

1/

Applying KVL in i_1 ,

$$10i_1 - 6 + 2(i_1 - i_2) = 0$$

$$\Rightarrow 12i_1 - 2i_2 = 6 \quad \text{--- (I)}$$

For i_2 :

$$10i_2 - 2(i_2 - i_1) + (1(i_2 - i_3)) + 8 + 4i_2 = 0$$

$$\Rightarrow -2i_1 + 7i_2 - i_3 = -8 \quad \text{--- (II)}$$

For i_3 :

$$6 + 5i_3 - 8 + 1(i_3 - i_2) = 0$$

$$\Rightarrow 6i_3 - i_2 = 2 \quad \text{--- (III)}$$

From calc,

$$i_1 = 0.329 \text{ A}$$

$$i_2 = -1.025 \text{ A}$$

$$i_3 = 0.162 \text{ A}$$

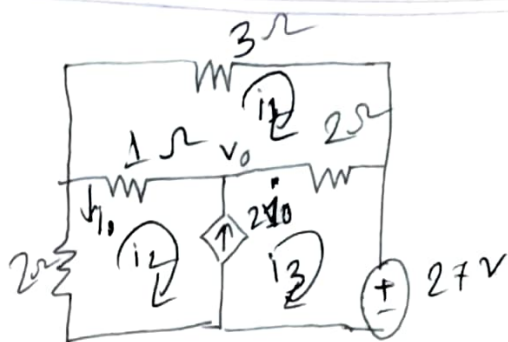
Now,

$$i_3 = i + i_2$$

$$\Rightarrow i = i_3 - i_2$$
$$= 0.162 + 1.025$$

$$\therefore i = \boxed{1.187 \text{ A}} \quad \text{Ans}$$

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Using mesh analysis,

$$i_0 = -i_2 \quad \text{--- (I)}$$

Supermesh,

$$2i_0 = i_3 - i_2 \quad \text{--- (II)}$$

$$2 + 1(i_2 - i_1) + 2(i_3 - i_1) + 27 = 0$$

$$\Rightarrow 29 + i_2 - i_1 + 2i_3 - 2i_1 = 0$$

$$\Rightarrow 3i_1 + i_2 + 2i_3 = -29 \quad \text{--- (III)}$$

From (I), $1(i_1 - i_2) + 3 + 2(i_1 - i_3) = 0$

$$\Rightarrow i_1 - i_2 + 3 + 2i_1 - 2i_3 = 0$$

$$\Rightarrow 3i_1 - i_2 - 2i_3 = -3 \quad \text{--- (IV)}$$

$$(II) + (III) + (IV), \quad -i_2 - i_3 = 0$$

$$-3i_1 + i_2 + 2i_3 = -29$$

$$3i_1 - i_2 - 2i_3 = -3$$

$$\underline{\underline{-i_2 - i_3 = -32}} \quad \text{--- (V)}$$

From (iv) & (v),

$$-i_2 - i_3 = 0$$

$$(+) \quad -i_2 - i_3 = -32$$

$$-2i_2 - 2i_3 = -32$$

$$\Rightarrow -2(-i_2 - i_3) = -32$$

$$\Rightarrow -i_2 - i_3 = \frac{32}{2}$$

$$\Rightarrow -i_2 - i_3 = 16 \quad \Rightarrow -i_3 =$$

$$\Rightarrow i_3 = -i_2 + 16$$

Putting this in (vi), ~~(vii)~~ (iv)

$$-i_2 - (-i_2 + 16) = 0$$

$$\Rightarrow -i_2 + i_2 \quad \quad -i_2 - (-i_2$$

$$3i_1 - i_2 - 2(-i_2 + 16) = -3$$

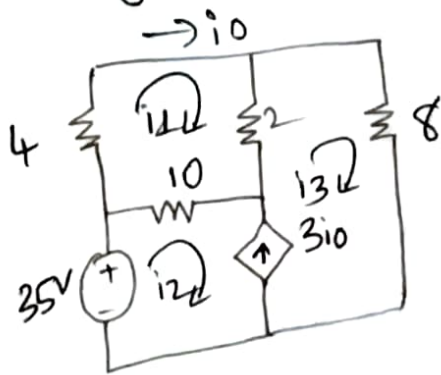
$$\Rightarrow 3i_1 - i_2 + 2i_2 - 32 = -3$$

$$\Rightarrow 3i_1 + i_2 = -35$$

From Calc,
 $V_1 = 36$ & $V_0 = \boxed{57V}$ Ans

$$i_0 = \frac{V_1}{2} = \boxed{18A} \text{ Ans}$$

3/ Using mesh analysis,



$$i_0 = i_1$$

Supermesh,

$$-35 + 10i_2 - 10i_1 + 2i_3 - 2i_1 + 8i_3 = 0$$

$$\Rightarrow -12i_1 + 10i_2 + 10i_3 = 35 \quad \text{--- (1)}$$

Also, $i_3 - i_2 = 3i_0 \quad \text{--- (II)}$

$$\Rightarrow i_0 = i_1 \quad \text{--- (III)}$$

From loop II,

$$2i_1 - 2i_3 + 10i_1 - 10i_2 + 4i_1 = 0$$

$$\Rightarrow 16i_1 - 10i_2 - 2i_3 = 0 \quad \text{--- (IV)}$$

From calc,

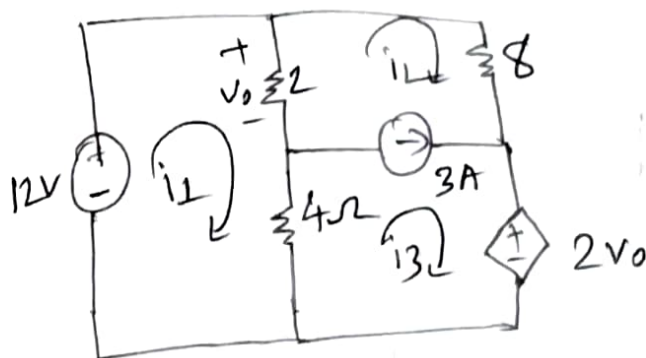
$$i_1 = 1.0096 \text{ A}$$

$$i_2 = 0.8413 \text{ A}$$

$$i_3 = 3.8701 \text{ A}$$

$$\text{So, } i_0 = i_1 = \boxed{1.0096 \text{ A}} \quad \underline{\text{Ans}}$$

4/

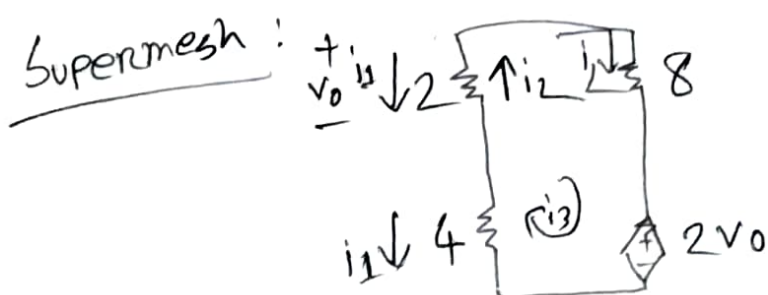


From i_1 ,

$$v_o + 4(i_1 - i_3) - 12 = 0$$

$$\Rightarrow v_o = 2(i_1 - i_2) \quad \text{--- (1)}$$

$$\text{So, } 2(i_1 - i_2) + 4(i_1 - i_3) = 12$$



$$8i_2 + 2v_0 + 4(i_3 - i_1) + 2(i_2 - i_1) = 0$$

$$-4i_1 - 2i_1 + (8+2)i_2 + 4i_3 + 2v_0 = 0$$

but, $v_0 = 2(i_1 - i_2)$ from (1),

$$\text{So, } -6i_1 + 10i_2 + 4i_3 + 2 \times 2(i_1 + i_2) = 0$$

$$\Rightarrow i_1 = 3i_2 + 2i_3 \quad \text{--- (11)}$$

$$\text{From (11) } i_3 - i_2 = 3$$

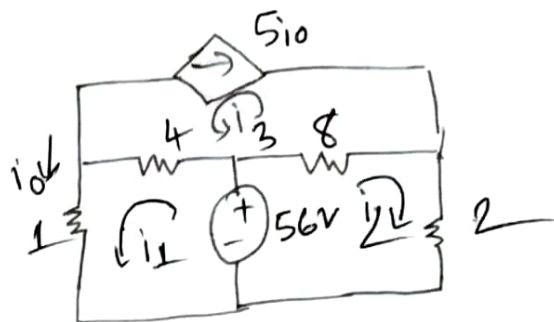
$$6i_1 - 2i_2 - 4i_3 = 12$$

using calculator we get,

$$i_1 = \boxed{3.5 \text{ A}}, i_2 = \boxed{-0.5 \text{ A}} \Rightarrow i_3 = \boxed{2.5 \text{ A}}$$

Ans

5/ using mesh,



$$-56 + 4(i_1 - i_3) + 1 \cdot i_1 = 0$$

$$\Rightarrow 5i_1 - 4i_3 = 56 \quad \text{--- (1)}$$

$$-56 + 8(i_2 + i_3) + 2i_2 = 0$$

$$10i_2 + 8i_3 = 56 \quad \text{--- (11)}$$

$$i_3 = -0.5i_0 = -0.5i_1$$

$$\text{as, } i_0 = i_1$$

$$\text{so, } 0.5i_1 + i_3 = 0 \quad \text{--- (iii)}$$

from calc,

$$i_1 = 8A, \quad i_2 = 8.8A \quad \& \quad i_3 = -4A$$

Powers,

$$P_{1\Omega} = i_1^2 (1) = 8^2 \times 1 = \boxed{64W}$$

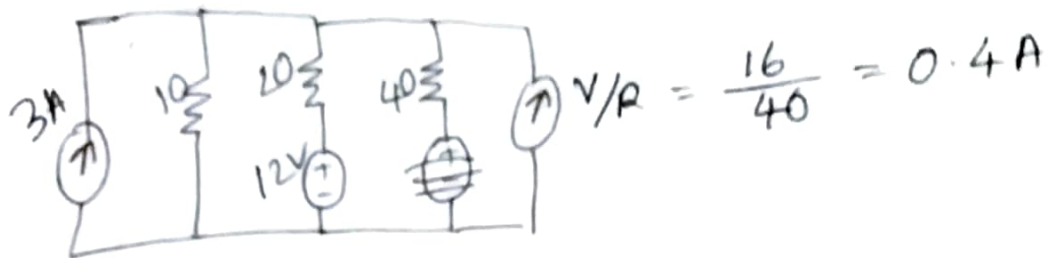
$$P_{4\Omega} = (i_1 - i_3)^2 \times 4 = (0.8)^2 \times 4 = \boxed{2.56W}$$

$$P_{8\Omega} = (i_2 + i_3)^2 \times 8 = (8-4)^2 \times 8 = \boxed{128W}$$

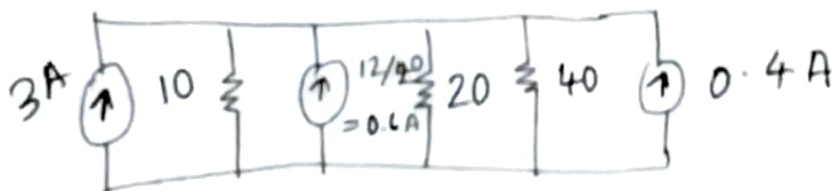
$$P_{2\Omega} = (i_2)^2 \times 2 = (8.8)^2 \times 2 = \boxed{154.88W}$$

Ans

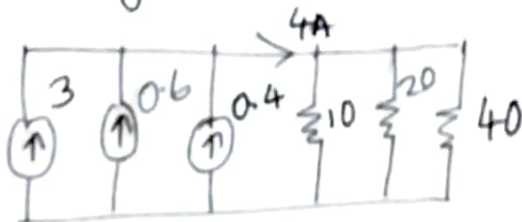
6/ Applying source transformation to ~~16v~~ & 4Ω



Now in $12V$ & 20Ω .



Now combining current sources & resistances.



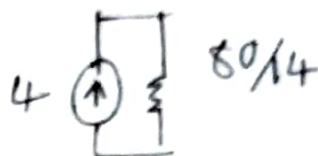
using KCL, $3A + 0.6A + 0.4A = \boxed{4A}$

& all parallel resistors,

$$\frac{1}{R_{eq}} = (10^{-1}) + (20^{-1}) + (40^{-1})$$

$$\therefore R_{eq} = \boxed{5.714 \Omega}$$

Now the circuit is,



applying source transformation,

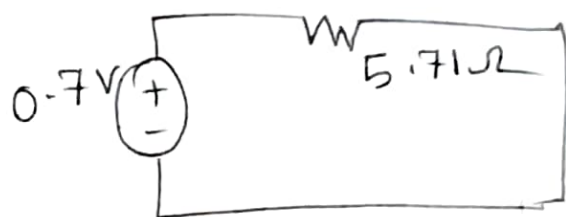
$$\frac{4}{R_{eq}} \quad R_{eq} = \frac{80}{14}$$

$$= 4 \times \frac{14}{80}$$

$$= 0.7V$$

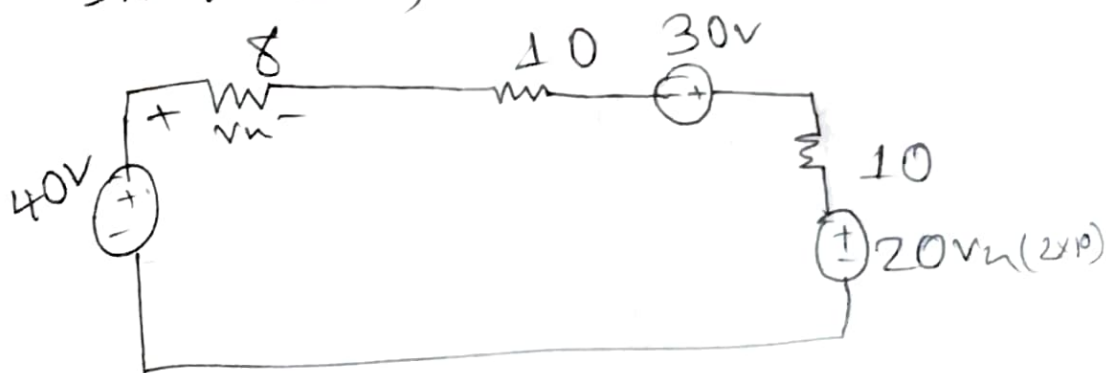
$$\frac{80}{14} = 5.71$$

So the final circuit is,



Ans

7/ Using source transformation on
3A & 10Ω,



Now,

$$\frac{40 - V_u + 30 - 20V_u}{20} = i$$

$$\Rightarrow \cancel{V_u} \cdot \frac{70 - 21V_u}{20} = \frac{V_u}{8}$$

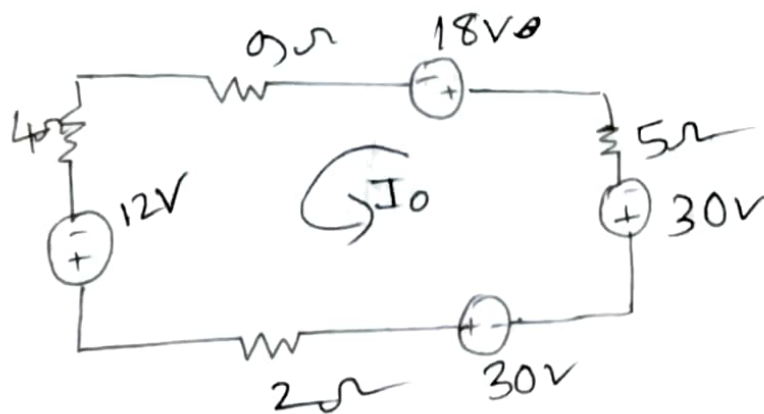
$$\therefore V_u = \boxed{3.11V} \quad \underline{\text{Ans}}$$

8/ Using source transformation,

$$E_1 = 3 \times 4 = 12V, R_1 = 4\Omega$$

$$E_2 = 9 \times 2 = 18V, R_2 = 3\Omega$$

$$E_3 = 5 \times 6 = 30V, R_3 = 5\Omega$$



$$I_0 = \left(\frac{12 - 30 - 30 - 18}{4 + 2 + 5 + 3} \right) = -3.3A$$

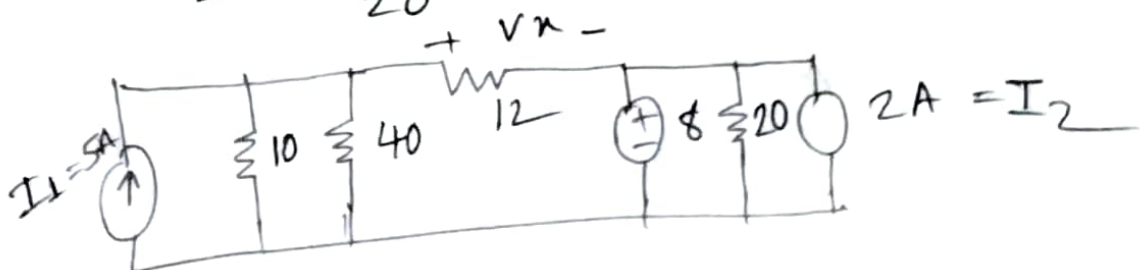
$$V_0 = I_0 \times 2 = (-3.3) \times 2 = \boxed{-6.6V}$$

9/ Using source transformation,

Ans

$$I_1 = \frac{50}{10} = 5A, R_1 = 10\Omega$$

$$I_2 = \frac{40}{20} = 2A, R_2 = 20\Omega$$



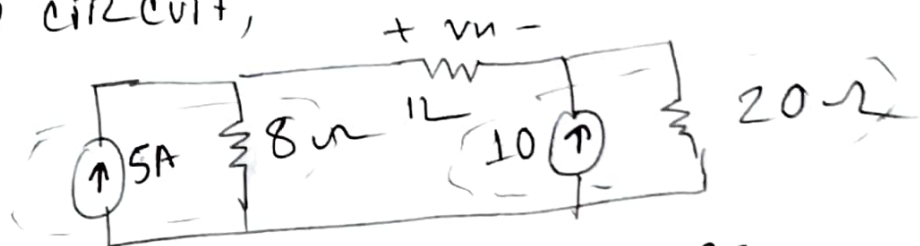
Now,

$$R_L = (10^{-1} + 40^{-1})^{-1}$$

$$R_L = 8\Omega$$

$$I_0 = 8 + 2 = 10A$$

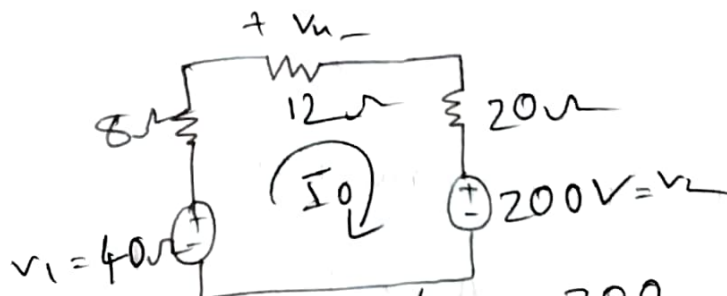
new circuit,



Current to voltage source,

$$V_1 = 5 \times 8 = 40V, R_1 = 8\Omega$$

$$V_2 = 10 \times 20 = 200V, R_2 = 20\Omega$$

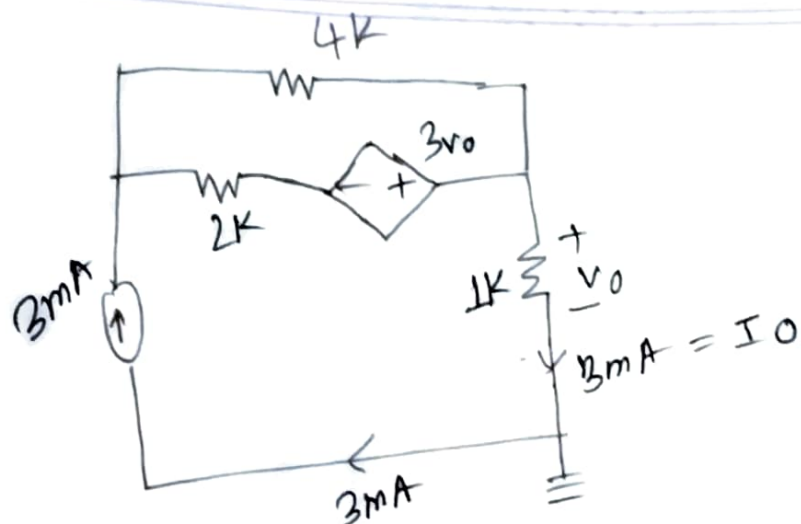


$$I_0 = \frac{40 - 200}{8 + 12 + 20} = -4A$$

$$v_L = I_0 \times 12 = -4 \times 12 = \boxed{-48V}$$

Ans

10/



by nodal analysis,

$$V_o = I_o \times 1 = 3 \times 1 = \boxed{3V}$$

Ans