

CSE 331: Automata & Computability
Spring 2025
Prepared By: KKP
Assignment 01 (DFA & NFA)
Total Mark: 103

[Or means you may solve any One question]

[Problems having multiple Or, mention the problem no properly. For example: 2a) 3b)]

Group Formation:

- This is a group assignment. You can make a group of **at most three students**.
- From each group you have to submit one copy only.
- Cross section group formation is not allowed.

Submission Deadline:

- Part A (Questions 1-10): February 18, 2024
- Part B (Questions 11-21): February 25, 2024
- Part C (Questions 01-04): March 2, 2025

Submission Link: <https://forms.gle/pjZc6uuqFrPXBCDG8>

Please note you have to submit both a hard copy and a soft copy. If you are unable to submit the hard copy within the deadline, you may submit the soft copy by the deadline and later [by next class] submit the hard copy.

Penalty:

- For each day delay, you will receive a 5 marks penalty.
- If you plagiarize, then each member of the group will receive (number of questions plagiarized * 3 * number of group members) points penalty.

Additional Resources

Please go through the video lectures of Mursalin Sir [**The first three video lectures on DFA**]

Link: https://drive.google.com/drive/folders/1790ApcX9k_8GBFM3Suea1_SEwTpyReRW

Part 0:

1. Do you understand that it is not possible to finish the assignment if you start solving the assignment 1-2 days before the deadline? (Yes/No)

2. Do you understand solving the assignment using AI or directly copy pasting from any available resources without understanding the solution will impact your quiz/midterm performance? (Yes/No)

Part A: Deterministic Finite Automata (DFA) [Each question contains 3 marks]

1. a) Draw a DFA for the set of strings that have three consecutive 0s. $\Sigma = \{0,1\}$

Or, b) Draw a DFA for the set of strings that don't contain 000. $\Sigma = \{0,1\}$

2. a) Construct a DFA that accept the language, $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with different symbols.} \}$

Or, b) Construct a DFA that accepts the language, $L = \{ w \in \{a,b\}^* : w \text{ starts and ends with the same symbol.} \}$

3. a) Draw a DFA of strings that ends with "0101". $\Sigma = \{0,1\}$

Or, b) Design a DFA that accepts the language $L = \{ w \mid w \text{ ends with the substring "yxy"} \}$ over the alphabet $\{x,y\}$

4. a) Construct a DFA defined as $L = \{ w \in \{0,1\}^* : \text{the length of } w \text{ is two more than multiple of four} \}$

Or, b) Construct a DFA defined as $L = \{ w \in \{0,1\}^* : \text{numbers of 1s in } w \text{ is two more than multiple of four} \}$

5. Construct a DFA defined as $L = \{ w \in \{0,1\}^* : w, \text{ when interpreted as a binary number, is divisible by 5.} \}$

6. a) $L = \{ w \in \{0, 1, \# \}^* : w \text{ does not contain } \# \text{ and the number of 0s in } w \text{ is not a multiple of 3} \}$

Or, b) let's $\Sigma = \{0,1\}$

$L1 = \{ w \text{ does't contain } \# \}$

$L2 = \{ \text{the number of 0s in } w \text{ is not a multiple of 3} \}$

$L = L1 \cap L2$

Prove L is a regular language by giving a state diagram for DFA.

7. Construct a DFA of the language L over the alphabet $\Sigma = \{a,b,c\}$ defined as follows-
 $L = \{ w \mid w \text{ does not contain "ba" and ends with "cb"} \}$

8. Draw a DFA of strings that contains at least three 0s or exactly two 1s. $\Sigma = \{0,1\}$
9. a) Draw a DFA of strings where the 2nd last symbol is a. $\Sigma = \{a,b\}$

Or, b) Draw a DFA of strings where the 3rd last symbol is 1. $\Sigma = \{0,1\}$ [You may draw the NFA for this problem if you find it difficult to solve using DFA]
10. $L = \{w \in \{a, b\}^* : \text{the last letter of } w \text{ appears at least twice in } w.\}$

Part B: More Deterministic Finite Automata (DFA) [Each question contains 3 marks]

11. a) Draw a DFA of strings that have 1 as every 3rd symbol. $\Sigma = \{0,1\}$

Or, b) The set of binary numbers has 0 in all even positions. $\Sigma = \{0,1\}$.
12. a) Draw a DFA that accepts exactly one "ab". $\Sigma = \{a,b\}$

Or, b) Draw a DFA that accepts exactly two "ab". $\Sigma = \{a,b\}$
13. Draw a DFA that accepts at least two "00" as a substring. $\Sigma = \{0,1\}$
14. a) Draw a DFA that accepts exactly two "00" as a substring. $\Sigma = \{0,1\}$

Or, b) Draw a DFA that accepts at most two "00" as a substring. $\Sigma = \{0,1\}$
15. Construct a DFA defined as $L = \{w \in \{0,1\}^* : \text{An even number of 0s follow the last 1 in } w\}$ $\Sigma = \{0,1\}$
16. Construct a DFA defined as $L = \{w \in \{a,b\}^* : \text{each "b" is followed by at least one "a"}\}$ $\Sigma = \{a,b\}$
For example: baaa
17. Construct a DFA where the set of binary strings where numbers of 0s between two successive 1s will be even. $\Sigma = \{0,1\}$.
18. Construct a DFA of the Language, $L = \{w \in \{0,1\}^* : \text{no 00 appears as a substring before the first 11 in } w.\}$
19. Construct a DFA of the Language, $L = \{w \in \{0,1\}^* : \text{no 00 appears as a subsequence before the first 11 in } w.\}$
20. a) Construct a DFA of the Language, $L = \{w \in \{0,1\}^* : w \text{ contains } 01^m0 \text{ as a substring where } m \text{ is divisible by } 3\}$

Or, b) Construct a DFA of the Language, $L = \{ w \in \{0,1\}^* : w \text{ contains } 01^m0 \text{ as a substring where } m \text{ leaves a remainder of 2 when divided by 3} \}$

Hints:

We denote by 1^m the string $\underbrace{111 \dots 111}_{m \text{ times}}$.

21. a) Construct a DFA of the Language, $L = \{ w \in \{0,1\}^* : w = 0^m1^n \text{ where } m \text{ and } n \text{ are both odd.} \}$

Or, b) Construct a DFA of the Language, $L = \{ w \in \{0,1\}^* : w = 0^m1^n \text{ where } m \text{ and } n \text{ are both even.} \}$

Or, c) The problem can also be designed as:

$$L1 = \{ w : w = 0^m, \text{ where } m \text{ is even} \}$$

$$L2 = \{ w : w = 1^n, \text{ where } n \text{ is even} \}$$

$$L = L1 \cdot L2$$

Prove L is a regular language by giving a state diagram for DFA.

Part C: Mursalin Sir's [MHB] Quiz Question from Previous semesters [Each question contains 10 marks.]

Question 1.

Let $\Sigma = \{0, 1\}$

$$L1 = \{ w : w = 1^m \text{ where } m \text{ is odd} \}$$

$$L2 = \{ w : w \text{ does not contain any } y \in L1 \text{ as a substring} \}$$

- Write down a length 6 string that is in L2. (1 point) .
- Give the state diagram for a DFA that recognizes L1. (5 points)
- Give the state diagram for a DFA that recognizes L2. (3 points)
- Give the state diagram for a DFA that recognizes $L1 \cap L2$. You can use the construction shown in class but there is a much simpler DFA. (2 points)

Question 2.

The symmetric difference of the languages L_1 and L_2 , denoted by $L_1 \Delta L_2$, is defined in the following way.

$$L_1 \Delta L_2 = \{w : w \text{ is in exactly one of } L_1 \text{ and } L_2\}$$

Let $\Sigma = \{0, 1\}$. Consider the following languages over Σ .

$A = \{w : \text{the length of } w \text{ is greater than or equal to 3 but less than or equal to 5}\}$

$B = \{w : \text{the length of } w \text{ is greater than or equal to 2 but less than or equal to 4}\}$

$C = \{w : \text{the length of } w \text{ is odd}\}$

- (a) Give the state diagram for a DFA that recognizes A . (2 points)
- (b) Give the state diagram for a DFA that recognizes B . (2 points)
- (c) Give the state diagram for a DFA that recognizes $A \Delta B$. (2 points)
- (d) If you use the construction from class to get a DFA for the language $(A \Delta B) \cup C$, how many states will it have? (1 point)
- (e) Give a 5-state DFA that recognizes $(A \Delta B) \cup C$. (3 points)

Question 3.

Let $\Sigma = \{0, 1\}$. Consider the following languages over Σ .

$L_1 = \{w : \text{every second letter of } w \text{ is } 0\}$

$L_2 = \{w : \text{every third letter of } w \text{ is } 1\}$

- (a) Write down a length 5 string that is in $L_1 \cap L_2$. (1 point)
- (b) Give the state diagram for a DFA that recognizes L_1 . (3 points)
- (c) Give the state diagram for a DFA that recognizes L_2 . (3 points)
- (d) Give the state diagram for a DFA that recognizes $L_1 \cap L_2$. (3 points)

Question 4.

Let $\Sigma = \{0, 1\}$. Consider the following languages over Σ .

$L_1 = \{0, 10\}$

$L_2 = L_1^*$

$L_3 = \{w : \text{the length of } w \text{ is four}\}$

- (a) Write down all the strings in $L_2 \cap L_3$. (2.5 points)
- (b) Give the state diagram for a DFA that recognizes L_1 . (4.5 points)
- (c) Give the state diagram for a DFA that recognizes L_2 . (3 points)

For Practice: [Don't have to submit]

Part D: Non-Deterministic finite automata (NFA)

1. Construct an NFA that recognizes the language $L = \{ w \in \{0,1\}^* : w \text{ contains both "000" and "111" as a substring} \}$
2. Construct a NFA which recognize the language $L = \{ w \in \{0,1\}^* : w \text{ contains at least two 0s or exactly two 1s} \}$
3. Construct an NFA for the languages $L = \{ w \in \Sigma : w \text{ does not start with a Punctuation or contains only Alphabets} \}$ where $\Sigma = D \cup A \cup P$

Digit, $D = \{0,1,2,3,4,5,6,7,8,9\}$

Alphabet, $A = \{a, b, c, \dots, x, y, z\}$

Punctuation, $P = \{*, \#\}$

You can use the sets above to label the transitions of your NFA.