

Quantitative Management Modeling

Assignment No. 3

Solution:

Part 4.

Define:

Let

$$L1 + M1 + S1 \leq 750 \quad \text{----}(y1)$$

$$L2 + M2 + S2 \leq 900 \quad \text{----}(y2)$$

$$L3 + M3 + S3 \leq 450 \quad \text{----}(y3)$$

$$20 L1 + 15 M1 + 12 S1 \leq 13000 \quad \text{----}(y4)$$

$$20 L2 + 15 M2 + 12 S2 \leq 12000 \quad \text{----}(y5)$$

$$20 L3 + 15 M3 + 12 S3 \leq 5000 \quad \text{----}(y6)$$

$$L1 + L2 + L3 \leq 900 \quad \text{----}(y7)$$

$$M1 + M2 + M3 \leq 1200 \quad \text{----}(y8)$$

$$S1 + S2 + S3 \leq 750 \quad \text{----}(y9)$$

$$900 L1 + 900 M1 + 900 S1 - 750 L2 - 750 M2 - 750 S2 = 0 \quad \text{----}(y10)$$

$$450 L1 + 450 M1 + 450 S1 - 750 L3 - 750 M3 - 750 S3 = 0 \quad \text{----}(y11)$$

Objective Function:

$$\text{Min } Z: +750 y1 + 900 y2 + 450 y3 + 13000 y4 + 12000 y5 + 5000 y6 + 900 y7 + 1200 y8 + 750 y9 + 0 y10 + 0 y11;$$

Constraints:

Subject to:

$$y1 + 20 y4 + y7 + 900 y10 + 450 y11 \geq 420;$$

$$y1 + 15 y4 + y8 + 900 y10 + 450 y11 \geq 360;$$

$$y1 + 12 y4 + y9 + 900 y10 + 450 y11 \geq 300;$$

$$y2 + 20 y5 + y7 - 750 y10 \geq 420;$$

$$y2 + 15 y5 + y8 - 750 y10 \geq 360;$$

$$y2 + 12 y5 + y9 - 750 y10 \geq 300;$$

$$y3 + 20 y6 + y7 - 750 y11 \geq 420;$$

$$y_3 + 15 y_6 + y_8 - 750 y_{11} \geq 360;$$
$$y_3 + 12 y_6 + y_9 - 750 y_{11} \geq 300;$$

non-negativity

$$y_1, y_2, y_3, y_4, y_5, y_6, y_7, y_8, y_9 \geq 0$$
$$y_{10}, y_{11} = \text{unrestricted}$$

The solution agrees with the Primal problem. The dual problem LP and R file has been attached.