

Finding Square Root of a number

* Square Root of a number is obviously less than that number.

⇒ Do binary search (sort of nos)

For example: $\text{sqrt}(36)$

PERECT SQUARE:

⇒ 0 - 36

⇒ Mid = 18

Is $18 * 18 = 36$ NO

$18 * 18 > 36$

Then $\text{end} = \text{Mid} - 1$

⇒ 0 - 17

⇒ Mid = 8

Is $8 * 8 = 36$ NO

$8 * 8 > 36$

Then $\text{end} = \text{Mid} - 1$

⇒ 0 - 8

Mid = 4

Is $4 * 4 = 36$ NO

~~Is~~ $4 * 4 < 36$

$\text{start} = \text{Mid} + 1$

⇒ 5 - 8

Mid = 6

Is $6 * 6 = 36$ Yes

* Then sqrt of 36 = 6.

General:

if $(m * m > n)$

end = $m - 1$;

else

start = $m + 1$;

Square root is^u decimal value :

For example :

$$\text{sqrt}(40) = 6.32$$

⇒ The Integer value can be gotten with above method.

⇒ But to get the decimal values.
* Increment the decimal values in its place.

⇒ $\text{sqrt} = 6$ got from above method.

1. Is $6 * 6 < 40$ Yes

2. Increment 1st decimal value

$$6.1 \Rightarrow 6.1 * 6.1 = 40 \text{ NO}$$

$$6.1 * 6.1 < 40$$

3. Increment 1st decimal value

$$6.2 \Rightarrow 6.2 * 6.2 < 40$$

4. Increment 1st decimal value

$$6.3 \Rightarrow 6.3 * 6.3 < 40$$

5. Increment 1st decimal value

$$6.4 \Rightarrow 6.4 * 6.4 > 40$$

6. Then decrement ⇒ 6.3 this is the answer

7. Then add second decimal value

$$6.3 + 0.01 \Rightarrow 6.31$$

$$\Rightarrow 6.31 * 6.31 < 40$$

8. Increment the 2nd decimal place

$$\Rightarrow \boxed{6.32} \rightarrow \text{Ans}$$