

Newton Raphson Method

$$\text{root} = \frac{\left(x + \frac{N}{x}\right)}{2}$$

where, root - Actual root

N - Number

x - Sqrt we guessed.

Why this formula works?

$$\sqrt{N} = \frac{\left(x + \frac{N}{x}\right)}{2}$$

* Imagine that our guess is correct

$$* \text{ Then } \sqrt{N} = \frac{\left(\sqrt{N} + \frac{N}{\sqrt{N}}\right)}{2} \quad [x = \sqrt{N}]$$

$$\begin{aligned}\sqrt{N} &= \frac{\left(\sqrt{N} + \frac{\sqrt{N} \times \cancel{\sqrt{N}}}{\cancel{\sqrt{N}}}\right)}{2} \\ &= \frac{2\sqrt{N}}{2}\end{aligned}$$

$$= \sqrt{N}$$

* If our guess is the actual answer, then the equation satisfies

* Try to minimize the error as minimal as possible

* If x is the square root we have assumed, is the actual square root, then what is the error.

* $\text{error} = |\text{root} - x|$

* Keep changing the value of x , till the error becomes minimal

* Steps - \therefore

1. Assign x to N
2. Start a loop.
3. The answer will be found when $\text{error} < 1$
4. What if error is > 1 , then update x .

Complexity : $O((\log N)F(N))$

$F(N)$ - Cost of complexity of calculating $\frac{f(N)}{f'(N)}$ with some n -digit precision