

Name of Experiment: Implementation of 4-bit Magnitude comparator

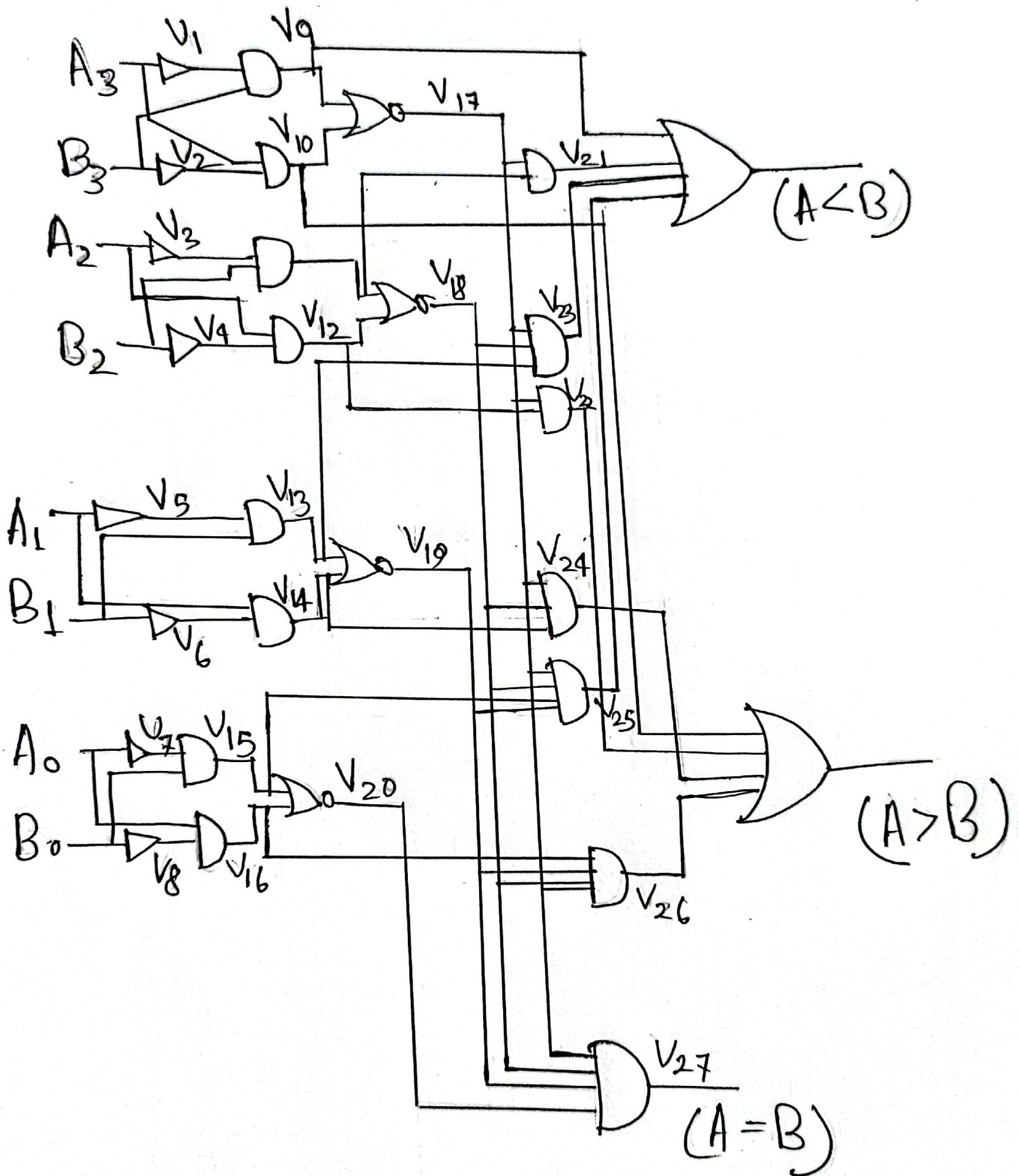
Objective:

1. Realization of 1-bit comparator using logic gates.
2. Understanding and implementation of 2-bit comparator using logic gates on breadboards.
3. Implementation of 4-bit magnitude comparator using IC-7485

Required components and equipments:

Logic state (8 pcs), Logic probe (Big) (3 pcs), An AND Gate (2) (10 pcs), AND-3 Gate (2 pcs), AND-4 Gate (3 pcs), NOR-2 (4 pcs), OR-4 Gate (2 pcs), NOT Gate (8 pcs)

Experimental setup:



□ Result and discussion:

A	B	$A < B$	$A = B$	$A > B$
0	0	0	1	0
0	1	1	0	0
1	0	0	0	1
1	1	0	1	0

□ Discussion:

* One-bit magnitude comparator:

A comparator used to compare ~~two~~ 1-bit binary numbers. It has two binary inputs A & B & 3 binary output which represents equal, less than and greater than relation.

When it is greater than, $(A > B) = AB'$

When it is less than, $(A < B) = A'B$

When it is equal $(A=B) = A'B' + AB$
 $= (A+B)'$

* Two-bit Magnitude Comparator:

A two bit comparator has 4 binary input which are $(A: A_1, A_0)$ & $(B: B_1, B_0)$ & where comes 3 binary outputs, which are greater than, less than & equal.

When it is greater than,

$$\begin{aligned}(A > B) &= A_1 B_1' + A_1' A_0 B_1' B_0' + A_1 A_0 B_1 B_0' \\&= A_1 B_1' + A_0 B_0' (A_1' B_1' + A_1 B_1) \\&= A_1 B_1' + A_0 B_0' (A_1 \oplus B_1)'\end{aligned}$$

When it is less than,

$$\begin{aligned}(A < B) &= A_1' B_1 + A_1' A_0' B_1' B_0 + A_1 A_0' B_1 B_0 \\&= A_1' B_1 + A_1' B_0 (A_1' B_1' + A_1 B_1) \\&= (A_1' B_1) + A_0 B_0' (A_1 \oplus B_1)'\end{aligned}$$

When it is equal,

$$\begin{aligned}(A=B) &= A_1' A_0' B_1' B_0' + A_1' A_0 B_1' B_0 + A_1 A_0 B_1 B_0 \\&= (A_1' B_1' + A_1 B_1) (A_0' B_0' + A_0 B_0) \\&= (A_1 \oplus B_1)' (A_0 \oplus B_0)'\end{aligned}$$

★ Three-bit magnitude comparator:

A three-bit magnitude comparator has 6 inputs

A (A_2, A_1, A_0) & B (B_2, B_1, B_0) & 3 outputs

which are, less than, greater than & equal.

All inputs & outputs are binary.

When it is greater than,

$$(A > B) = A_2 B_2 + [(A_2' B_2' + A_2 B_2) \cdot A_1 B_1'] + [(A_2' B_2' + A_2 B_2) \cdot (A_1' B_1' + A_1 B_1) \cdot A_0 B_0']$$

When it is less than,

$$(A < B) = A_2' B_2 + [(A_2' B_2' + A_2 B_2) \cdot A_1' B_1] + [(A_2' B_2' + A_2 B_2) \cdot (A_1' B_1' + A_1 B_1) \cdot A_0 B_0']$$

When it is equal,

$$(A=B) = (A_0' B_0' + A_0 B_0) \cdot (A_1' B_1' + A_1 B_1) \cdot (A_2' B_2' + A_2 B_2)$$

* 4-bit magnitude operator:

4-bit magnitude operators have 8 inputs & 3 outputs. 4 inputs are $A(A_3, A_2, A_1, A_0)$, $B(B_3, B_2, B_1, B_0)$. Outputs are $(A > B)$, $(A < B)$, $(A = B)$. All are boolean inputs & outputs.

$$\text{for } (A > B) = A_3 B_3 + (A_3 \oplus B_3) \cdot A_2 B_2 + (A_3 \oplus B_3) (A_2 \oplus B_2) A_1 B_1 + (A_3 \oplus B_3) (A_2 \oplus B_2) (A_1 \oplus B_1) (A_0 B_0)$$

$$\text{for } (A < B) = A_3' B_3 + (A_3 \oplus B_3) A_2' B_2 + (A_3 \oplus B_3) (A_2 \oplus B_2) A_1' B_1 + (A_3 \oplus B_3) (A_2 \oplus B_2) (A_1 \oplus B_1) (A_0' B_0)$$

$$\text{for } (A = B) = (A_3 \oplus B_3)' (A_2 \oplus B_2)' (A_1 \oplus B_1)' (A_0 \oplus B_0)'$$

* Working procedure of 4-bit magnitude comparison-

When it is equal, $A_3 = B_3$, $A_2 = B_2$, $A_1 = B_1$ & $A_0 = B_0$

During Inequality:

① If $A_3 = 1$ & $B_3 = 0$ then $A > B$, or

② If A_3 & B_3 are equal & $A_2 = 1$ & $B_2 = 0$ then $A > B$, or

③ If A_3 & B_3 are equal & A_2 & B_2 are equal & if $A_1 = 1$ & $B_1 = 0$ then $A > B$, or

④ If A_3 & B_3 are equal, A_2 & B_2 are equal & A_1 & B_1 are equal & $A_0 = 1$, $B_0 = 0$ then $A > B$.

⑤ If $A_3 = 0$ & $B_3 = 1$ then $(A < B)$, or

⑥ If A_3 & B_3 are equal & if $A_2 = 0$ & $B_2 = 1$ then $A < B$, or

⑦ If A_3 & B_3 are equal & A_2 & B_2 are equal & if $A_1 = 0$ & $B_1 = 1$ then $A < B$ or

⑧ If A_3 & B_3 are equal, A_2 & B_2 are equal & A_1 & B_1 are equal & if $A_0 = 0$ & $B_0 = 1$ then $A < B$