

Statistics for Health Care

("Statistics in Medicine" Christen Sainani @ Stanford University)

Unit 1 Overview/Teasers



First rules of statistics...

Use common sense!

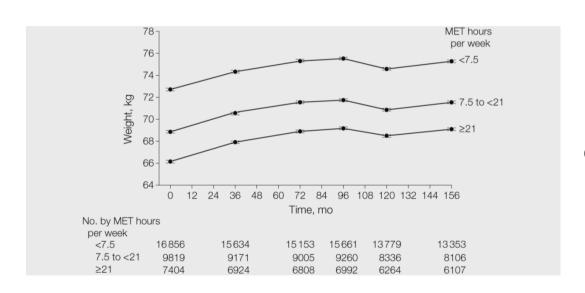
Draw lots of pictures!

What's wrong with this?

- Study with sample size of 10 (N=10)
- Results: "Objective scoring by blinded investigators indicated that the treatment resulted in improvement in all (100%) of the subjects. Of patients showing overall improvement, 78% were graded as having either excellent or moderate improvement."



Take-home message?



Do the three groups differ meaningfully in weight change over time?



 How to think about, look at, and describe data

Teaser 1, Unit 1

- Hypothetical randomized trial comparing two diets:
- Those on diet 1 (n=10) lost an average of 34.5 lbs.
- Those on diet 2 (n=10) lost an average of 18.5 lbs.
- Conclusion: diet 1 is better?

Teaser 2, Unit 1

- "400 shades of lipstick found to contain lead", FDA says" Washington Post, Feb. 14, 2012
- "What's in Your Lipstick? FDA Finds Lead in 400 Shades," *Time.com* February 15, 2012

How worried should women who use lipstick be?



Statistics for Health Care

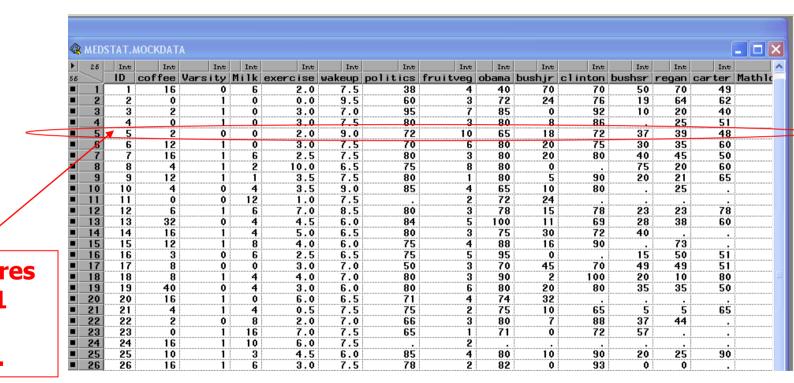
Introduction to Data

Example Data

- Data compiled from previous Stanford students (anonymous, non-identifiable)
- Sample size = 50

Example Data Set

MED:	STAT.	MOCKDAT														×
25	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int		
	ID	coffee	Varsity	Milk	exercise	wakeup	politics	fruitveg	obama	bushjr	clinton	bushsr	regan	carter	Mathl	C
1	1	16	0	6	2.0	7.5	38	4	40	70	70	50	70	49		
2	2	0	1	0	0.0	9.5	60	3	72	24	76	19	64	62		
3	3	2	1	0	3.0	7.0	95	7	85	0	92	10	20	40		
4	4	0	1	0	3.0	7.5	80	3	80	8	86		25	51		
5	5	2	0	0	2.0	9.0	72	10	65	18	72	37	39	48		
6	6	12	1	0	3.0	7.5	70	6	80	20	75	30	35	60		
7	7	16	1	6	2.5	7.5	80	3	80	20	80	40	45	50		
8	8	4	1	2	10.0	6.5	75	8	80	0		75	20	60		
9	9	12	1	1	3.5	7.5	80	1	80	5	90	20	21	65		
10	10	4	0	4	3.5	9.0	85	4	65	10	80		25			
11	11	0	0	12	1.0	7.5		2	72	24						
12	12	6	1	6	7.0	8.5	80	3	78	15	78	23	23	78		
13	13	32	0	4	4.5	6.0	84	5	100	11	69	28	38	60		
14	14	16	1	4	5.0	6.5	80	3	75	30	72	40				
15	15	12	1	8	4.0	6.0	75	4	88	16	90		73			
16	16	3	0	6	2.5	6.5	75	5	95	0		15	50	51		
17	17	8	0	0	3.0	7.0	50	3	70	45	70	49	49	51		
18	18	8	1	4	4.0	7.0	80	3	90	2	100	20	10	80		
19	19	40	0	4	3.0	6.0	80	6	80	20	80	35	35	50		
20	20	16	1	0	6.0	6.5	71	4	74	32						
21	21	4	1	4	0.5	7.5	75	2	75	10	65	5	5	65		_
22	22	2	0	8	2.0	7.0	66	3	80	7	88	37	44			_
23	23	0	1	16	7.0	7.5	65	1	71	0	72	57				
24	24	16	1	10	6.0	7.5		2								_
25	25	10	1	3	4.5	6.0	85	4	80	10	90	20	25	90		_
26	26	16	1	6	3.0	7.5	78	2	82	0	93	0	0			
27	27	12	1	5	2.0	7.5	64	4	66	37	61					
28	28	12	1	12	12.0	7.0	67	4	71	14	73	12	18			



Each row stores the data for 1 student (1 observation). Each column stores the values for 1 variable (e.g., ounces of coffee per day).

a	MED	CTAT2	москрат	-Λ												
P	25	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	ال ال
<u>.</u> 56	\"							politics								Mathle
	1	1	16	0		2.0	7.5	38	4	40	70			70	49	
	2	2	0		. 	0.0	9.5	60	3	72	24	76	19	64	62	
3	3	3	2	1		3.0	7.0	95	7	85	0	92		20	40	
3	4	4	0	1		3.0	7.5	80	3	80	8	86		25	51	
1	5	5	2	0	0	2.0	9.0	72	10	65	18	72	37	39	48	
1	6	6	12	1	0	3.0	7.5	70	6	80	20	75	30	35	60	
1	7	7	16	1	6	2.5	7.5	80	3	80	20	80	40	45	50	
1	8	8	4	1	2	10.0	6.5	75	8	80	0		75	20	60	
1	9	9	12	1	1	3.5	7.5	80	1	80	5	90	20	21	65	
I	10	10	4	0	4	3.5	9.0	85	4	65	10	80		25		
I	11	11	0	0	12	1.0	7.5		2	72	24					
ij	12	12	6	1	6	7.0	8.5	80	3	78	15	78	23	23	78	
I	13	13	32	0	4	4.5	6.0	84	5	100	11	69	28	38	60	
ji	14	14	16	1	4	5.0	6.5	80	3	75	30	72	40			
I	15	15	12	1	8	4.0	6.0	75	4	88	16	90		73		
	16	16	3	0	6	2.5	6.5	75	5	95	0		15	50	51	
	17	17	8	0	0	3.0	7.0	50	3	70	45	70	49	49	51	
1	18	18	8	1	4	4.0	7.0	80	3	90	2	100	20	10	80	
I	19	19	40	0	4	3.0	6.0	80	6	80	20	80	35	35	50	
I	20	20	16	1	0	6.0	6.5	71	4	74	32					
l	21	21	4	1	4	0.5	7.5	75	2	75	10	65	5	5	65	
l	22	22	2	0	8	2.0	7.0	66	3	80	7	88	37	44		
	23	23	0	1	16	7.0	7.5	65	1	71	0	72	57			
I	24	24	16	1	10	6.0	7.5		2							
	25	25	10	1	3	4.5	6.0	85	4	80	10	90	20	25	90	
	26	26	16	1	6	3.0	7.5	78	2	82	0	93	0	0		
jj	27	27	12	1	5	2.0	7.5	64	4	66	37	61				
	28	28	12	1	12	12.0	7.0	67	4	71	14	73	12	18		
	29	29	20	0	0	2.0	5.5	39	3	32	29	61	39	76	47	
	30	30	\ 2	1	50	7.0	5.0	27	5	59	96	92	90	11	12	
j	31	31	12	0	6	2.5	7.0	99	1	100	10	80	1	1	8	
	32	32	\ /0	0	16	8.0	7.0	82	1	90	0	86	1	4	8	
ı	33	33	12	1	0	3.0	9.0	72	5	82	22	72	3	4	4	

Missing Data!

🔉 MED	STAT.	MOCKDAT	A												
25	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	Int	
5.5	ID	coffee	Varsity	Milk	exercise	wakeup	politics	fruitveg	obama	bushjr	clinton	busisr	kegan	carter	Mathle
1	1	16	0		2.0	7.5	38	4	40	70	70	50		49	
2	2	0	1	0	0.0	9.5	60	3	72	24	76	19	64	62	
3	3	2	1	0	3.0	7.0	95	7	85	0	92	10	20	40	
4	4	0	1	0	3.0	7.5	80	3	80	8	86	.	25	51	
5	5	2	0	0	2.0	9.0	72	10	65	18	72	37	39	48	
6	6	12	1	0	3.0	7.5	70	6	80	20	75	30	35	60	
7	7	16	1	6	2.5	7.5	80	3	80	20	80	40	45	50	
8	8	4	1	2	10.0	6.5	75	8	80	0		75	20	\ 60	
9	9	12	1	1		7.5	80	1	80	5	90	20	·····	65	
10	10	4	0	. . .	3.5	9.0	85	4	65	10	80	▼.	25		
_11	11		.: .	12	1.0	7.5		2	72	24					
12	12	······ ·		6	7.0	8.5	80	3	78	15	78	23	·····	78	
13	13		0	4	4.5	6.0	84	5	100	11	69	28		60	
14	14		1	4		6.5	80	3	.i	30	72	40	. . .		
15	15		1	8	4.0	6.0	75	4	88	16	90		73		
16	16	·•			2.5	6.5	75	5		0		15	50	51	
17	17			0		7.0	50	3	70	45	70	49	.i	51	
18	18		. <u>.</u> .	4		7.0	80	3		2	100	20		80	
19	19					6.0	80	6	80	20	80	35	35	50	
20	20		1	0	6.0	6.5	71	4	74	32		<u>.</u>	<u>.</u>	•	
21	21			4		7.5	75	2	75	10	65	5	·•···· -	65	
22	22	.i .		.	2.0	7.0	66	3	80	7	88	37	44	•	
23	23	.	·[·······	16	7.0	7.5	65	1	71	0	72	57	·		
24	24		1	10	6.0	7.5	<u>.</u>	2			<u>.</u>		<u>.</u>		
25	25			3	4.5	6.0	85	4	80	10	90	20		90	
26	26		1	6	3.0	7.5	78	2	82	0	93	0	0		
27	27		1	5	2.0	7.5	64	4	66	37	61	<u>.</u>			
28	28	·····	1	12	12.0	7.0	67	4	71	14	73	12		<u> </u>	
29	29	20	0	0	2.0	5.5	39	3	32	29	61	39	76	47	



Statistics for Health Care

Module 2:

Types of Data

Types of data

- Quantitative
- Categorical (bin ary, nominal or ordinal)
- Time-to-event

Quantitative variable

- Numerical data that you can add, subtract, multiply, and divide
- Examples:
 - Age
 - Blood pressure
 - BMI
 - Pulse
- Examples from our example data:
 - Optimism on a 0 to 100 scale
 - Exercise in hours per week
 - Coffee drinking in ounces per day

Quantitative variable

- Continuous vs. Discrete
 - Continuous: can theoretically take on any value within a given range (e.g., height=68.99955... inches)
 - Discrete: can only take on certain values (e.g., count data)

Categorical Variables

- Binary = two categories
 - Dead/alive
 - Treatment/placebo
 - Disease/no disease
 - Exposed/Unexposed
 - Heads/Tails
 - Example data: played varsity sports in high school (yes/no)

Categorical Variables

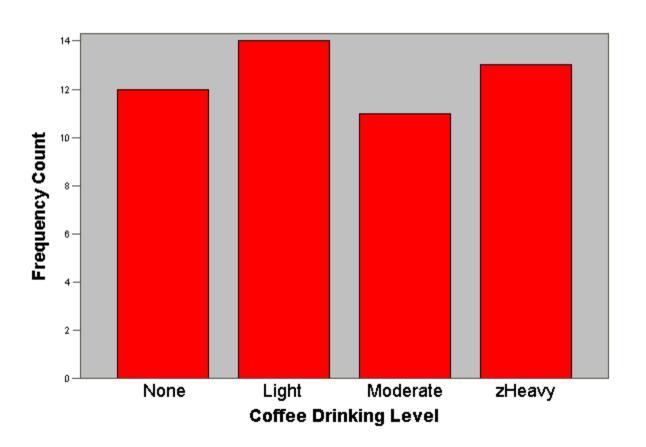
- Nominal = unordered categories
 - The blood type of a patient (O, A, B, AB)
 - Marital status
 - Occupation

Categorical Variables

Ordinal = Ordered categories

- Staging in breast cancer as I, II, III, or IV
- Birth order—1st, 2nd, 3rd, etc.
- Letter grades (A, B, C, D, F)
- Ratings on a Likert scale (e.g., strongly agree, agree, neutral, disagree, strongly disagree)
- Age in categories (10-20, 20-30, etc.)
- Example data: non-drinker, light drinker, moderate drinker, and heavy drinker of coffee

Coffee Drinking Categories (Ordinal)





- The time it takes for an event to occur, if it occurs at all
- Hybrid variable—has a continuous part (time) and a binary part (event: yes/no)
- Only encountered in studies that follow participants over time such as cohort studies and randomized trials
- Examples:
 - Time to death
 - Time to heart attack
 - Time to chronic kidney disease



Statistics for Health Care

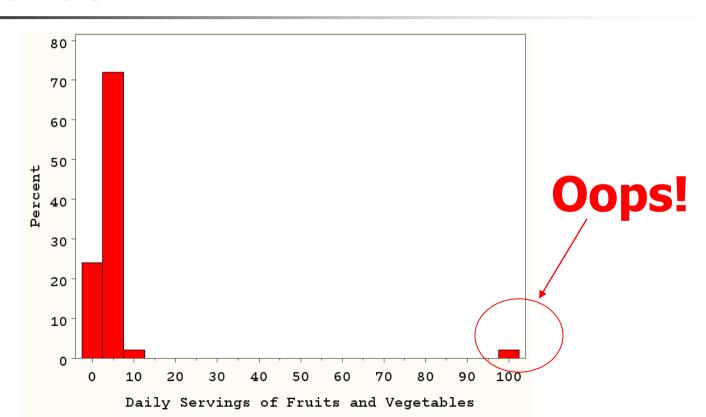
Module 3:

Looking at Data

Always Plot Your Data!

- ✓ Are there "outliers"? **somethings that abnormal
- ✓ Are there data points that don't make sense?
- ✓ How are the data distributed?

Are there points that don't make sense?





How are the data distributed?

Categorical data:

• What are the N's and percents in each category?

Quantitative data:

- What's the shape of the distribution (e.g., is it normally distributed or skewed)?
- Where is the center of the data?
- What is the spread/variability of the data?

Frequency Plots (univariate)

Categorical variables

Bar Chart

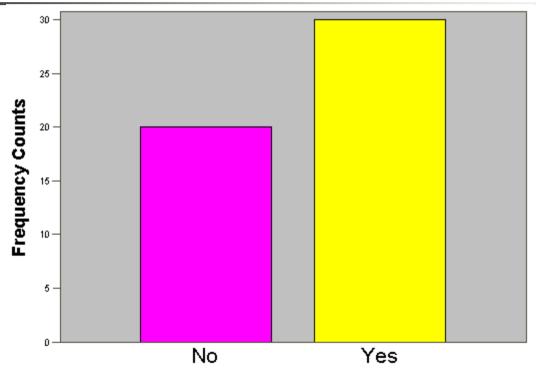
Quantiative/continuous variables

- Box Plot
- Histogram



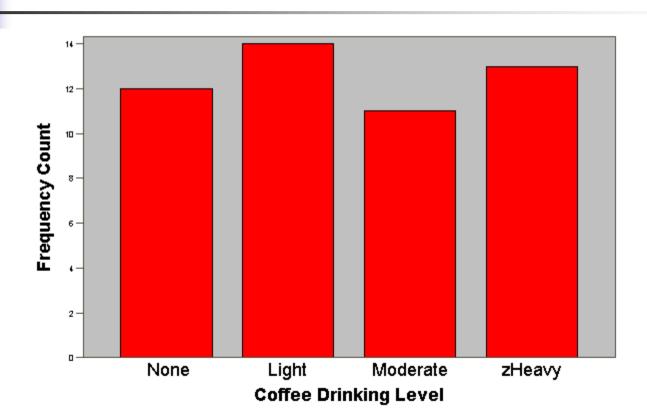
 Used for categorical variables to show frequency or proportion in each category.

Bar Chart: categorical variables



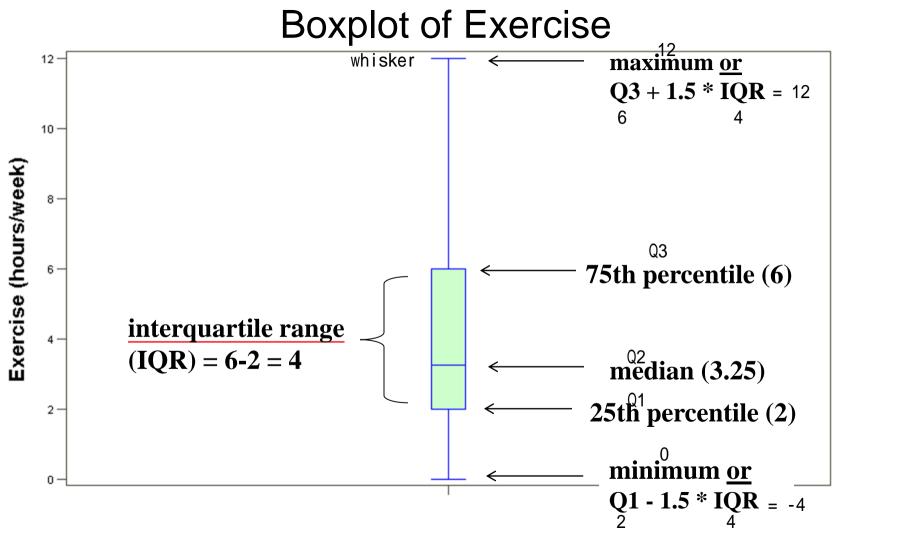
Played Varsity Sports in High School?

Bar Chart: categorical variables

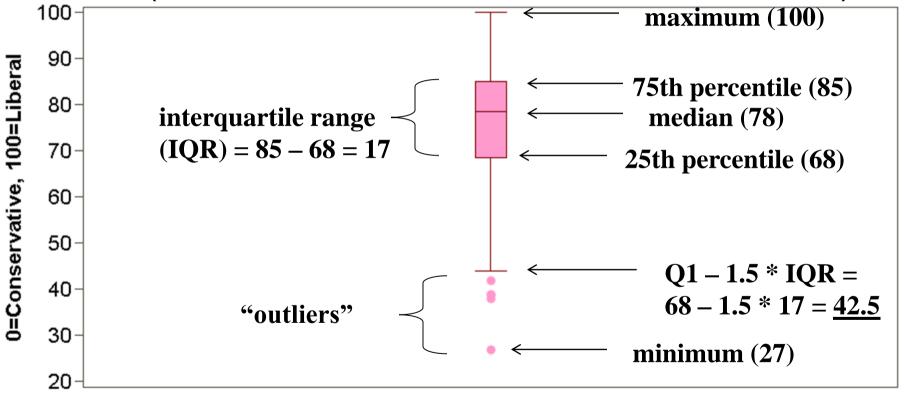


Box plot and histograms: for quantitative variables

 To show the <u>distribution</u> (shape, center, range, variation) of quantitative variables.



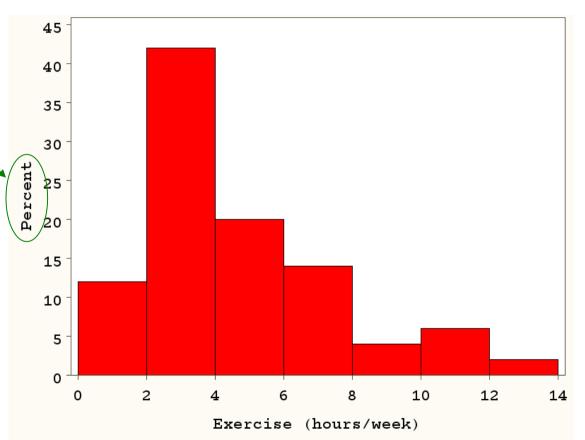
Boxplot of Political Bent (0=Most Conservative, 100=Most Liberal)



Y-axis: The percent of observations that fall within each bin.

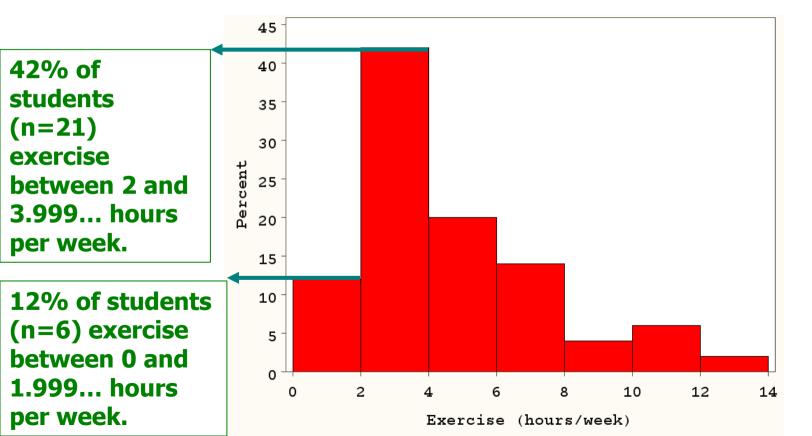
Histogram of Exercise

Bins of size = 2 hours/week



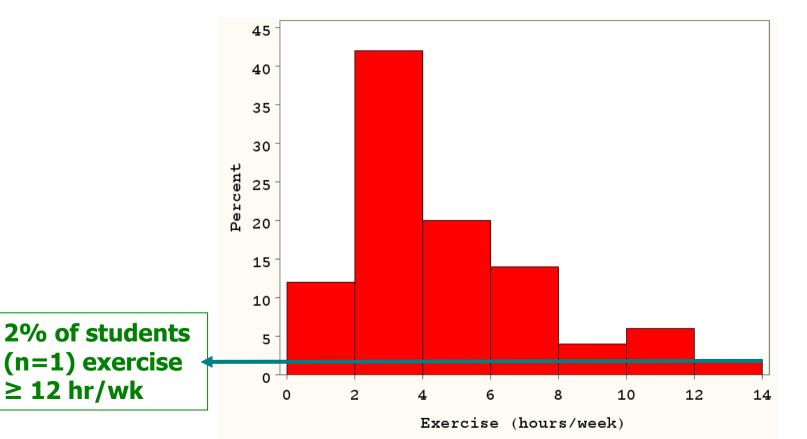
Histogram of Exercise

Bins of size = 2 hours/week



Histogram of Exercise

Bins of size = 2 hours/week



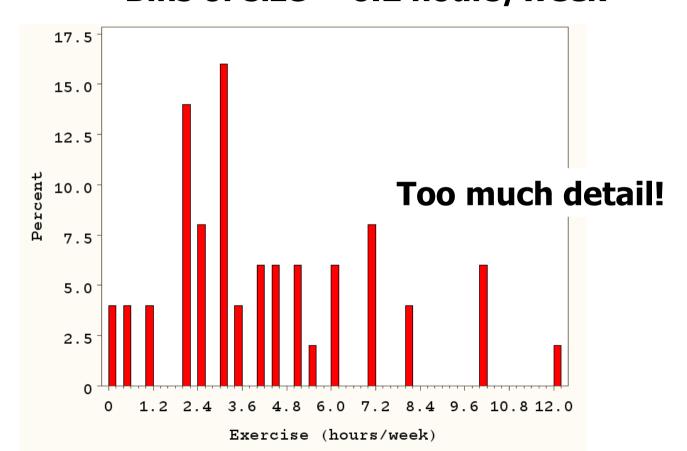
≥ 12 hr/wk

Histogram of Exercise

Bins of size = 2 hours/week



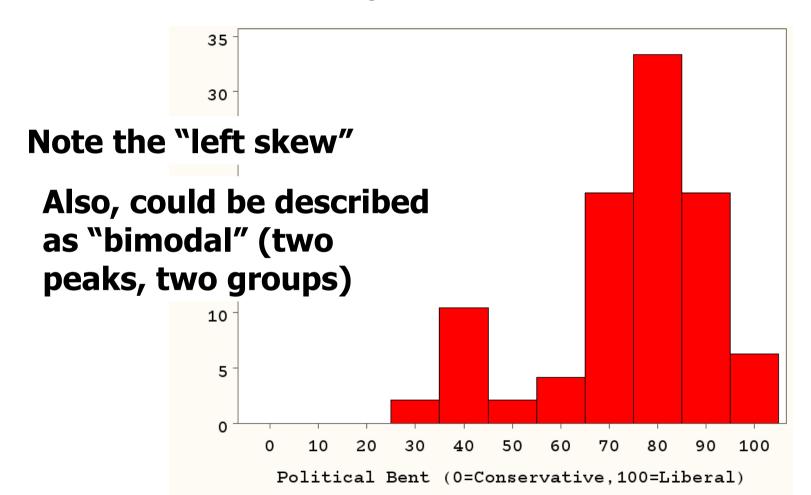
Histogram of Exercise Bins of size = 0.2 hours/week



Histogram of Exercise Bins of size = 8 hours/week



Histogram of Political Bent





Shape of a Distribution

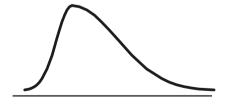
Left-skewed/right-skewed/symmetric

Left-Skewed

Symmetric



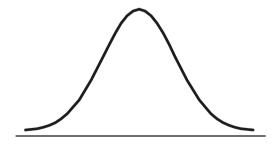
Right-Skewed



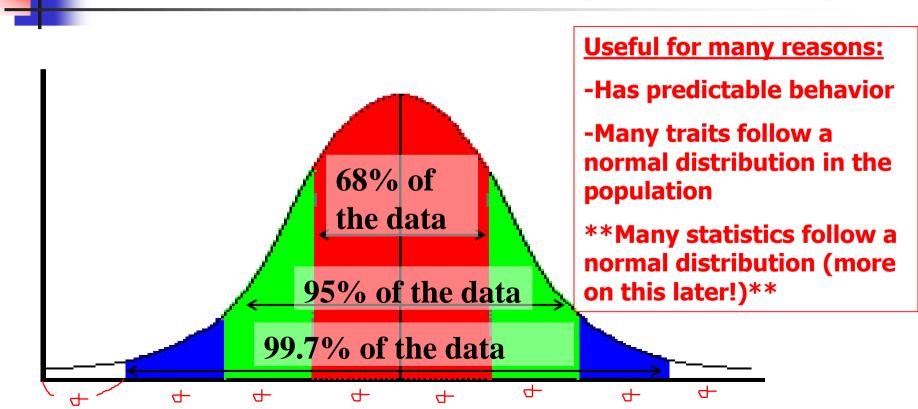


Shape of a Distribution

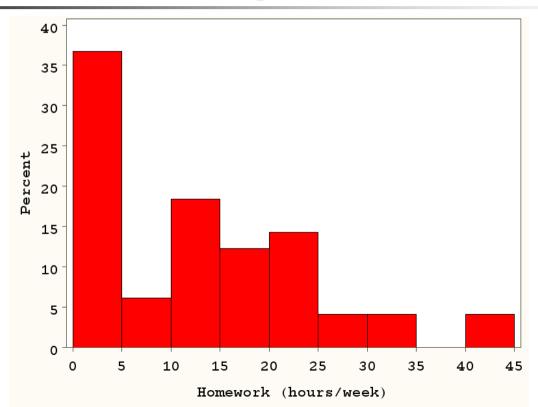
- Symmetric
- Gaussian
- Bell curve ("normal distribution")



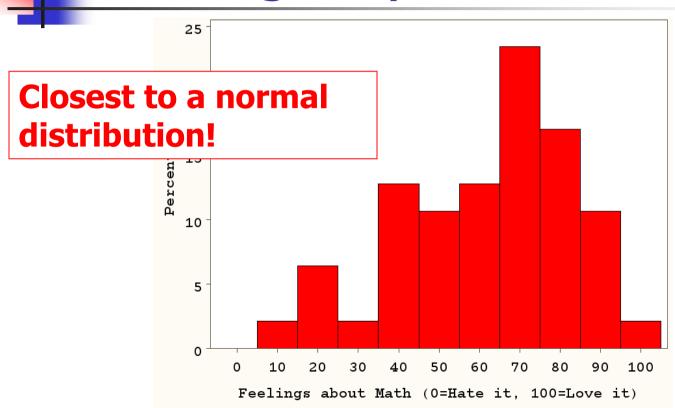
Normal distribution (bell curve)



Homework (hours/week)...



Feelings about math (0=lowest, 100=highest)





Statistics for Health Care

Describing Quantitative Data: Where is the center?



Measures of "central tendency"

- Mean
- Median

Mean

Mean – the average; the balancing point

calculation: the sum of values divided by the sample size

In math shorthand: \overline{X}

$$\overline{X} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

-

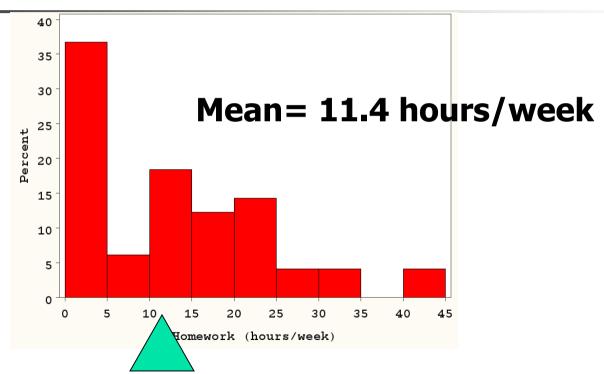
Mean: example

Some data:

Age of participants: 17 19 21 22 23 23 38

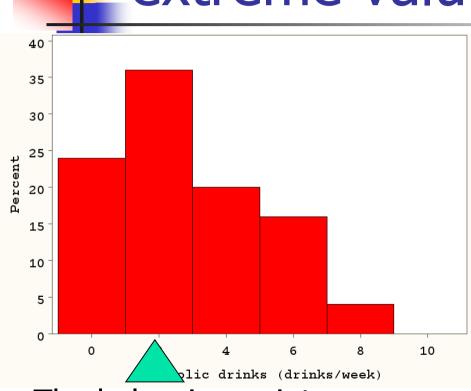
$$\overline{X} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{17 + 19 + 21 + 22 + 23 + 23 + 23 + 38}{8} = 23.25$$

Mean of homework



The balancing point

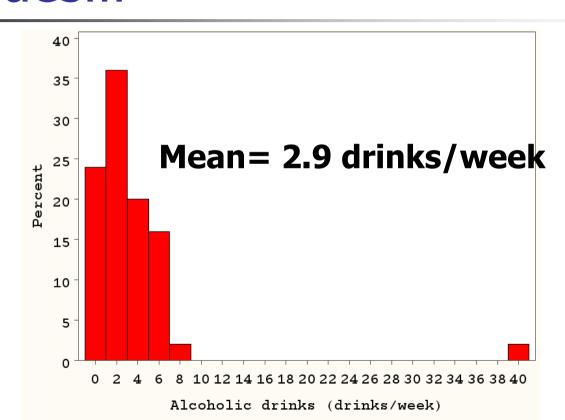
The mean is affected by extreme values...



Mean = 2.3 drinks/week

The balancing point

The mean is affected by extreme values...

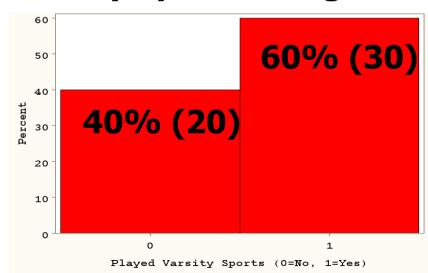


Does a binary variable have a mean?

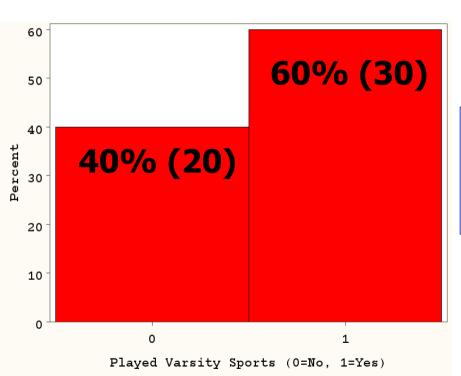
Yes! If coded as a 0/1 variable...

Example: Played Varsity Sports in High School

(0=no, 1=yes)



Does a binary variable have a mean?



$$\overline{X} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{30*1+20*0}{50} = \frac{30}{50} = .60$$

Central Tendency

Median – the exact middle value

Calculation:

- If there are an odd number of observations, find the middle value
- If there are an even number of observations, find the middle two values and average them.

Median: example

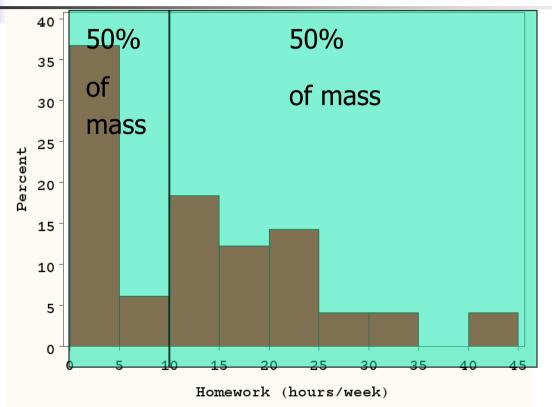
Some data:

Age of participants: 17 19 21 22 23 23 38

Median = (22+23)/2 = 22.5

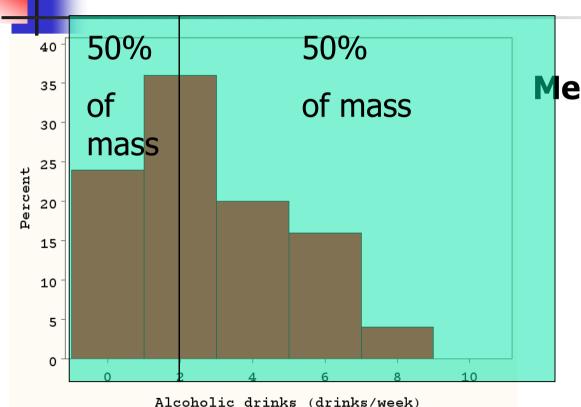


Median of homework



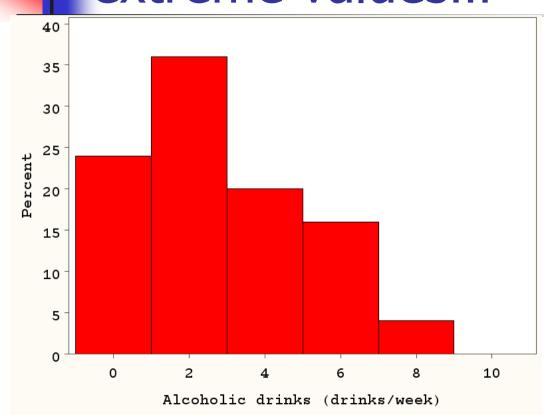
Median = 10 hours/week

Median of alcohol drinking

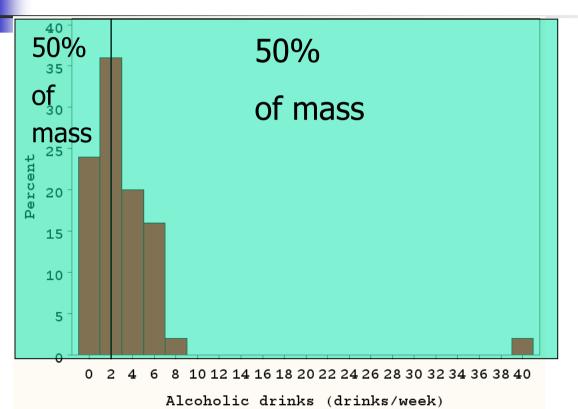


Median = 2.0 drinks/wk

The median is NOT affected by extreme values...



The median is NOT affected by extreme values...



Median = 2.0 drinks/week

Does Varsity Sports (binary variable) have a median?

Yes, if you line up the 0's and 1's, the middle number is 1.

60% (30) 50 40% (20) 20 10 Played Varsity Sports (0=No, 1=Yes)

Should I present means or medians?

 For skewed data, the median is preferred because the mean can be highly misleading...

Hypothetical example: means vs. medians...

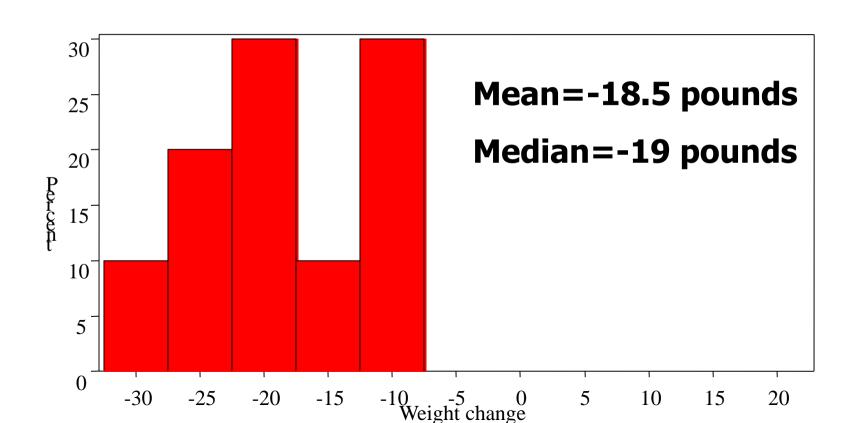
10 dieters following diet 1 vs. 10 dieters following diet 2

Group 1 (n=10) loses an average of 34.5 lbs.

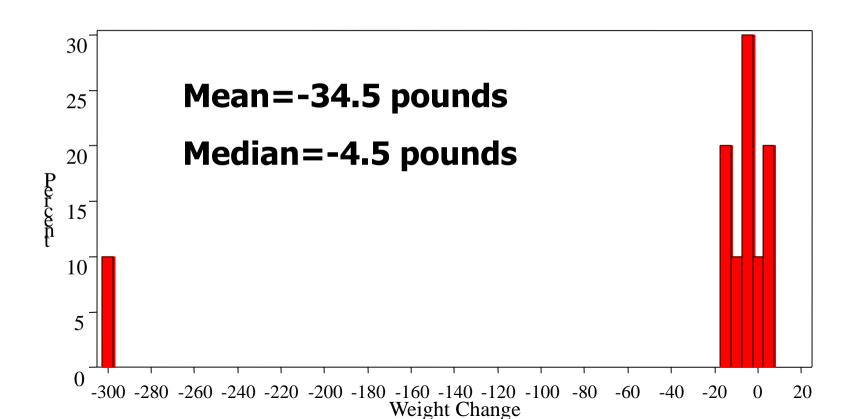
Group 2 (n=10) loses an average of 18.5 lbs.

Conclusion: diet 1 is better?

Histogram, diet 2...



Histogram, diet 1...



The data...

Diet 2, change in weight (lbs)
-8, -10, -12, -16, -18, -20, -21, -24, -26, -30

Compare medians via a "nonparametric test"

We need to compare medians (ranked data) rather than means; requires a "non-parametric test"

Apply the Wilcoxon rank-sum test (also known as the Mann-Whitney U test) as follows...

Rank the data...

Diet 2, change in weight (lbs)
-8, -10, -12, -16, -18, -20, -21, -24, -26, -30

Ranks: 7 8 10 13 14 15 16 17 18 19

Sum the ranks...

Diet 1, change in weight (lbs):

Ranks: 1 2 3 4 5 6 9 11 12 20

Sum of the ranks: 1+2+3+4+5+6+9+11+12+20=73

Diet 2, change in weight (lbs)

Ranks: 7 8 10 13 14 15 16 17 18 19

Sum of the ranks: 7+8+10+13+14+15+16+17+18+19=137

Diet 2 is superior to Diet 1, n=.018.



Statistics for Health Care

Module 5:

Describing Quantitative Data: What is the variability in the data?



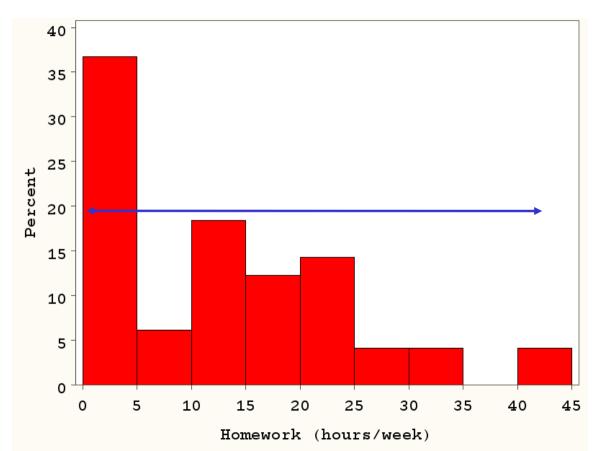
Measures of Variability

- Range
- Standard deviation/Variance
- Percentiles
- Inter-quartile range (IQR)



 Difference between the largest and the smallest observations.

Range of homework: 40 hours - 0 hours = 40 hours/wk





Standard deviation

- Challenge: devise a statistic that gives the average distance from the mean.
- Distance from the mean:

$$x_i - \overline{X}$$

Average distance from the mean??:

$$\frac{\sum_{i}^{n} (x_{i} - \overline{X})}{n}$$
?

4

Standard deviation

But this won't work!

$$\frac{\sum_{i}^{n} (x_i - \overline{X})}{n} = 0$$

4

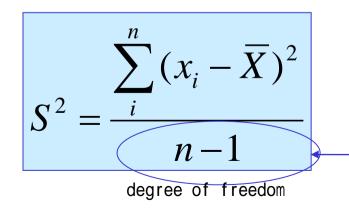
How can I get rid of negatives?

- Absolute values?
 - Too messy mathematically!
- Squaring eliminates negatives!

$$S^{2} = \frac{\sum_{i}^{n} (x_{i} - \overline{X})^{2}}{n}$$



Average squared distance from the mean:



-We lose a "degree of freedom because we have already estimated the mean.

Standard Deviation

- Gets back to the units of the original data
- Roughly, the average spread around the mean.

$$S = \sqrt{\frac{\sum_{i}^{n} (x_i - \overline{X})^2}{n-1}}$$

The standard deviation is affected by extreme values

 Because of the squaring, values farther from the mean contribute more to the standard deviation than values closer to the mean:

$$\overline{X} = 5$$
 $(6-5)^2 = 1$
 $(10-5)^2 = 25$

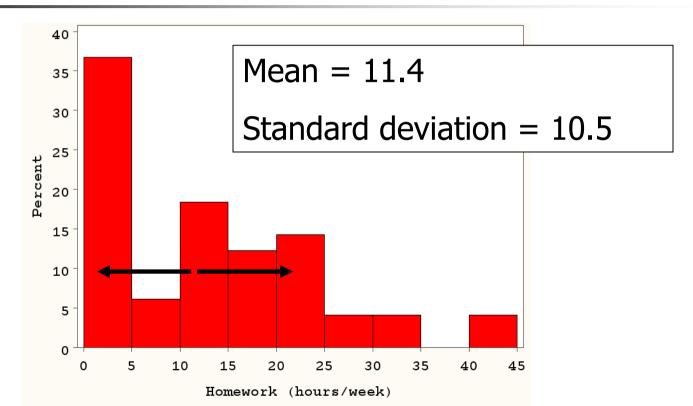
Calculation Example: Standard Deviation

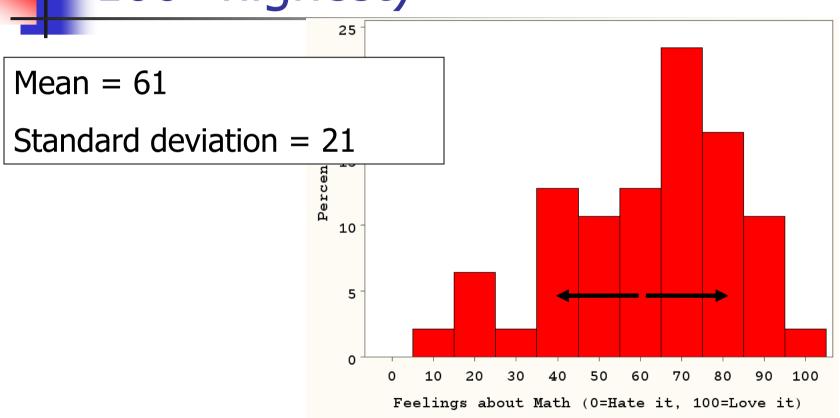
Age data (n=8): 17 19 21 22 23 23 23 (38)

$$n = 8$$
 Mean = 23.25

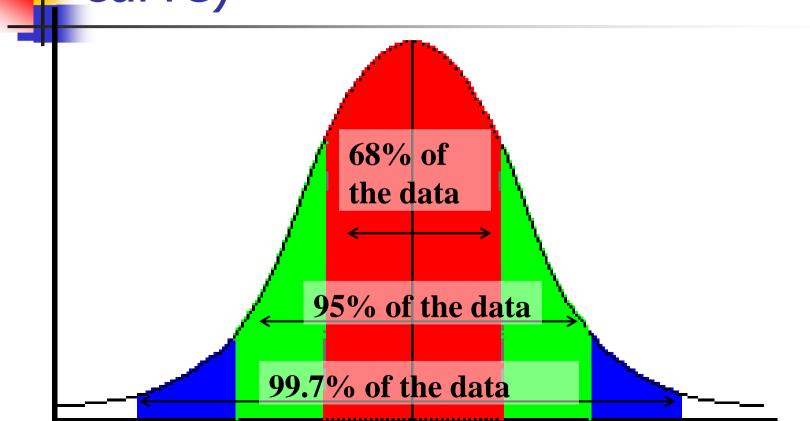
$$S = \sqrt{\frac{(17 - 23.25)^2 + (19 - 23.25)^2 + \dots + (38 - 23.25)^2}{8 - 1}}$$
$$= \sqrt{\frac{280}{7}} = 6.3$$

Homework (hours/week)

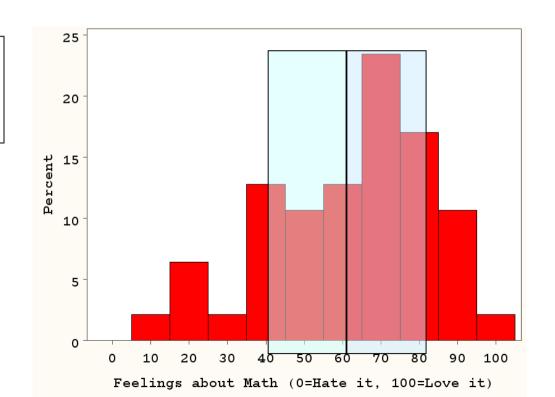




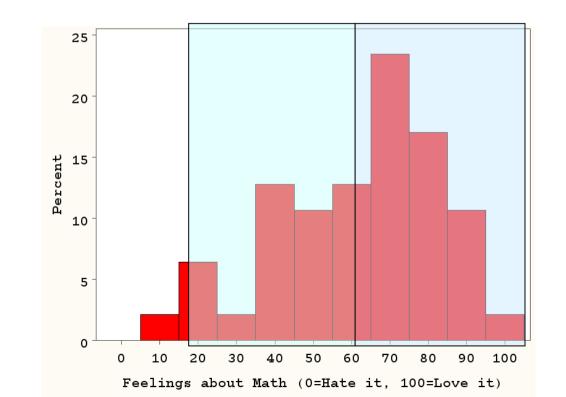
68-95-99.7 rule (for a perfect bell curve)



Percent between 40 and 82 = 34/47 = **72%**

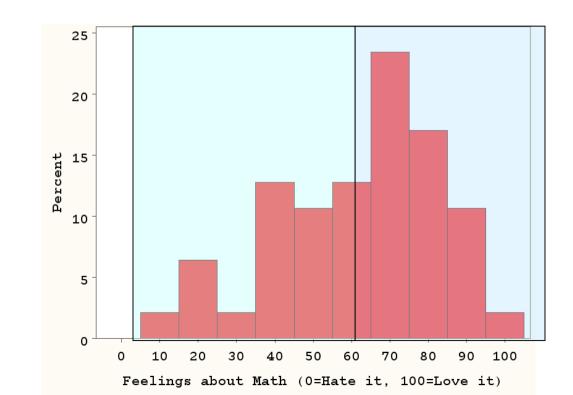


Percent between 19 and 100 = 46/47= **98%**



Mean
$$+/- 3$$
 std $= 0 - 100$

100% of the data!

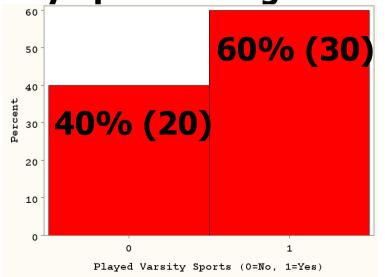


Does a binary variable have a standard deviation?

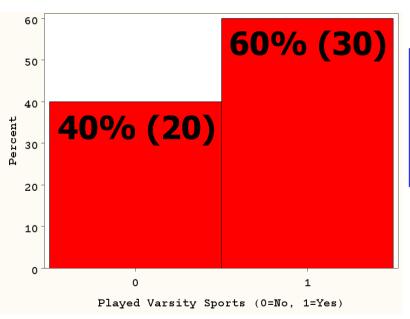
Yes! If coded as a 0/1 variable...

Example: Played Varsity Sports in High School

(0=no, 1=yes)

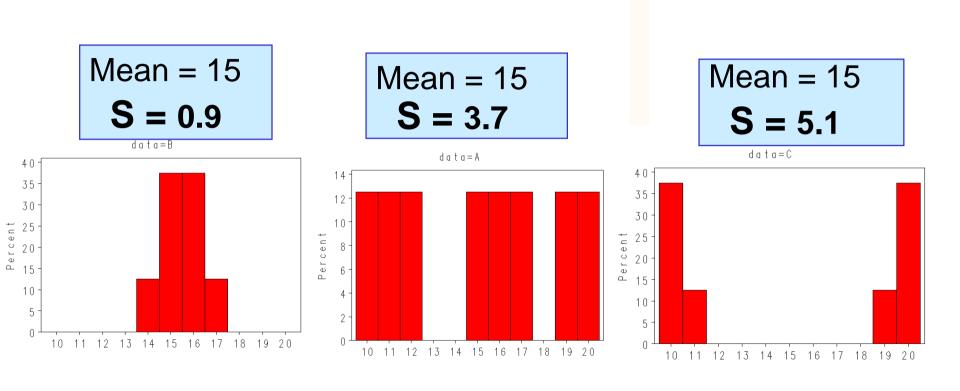


Does a binary variable have a standard deviation?



$$S = \sqrt{\frac{30*(1-.60)^2 + 20*(0-.60)^2}{50-1}}$$
$$= \sqrt{\frac{30(.16) + 20(.36)}{49}} = \sqrt{\frac{12}{49}} = .49$$

Understanding Standard Deviation:



Standard deviations vs. standard errors

- Standard deviation measures the variability of a trait.
- Standard error measures the variability of a statistic, which is a theoretical construct! (much more on this later!)

Percentiles

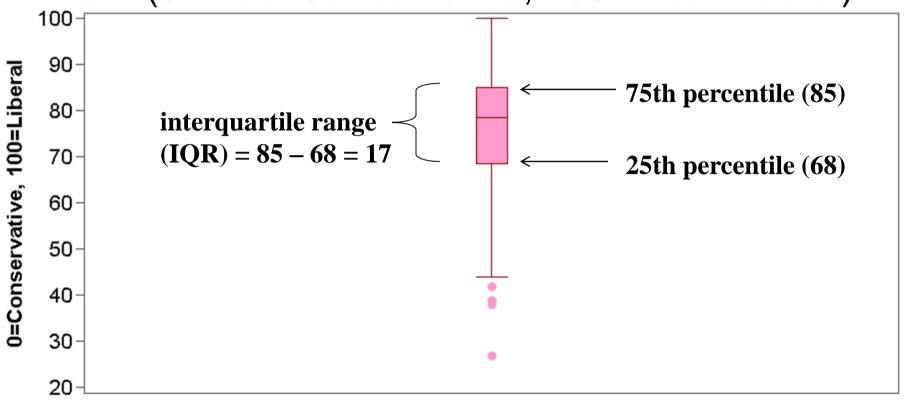
- Based on ranking the data
 - The 90th percentile is the value for which 90% of observations are lower
 - The 50th percentile is the median
 - The 10th percentile is the value for which 10% of observations are lower
- Percentiles are not affected by extreme values (unlike standard deviations)



Interquartile Range (IQR)

- Interquartile range = 3rd quartile − 1st quartile
- The middle 50% of the data.
- Interquartile range is not affected by outliers.

Boxplot of Political Bent (0=Most Conservative, 100=Most Liberal)



Symbols

- S² = Sample variance
- S = Sample standard deviation
- σ^2 = Population (true or theoretical) variance
- g = Population standard deviation
- X = Sample mean
- μ = Population mean
- IQR = interquartile range (middle 50%)



Statistics for Health Care

Module 6:

Exploring real data: Lead in lipstick



- "Lipsticks Contain Excessive Lead, Tests Reveal"
- "One third of lipsticks on the market contain high lead"

Link to example news coverage:

http://www.reuters.com/article/2007/10/11/us-lipstick-lead-idUSN1140964520071011

2007 report by a consumer advocacy group...

"One-third of the lipsticks tested contained an amount of lead that exceeded the U.S. Food and Drug Administration's 0.1 ppm limit for lead in candy—a standard established to protect children from ingesting lead."

2007 report by a consumer advocacy group...

- "One-third of the lipsticks tested contained an amount of lead that exceeded the U.S. Food and Drug Administration's 0.1 ppm limit for lead in candy—a standard established to protect children from ingesting lead."
- 1 ppm = 1 part per million = 1 microgram/gram



Recent Headlines

- "400 shades of lipstick found to contain lead", FDA says" Washington Post, Feb. 14, 2012
- "What's in Your Lipstick? FDA Finds Lead in 400 Shades," *Time* February 15, 2012

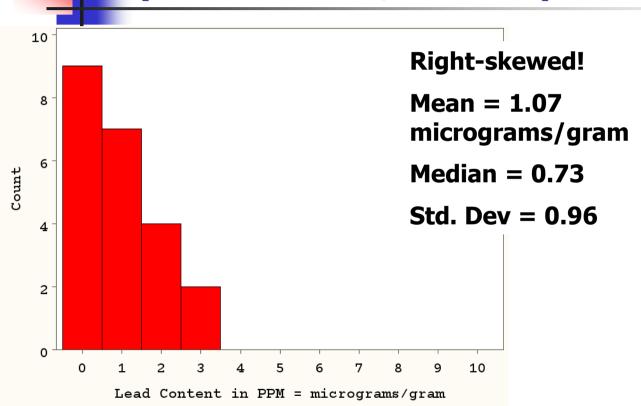
Link to example news coverage:



How worried should women be?

- What is the dose of lead in lipstick?
- How much lipstick are women exposed to?
- How much lipstick do women ingest?

Distribution of lead in lipstick (FDA 2009, n=22)



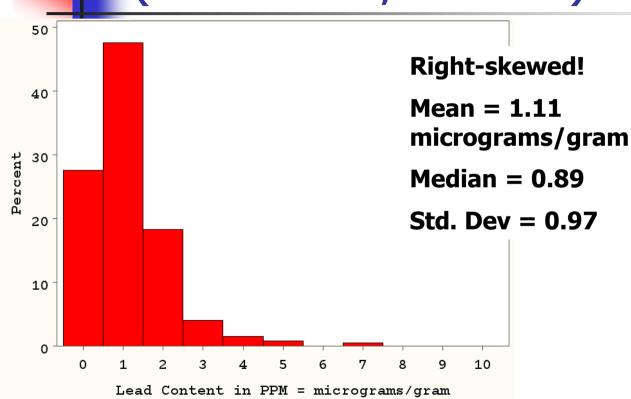
max = 3.06

99th percentile: 3.06

95th percentile: 3.05

90th percentile: 2.38

Distribution of lead in lipstick (FDA 2012, n=400)



max = 7.19

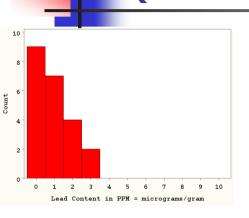
99th percentile: 4.91

95th percentile: 2.76

90th percentile: 2.23

FDA 2009 (n=22) vs. FDA 2012

(n=400)

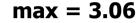


2009 (n=22)

Mean = 1.07 micrograms/gram

Median = 0.73

Std. Dev = 0.96



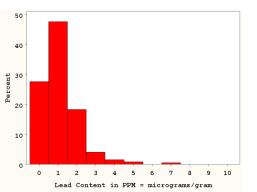
99th percentile: 3.06

95th percentile: 3.05

90th percentile: 2.38

75th percentile: 1.76

Did lead increase?



<u>2012 (n=400)</u>

Mean = 1.11 micrograms/gram

Median = 0.89

Std. Dev = 0.97

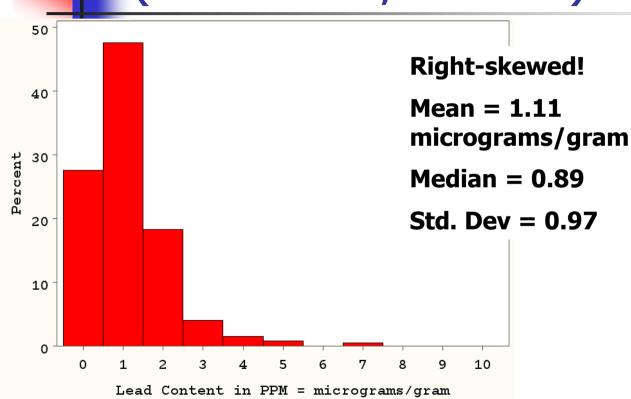
99th percentile: 4.91

95th percentile: 2.76

max = 7.19

90th percentile: 2.23

Distribution of lead in lipstick (FDA 2012, n=400)



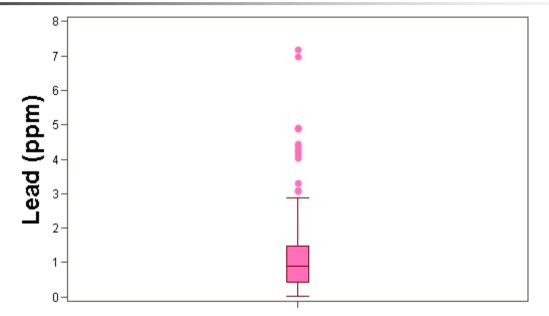
max = 7.19

99th percentile: 4.91

95th percentile: 2.76

90th percentile: 2.23

Distribution of lead in lipstick (n=400 samples, FDA 2012)

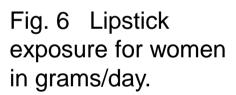


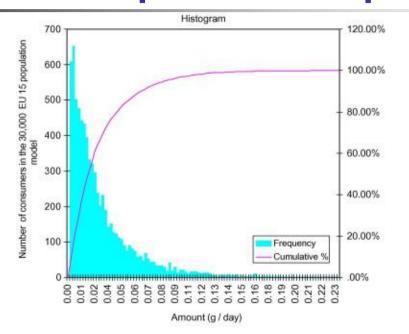
FDA data available at.

http://www.fda.gov/Cosmetics/ProductandIngredientSafety/ProductInformation/ucm137224.htm#expanalyses

4

Data on lipstick exposure



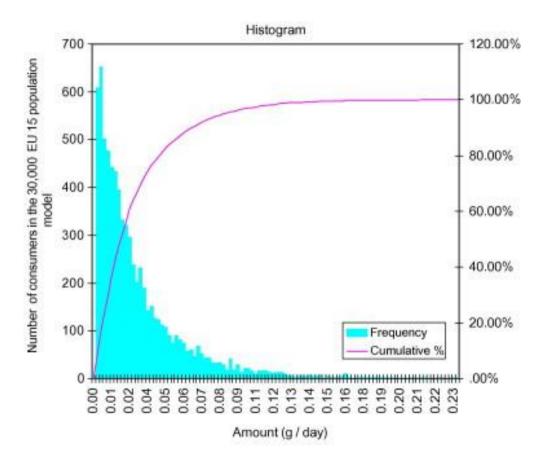


	Amount
1999	(mg/
Value	day)
mean	24.61
std	24.05
median	17.11
minimum	0.13
maximum	217.53
p01	0.57
p02.5	1.00
p05	1.68
p10	2.95
p20	5.69
p30	9.20
p40	12.93
p50	17.11
p60	22.37
p70	29.43
p80	39.70
p90	56.53
p92	61.66
p94	68.29
p95	72.51
p96	77.78
p97.5	89.08
p98	94.46
p99	110.98
p99.5	126.71
p99.9	160.06

Percentiles in mg/day

Hall B, Tozer S, Safford B, Coroama M, Steiling W, Leneveu-Duchemin MC, McNamara C, Gibney M. European consumer exposure to cosmetic products, a framework for conducting population exposure assessments. *Food and Chemical Toxicology* 2007; 45: 2097 – 2108.

Distribution of lipstick exposure:



	Amount
14575	(mg/
Value	day)
mean	24.61
std	24.05
median	17.11
minimum	0.13
maximum	217.53
p01	0.57
p02.5	1.00
p05	1.68
p10	2.95
p20	5.69
p30	9.20
p40	12.93
p50	17.11
p60	22.37
p70	29.43
p80	39.70
p90	56.53
p92	61.66
p94	68.29
p95	72.51
p96	77.78
p97.5	89.08
p98	94.46
p99	110.98
p99.5	126.71
p99.9	160.06

Percentiles in mg/day

Food and Chemical Toxicology 2007; 45: 2097 – 2108.

Highest use (1 in 30,000 women)

- 1 in 30,000 women uses 218 milligrams of lipstick per day.
- 1 tube of lipstick contains 4000 milligrams.
- 4000 mg/tube ÷ 218 mg/day = 18 days per tube.
- The heaviest user goes through an entire tube of lipstick in 18 days.

Exercise

Assuming that women ingest 50% of the lipstick they apply daily, calculate:

- What is the typical lead exposure to lipstick for women, in micrograms (mcg) of lead (based on medians)?
- What is the highest daily lead exposure to lipstick for women, in mcg of lead?

Lead in lipstick:

Median = 0.89 micrograms/gram

Maximum = 7.19 mcg/g

Daily lipstick usage:

Median = 17.11 milligrams

Maximum = 217.53 mg

Typical user

Daily exposure:

Daily ingestion:

Typical user

Daily exposure:

0.89 mcg/g x 17.11 mg x1 g/1000 mg = **0.0152 mcg**

Daily ingestion:

0.0152 mcg/2 = 0.0076 mcg

4

Highest user

Daily exposure:

7.19 mcg/g x 217.53 mg x 1 g/1000 mg =

1.56 mcg

Daily ingestion:

1.56 mcg/2 = 0.78 mcg

```
Frequency of usage this high: 1/30,000 * 1/400 = 1 woman in 12 million
```

To put these numbers in perspective:

- "Provisional tolerable daily intake" for an adult is 75 micrograms/day
- 0.0076 mcg / 75 mcg = 0.02% of your PTDI
- 0.78 mcg / 75 mcg = 1% of your PTDI (1 in 12 million women)
- Average American consumes 1 to 4 mcg of lead per day from food alone.

Comparison with candy:

Median level of lead in milk chocolate = 0.016 mcg/g (FDA limit = 0.1 mcg/g)

Comparing concentrations of lead in lipstick and chocolate:

0.016 mcg/g << 0.89 mcg/g << 7.19 mcg/g

Comparison with candy:

1 bar of chocolate has about 43 grams

Exposure from 1 chocolate bar:

0.016 mcg/g x 43 g = 0.69 mcg

Average American consumes 13.7 grams/day (11 pounds per year)

Typical daily exposure from chocolate:

0.016 mcg/g x 13.7 g = 0.22 mcg

It all comes down to dose!

Typical daily exposure from chocolate (0.22 mcg) is 29 times the typical exposure from lipstick (0.0076 mcg)

And extreme daily exposure to lead from lipstick (0.78 mcg) is similar to exposure from daily consumption of an average chocolate bar (0.69 mcg)