

1. Extended definition of Regular Language.

2. Write the strings that the following Regular Expressions will generate:

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|--------------|--------------------------|---------------------|
| 1. $(0+1)^*$ | 5. $(0^*1^*)^*$ | 9. $a(0+1)b$ |
| 2. $0+1$ | 6. $(01^*)^*$ | 10. $a(0+1)^*b$ |
| 3. $(00)^*$ | 7. $0^*1^* + (ab)^*$ | 11. $(a(0+1)^*b)^*$ |
| 4. 0^*1^* | 8. $(0^*1^* + (ab)^*)^*$ | 12. $ab + 1^*01^*$ |

3. Is $(0+1)^*$ and $(0^*1^*)^*$ the same? Justify your answer.

4. Write the shortest string that will be generated by this regular expression -

- $aa^*b(0+1) + 1^*0(baa^*)$
- $(0+1)1(00 + 0(11)^* + 100) + 1^*(00(010 + 01^*0))01$

5. Construct a Regular Expression that generates the language $L = \{w \in \{0,1\}^* : w \text{ contains "101" as a substring.}\}$

6. Construct a Regular Expression that generates the language $L = \{w \in \{0,1\}^* : w \text{ starts with "101"}. \}$

7. Construct a Regular Expression that generates the language $L = \{w \in \{0,1\}^* : w \text{ ends with "101"}. \}$

8. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't start with "1"} \}$

9.

a. Construct a Regular Expression that generates the language $L1 = \{ w \in \{0,1\}^* : w \text{ contains "00" or "11"} \}$

b. Construct a Regular Expression that generates the language $L2 = \{ w \in \{0,1\}^* : w \text{ contains "00" and "11"} \}$

c. Construct a regular expression for $\overline{L1}$

d. Construct a regular expression for $\overline{L2}$

10.

a. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ contains exactly two 1s} \}$

b. For the previous question, your three friends write three different solutions.

$(0+1)^* 1 (0+1)^* 1 (0+1)^*$, $(0+1)^* 1 0^* 1 0^*$ and $0^* 1 0^* 1 (0+1)^*$

Find the correct solution.

11. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ contains at least two 1s} \}$

12.

- a. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ contains at most two 1s.} \}$
- b. Your friend claims that one of the correct regular expressions for the previous question is $0^* (0+1) 0^* (0+1) 0^* + \epsilon$. Do you agree or disagree?

13.

- a. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The length of } w \text{ is even or multiple of 2.} \}$
- b. Your friend claims that one of the correct regular expressions for the previous question is $(00)^* + (01)^* + (10)^* + (11)^*$. Do you agree or disagree?

14. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The length of } w \text{ is odd.} \}$

15. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The length of } w \text{ is multiple of 3.} \}$

16. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The length of } w \text{ is two more than multiple of four.} \}$
17. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The length of } w \text{ is **not** multiple of 3.} \}$
18. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : \text{The number of 1s in } w \text{ is a multiple of 3.} \}$
19. Construct a Regular Expression that generates the language $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with different symbols.} \}$
20. Construct a Regular Expression that generates the language $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with the same symbols.} \}$
21. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't end with 01.} \}$

22. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : 0\text{'s and } 1\text{'s alternates in } w. \}$
23. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain } 00. \}$
24. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain } 11. \}$
25. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain } 111. \}$ [Practice]
26. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain } 10. \}$
27. Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ doesn't contain } 00 \text{ and } 11. \}$ Or, **Similar to Question:**

28.

a) Construct a Regular Expression that generates the language $L = \{ w \in \{0,1\}^* : w \text{ contains 0 in every third position.} \}$

b) Regular language for \overline{L}

29.

Consider the following languages over $\Sigma = \{0,1\}$.

$$L_1 = \{w : w \text{ does not contain } 11\}$$

$$L_2 = \{w : \text{every } 1 \text{ in } w \text{ is followed by at least one } 0\}$$

$$L_3 = \{w : \text{the number of times } 1 \text{ appears in } w \text{ is even}\}$$

Now solve the following problems.

- (a) **Give** a regular expression for the language L_1 . (2 points)
 - (b) Your friend claims that $L_1 = L_2$. **Prove** her wrong by writing down a five-letter string in $L_1 \setminus L_2$. Recall that $L_1 \setminus L_2$ contains all strings that are in L_1 but not in L_2 . (2 points)
 - (c) **Give** a regular expression for the language $L_1 \setminus L_2$. (2 points)
 - (d) **Give** a regular expression for the language L_3 . (2 points)
 - (e) **Give** a regular expression for the language $L_2 \setminus L_3$. (2 points)
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