Due Date: April 12, 2023

Instructions for preparing the solution script:

- Write your name, ID#, and Section number clearly in the very front page.
- Write all answers sequentially.
- Start answering a question (not the part of the question) from the top of a new page.
- Write legibly and in orderly fashion maintaining all mathematical norms and rules. Prepare a single solution file.
- Start working right away. There is no late submission form. If you miss the deadline, you need to use the make-up assignment to cover up the marks.
- 1. A linear system is described by the following equations.

$$2x - 2y + z = -3$$

 $x + 3y - 2z = 1$
 $3x - y - z = 2$

- (a) (3 marks) From the given linear equations, identify the matrices A, x and b such the linear system can be expressed as a matrix equation.
- (b) (2 marks) Does this system have any unique solution? Explain.
- (c) (6 marks) Evaluate the upper triangular matrix U by Gaussian elimination method. Note that you have to show the row multipliers m_{ij} for each step as necessary.
- (d) (4 marks) Using the upper triangular matrix found in the previous question, compute the solution of the given linear system by Gaussian elimination method.
- 2. A linear system is described by the following equations.

$$\begin{array}{rcl} x + 2y - z & = & 0 \\ 2x - y + z & = & 1 \\ -x + y + 2z & = & 2 \end{array}$$

- (a) (2 marks) From the given linear equations, identify the matrices A. Examine if the matrix A has any pivoting problem? Explain why or why not?
- (b) (4 marks) State how many Frobenius matrices, $F^{(i)}$, $i = 1, 2, \dots$, can be computed, and evaluate them for the given system.
- (c) (3 marks) Evaluate the unit lower triangular matrix L, and the upper triangular matrix U.
- (d) (6 marks) Now compute the solution of the given linear system using LU-decomposition method. Use the matrices L and U found in the previous question. Show your works.