hint: use a normal approximation to the binomial. Please answer as a percentage and round your answer to the nearest hundredth. Do not include the % sign.

Question 11:

Below are the histogram, normal probability plot, and results from a formal tests of normality for the variable wake-up times from a dataset where $n=24$





Formal test of normality:

$p > .25$

TRUE or FALSE: Wake-up times approximately follow a normal distribution.

1. True
2. False