

## Exercise 8: Multi-Stage Production Line

**Problem:**

Model a production line with three stages:

1. Stage 1 ( $\mu=10$  \mu = 10  $\mu=10$ )
2. Stage 2 ( $\mu=8$  \mu = 8  $\mu=8$ )
3. Stage 3 ( $\mu=12$  \mu = 12  $\mu=12$ ).

```
# Install and load the required package
```

```
if (!require("queueing")) install.packages("queueing", dependencies = TRUE)
```

```
library(queueing)
```

```
# Define the production line stages as M/M/1 queues
```

```
stage1 <- NewInput.MM1(lambda = 7, mu = 10)
```

```
stage2 <- NewInput.MM1(lambda = 7, mu = 8)
```

```
stage3 <- NewInput.MM1(lambda = 7, mu = 12)
```

```
# Create queueing models for each stage
```

```
model1 <- QueueingModel(stage1)
```

```
model2 <- QueueingModel(stage2)
```

```
model3 <- QueueingModel(stage3)
```

```
# Output performance measures for each stage
```

```
cat("=== Stage 1 Performance ===\n")
```

```
summary(model1)
```

```
cat("\n=== Stage 2 Performance ===\n")
```

```
summary(model2)
```

```
cat("\n=== Stage 3 Performance ===\n")
```

```
summary(model3)
```

output:

```
# Install and load the required package
> if (!require("queueing")) install.packages("queueing", dependencies = TRUE)
> library(queueing)
>
> # Define the production line stages as M/M/1 queues
> stage1 <- NewInput.MM1(lambda = 7, mu = 10)
> stage2 <- NewInput.MM1(lambda = 7, mu = 8)
> stage3 <- NewInput.MM1(lambda = 7, mu = 12)
>
> # Create queueing models for each stage
> model1 <- QueueingModel(stage1)
> model2 <- QueueingModel(stage2)
> model3 <- QueueingModel(stage3)
>
> # Output performance measures for each stage
> cat("=== Stage 1 Performance ===\n")
=== Stage 1 Performance ===
> summary(model1)
  lambda mu c  k  m   RO  PO      Lq      Wq X      L      W      Wq  Lq
1      7 10 1 NA NA 0.7 0.3 1.633333 0.2333333 7 2.333333 0.3333333 0.3333333 3.333333
> cat("\n=== Stage 2 Performance ===\n")

=== Stage 2 Performance ===
> summary(model2)
  lambda mu c  k  m   RO  PO      Lq      Wq X  L  W  Wq  Lq
1      7  8 1 NA NA 0.875 0.125 6.125 0.875 7 7 1  1  8
> cat("\n=== Stage 3 Performance ===\n")

=== Stage 3 Performance ===
> summary(model3)
  lambda mu c  k  m   RO  PO      Lq      Wq X  L  W  Wq  Lq
1      7 12 1 NA NA 0.5833333 0.4166667 0.8166667 0.1166667 7 1.4 0.2 0.2 2.4

>
```