

## CSE 331: Automata & Computability

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### Practice Sheet: Equivalence between Regular Expressions and Finite Automata

## Converting DFAs to Regular Expressions Using State Elimination Method

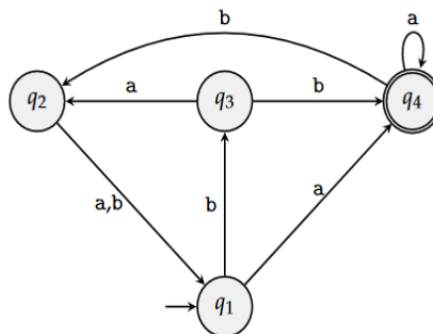
### Notes:

- If you use any other method apart from the State Elimination Method, you will be awarded 0 points
- If you don't follow the order of elimination mentioned in the question, you will be awarded 0 points.

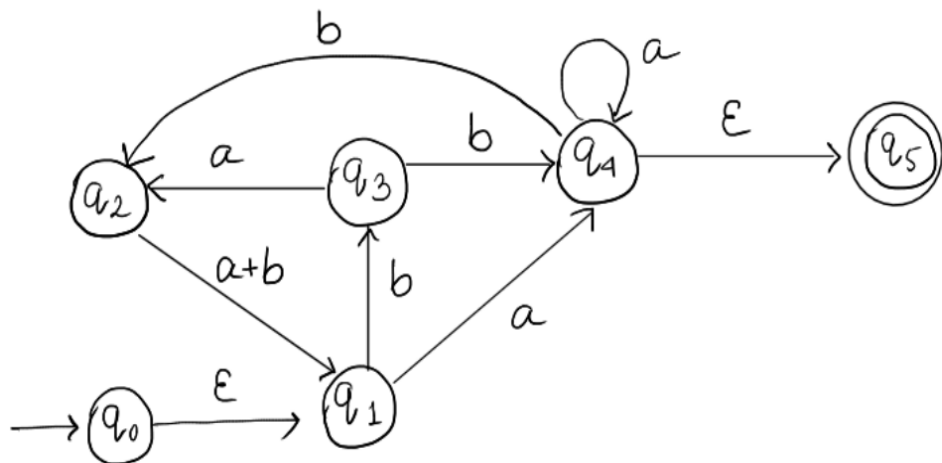
### Practice

#### Problem 4 (CO2): Converting Finite Automata to Regular Expressions (10 points)

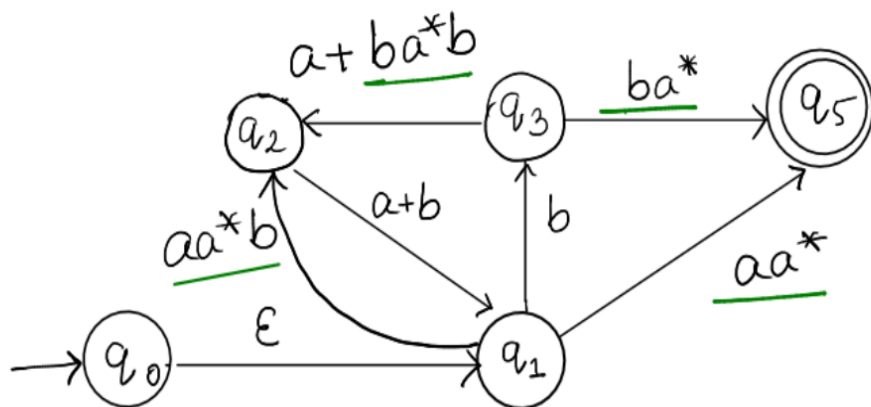
Convert the following DFA into an equivalent regular expression using the state elimination method. First eliminate  $q_4$ , then  $q_2$ , next  $q_3$ , and finally  $q_1$ . You must show work.



GNFA:

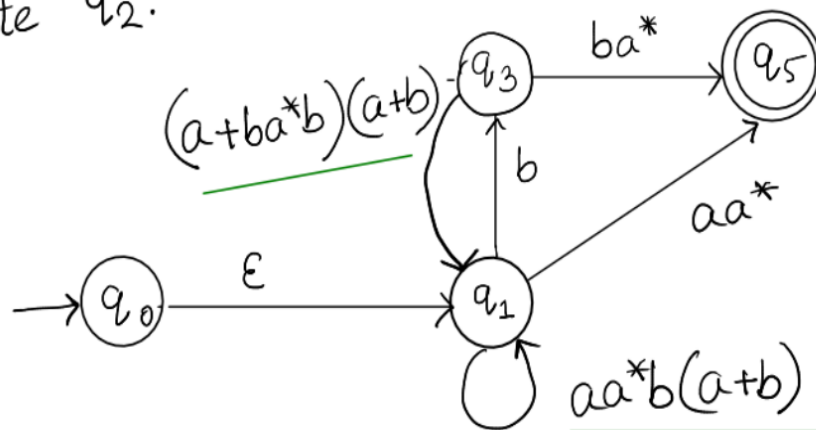


Eliminate  $q_4$ :

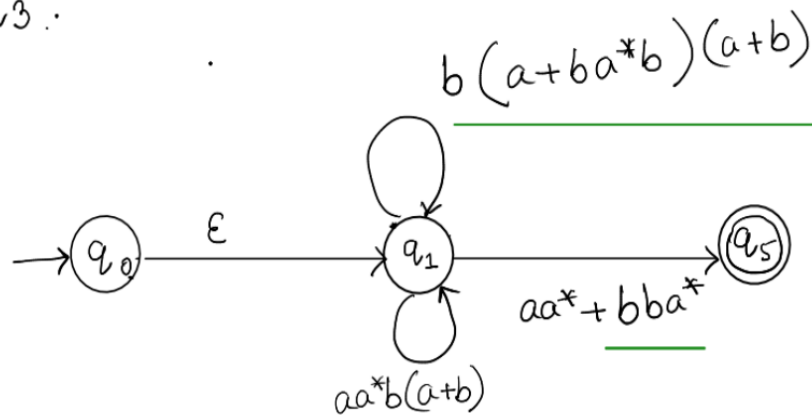


The parenthesis is a must ( $q_3$ - $q_1$ )

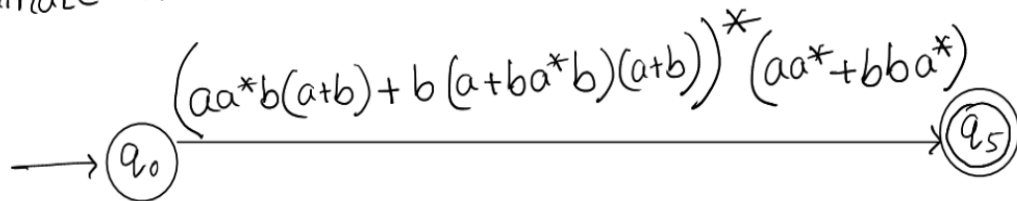
Eliminate  $q_2$ :



Eliminate  $q_3$ :



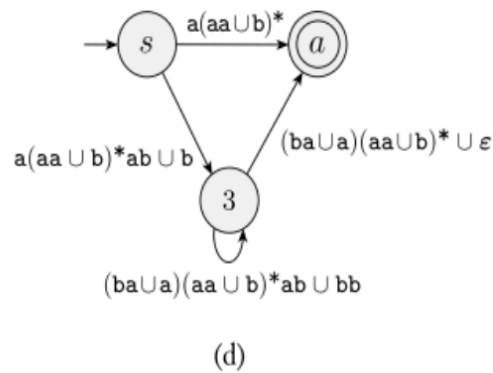
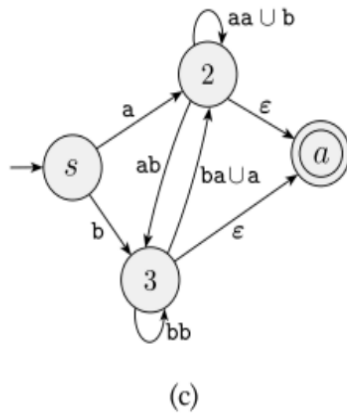
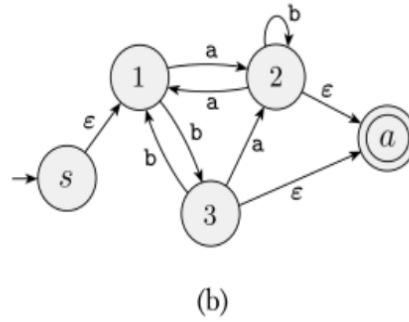
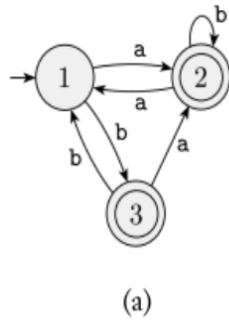
Eliminate  $q_1$ :



Book's Example

### EXAMPLE 1.68

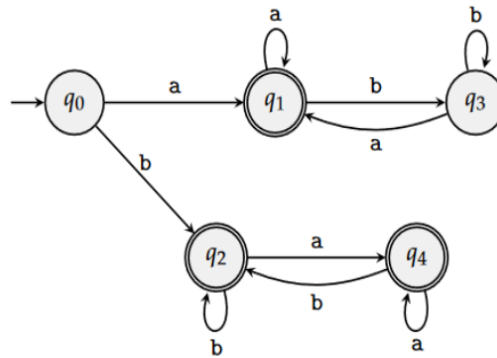
In this example, we begin with a three-state DFA. The steps in the conversion are shown in the following figure.



$$(a(aa \cup b)^*ab \cup b)((ba \cup a)(aa \cup b)^*ab \cup bb)^*((ba \cup a)(aa \cup b)^* \cup \epsilon) \cup a(aa \cup b)^*$$

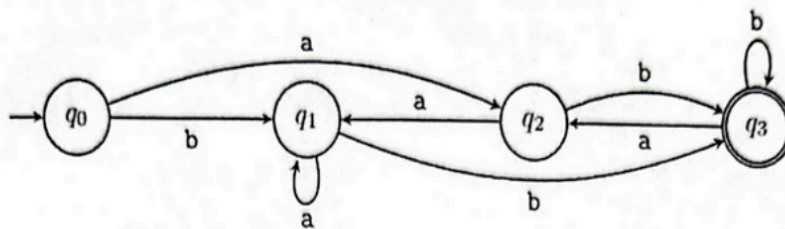
Problem 1:

Convert the following DFA into an equivalent regular expression using the state elimination method. First eliminate  $q_1$ , then  $q_2$ , next  $q_3$  and then finally  $q_4$ . You must show work.



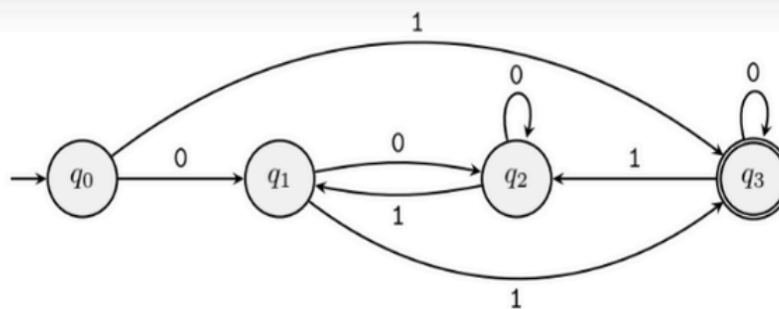
## Problem 2:

Convert the following DFA into an equivalent regular expression using the **state elimination method**. First eliminate  $q_2$ ,  $q_1$  and finally  $q_3$ . You must show work.



## Problem 3:

Convert the following DFA into an equivalent regular expression using the **state elimination method**. First eliminate  $q_3$ ,  $q_1$  and finally  $q_2$ . You must show work.



## Converting Regular Expressions to NFAs

Problem 4:

$$(a^* b^* + (ac + b^* c) b^* a)^*$$

Problem 5:

$$a (bca^*)^* + (ba + ca) a^+ (ab + ac) + ((c^* a) ab)^* b^*$$