

Answer to the question number : 1

$$\begin{aligned}(a) (101110010001)_2 &= 1 \times 2^{11} + 0 \times 2^{10} + 1 \times 2^9 + 1 \times 2^8 \\ &+ 1 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 \\ &+ 0 \times 2^1 + 1 \times 2^0 \\ &= 2048 + 0 + 512 + 256 + 128 + 0 + 0 \\ &+ 16 + 0 + 0 + 0 + 1 \\ &= (2961)_{10} \\ &\quad \underline{\text{Ans}}\end{aligned}$$

$$\begin{aligned}(b) (11011.101)_2 &= 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} \\ &+ 0 \times 2^{-2} + 1 \times 2^{-3} \\ &= 16 + 8 + 0 + 2 + 1 + 0.5 + 0 + 0.125 \\ &= (27.625)_{10} \\ &\quad \underline{\text{Ans}}\end{aligned}$$

Answer to the question no: 2

$(4195)_{10}$ to binary.

		remainder
2	4195	
2	2097	1 \rightarrow LSB
2	1048	0
2	524	0
2	262	0
2	131	0
2	65	1
2	32	1
2	16	0
2	8	0
2	4	0
2	2	0
2	1	0
2	0	1 \rightarrow MSB

So, $(4195)_{10} = (1000001100011)_2$ Ans

Answer to the question no: 3

$$\begin{aligned}(a) \quad (45)_8 &= 4 \times 8^1 + 5 \times 8^0 \\ &= 32 + 5 \\ &= (37)_{10} \text{ Ans}\end{aligned}$$

$$\begin{aligned}(b) \quad (2173)_8 &= 2 \times 8^3 + 1 \times 8^2 + 7 \times 8^1 + 3 \times 8^0 \\ &= 1024 + 64 + 56 + 3 \\ &= (1147)_{10} \text{ Ans}\end{aligned}$$

Answer to the question no: 4

$(513)_{10}$ to hexadecimal.

16	513	remainder
16	32	1 \rightarrow LSB
16	2	0
16	0	2 \rightarrow MSB

$$\text{So, } (513)_{10} = (201)_{16} \text{ Ans}$$

Answer to the question no: 5

$(101101110)_2$ to hexadecimal

~~Don~~ we need to convert the binary number in group of 4 partition.

$$1101100_2 = 110\ 1100 = (6C)_{16}$$

Ans

Answer to the question no: 6

$$(a) (29)_{12} = (?)_7$$

Firstly, base 12 to base 10,

$$(29)_{12} = (2 \times 12^1) + (9 \times 12^0) = (33)_{10}$$

secondly, base 10 to 7,

7	33	remainder	
7	4	5	→ LSB
7	0	4	→ MSB

$$\text{So, } (29)_{12} = (45)_7 \quad \underline{\text{Ans}}$$

$$(b) (10110111)_5 = (?)_4$$

Firstly, Base 5 to Base 10,

$$\begin{aligned} (10110111)_5 &= (1 \times 5^7) + (0 \times 5^6) + (1 \times 5^5) + (1 \times 5^4) \\ &\quad + (0 \times 5^3) + (1 \times 5^2) + (1 \times 5^1) + (1 \times 5^0) \\ &= 78125 + 0 + 3125 + 625 + 1250 \\ &\quad + 25 + 5 + 1 \\ &= (81906)_{10} \end{aligned}$$

Secondly, Base 10 to base 4 calculation,

4	81906	remainder
4	20476	2 \rightarrow LSB
4	5119	0
4	1279	3
4	319	3
4	79	3
4	19	3
4	4	3
4	1	0
4	0	1 \rightarrow MSB

So, $(10110111)_5 = (103333302)_4$ Ans

Answer to the question no: 7

Addition

$$\begin{array}{r} (412)_9 \\ + (134)_9 \\ \hline (546)_9 \end{array}$$

$2+4=6<9$
 $1+3=4<9$
 $4+1=5<9$

Ans

Converting the value
into decimal,

$$\begin{aligned} & (546)_9 \\ &= \cancel{5 \times 10^2} + \cancel{4 \times 10^1} + 6 \times 10^0 \\ &= 5 \times 9^2 + 4 \times 9^1 + 6 \times 9^0 \\ &= (447)_{10} \end{aligned}$$

Ans

Substraction

$$\begin{array}{r} (349)_9 \\ - (134)_9 \\ \hline (267)_9 \end{array}$$

$9+2=11$
 $0+9=9$

Converting the value
into decimal,

$$\begin{aligned} & (267)_9 \\ &= 2 \times 9^2 + 6 \times 9^1 + 7 \times 9^0 \\ &= \cancel{36} + \cancel{18} + 7 \\ &= \cancel{162} + 54 + 7 \\ &= (223)_{10} \end{aligned}$$

Ans

Multiplication

$$\begin{array}{r} (412)_9 \\ \times (134)_9 \\ \hline 1748 \\ 1336 \times \\ 412 \times \times \\ \hline (56418)_9 \end{array}$$

$9)12(1 \text{ } 9)6(7(1$
 $\frac{9}{3} \quad \frac{9}{7}$

Converting the value
into decimal,

$$\begin{aligned} & (56418)_9 \\ &= 5 \times 9^4 + 6 \times 9^3 + 4 \times 9^2 \\ & \quad + 1 \times 9^1 + 8 \times 9^0 \\ &= 32805 + 4374 + 324 \\ & \quad + 9 + 8 \\ &= (37520)_{10} \end{aligned}$$

Ans

for verifying the addition value converting
base-5 to base-10,

$$(412)_5 = 4 \times 5^2 + 1 \times 5^1 + 2 \times 5^0 = (335)_{10}$$

$$(134)_5 = 1 \times 5^2 + 3 \times 5^1 + 4 \times 5^0 = (112)_{10}$$

Addition of decimal,

$$\begin{array}{r} (335)_{10} \\ (112)_{10} \\ \hline (447)_{10} \end{array}$$

Now converting the decimal to ~~binary~~ ^{base-5} for verification..

5	447	
5	49	6 → LSB
5	5	4
5	0	5 → MSB

$$(546)_5 = (545)_5 \quad (\text{verified})$$

Now, ~~converting the~~ subtracting
two decimal values,

$$\begin{array}{r} (335)_{10} \\ (112)_{10} \\ \hline (223)_{10} \end{array}$$

Converting two base-5,

5	223	
5	24	7
5	2	6
	0	2

$$(267)_5 = (267)_5 \quad (\text{verified})$$

multiplying the decimal value,

$$\cancel{(412)}_{10} \quad (335)_{10}$$

$$\times (112)_{10}$$

$$\begin{array}{r} 670 \\ 335 \times \\ 335 \times \times \\ \hline (37520)_{10} \end{array}$$

converting to base-9,

$$\begin{array}{r|l} 9 & 37520 \\ \hline 9 & 4168 \quad 8 \\ 9 & 51 \quad 1 \\ 9 & 5 \quad 4 \\ 9 & 0 \end{array}$$

$$\begin{array}{r|l} 9 & 37520 \\ \hline 9 & 4168 \quad 8 \\ 9 & 463 \quad 1 \\ 9 & 51 \quad 4 \\ 9 & 5 \quad 6 \\ 9 & 0 \quad 5 \end{array}$$

$$(37520)_{10} = (56418)_9$$

$$(56418)_9 = (56418)_9 \text{ (verified)}$$

Ans

Answer to the question no: 8

Given, $(01000010)_{16}$

First, Converting into decimal,

$(01000010)_2$

$$= 0 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$$

$$= 0 + 64 + 0 + 0 + 0 + 0 + 2 + 0$$

$$= (66)_{10}$$

Lastly, Converting into 8 bit - ones,

$$(01000010)_{16} = (+66)_{10}$$

Ans

Answer to the question no. 9

Given,

$$(10111100)_{2's}$$

First, inverting, (10111100) , $-(01000100)$

$$\begin{array}{r} \cancel{0110} \cancel{(10111100)} \Rightarrow \cancel{1010000} \\ \quad \quad \quad \cancel{(0111100)} \end{array}$$

Secondly, converting binary to decimal ,

$$-(01000100)$$

$$= 0 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 \\ + 0 \times 2^1 + 0 \times 2^0$$

$$= 0 + 64 + 0 + 0 + 0 + 4 + 0 + 0$$

$$= (68)_{10}$$

$$\therefore (10111100)_{2's} = -(68)_{10}$$

Ans

Answer to the question no: 10

Given, 91 - 455 in 2's & 1's complement

First, converting in 1's complement

Now, converting this two numbers in decimal.

2	91	remainder
2	45	1 → LSB
2	22	1
2	11	0
2	5	1
2	2	1
2	1	0
2	0	1 → MSB

2	455	remainder
2	245	1 → LSB
2	124	1
2	62	0
2	31	0
2	15	0
2	7	1
2	3	1
2	1	1
2	0	1 → MSB

$$(91)_{10} = (1011011)_2$$

$$(455)_{10} = (11110011)_2$$

Converting in 1's complement,

$$(1011011)_2 \rightarrow (1011011)_2$$

$$- (11110011)_2 \rightarrow (000001100)_2$$

$$\begin{array}{r} 001011011 \\ 000001100 \\ \hline \end{array}$$

$$(0001100111)_{13}$$

[No overflow]
[converted to 10 bit]

converting binary to decimal,

$$(0001100111)_2 = 0 \times 2^9 + 0 \times 2^8 + 0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$= 0 + 0 + 0 + 64 + 32 + 0 + 0 + 4 + 2 + 1$$

$$= (103)_{10} \text{ Ans}$$

Secondly, converting into 1's complement,

Now, inverting second value's binary number, $(111110011)_2 \rightarrow (000001100)_2$

So, adding 1,

$$\begin{array}{r} 000001100_2 \\ + 1 \\ \hline 000001101_2 \end{array}$$

Now, Let's add,

$$\begin{array}{r} 001011011_2 \\ + 000001101_2 \\ \hline (000110100)_2 \end{array} \quad \begin{array}{l} \text{[No carry]} \\ \text{[No overflow]} \end{array}$$

Ans [in 10 bit]

Lastly, converting into decimal,

$$\begin{aligned} (0001101000)_2 &= 0 \times 2^8 + 0 \times 2^7 + 1 \times 2^6 \\ &+ 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 \\ &+ 0 \times 2^0 \\ &= 0 + 0 + 64 + 32 + 0 + 8 + 0 + 0 + 0 \\ &= (104)_{10} \text{ Ans} \end{aligned}$$

Answer to the question no: 11

Given, 2 8GB DDR4 RAMs costs
 $(102)_{16}$ each

Also, RTX costs $(10010110000)_2$ dollars

Friend gave $(4064)_8$ dollars

Now, converting all the values in decimal,

$$(102)_{16} = 1 \times 16^2 + 12 \times 16^1 + 2 \times 16^0$$

$$= 256 + 192 + 2$$

$$= (450)_{10}$$

$$(10010110000)_2 = 1 \times 2^{10} + 0 \times 2^9 + 0 \times 2^8 + 1 \times 2^7$$

$$+ 0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$$

$$= 1024 + 0 + 0 + 128 + 0 + 32 + 16 + 0 + 0 + 0$$

$$= (1200)_{10}$$

$$(4064)_8 = 4 \times 8^3 + 0 \times 8^2 + 6 \times 8^1 + 4 \times 8^0$$

$$= 2048 + 0 + 48 + 4$$

$$= (2100)_{10}$$

I have 2100_{10} dollars, If I buy those two components I will have $= 2100_{10} - (450 + 1200)_{10}$

$$= (450)_{10}$$

\therefore I have left $(450)_{10}$ dollars.

Ans