

Transverse field Ising model spectrum

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Abstract

We calculate $\chi''(\omega)/\omega$ spectrum by interpolating the $G(i\omega_n)$ data obtained by cmipo method using Nevalinna analytical continuation algorithm.

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I. THE ISING CHAIN IN A TRANSVERSE FIELD

Hamiltonian:

$$H = -J \sum_{\langle i,j \rangle} \sigma_i^z \sigma_j^z - \Gamma \sum_i \sigma_i^x = -J \sum_{\langle i,j \rangle} \sigma_i^z \sigma_j^z - Jg \sum_i \sigma_i^x \quad (1)$$

where σ_i^α , $\alpha = x, y, z$ are Pauli matrices, $\langle \dots \rangle$ stands for nearest neighbor, $g = \Gamma/J$ and we set $J = 1.0$.

At finite temperature, the local two time correlation $\chi(\tau)$ is defined as:

$$\chi(\tau) = \langle \sigma_i^z(\tau) \sigma_i^z(0) \rangle \quad (2)$$

We ca limit ourselves to $\tau \in [0, \beta]$ by the boundary conditions in τ .

Its Fourier transform is:

$$\chi(i\omega_n) = \int_0^\beta d\tau \chi(\tau) e^{i\omega_n \tau} \quad (3)$$

Let $\chi(\omega) = \chi(i\omega_n \rightarrow \omega + i0^+)$, define $\chi''(\omega) = 2\text{Im}\chi(\omega)$, it related to the structure factor $S(\omega)$ via:

$$S(\omega) = \frac{\chi''(\omega)}{1 - e^{-\beta\omega}} \quad (4)$$

then $\chi''(\omega)$ has the following sum rule:

$$\int_{-\infty}^{\infty} d\omega \frac{\chi''(\omega)}{\omega} = \chi(T) = -G(i\omega_n = 0) \quad (5)$$

II. QUANTUM CRITICAL POINT

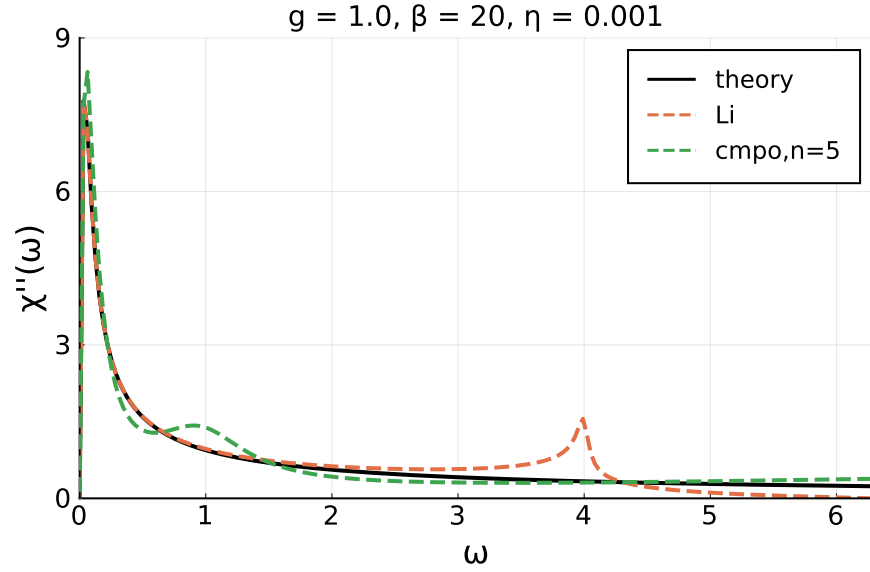


FIG. 1. The solid line is the semi-classical theoretical results. The orange dash line is the numerical results obtain by Zi-Long Li; the green dash line is the Nevalinna analytical continuation results. $n = 5$ means we use the first 5 Mausbara frequencies data, start from $i\omega_1$, which is the best fit.

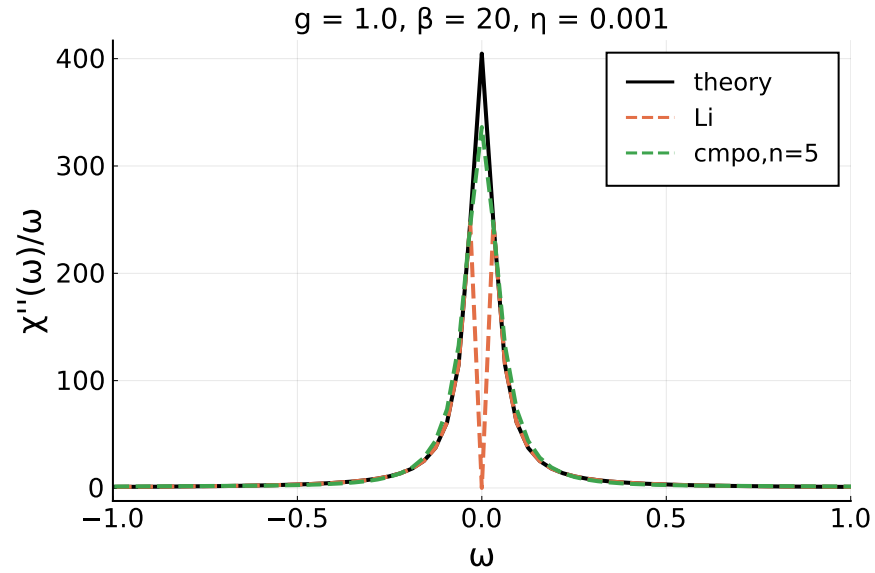


FIG. 2.

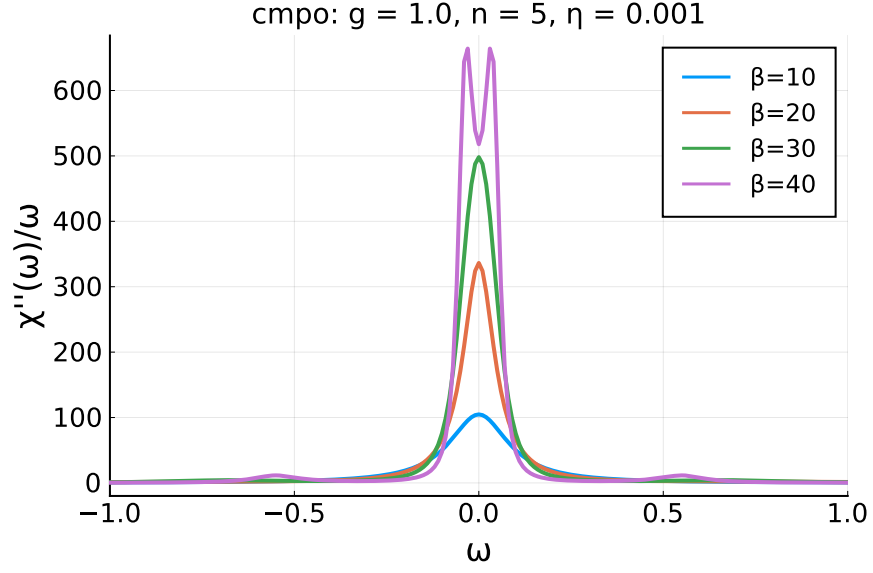


FIG. 3. $\chi''(\omega)/\omega$ at different temperatures. $\chi''(\omega)/\omega$ should diverge at $T = 0$.

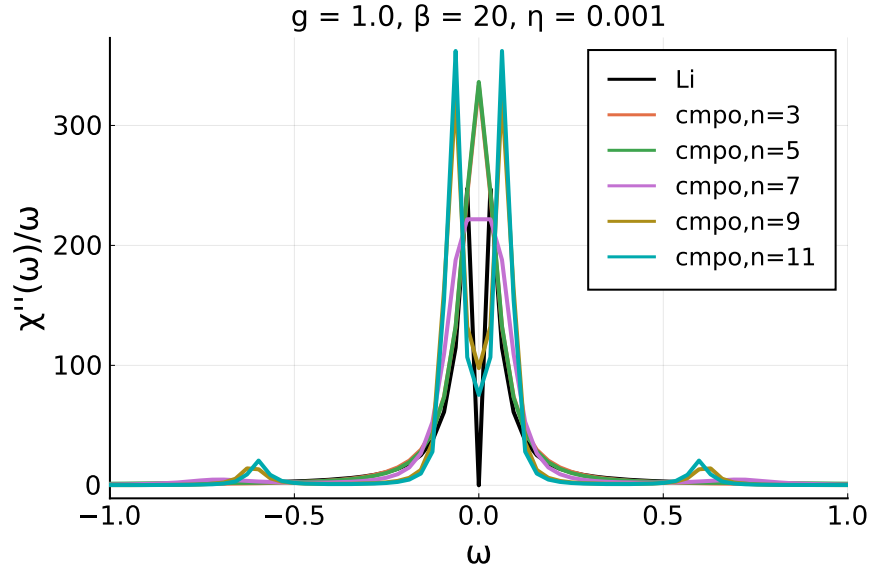


FIG. 4. $\chi''(\omega)/\omega$ obtained from fitting different number of data points.

III. PARAMAGNETIC PHASE

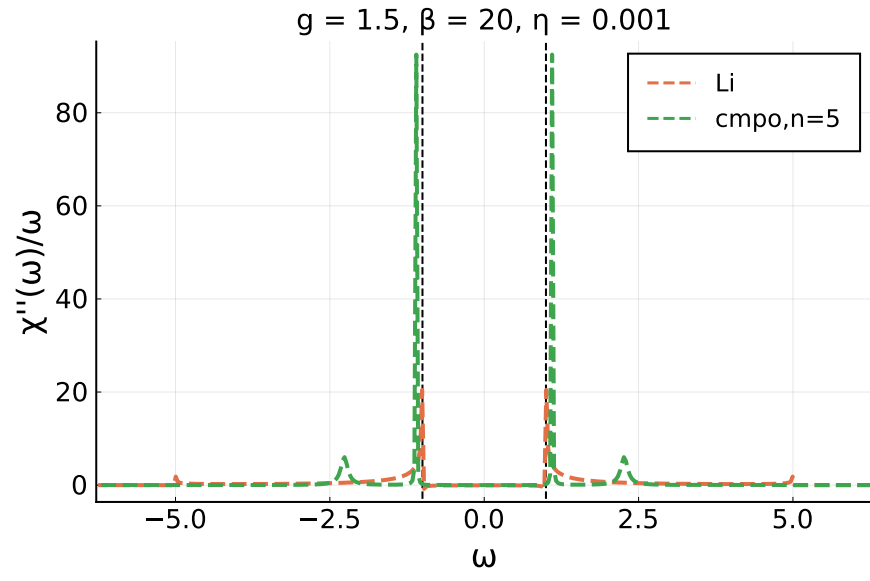


FIG. 5.

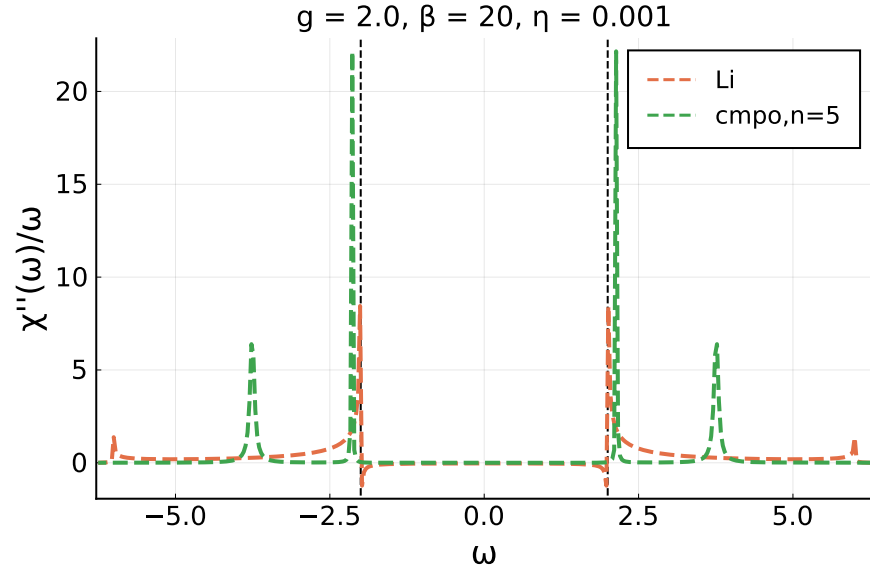


FIG. 6.