

Diodes - 2

Prepared By:

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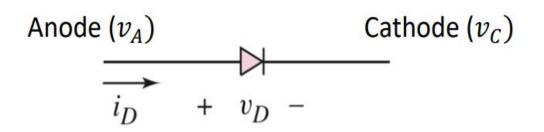
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### Topics Covered

- Diode Logic OR operation
- Diode Logic AND operation
- Diode Logic circuits and operation
- Exponential Converter
- Logarithmic Converter
- Multiplier
- Divider

#### Review: Ideal Diode Model



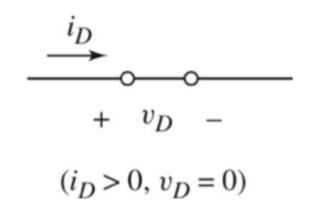
OFF State: Open circuit

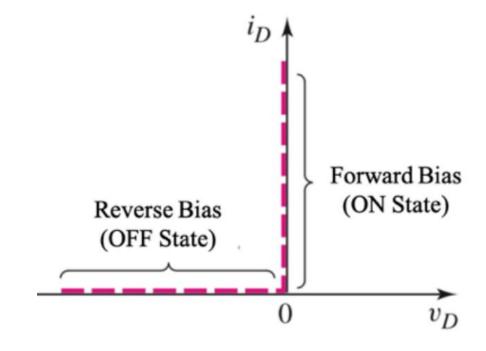
$$i_D = 0$$

$$+ v_D -$$

$$(v_D < 0, i_D = 0)$$

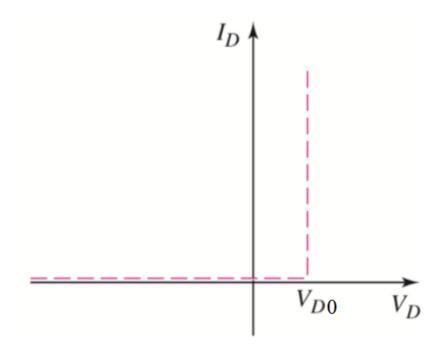
ON State: Short circuit





# Modeling the real diode

- 1. Ideal diode model
- 2. Constant voltage drop (CVD) model
- 3. CVD+R model



**OFF State: Open circuit** 

$$\begin{array}{c}
i_D = 0 \\
+ v_D - \\
\end{array}$$

$$(v_D < V_{D0}, i_D = 0)$$

ON State: Voltage source

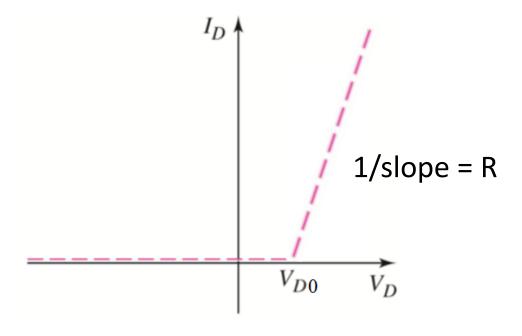
$$\begin{array}{c|c}
 & i_D + V_{D0} - \\
 & + v_D - \\
\end{array}$$

$$(i_D > 0, v_D = V_{D0})$$

# Modeling the real diode

- 1. Ideal diode model
- 2. Constant voltage drop (CVD) model

#### 3. CVD+R model



OFF State: Open circuit

$$\begin{array}{c}
i_D = 0 \\
+ v_D -
\end{array}$$

$$(v_D < V_{D0}, i_D = 0)$$

ON State: Voltage source

$$(i_D > 0, v_D = V_{D0} + i_D r_D)$$

## Digital Representation

- Binary → Two states (0/False, 1/True)
- Binary variables in circuit, need to use two states of device/parameters

 Voltage
 Current
 State

 5∨ → 1
 0∨ → 0

#### Logic Truth Table

| INPUTS |   | OUTPUT |
|--------|---|--------|
| Х      | Υ | z      |
| 0      | 0 | 0      |
| 0      | 1 | 1      |
| 1      | 0 | 1      |
| 1      | 1 | 1      |

#### Voltage Truth Table

| INPUTS |     | OUTPUT |
|--------|-----|--------|
| ×      | Y   | z      |
| 0 V    | 0 V | 0 V    |
| 0 V    | 5 V | 5 V    |
| 5 V    | 0 V | 5 V    |
| 5 V    | 5 V | 5 V    |

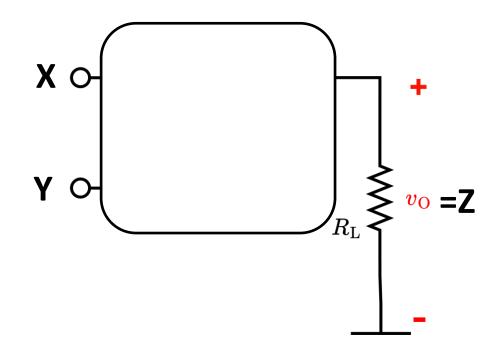
Low/False High/True

Logic Levels: 0

Corresponding voltage levels: 0V 5V

#### Voltage Truth Table

| INPUTS  | OUTPUT |
|---------|--------|
| X Y     | z      |
| 0 V 0 V | 0 V    |
| 0 V 5 V | 5 V    |
| 5 V 0 V | 5 V    |
| 5 V 5 V | 5 V    |

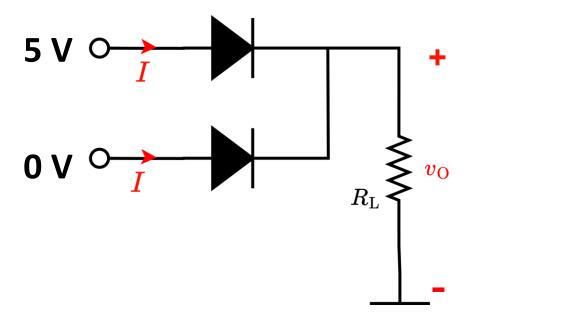


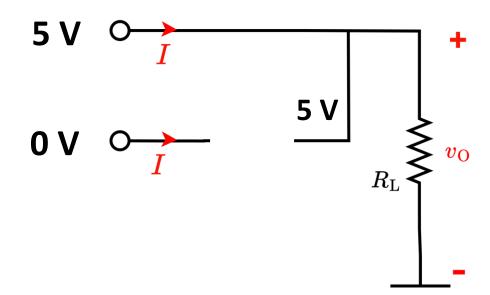
#### **PULL DOWN NETWORK**

When all inputs are completely disconnected,  $v_0$  is pulled down to GND

Degrades the HIGHEST output voltage

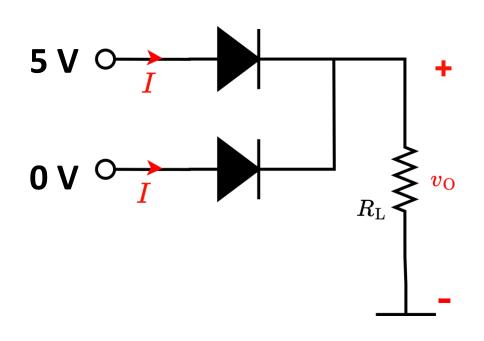
#### Ideal diode

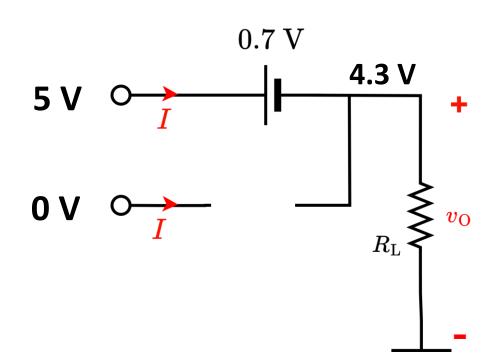




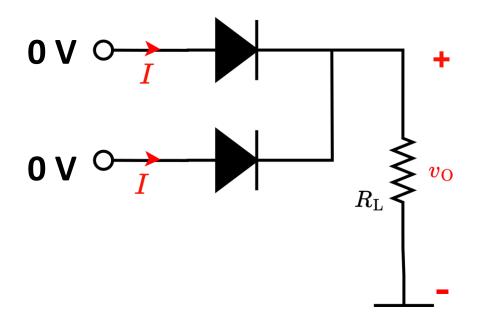
$$Z = 5 V$$

#### CVD diode





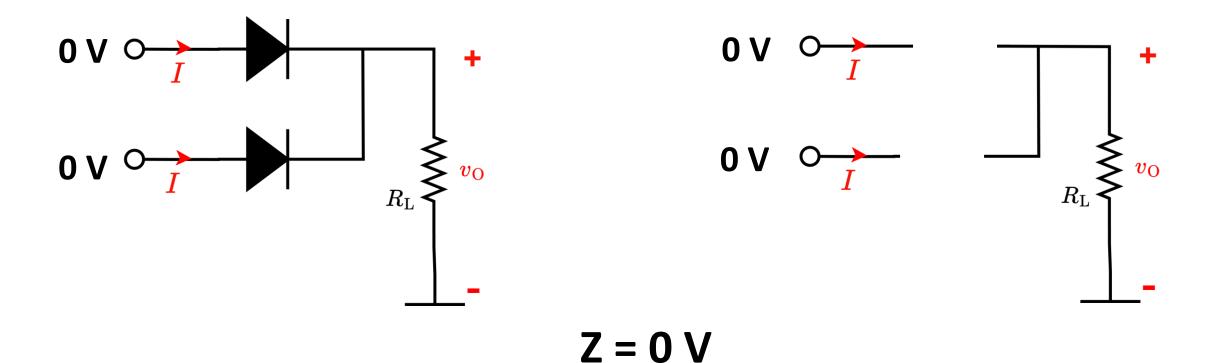
#### Ideal diode



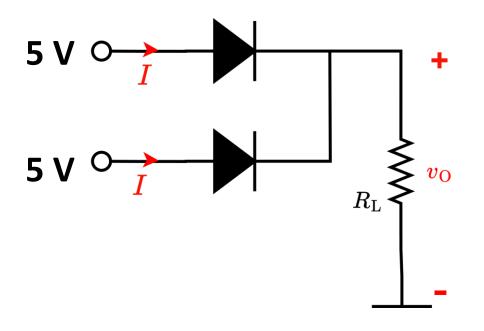
$$\begin{array}{c|c}
0 & V & \bigcirc & I & = 0 \\
0 & V & \bigcirc & I & = 0
\end{array}$$

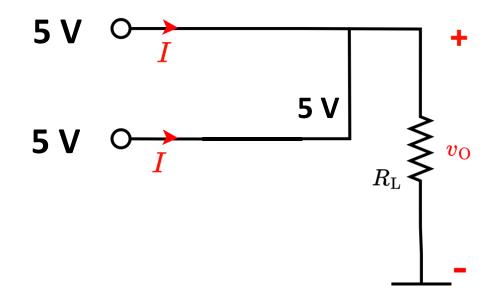
$$Z = 0 V$$

#### CVD diode



#### Ideal diode

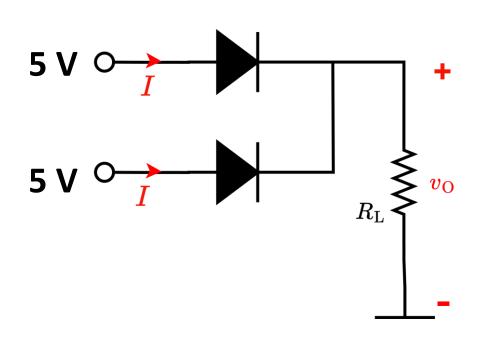


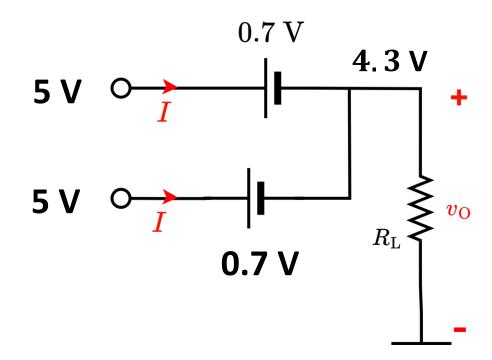


$$Z = 5 V$$

Degraded 5 V

#### CVD diode





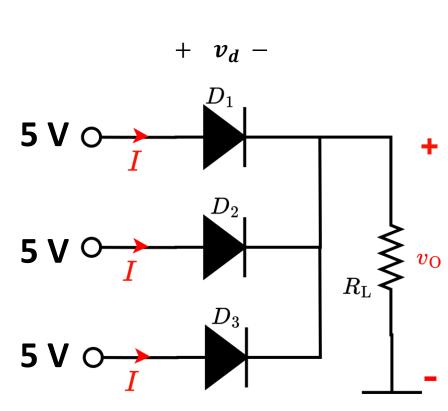
#### **CVD** diode

What if the diodes have different  $V_{DO}$ ?

$$V_{D1} = 1 \text{ V}$$

$$V_{D2} = 0.7 \text{ V}$$

$$V_{D3} = 0.5 \text{ V}$$



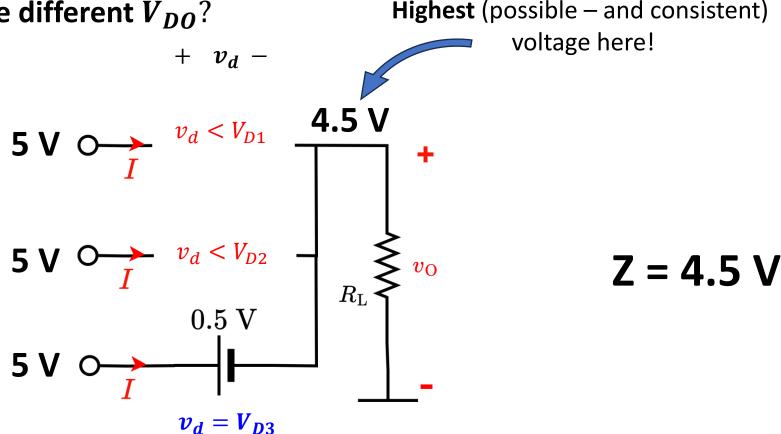
#### CVD diode



$$V_{D1} = 1 \text{ V}$$

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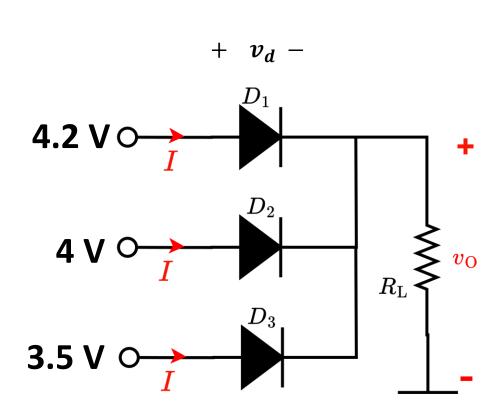
#### CVD diode

What if the input voltages are different?

$$V_{D1} = 1 \text{ V}$$

$$V_{D2} = 0.7 \text{ V}$$

$$V_{D3} = 0.5 \text{ V}$$



#### CVD diode

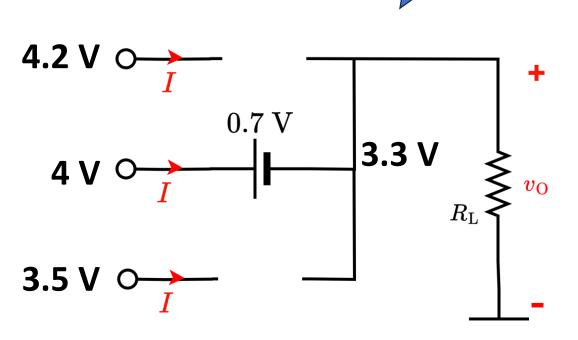
What if the input voltages are different?

**Highest** (possible – and consistent) voltage here!

$$V_{D1} = 1 \text{ V}$$

$$V_{D2} = 0.7 \text{ V}$$

$$V_{D3} = 0.5 \text{ V}$$



$$Z = 4.5 V$$

#### Logic Truth Table

| INPUTS |   | OUTPUT |
|--------|---|--------|
| Х      | Υ | Z      |
| 0      | 0 | 0      |
| 0      | 1 | 0      |
| 1      | 0 | 0      |
| 1      | 1 | 1      |

Logic Levels:

#### **Voltage Truth Table**

| INF | PUTS | OUTPUT |
|-----|------|--------|
| X   | Y    | Z      |
| 0 V | 0 V  | 0 V    |
| 0 V | 5 V  | 0 V    |
| 5 V | 0 V  | 0 V    |
| 5 V | 5 V  | 5 V    |

Low/False

0

Corresponding voltage levels: 0V

High/True

1

5V

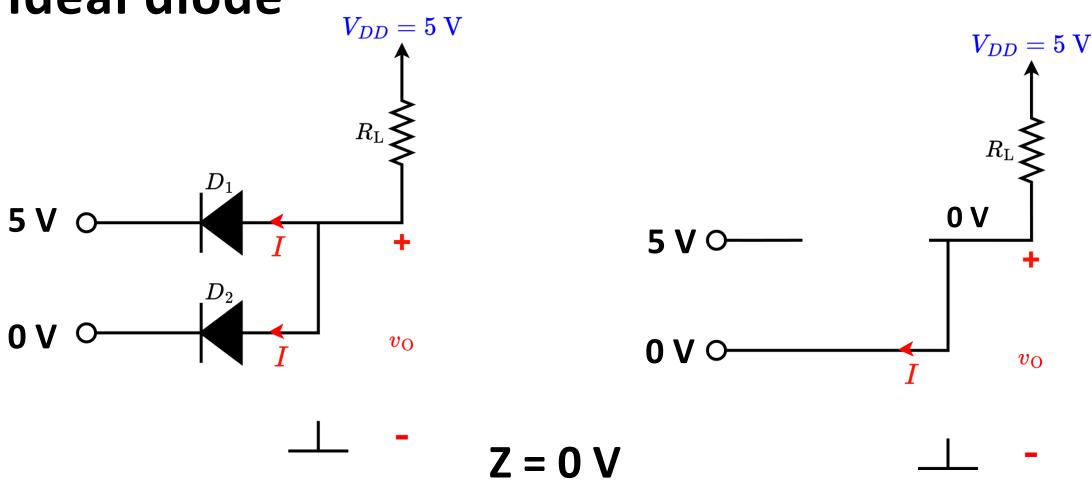
## Logical Operations with Diode (AND) $V_{DD}=5~\mathrm{V}$ Voltage Truth Table **INPUTS** OUTPUT X Z XO $v_{ m O}$

When all inputs are completely disconnected,  $oldsymbol{v_0}$  is <u>pulled up</u> to  $oldsymbol{V_{DD}}$ 

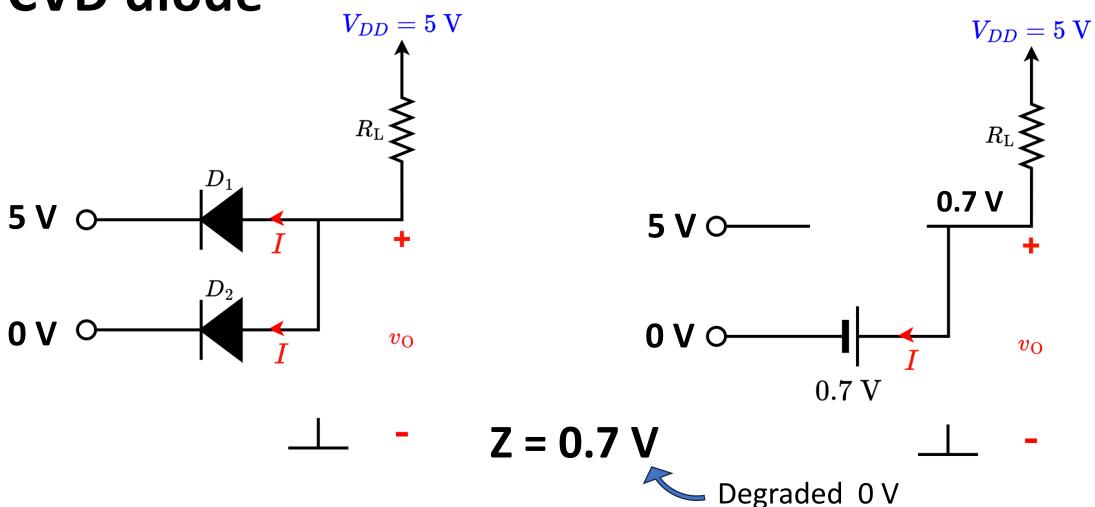
**PULL UP NETWORK** 

Degrades the **LOWEST** output voltage

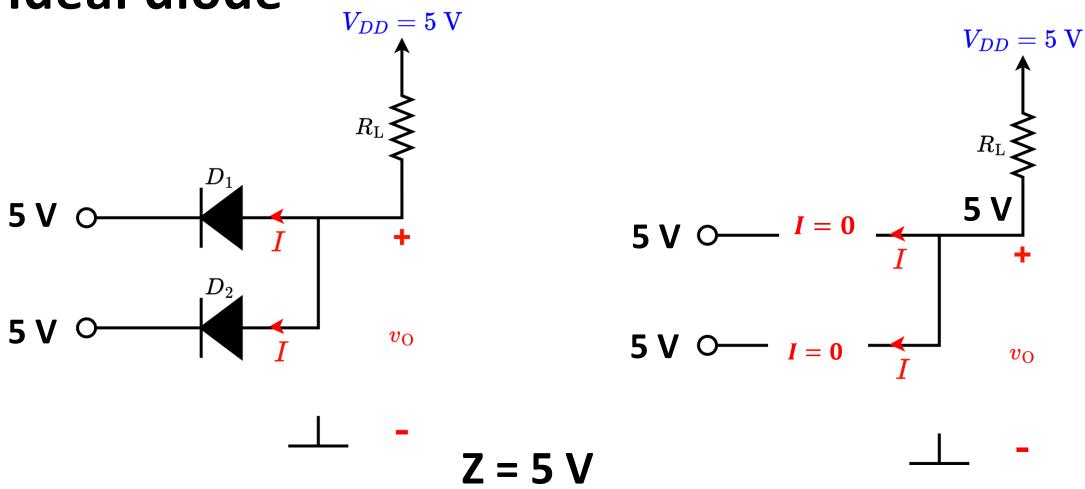
#### Ideal diode

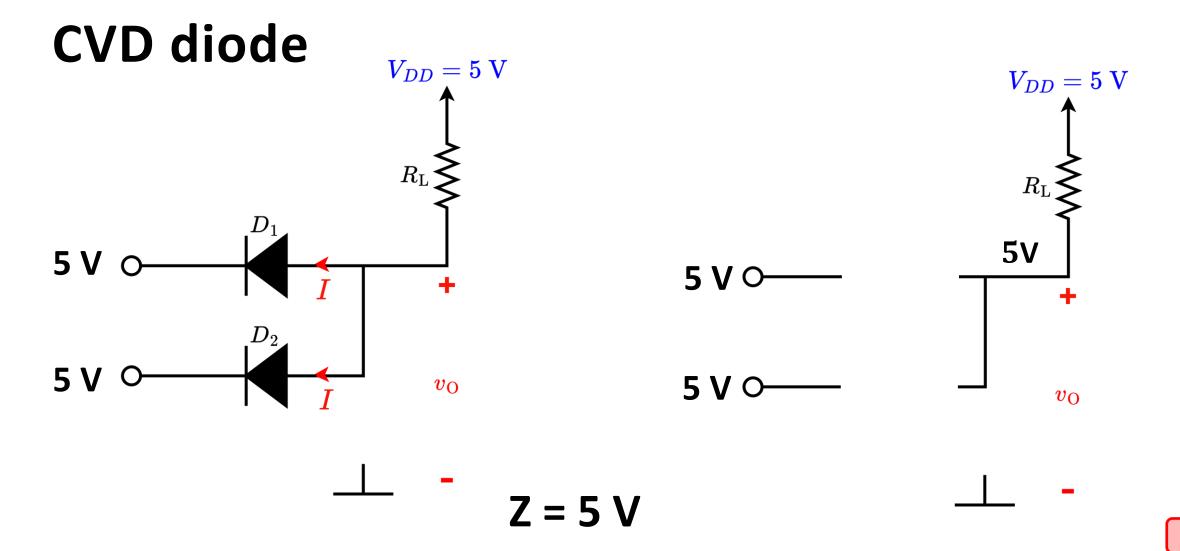


#### **CVD** diode

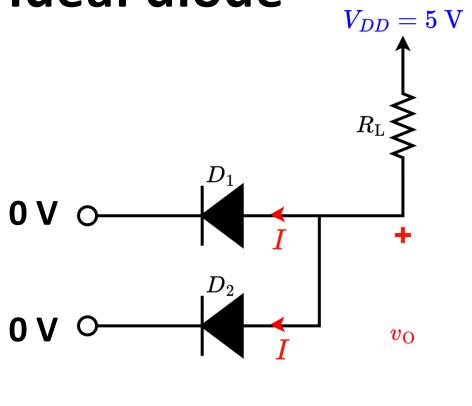


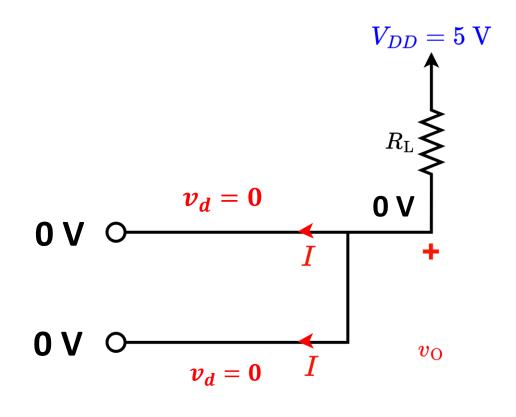
#### Ideal diode





#### Ideal diode



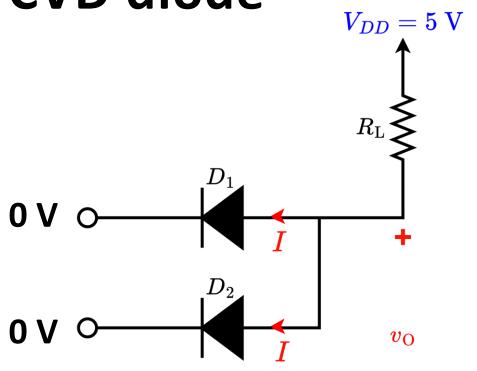


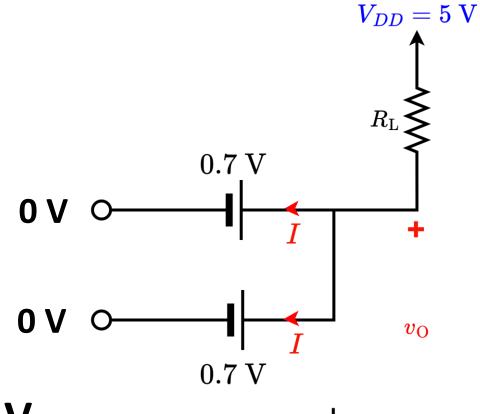
$$Z = 0 V$$





#### **CVD** diode







Both diodes have same  $V_{DO}$ 

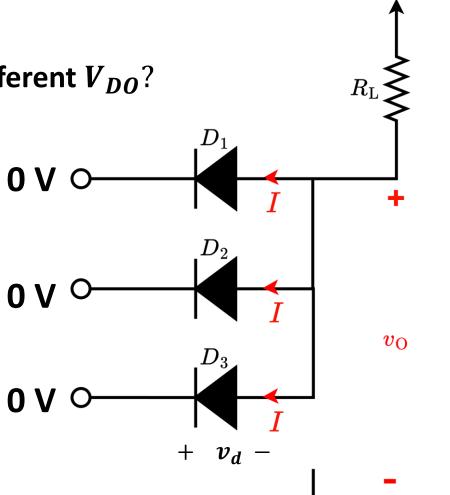
#### **CVD** diode

What if the diodes have different  $V_{DO}$ ?

$$V_{D1} = 1 \text{ V}$$

$$V_{D2} = 0.7 \text{ V}$$

$$V_{D3} = 0.5 \text{ V}$$



 $V_{DD}=5~
m V$ 

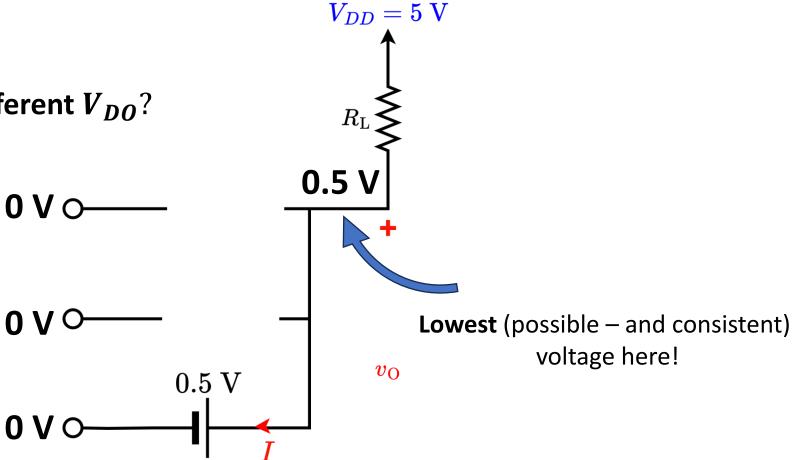
#### CVD diode

What if the diodes have different  $V_{DO}$ ?

$$V_{D1} = 1 \text{ V}$$

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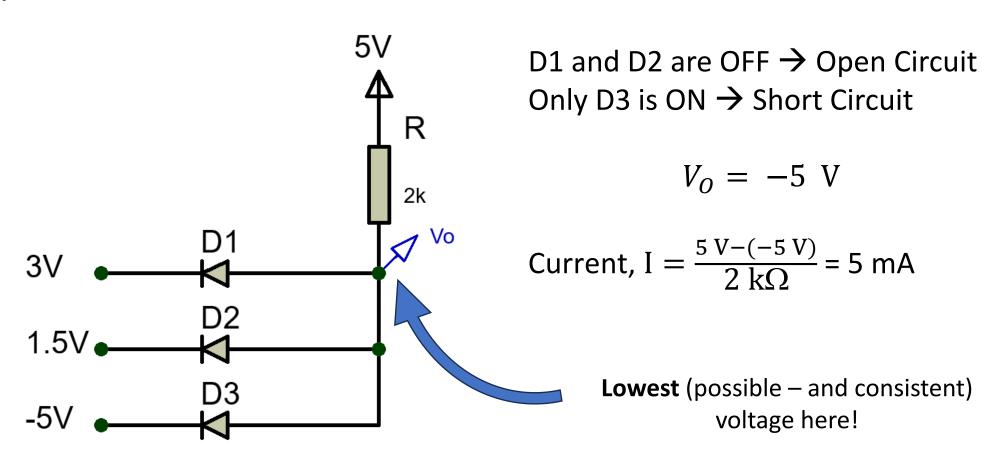


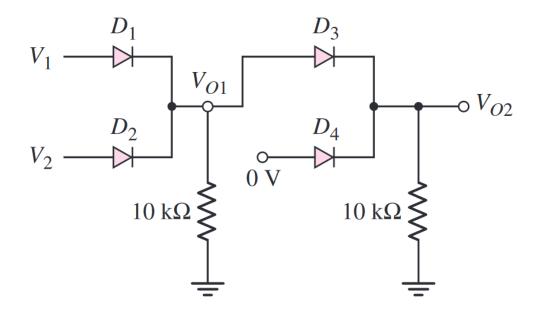
 $+ v_d -$ 

voltage here!

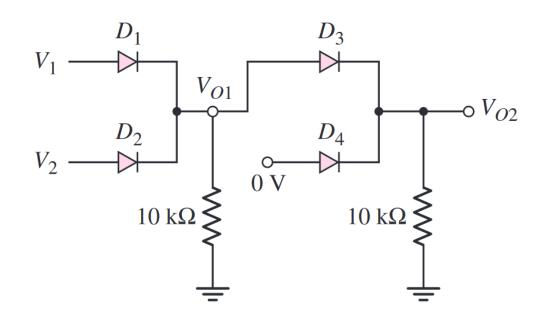
### Effect of input Voltage Variation in Logic Gates (AND)

#### Example 5: Find the value of Vo





$$V_{01} = V_1 \text{ OR } V_2 = V_1 | V_2$$
 
$$V_{02} = (V_{01} \text{ OR } \mathbf{0}) = V_{01} = V_1 | V_2$$



\*\* In CVD diode models, we are assuming that all diodes have equal drop.

#### *Suppose:* $V_1 = 3 \text{ V}, V_2 = 2 \text{ V}.$

#### For Ideal diodes assumption:

 $V_{O1} = V_1 \text{ OR } V_2 \rightarrow \text{Largest Value of the inputs}$ 

$$V_{01} = 3 \text{ V}$$

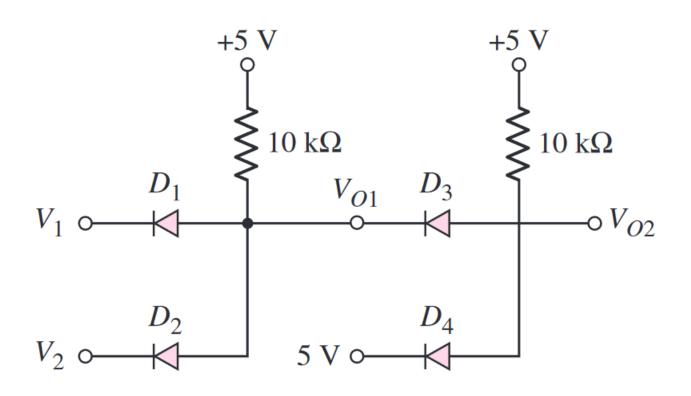
$$V_{O2} = (V_{O1} \text{ OR } 0) = V_{O1} = 3 \text{ V}$$

#### For CVD diodes assumption:

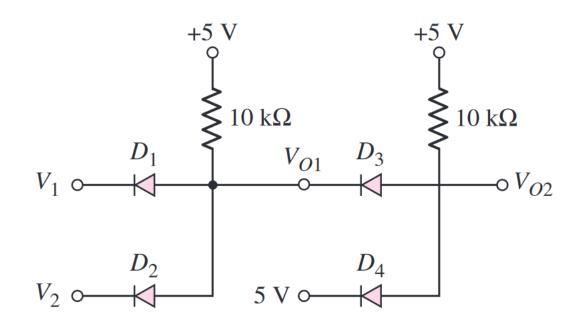
 $V_{O1} = V_1 \text{ OR } V_2 \rightarrow \text{Largest Value of the inputs - } V_{D0}$ 

$$\therefore V_{O1} = (3 - V_{DO}) V$$

$$V_{O2} = (V_{O1} \text{ OR } 0) = V_{O1} - V_{DO} = (3 - 2 V_{DO}) V$$



$$V_{01} = V_1 \; \text{AND} \; V_2 = V_1 \cdot \; V_2$$
  $V_{02} = (V_{01} \; \text{AND} \; \mathbf{5}) = V_{01} = V_1 \cdot \; V_2$ 



Suppose:  $V_1 = 3 \text{ V}$ ,  $V_2 = 1.5 \text{ V}$ .

#### For Ideal diodes assumption:

 $V_{O1} = V_1 \text{ AND } V_2 \rightarrow \text{Smallest Value of the inputs}$ 

$$V_{01} = 1.5 \text{ V}$$

$$V_{02} = (V_{01} \text{ AND 5}) = V_{01} = 1.5 \text{ V}$$

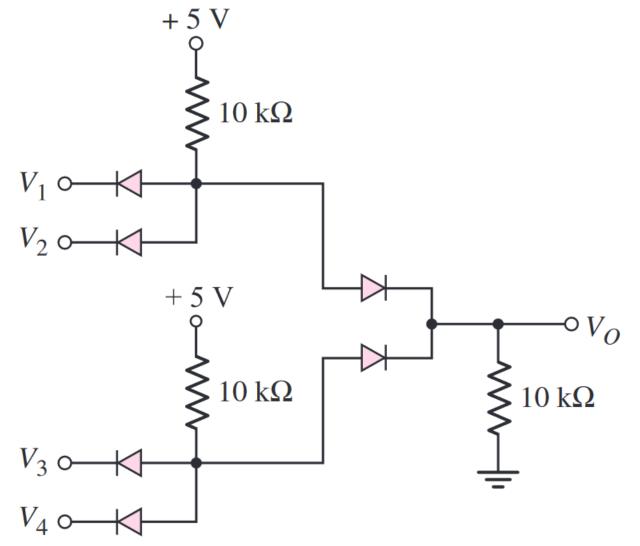
#### For CVD diodes assumption:

 $V_{O1} = V_1 \text{ AND } V_2 \rightarrow \text{Smallest Value of the inputs } + V_{D0}$ 

$$V_{O1} = (1.5 + V_{DO}) \text{ V}$$

$$V_{02} = (V_{O1} \text{ AND 5}) = V_{O1} + V_{DO} = (1.5 + 2 V_{D0}) \text{ V}$$

<sup>\*\*</sup> In CVD diode models, we are assuming that all diodes have equal drop.

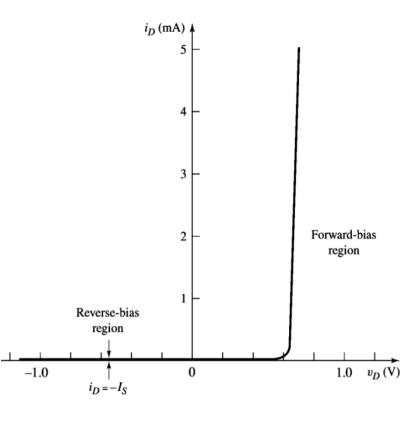


Express  $V_0$  as a Boolean expression of  $V_1, V_2, V_3$  and  $V_4$ 

$$V_O = (V_1 \cdot V_2) | (V_3 \cdot V_4)$$

$$V_O = (V_1 \text{AND } V_2) \text{ OR } (V_3 \text{ AND } V_4)$$

#### Real diode



I-V characteristics of a real diode

Relation between diode current and diode voltage:

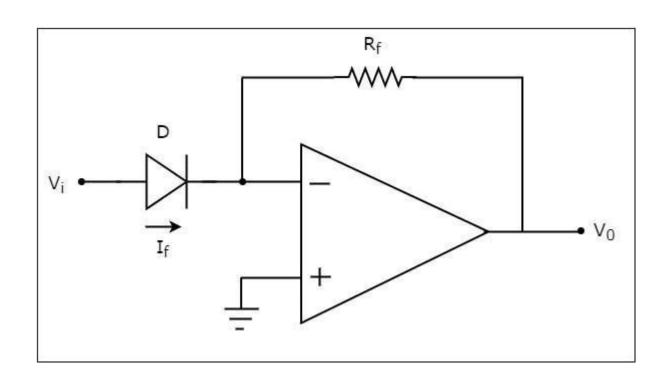
$$i_D = I_S \left( e^{\frac{v_D}{\eta V_T}} - 1 \right)$$

Anode 
$$(v_A)$$
 Cathode  $(v_C)$ 

$$\downarrow i_D + v_D -$$

 $\eta$  is called the ideality factor (try to recall, you measured this in the lab!)

## Exponential (Anti-log) Converter

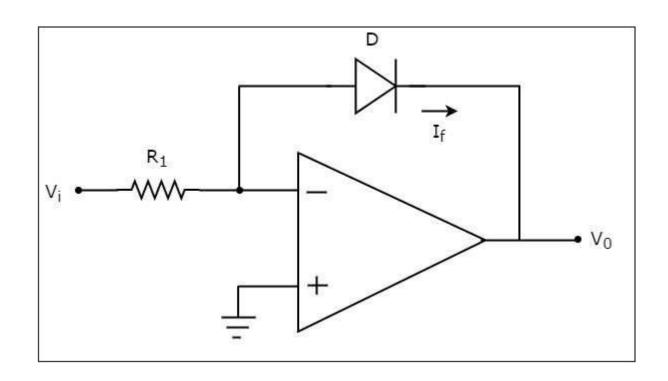


$$I_f = I_S \exp\left(\frac{V_i - 0}{V_T}\right)$$

$$\frac{0 - V_O}{R_f} = I_S \exp(\frac{V_i}{V_T})$$

$$V_{O} = I_{s}R_{f} \cdot \exp(\frac{V_{i}}{V_{T}})$$

## Logarithmic Amplifier



$$I_f = I_S \exp\left(-\frac{V_O}{V_T}\right)$$

$$\frac{V_i}{R_1} = I_S \exp(-\frac{V_O}{V_T})$$

$$\frac{V_i}{I_S R_1} = \exp(-\frac{V_O}{V_T})$$

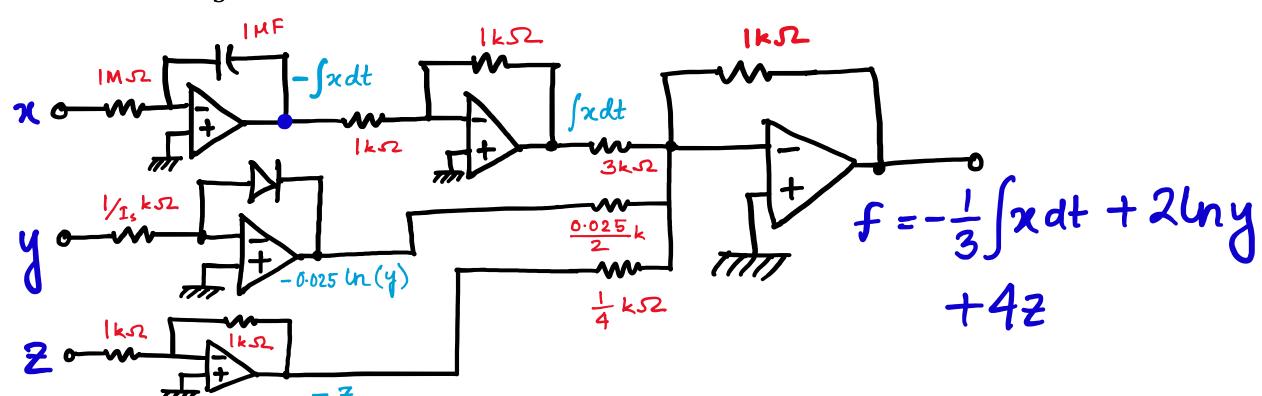
$$V_{O} = -V_{T} \cdot \ln \left( \frac{V_{i}}{I_{S}R_{1}} \right)$$

#### **APPLICATIONS:**

$$\begin{cases}
R_f = 0.025 \text{ V} \\
R_f = \frac{1}{I_s} \text{ k}
\end{cases}$$

Implementing operational functions

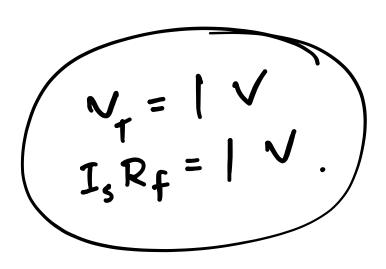
$$f = -\frac{1}{3} \int x \cdot dt + 2 \ln y + 4z = -\left(\frac{1}{3} \int x dt - 2 \ln(y) - 4z\right)$$

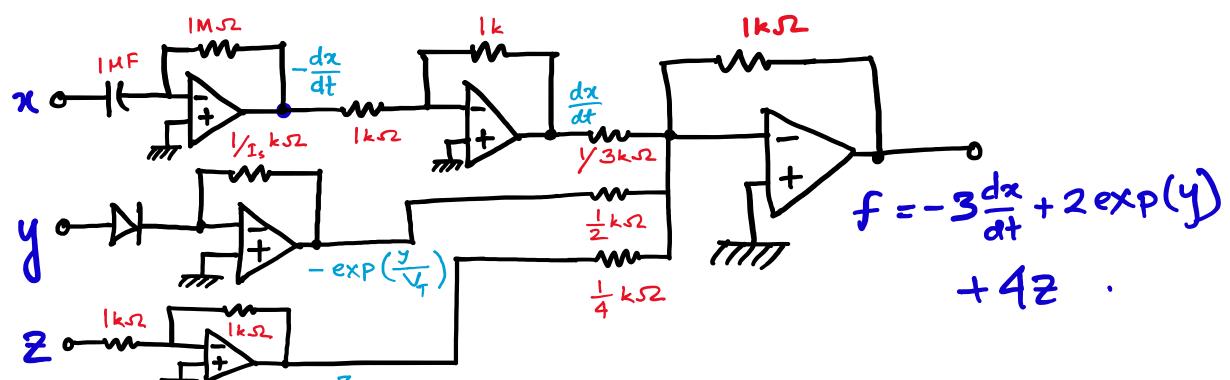


#### **APPLICATIONS:**

#### Implementing operational functions

$$f = -3\frac{dx}{dt} + 2\exp(y) + 4z$$





### Multiplier

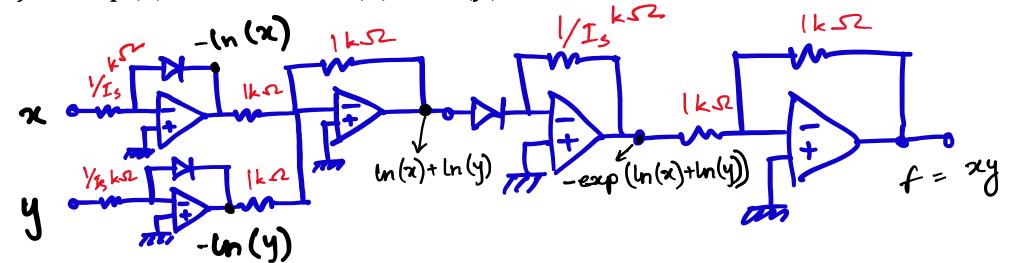
$$f = xy$$

$$\ln(f) = \ln(xy) = \ln(x) + \ln(y)$$

$$f = \exp(\ln(x) + \ln(y))$$

$$1 \cdot R_f = 1$$

So,  $f = \exp(z)$  where  $z = \ln(x) + \ln(y)$ 



### Divider

$$f = xy/z$$

$$\ln(f) = \ln(xy/z) = \ln(x) + \ln(y) - \ln(z)$$

$$f = \exp(\ln(x) + \ln(y) - \ln(z))$$

So,

$$f = \exp(z)$$
 where  $z = \ln(x) + \ln(y) - \ln(z)$ 

