## Part C: Designing DFAs [10 Points]

Let  $\Sigma = \{0, 1\}$ . Consider the following languages over  $\Sigma$ .

 $L_1 = \{w : \text{the length of } w \text{ is at most three} \}$ 

 $L_2 = \{w : 00 \text{ appears at least twice as a substring in } w\}$ 

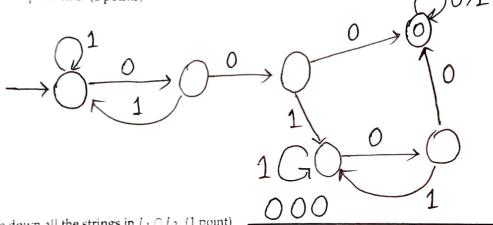
Now solve the following problems.

0001, 1000, 0000 (a) Write down all the length-four strings in  $L_2$ . (1.5 points)

(b) Give the state diagram of a DFA that recognizes L<sub>1</sub>. (3.5 points)

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(c) Give the state diagram of a DFA that recognizes L2. You might want to do this after you have completed all the other problems. (2 points)



(d) Write down all the strings in L<sub>1</sub> ∩ L<sub>2</sub>. (1 point)

(e) Give a five-state DFA that recognizes  $L_1 \cap L_2$ . Your answer to (d) should help you here. (2 points)

