Abou, 
$$\vec{u}_1, \vec{u}_2 = \frac{1}{\sqrt{5} \cdot \sqrt{30}} (2.1 - 1/2 - 0.5) = 0$$

$$\vec{u}_2 \cdot \vec{u}_3 = \frac{1}{\sqrt{30 \cdot \sqrt{24}}} \left( \sqrt{12 + 2 \cdot 4} - 5 \cdot 2 \right) = 0$$

Since, each voctor has norm or magnitude I and all pours have dot product zero, The set Si an orthonormal set &

(6) the dada volues are:

the days volues are:  

$$x_0 = 4 = 7 + (x_0) = 5 - 6 = -0.757$$
.

Eine, me best tit curve in a straight line, me have, n=1. Hence, me watress are:

$$A = \begin{pmatrix} 1 & x_{0} \\ 1 & x_{1} \\ 1 & x_{2} \end{pmatrix} = \begin{pmatrix} 1 & 4 \\ 1 & 9 \\ 1 & -6 \end{pmatrix} \Rightarrow x = \begin{pmatrix} a_{0} \\ a_{1} \end{pmatrix} = ?? + b = \begin{pmatrix} f(x_{0}) \\ f(x_{1}) \\ f(x_{2}) \end{pmatrix} = \begin{pmatrix} -0.757 \\ 0.412 \\ 0.279 \end{pmatrix}.$$

Ax=b, ne calculatio.

$$= \frac{1}{4} \left( \frac{1}{9} - \frac{1}{6} \right) \left( \frac{1}{9} - \frac{1}{6} \right) \left( \frac{1}{4} - \frac{1}{9} - \frac{1}{6} \right) \left( \frac{-0.757}{0.412} \right) \left( \frac{1}{0.279} \right)$$

$$\Rightarrow \begin{pmatrix} 3 & 7 \\ 7 & 133 \end{pmatrix} \begin{pmatrix} \alpha_0 \end{pmatrix} = \begin{pmatrix} -0.066 \\ -0.994 \end{pmatrix}$$

$$= \begin{pmatrix} 0.38 & -0.02 \\ -0.02 & 8.5 \times 10^{3} \end{pmatrix} \begin{pmatrix} -0.066 \\ -0.994 \end{pmatrix}$$

Same best fit straight line as

$$P_1(x) = a_0 + a_1 x = -0.0052 - 0.0072 x x$$

#2 (a) From me given daba, me find, n=2, and chenco.

$$A = \begin{pmatrix} 1 & \kappa_0 & \kappa_0^2 \\ 1 & \kappa_1 & \kappa_1^2 \\ 1 & \kappa_2 & \kappa_2^2 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 4 & 16 \\ 1 & -1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \quad b = \begin{pmatrix} f(\kappa_1) \\ f(\kappa_1) \\ f(\kappa_2) \\ f(\kappa_2) \\ f(\kappa_3) \end{pmatrix} = \begin{pmatrix} 3 \\ -2 \\ 1 \\ 1 \end{pmatrix}$$

and  $X = (a_0, a_1, a_2)^T = ??$ 

From A me identify:  $u_1 = (1 \ 1 \ 1)^T; u_2 = (0 \ 4 - 1 \ 1)^T + u_3 = (0 \ 16 \ 1 \ 1)^T$ 

Since here are only 3 columns (because n = 2,000) por mehanismy 3 linearly independent kectors.

$$p_2 = u_2 - (u_2 T q_1) q_1 = \begin{pmatrix} 0 \\ 4 \\ -1 \end{pmatrix} - \begin{pmatrix} 0 & 4 - 1 & 1 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

$$\Rightarrow p_2 = \begin{pmatrix} 0 \\ 4 \\ -1 \end{pmatrix} \xrightarrow{q} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 3 \\ -2 \\ 0 \end{pmatrix}$$

And brulles:

$$= \begin{pmatrix} 0 \\ 16 \\ 1 \end{pmatrix} - \begin{pmatrix} 14 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} 0 \\ 16 \\ 1 \\ 1 \end{pmatrix} - \begin{pmatrix} 14 \\ 14 \\ 1 \end{pmatrix} \begin{pmatrix} 0 \\ 16 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} -1 \\ 3 \\ -2 \\ 0 \end{pmatrix} \begin{pmatrix} -1 \\ 3 \\ -2 \\ 0 \end{pmatrix} \begin{pmatrix} -1 \\ 3 \\ -2 \\ 0 \end{pmatrix}$$

$$= \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} - \frac{9}{2} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \frac{23}{7} \begin{pmatrix} -1 \\ 3 \\ -2 \\ 0 \end{pmatrix} = \frac{1}{14} \begin{pmatrix} -17 \\ 23 \\ 43 \\ -49 \end{pmatrix}$$

$$\frac{1}{(70)} = \frac{1}{(70)} = \frac{1}{5.085} \begin{pmatrix} -\frac{17}{14} \\ \frac{23}{14} \\ \frac{43}{14} \\ \frac{1}{-40} \end{pmatrix} = \frac{1}{63} = \begin{pmatrix} -0.239 \\ 0.323 \\ 0.604 \\ -0.688 \end{pmatrix}$$

(c) There: 
$$R = \left( u_1^T q_1, u_2^T q_1, u_3^T q_1 \right)$$
 From Part—(h), me already hano.

 $\left( u_2^T q_2, u_3^T q_2 \right)$   $\left( u_3^T q_1 = 2^{-\frac{1}{2}}, u_3^T q_1 = 9^{-\frac{1}{2}} \right)$ 
 $\left( u_3^T q_2 = 12.294^{-\frac{1}{2}} \right)$ 
 $\left( u_3^T q_3 \right)$ 
 $\left( u_3^T q_3 \right)$ 
 $\left( u_3^T q_1 = (1111) \right) \left( \frac{1}{2} \right)^2 = 2^{-\frac{1}{2}}$ 

$$u_{1}^{T}\theta_{1} = (0 \ 4 \ -1 \ 1) \begin{pmatrix} -1 \\ 3 \\ -2 \end{pmatrix} \cdot \sqrt{1}u^{2} = 3.742^{\frac{1}{2}}$$

$$adu_{3}q_{3}=(0.1611)\begin{pmatrix} -0.139\\ 0.323\\ 0.604\end{pmatrix}=5.084$$

(d) 
$$Rx = \begin{pmatrix} 2 & 2 & 9 \\ 0 & 3.7412 & 12.794 \end{pmatrix} \begin{pmatrix} \alpha_6 \\ \alpha_1 \\ 0 & 0 & 5.084 \end{pmatrix} = \begin{pmatrix} 2\alpha_6 + 7\alpha_1 + 9\alpha_2 \\ 3.7412\alpha_1 + 12.794\alpha_2 \\ 5.084\alpha_2 \end{pmatrix} 42$$

and to Nov. me & metria is

$$Q = \begin{cases} 9, 92 & 0.00 \\ 0.5 & 0.00 \\ 0.5 & 0.00 \end{cases} = \begin{pmatrix} \frac{1}{2} & -\frac{1}{114} & -0.239 \\ \frac{1}{2} & \frac{3}{114} & 0.323 \\ \frac{1}{2} & -\frac{2}{114} & 0.604 \\ \frac{1}{2} & 0 & -0.668 \end{pmatrix} = \begin{pmatrix} 0.5 & -0.267 & -0.239 \\ 0.5 & 0.802 & 0.323 \\ 0.5 & 0.535 & 0.604 \\ 0.5 & 0 & -0.668 \end{pmatrix}$$

$$\frac{1.816}{-0.167} = \begin{vmatrix} 0.5 & 0.5 & 0.5 \\ -0.167 & 0.802 & -0.535 & 0 \\ -0.239 & 0.323 & 0.609 & -0.688 \end{vmatrix} \begin{pmatrix} 3 \\ -2 \\ 2 \\ 1 \end{pmatrix} = \begin{vmatrix} 2 \\ -3.475 \\ -0.843 \end{vmatrix}$$

(e) Size : 
$$2x = Q^{T}b$$
, we have
$$\begin{vmatrix}
2a_0 + 2a_1 + 9a_2 \\
3.7429_1 + 12.7949_2
\end{vmatrix} = \begin{vmatrix}
-3.475 \\
-0.843
\end{vmatrix}$$
Cumpairy 2)  $Q_2 = -\frac{843}{5.084}$   $\Rightarrow$   $|Q_2 = -0.166|$ 

And 
$$3.7429_1 + 12.2949_2 = -3.475$$
  

$$\Rightarrow 9_1 = \frac{-3.475 - 12.294(-0.166)}{3.742} \Rightarrow 9_1 = -0.383$$

Anally: 
$$2a_0 + 2a_1 + 9a_2 = 2$$
  
=  $3a_0 = \frac{2-2(-0.383) - 9(-0.166)}{2} = \sqrt{a_0} = 2.130$ 

Therefore, me polynomial pr(x) 4  $p_2(x) = 0.401x + 0.2x^2 = 2.13 - 0.383x - 0.166x^2$