

CS101A (H) Week1

C++ Introduction

Contents

- Four Languages
- Overview
- Arithmetic types
- Pointers and Arrays
- References
- `std::vector`

Four languages

C, C++, Java, Python

C: The Foundation of Manual Control

As a foundational and relatively low-level language, C places the onus of initialization squarely on the programmer. Local variables must be manually initialized; otherwise, their values are unknown.

```
#include <stdio.h>
struct Point { int x; int y;};
int global_var; // Global variables, if not explicitly initialized, will be automatically
// initialized to 0
int main() {
    int local_var = 100; // Local variables must be explicitly initialized
    int uninitialized_local; // If not initialized, this variable will contain an
    // uncertain "junk value"
    // printf("Uninitialized local: %d\n", uninitialized_local); // warning, output a random value

    int numbers[] = {1, 2, 3, 4, 5};
    // Initialize the structure using the specified initializer of C99
    struct Point p1 = {.y = 20, .x = 10}; // It doesn't have to be in any order
    return 0;
}
```

C++: Building on C with Abstraction and Safety

C++ inherits C's initialization syntax but vastly expands upon it with features.

- A Multitude of Initialization Forms
 - **Aggregate initialization:** Similar to C for arrays and simple structs.
 - **Copy-initialization:** Using the `=` operator.
 - **Direct-initialization:** Using parentheses `()`.
 - **List-initialization (since C++11):** Using curly braces `{}`, which is often recommended for its ability to prevent certain types of narrowing conversions, making it a safer option.

C++: Building on C with Abstraction and Safety

- **Constructors:** A significant difference from C is the concept of a constructor. When an object of a class is created, a constructor is called to initialize its members. C++ supports multiple constructors (overloading), default constructors (called when no arguments are provided), copy constructors (for creating a new object from an existing one), and move constructors (for efficiently transferring resources).
- **Member Initializer Lists:** C++ constructors can use a member initializer list to initialize class members before the constructor's body is executed. This is the only way to initialize `const` and reference members.

```

#include <iostream>
#include <string>
class Rectangle {
private:
    int width;
    int height;
    std::string name;
public:
    // The constructor uses members to initialize the list, which is the recommended way
    Rectangle(int w, int h, std::string n) : width(w), height(h), name(n) {
        std::cout << "Rectangle '" << name << "' constructed." << std::endl; }
};

int main() {
    Rectangle r1 = Rectangle(10, 5, "R1"); // Copy-initialization
    Rectangle r2(12, 6, "R2"); // Direct-initialization
    Rectangle r3{14, 7, "R3"}; // List-initialization
    int a = 1; // copy-initialization
    int b(2); // direct-initialization
    int c{3}; // list-initialization
    return 0;
}

```

Java: Safety and Simplicity through the JVM

Java prioritizes safety and simplicity, and its initialization rules reflect this by eliminating some of the "dangers" present in C and C++.

- **Default Values:** In Java, all instance variables (class members) are automatically initialized to a default value if not explicitly initialized by the programmer (0 for numeric types, `false` for booleans, and `null` for object references). This prevents the use of uninitialized variables at the class level.
- **Mandatory Local Variable Initialization:** Conversely, Java's compiler enforces a strict rule that all local variables must be explicitly initialized before they are used. This compile-time check eliminates a common source of errors.

Java

- **Constructors and the `new` Keyword:** Similar to C++, objects in Java are initialized via constructors. The `new` keyword is used to allocate memory for a new object and invoke its constructor. Java also supports constructor overloading.
- **No Multiple Initialization Forms:** Unlike C++, Java does not have different syntactic forms of initialization for objects. The `new` keyword is the standard way.

```

public class Box {
    // Instance variables will be assigned default values if they are not initialized
    private int width;        // 0
    private String label;     // null
    // Constructor, used for initializing objects
    public Box(int width, String label) {
        this.width = width;
        this.label = label;
    }
    public Box() {}

    public static void main(String[] args) {
        Box box1 = new Box(10, "MyBox");
        Box defaultBox = new Box(); // Label: null, Height: 0
        // Local variables must be explicitly initialized before use
        // int localValue;
        // System.out.println(localValue); // This line will cause a compilation error!
        int localValue = 200; // A value must be assigned first
        System.out.println("Initialized local variable: " + localValue);
    }
}

```

Python: Dynamic and Flexible Initialization

Python's dynamic nature leads to a more flexible and conceptually simpler model of initialization.

- **Dynamic Typing:** In Python, variables are not declared with a type. A variable is created when a value is first assigned to it. The type of the variable is the type of the object it currently refers to.
- **The `__init__` Method:** In the context of classes, the `__init__` method serves as the constructor. It is automatically called when a new instance of a class is created. The first argument to `__init__` is conventionally named `self` and refers to the instance being created. Programmers use `__init__` to set the initial state (attributes) of an object.
- **No Formal "Declaration":** There is no separate declaration step for variables in Python. Initialization happens at the point of assignment.

```
# Variables are created and initialized when assigned values
# There is no need to declare types
message = "Hello, Python!"
count = 100

class Car:
    def __init__(self, make, model, year):
        self.make = make
        ...
# Create a Car object
# This will automatically call the __init__ method of the Car class
my_car = Car("Tesla", "Model S", 2023)
```

Overview

What do **embedded systems**, **game development**, **high frequency trading**, and **particle accelerators** have in common? - C++, of course!

Effective C++ Item 1 (by Scott Meyers): **View C++ as a federation of languages.**

The easiest way is to view C++ not as a single language but as a federation of related languages ... Fortunately, there are only four:

- C.
- Object-Oriented C++.
- Template C++.
- The STL.

Standardization of C and C++

Standardization: C++98, C++11, C++14, C++17, C++20, C++23, C++26, ...

- C++98: The first ISO standard in 1998.
- C++11: Marks the beginning of **modern C++**.
- C++14/17: Some slight fixes and improvements of C++11.
- C++20: The first standard that delivers on virtually all the features that Bjarne Stroustrup dreamed of in *The Design and Evolution of C++* in 1994.
 - "D&E Complete"

CS101A is based on C++17.

Arithmetic types

signed
char

unsigned
char

char

bool

(signed)
short (int)

unsigned
short (int)

char8_t

float

signed / int /
signed int

unsigned (int)

char16_t

double

(signed) long (int)

unsigned long (int)

char32_t

long double

(signed) long long (int)

unsigned long long (int)

wchar_t

Arithmetic types

- `1 == sizeof(char) <= sizeof(short) <= sizeof(int) <= sizeof(long) <= sizeof(long long)`
- `sizeof(signed T) == sizeof(unsigned T)` for every `T` $\in \{ \text{char}, \text{short}, \text{int}, \text{long}, \text{long long} \}$
- Range of signed types: $[-2^{N-1}, 2^{N-1} - 1]$. Range of unsigned types: $[0, 2^N - 1]$
- Whether `char` is signed or not is **implementation-defined**. (An implementation-defined behavior depends on the compiler and the standard library, and is often also related to the hosted environment (e.g. the operating system).)
- Signed integer overflow is **undefined behavior**.
- Unsigned arithmetic **never overflows**: It is performed modulo 2^N , where N is the number of bits of that type.

Arithmetic types

type	width (at least)	width (usually)
short	16 bits	16 bits
int	16 bits	32 bits
long	32 bits	32 or 64 bits
long long	64 bits	64 bits

Arithmetic types

type	min	max
short	min=-32768	max=32767
unsigned short	min=0	max=65535

```
// the largest unsigned int
unsigned int u = std::numeric_limits<unsigned int>::max();
unsigned int u2 = u + 1; // u2 = 0
```

Pointer types

PointeeType *

- For $T \neq U$, $T *$ and $U *$ are **different types**. (For example, `int *` and `double *` are different types.)
- **Null pointer**: The pointer holding the **null pointer value**, which is a special value indicating that the pointer is "pointing nowhere".
 - A null pointer can be obtained from `nullptr`.
 - Global or local static pointers will be zero-initialized to null.

```
int* p_null = nullptr;
```

Pointer types

- The value of a pointer of type `T *` is **the address of** an object of type `T`.
- `&var` returns the address of `var`. The return type is pointer to the type of `var`.
- Only when a pointer is actually pointing to an object is it **dereferenceable**, otherwise `*ptr` is **undefined behavior**.

```
int x = 42;
int* px = &x;
std::cout << "*px = " << *px << "\n"; // *px = 42
std::cout << "px = " << px << "\n"; // px = 0x6283bffb24
std::cout << "&x = " << &x << "\n"; // &x = 0x6283bffb24
// the return type of &x is int *
```

Pointer types

- `const T* p`
 - You cannot modify the object through p: `*p = value` is ill-formed.
 - The pointer value itself (where p points) can change: `p = other_ptr` is allowed.
- `T* const p`
 - The pointer itself is const: `p = other_ptr` is wrong.
 - The pointee is modifiable via p: `*p = value` is allowed.
- `const T* const p`
 - Neither can change: cannot reseat p, cannot modify the object through p.

Array types

`ElemType [N]`

- `T [N]`, `U [N]` and `T [M]` are **different types** for `T` \neq `U` and `N` \neq `M`. (For example, `int [5]` and `double [5]` are different types, `int [5]` and `int [10]` are different types.)
- Array sizes must be compile-time constants. Code like `int a[n]`, is ill-formed if `n` is not a constant expression. When the size is only known at run time, use dynamic containers such as `std::vector<Type>`, or other dynamic allocation mechanisms.
- In C (since C99), a VLA is an array whose size is determined at run time `int a[n]`.

Array types

- Valid index range: $[0, N)$. Subscript out of range is **undefined behavior**.

```
int a[5] = {10, 20, 30, 40, 50};
std::size_t N = sizeof(a) / sizeof(a[0]);
// valid subscript [0, N)
std::cout << "a[0] = " << a[0] << ", a[N-1] = " << a[N-1] << "\n";
// a[N] or a[-1] are undefined behavior
```

- Decay: `a` \rightarrow `&a[0]`, `T [N]` \rightarrow `T *`.

```
// The array name decays into a pointer to the first element
int* p = a;           // equal to &a[0], sizeof(p) = 8 bytes (pointer size)
std::cout << "*p = " << *p ;// *p = 10
// However, what is obtained by using the address symbol &a is a "pointer to
//the entire array", which is of a different type
int (*pa)[5] = &a;    // T (*)[N], sizeof(*pa) = 20 bytes (array of 5 ints)
std::cout << "(*pa)[2] = " << (*pa)[2] << "\n"; //(*pa)[2] = 30
```

Array types

- Decay: `a` \rightarrow `&a[0]` , `T [N]` \rightarrow `T *` .

```
void takes_pointer(int* p, std::size_t n) {  
    // 'p' points to the first element of the array argument (after decay)  
    std::cout << "sizeof(p) = " << sizeof(p) << "\n";  
}  
int main() {  
    int a[5] = {10, 20, 30, 40, 50};  
    takes_pointer(a, 5); // T[N] decays when passing to a function, T[N] to T*  
}
```

the output is: sizeof(p) = 8 bytes. (bytes of a pointer)

struct types

A special data type consisting of a sequence of **members**.

- The type name is `struct StructName` .
- $\text{sizeof}(\text{struct } X) \geq \sum_{\text{member} \in X} \text{sizeof}(\text{member})$

Alignment and padding make `sizeof(Mixed)` typically bigger than or equal to the sum of the members' `sizeof` values; the exact size depends on member order and alignment rules.

```
struct Mixed {  
    char c;    // 1 byte  
    int i;     // 4 bytes  
    short s;   // 2 bytes  
}; // There may be padding bytes to satisfy the maximum alignment requirement  
std::cout << sizeof(Mixed) << "\n"; // sizeof(Mixed) = 12 (c=1, i=4, s=2)  
std::cout << alignof(Mixed) << "\n"; // alignof(Mixed) = 4
```

Variables

Declare a variable: `Type varName`

- `ElemType varName[N]` for array type `ElemType[N]` .
- `T (*varName)[N]` for pointer to array type `T (*)[N]` .

```
int a[2][4];           // 2 rows, each row is int[4]
// Pointer to "array of 4 int"
int (*row)[4] = &a[0]; // row points to the first row (type: int (*)[4])
(*row)[1] = 42;        // assign a[0][1] = 42
row = row + 1;         // advance by one whole row (skips 4 ints)
(*row)[3] = 7;         // assign a[1][3] = 7
```

Variables

Initialize a variable: `= initializer`

- Designators for arrays: `= {[3] = 5, [7] = 4}`
- Designators for `struct s`: `= {.mem1 = x, .mem2 = y} .`
- Brace-enclosed list initializer for arrays and `struct s`: `= { ... } .`

```
int a[5] = {1, 2, 3};           // remaining elements zero-initialized: {1,2,3,0,0}
int b[10]{ [3] = 5, [7] = 4 }; // C++20

struct Point { int mem1, mem2; };
Point p = {10, 20};             // aggregate initialization
Point s{ .mem1 = 7, .mem2 = 9 }; // C++20
```

Initialization

If a variable is declared without explicit initializer:

- For global or local `static` variables, they are **empty-initialized**:
 - `0` for integer types,
 - `+0.0` for floating-point types,
 - null pointer value for pointer types.
- For local non-`static` variables, they are **uninitialized**, holding indeterminate values.

These rules apply recursively to the elements of arrays and the members of `struct` s. Any use of the value of an uninitialized variable is **undefined behavior**.

Initialization

```
int g_int;           // zero-initialized -> 0
double g_dbl;        // +0.0
int* g_ptr;          // null pointer
int g_arr[3];        // {0,0,0}
struct S { int x; double y; };
S g_s;               // {0, +0.0}

void func() {
    static int s_int;      // 0
    static double s_dbl;   // +0.0
    static int* s_ptr;     // nullptr
    static int s_arr[2];   // {0,0}
    static S s;            // {0, +0.0}

    int l_int;            // uninitialized
    double l_dbl;         // uninitialized
    int* l_ptr;           // uninitialized
    int l_arr[2];         // elements uninitialized
    S ls;                 // members uninitialized
}
```

Expressions

Expressions = operators + operands.

- Operator precedence, associativity, and evaluation order of operands
 - `f() + g() * h()` , `f() - g() + h()`
- The only four operators whose operands have deterministic evaluation order:
 - `&&` and `||` : short-circuit evaluation
 - `?:`
 - `,` (not in a function call or in an initializer list)

Expressions

- If the evaluation order of **A** and **B** is unspecified, and if
 - both **A** and **B** contain a write to an object, or
 - one of them contains a write to an object, and the other one contains a read to that object

then the behavior is undefined.

Arithmetic operators

`+`, `-`, `*`, `/`, `%`

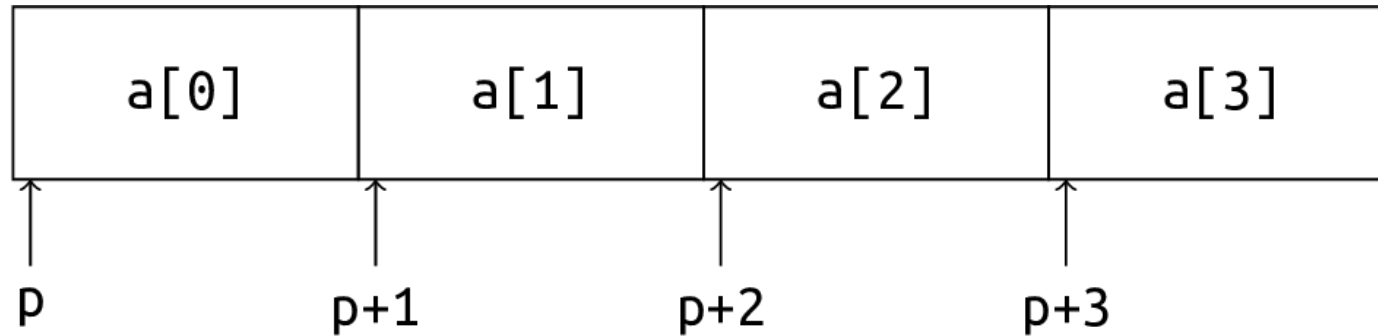
- Division: truncated towards zero.
- Remainder: `(a / b) * b + (a % b) == a` always holds.
- For `+`, `-`, `*` and `/`, the operands undergo a series of type conversions to a common type.

Bitwise operators: `~`, `&`, `|`, `^`, `<<`, `>>`

Compound assignment operators: `a op= b` is equivalent to `a = a op b`.

Be careful with signed overflows.

Pointer arithmetic



- Pointer arithmetic: `p++`, `++p`, `p--`, `--p`, `p + i`, `i + p`, `p - i`, `p += i`, `p -= i`, `p1 - p2`.
- Pointer arithmetic uses the units of the pointed-to type.
 - `p + i == (char *)p + i * sizeof(*p)`
- Pointer arithmetic must be performed within an array (including its past-the-end position), otherwise **the behavior is undefined**.

Operators

`++` , `--`

- `++a` and `--a` returns the value of `a` after incrementation/decrementation.
- `a++` and `a--` returns the original value of `a`.

`<` , `<=` , `>` , `>=` , `==` , `!=`

- The operands undergo a series of type conversions to a common type before comparison.

Operators

Member access: `obj.member` .

Member access through pointer: `ptr->member` , which is equivalent to `(*ptr).member` .

- `.` has higher precedence than `*` , so the parentheses around `*ptr` are necessary.

Control flow

- `if (cond) stmt`
- `if (cond) stmt1 else stmt2`
- `for (init_expr; cond; inc_expr) stmt`
- `while (cond) stmt`
- `do stmt while (cond);`
- `switch (integral_expr) { ... }`
- `break` and `continue`

Functions

Function declaration: `RetType funcName(Parameters);`

- Parameter names are not necessary, but types are required.
- A function can be declared multiple times.

Function definition: `RetType funcName(Parameters) { functionBody }`

- A function can be defined only once.

Functions

- Argument passing:
 - Use the argument to initialize the parameter.
 - The semantic is **copy**.
 - **Decay** always happens: One can never declare an array parameter.

Namespace `std`

`std::cin` and `std::cout` : names from the standard library.

C++ has a large standard library with a lot of names declared.

To avoid **name collisions**, all the names from the standard library are placed in a **namespace** named `std`.

- Example of name collisions in C: Suppose we want to write our own quick-sort:

```
#include <stdlib.h>
void qsort(int *a, int n) { // Oops! stdlib already has one named `qsort`.
    // ...
}
```

Namespace `std`

`std::cin` and `std::cout` : names from the standard library.

C++ has a large standard library with a lot of names declared.

To avoid **name collisions**, all the names from the standard library are placed in a namespace named `std`.

- You can write `using std::cin;` to introduce `std::cin` into **the current scope**, so that `cin` can be used without `std::`.
- You may write `using namespace std;` to introduce **all the names in** `std` into the current scope, but **you will be at the risk of name collisions again**.

`std::string`

- Automatic memory management.
- `s.size()` returns the length. `s.empty()` returns whether `s` is empty.
- Use `+` and `+=` for concatenation. Use `<`, `<=`, `>`, `>=`, `==`, `!=` for comparison. Use `=` for copying.
- Use `>>` and `<<` for IO, as well as `std::getline`.
- Use `s[i]` to access the elements.
- Use range-based `for` loops to traverse a string.
- Use `std::to_string` and `std::stoi`, `std::stol`, ... for numeric conversions.
- Full list of functions related to `std::string`:

Pointers and Arrays

Pointers

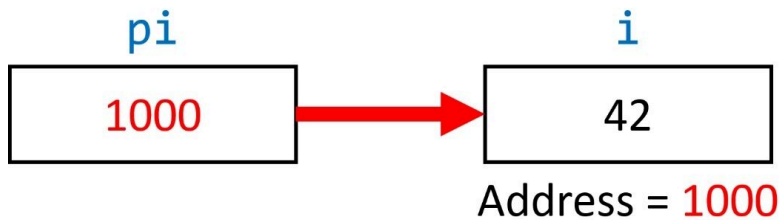
A pointer *points to* a variable. The **value** of a pointer is the address of the variable that it points to.

```
int i = 42;  
int* pi = &i;  
printf("%d\n", *pi);
```

- `int* pi;` declares a pointer named `pi`.
 - The type of `pi` is `int*`.
 - The type of the variable that `pi` points to ("pointee") is `int`.
- `&` is the **address-of operator**, used for taking the address of a variable.
- `*` in the expression `*pi` is the **indirection (dereference) operator**, used for obtaining the variable that a pointer points to.

Pointers

A pointer *points to* a variable.



We can access and modify a variable through its address (or a pointer pointing to it).

```
int num = 3;
int* ptr = &num;
printf("%d\n", *ptr); // 3
*ptr = 10;
printf("%d\n", num);  // 10
++num;
printf("%d\n", *ptr); // 11
```

Declare a pointer

To declare a pointer: `PointeeType* ptr;`

- The type of `ptr` is `PointeeType*`.
 - Pointer types with different pointee types are **different types**: `int*` and `double*` are different.
- The asterisk `*` can be placed near either `PointeeType` or `ptr`:
 - `PointeeType* ptr;` and `PointeeType *ptr;` are the same declaration.
 - `PointeeType * ptr;`, `PointeeType * ptr;` and `PointeeType*ptr;` are also correct.

Declare a pointer

The asterisk `*` can be placed near either `PointeeType` or `ptr`:

- `PointeeType* ptr;` may be more intuitive?

However, when declaring more than one pointers in one declaration statement, an asterisk is needed **for every identifier**:

```
int* p1, p2, p3;    // `p1` is of type `int*`, but `p2` and `p3` are ints.
int *q1, *q2, *q3;  // `q1`, `q2` and `q3` all have the type `int*`.
int* r1, r2, *r3;   // `r1` and `r3` are of the type `int*`,
                   // while `r2` is an int.
```

[Best practice] Either `PointeeType *ptr` or `PointeeType* ptr` is ok. Choose one style and stick to it. But if you choose the second one, never declare more than one pointers in one declaration statement.

& and *

`&var` returns the address of the variable `var`.

- The result type is `Type *`, where `Type` is the type of `var`.
- `var` must be an object that has an identity (an *lvalue*): `&42` or `&(a + b)` are not allowed.

`*expr` returns **the variable** whose address is the value of `expr`.

- `expr` must have a pointer type `PointeeType *`. The result type is `PointeeType`.
- **The variable** is returned, not only its value. This means that we can modify the returned variable: `++*ptr` is allowed.

*

In a **declaration** `PointeeType *ptr`, `*` is a part of the pointer type `PointeeType *`.

In an **expression** like `*ptr`, `*` is the **indirection (dereference) operator** used to obtain the variable whose address is the value of `ptr`.

Do not mix them up!

The null pointer

The **null pointer value** is the "zero" value for pointer types.

A null pointer compares unequal to any pointer pointing to an object.

It is used for representing a pointer that "points nowhere".

Dereferencing a null pointer is undefined behavior, and often causes severe runtime errors!

- Because it is not pointing to an object.

```
int *ptr = nullptr; // `ptr` is a null pointer.  
printf("%d\n", *ptr); // undefined behavior  
*ptr = 42; // undefined behavior
```

Implicit initialization of pointers

If a pointer is not explicitly initialized:

- Global or local `static` : Initialized to the null pointer value.
- Local non-`static` : Initialized to indeterminate values, or in other words, **uninitialized**.
 - Uninitialized pointers are often called **wild pointers**.

A wild pointer do not point to a specific object, and is not a null pointer either.

Dereferencing a wild pointer is undefined behavior, and often causes severe runtime errors.

[Best practice] Avoid wild pointers.

Pointers that are not dereferenceable

Dereferencing such a pointer is undefined behavior, and usually causes severe runtime errors.

```
if (ptr != nullptr && *ptr == 42) { /* ... */ }
```

When `ptr` is a null pointer, the right-hand side operand `*ptr == 42` won't be evaluated, so `ptr` is not dereferenced.

Arrays

An array is a sequence of `N` objects of an *element type* `ElemType` stored **contiguously** in memory, where `N` $\in \mathbb{Z}_+$ is the *length* of it.

```
ElemType arr[N];
```

`N` must be a **constant expression** whose value is known at compile-time.

```
int a1[10];           // OK. A literal is a constant expression.
#define MAXN 10
int a2[MAXN];         // OK. `MAXN` is replaced with `10` by the preprocessor.
int n; scanf("%d", &n);
int a[n];              // A C99 VLA (Variable-Length Array), whose length is
                      // determined at runtime.
```

Array type

An array is a sequence of `N` objects of an *element type* `ElemType` stored **contiguously** in memory, where `N` $\in \mathbb{Z}_+$ is the *length* of it.

```
ElemType arr[N]; // The type of `arr` is `ElemType [N]`.
```

The type of an array consists of two parts:

1. the element type `ElemType` , and
2. the length of the array `[N]` .

Array initialization

If an array is declared without explicit initialization:

- Global or local `static`: Empty-initialization \Rightarrow Every element is empty-initialized.
- Local non-`static`: Every element is initialized to indeterminate values (uninitialized).

Arrays can be initialized from [brace-enclosed lists](#):

- Initialize the beginning few elements:

```
int a[10] = {2, 3, 5, 7}; // Correct: Initializes a[0], a[1], a[2], a[3]
int b[2] = {2, 3, 5};    // Error: Too many initializers
int c[] = {2, 3, 5};     // Correct: 'c' has type int[3].
int d[100] = {};         // Correct.
```

Array initialization

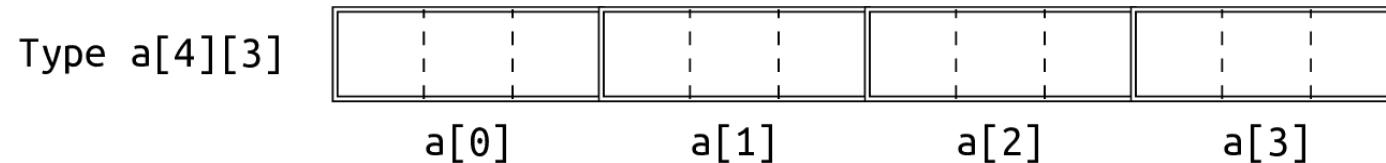
If an array is explicitly initialized, all the elements that are not explicitly initialized are empty-initialized.

```
int main(void) {  
    int a[10] = {1, 2, 3}; // a[3], a[4], ... are all initialized to zero.  
    int b[100] = {0};      // All elements of b are initialized to zero.  
    int c[100] = {1};      // c[0] is initialized to 1,  
                           // and the rest are initialized to zero.  
}
```

`= {x}` is not initializing all elements to `x` !

Nested arrays

Nested arrays can be achieved as **arrays of arrays**:



```
int a[4][3] = { // array of 4 arrays of 3 ints each (4x3 matrix)
    { 1 },      // row 0 initialized to {1, 0, 0}
    { 0, 1 },   // row 1 initialized to {0, 1, 0}
    { [2]=1 },  // row 2 initialized to {0, 0, 1}
    // row 3 initialized to {0, 0, 0}
};

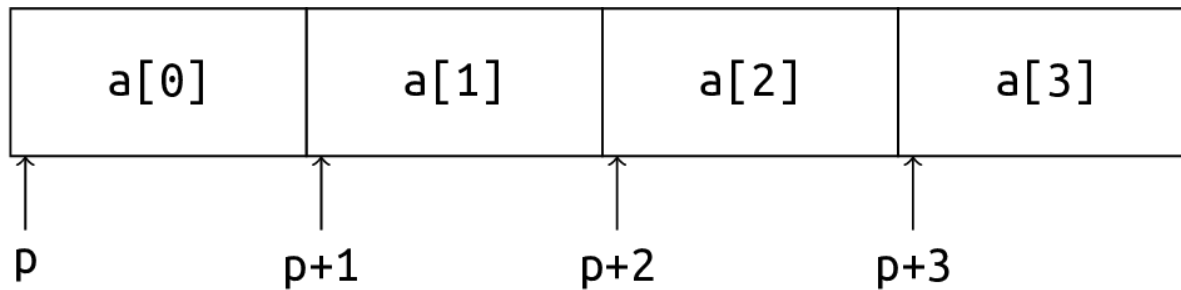
int b[4][3] = { // row 0 initialized to {1, 3, 5}
    1, 3, 5, 2, 4, 6, 3, 5, 7 // row 1 initialized to {2, 4, 6}
    // row 2 initialized to {3, 5, 7}
    // row 3 initialized to {0, 0, 0}
};

int y[4][3] = {[0][0]=1, [1][1]=1, [2][0]=1}; // row 0 initialized to {1, 0, 0}
                                                // row 1 initialized to {0, 1, 0}
                                                // row 2 initialized to {1, 0, 0}
                                                // row 3 initialized to {0, 0, 0}
```


Pointer arithmetic

Let `p` be a pointer of type `T *` and let `i` be an integer.

- `p + i` returns the address equal to the value of `(char *)p + i * sizeof(T)`. In other words, pointer arithmetic uses the unit of the pointed-to type.
- If we let `p = &a[0]` (where `a` is an array of type `T [N]`), then
 - `p + i` is equivalent to `&a[i]`, and
 - `*(p + i)` is equivalent to `a[i]`.

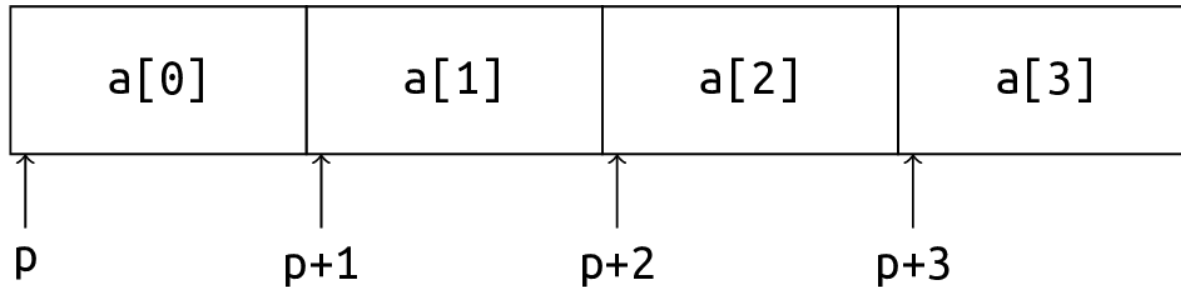


- Arithmetic operations `i + p`, `p += i`, `p - i`, `p -= i`, `++p`, `p++`, `--p`, `p--` are defined in the same way.

Array-to-pointer conversion

If we let $p = \&a[0]$ (where a is an array of type $T[N]$), then

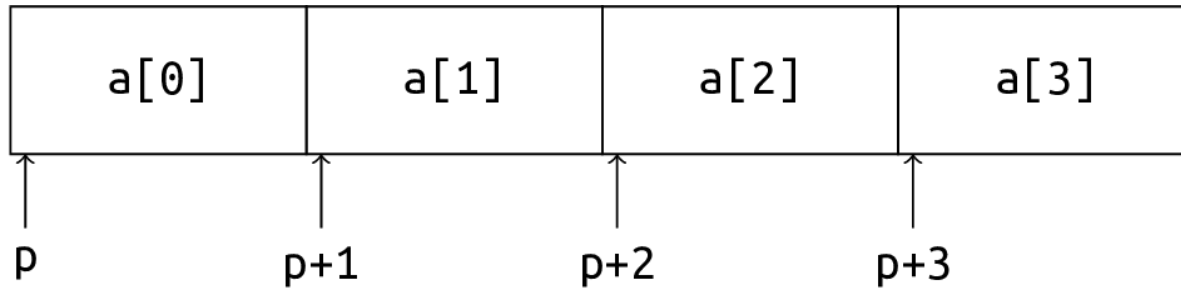
- $p + i$ is equivalent to $\&a[i]$, and
- $*(p + i)$ is equivalent to $a[i]$.



Considering the close relationship between arrays and pointers, an array can be **implicitly converted** to a pointer to the first element: $a \rightarrow \&a[0]$, $T[N] \rightarrow T^*$.

- $p = \&a[0]$ can be written as $p = a$ directly.
- $*a$ is equivalent to $a[0]$.

Subtraction of pointers



Let `a` be an array of length `N`. If `p1 == a + i` and `p2 == a + j` (where `i` and `j` are nonnegative integers), the expression `p1 - p2`

- has the value equal to `i - j`, and
- has the type `ptrdiff_t`, which is a **signed** integer type declared in `<stddef.h>`.
 - The size of `ptrdiff_t` is implementation-defined. For example, it might be 64-bit on a 64-bit machine, and 32-bit on a 32-bit machine.
- Here `i, j ∈ [0, N]` (closed interval), i.e. `p1` or `p2` may point to the "*past-the-end*" position of `a`.

Pointer arithmetic

Pointer arithmetic can only happen within the range of an array and its "past-the-end" position (indexed $[0, N]$). For other cases, **the behavior is undefined**.

Examples of undefined behaviors:

- $p1 - p2$, where $p1$ and $p2$ point to the positions of two different arrays.
- $p + 2 * N$, where p points to some element in an array of length N .
- $p - 1$, where p points to the first element $a[0]$ of some array a .

Note that the evaluation of the innocent-looking expression $p - 1$, without dereferencing it, is still undefined behavior and may fail on some platforms.

Pass an array to a function

The only way of passing an array to a function is to **pass the address of its first element**.

The following declarations are equivalent:

```
void fun(int *a);  
void fun(int a[]);  
void fun(int a[10]);  
void fun(int a[2]);
```

In all these declarations, the type of the parameter `a` is `int *`.

- How do you verify that?

Pass an array to a function

```
void fun(int a[100]);
```

The type of the parameter `a` is `int *`. How do you verify that?

```
void fun(int a[100]) {  
    printf("%d\n", (int)sizeof(a));  
}
```

Output: (On 64-bit Ubuntu 22.04, GCC 13)

```
8
```

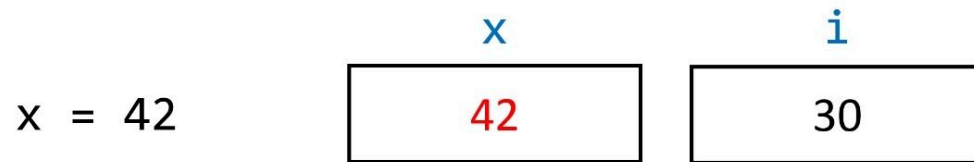
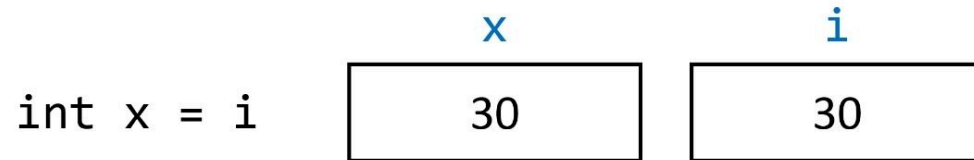
- If the type of `a` is `int[100]` as declared, the output should be `400` (assuming `int` is 32-bit).

Argument passing

What is the output? Is the value of `i` changed to `42` ?

```
void fun(int x) {  
    x = 42;  
}  
int main(void) {  
    int i = 30;  
    fun(i);  
    printf("%d\n", i);  
}
```

Argument passing

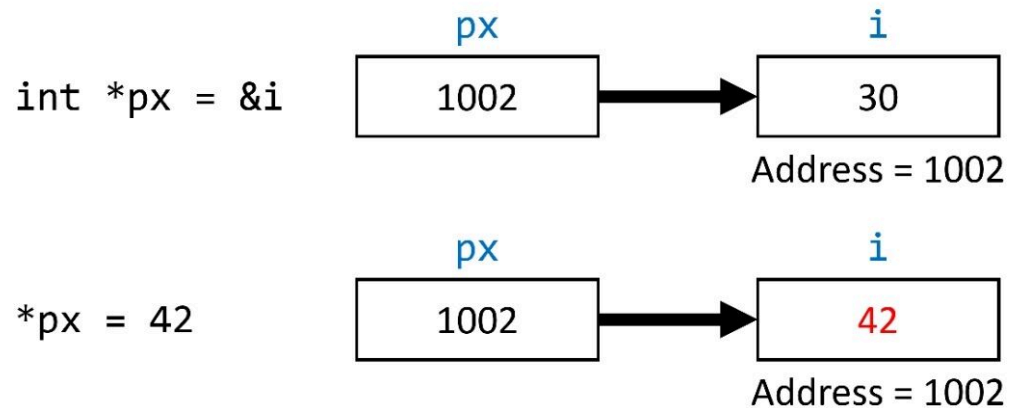


The output is still 30. `i` is not changed.

- The parameter `x` is initialized as if `int x = i;`, thus obtaining the **value** of `i`.
 - `x` and `i` are two independent variables.
- Modification on `x` does not influence `i`.

Argument passing

To make the modification happen on a variable outside, pass its address into the function.



```
void fun(int *px) {*px = 42;}
int main(void) {
    int i = 30;
    fun(&i); // int *px = &i
    printf("%d\n", i); // 42
}
```

Pass an array to a function

Even if you declare the parameter as an array (either `T a[N]` or `T a[]`), its type is still a pointer `T*`: **You are allowed to pass anything of type `T*` to it.**

- Array of element type `T` with any length is allowed to be passed to it.

```
void print(int a[10]) {
    for (int i = 0; i < 10; ++i)
        printf("%d\n", *(a + i));
}

int main(void) {
    int x[20] = {0}, y[10] = {0}, z[5] = {0}, w = 42;
    print(x);    // OK
    print(y);    // OK
    print(z);    // Allowed by the compiler, but undefined behavior!
    print(&w);   // Still allowed by the compiler, also undefined behavior!
}
```

Pass an array to a function

Even if you declare the parameter as an array (either `T a[N]` or `T a[]`), its type is still a pointer `T*`: **You are allowed to pass anything of type `T*` to it.**

- Array of element type `T` with any length is allowed to be passed to it.

The length `n` of the array is often passed explicitly as another argument, so that the function can know how long the array is.

```
void print(int *a, int n) {  
    for (int i = 0; i < n; ++i)  
        printf("%d\n", *(a + i));  
}
```

Subscript on pointers

```
void print(int *a, int n) {  
    for (int i = 0; i < n; ++i)  
        printf("%d\n", a[i]); // Look at this!  
}
```

Subscript on pointers is also allowed! `a[i]` is equivalent to `*(a + i)`.

Return an array?

There is no way of returning an array from the function.

Returning the address of its first element is ok, **but be careful**:

This is OK:

```
int a[10];  
int *foo(void) { return a;}
```

This returns an **invalid address** — it returns the address of a local variable.

```
int *foo(void) {  
    int a[10] = {0};  
    return a;  
}
```

Pass a nested array to a function

When passing an array to a function, we make use of the **array-to-pointer conversion**:

- `Type [N]` will be implicitly converted to `Type *`.

A "2d-array" is an "array of array":

- `Type [N][M]` is an array of `N` elements, where each element is of type `Type [M]`.
- `Type [N][M]` should be implicitly converted to a "pointer to `Type[M]`".

What is a "pointer to `Type[M]`"?

Pointer to array

A pointer to an array of `N` `int`s:

```
int (*parr)[N];
```

An array of `N` pointers (pointing to `int`):

```
int *arrp[N];
```

Too confusing! How can I remember them?

Pointer to array

Too confusing! How can I remember them?

- `int (*parr)[N]` has a pair of parentheses around `*` and `parr`, so
 - `parr` is a pointer (`*`), and
 - points to something of type `int[N]`.
- Then the other one is different:
 - `arrp` is an array, and
 - stores `N` pointers, with pointee type `int`.

Pass a nested array to a function

The following declarations are equivalent: The parameter is of type `int (*)[N]`, which is a pointer to `int[N]`.

```
void fun(int (*a)[N]);  
void fun(int a[][N]);  
void fun(int a[2][N]);  
void fun(int a[10][N]);
```

We can pass an array of type `int[K][N]` to `fun`, where `K` is arbitrary.

- The size for the second dimension must be `N`.
 - `T[10]` and `T[20]` are different types, so the pointer types `T(*)[10]` and `T(*)[20]` are not compatible.

Pass a nested array to a function

```
void print(int (*a)[5], int n) {
    for (int i = 0; i < n; ++i) {
        for (int j = 0; j < 5; ++j)
            printf("%d ", a[i][j]);
        printf("\n");
    }
}

int main(void) {
    int a[2][5] = {{1, 2, 3, 4, 5}, {6, 7, 8, 9, 10}};
    int b[3][5] = {0};
    print(a, 2); // OK
    print(b, 3); // OK
}
```

Pass a nested array to a function

In each of the following declarations, what is the type of `a`? Does it accept an argument of type `int[N][M]`?

1. `void fun(int a[N][M])`

2. `void fun(int (*a)[M])`

3. `void fun(int (*a)[N])`

4. `void fun(int **a)`

5. `void fun(int *a[])`

6. `void fun(int *a[N])`

7. `void fun(int a[100][M])`

8. `void fun(int a[N][100])`

Pass a nested array to a function

In each of the following declarations, what is the type of `a`? Does it accept an argument of type `int[N][M]`?

1. `void fun(int a[N][M])` : A pointer to `int[M]` . Yes.
2. `void fun(int (*a)[M])` : Same as 1.
3. `void fun(int (*a)[N])` : A pointer to `int[N]` . Yes iff `N == M` .
4. `void fun(int **a)` : A pointer to `int *` . **No**.
5. `void fun(int *a[])` : Same as 4.
6. `void fun(int *a[N])` : Same as 4.
7. `void fun(int a[100][M])` : Same as 1.
8. `void fun(int a[N][100])` : A pointer to `int[100]` . Yes iff `M == 100` .

Notes

In fact, you can pass the address of an array:

```
void print_array_10(int (*pa)[10]) {  
    for (int i = 0; i < 10; ++i)  
        printf("%d\n", (*pa)[i]);  
}  
int main(void) {  
    int a[10], b[100], c = 42;  
    print_array_10(&a); // OK  
    print_array_10(&b); // Error  
    print_array_10(&c); // Error  
}
```

In the function `print_array_10` above, the parameter type is `int (*)[10]`, a pointer to an array of 10 `int` s. The pointee type must be `int[10]`. Passing the address of anything else to it would not work.

References

Declare a reference

A **reference** defines an **alternative name** for an object ("refers to" that object).

Similar to pointers, the type of a reference is `ReferredType &`, which consists of two things:

- `ReferredType` is the type of the object that it refers to, and
- `&` is the symbol indicating that it is a reference.

Example:

```
int ival = 42;
int &ri = ival; // `ri` refers to `ival`.
                // In other words, `ri` is an alternative name for `ival`.
std::cout << ri << '\n'; // prints the value of `ival`, which is `42`.
++ri;                  // Same effect as `++ival`.
```

Declare a reference

```
int ival = 42;
int x = ival;           // `x` is another variable.
++x;                   // This has nothing to do with `ival`.
std::cout << ival << '\n'; // 42
int &ri = ival;         // `ri` is a reference that refers to `ival`.
++ri;                  // This modification is performed on `ival`.
std::cout << ival << '\n'; // 43
```

Ordinarily, when we initialize a variable, the value of the initializer is **copied** into the object we are creating.

When we define a reference, instead of copying the initializer's value, we **bind** the reference to its initializer.

A reference is an alias

When we define a reference, instead of copying the initializer's value, we **bind** the reference to its initializer.

```
int ival = 42;  
int &ri = ival;  
++ri;           // Same as `++ival;`.  
ri = 50;        // Same as `ival = 50;`.  
int a = ri + 1; // Same as `int a = ival + 1;`.
```

After a reference has been defined, **all** operations on that reference are actually operations on the object to which the reference is bound.

```
ri = a;
```

What is the meaning of this?

A reference is an alias

```
int ival = 42;  
int &ri = ival;  
++ri;           // Same as `++ival;`.  
ri = 50;        // Same as `ival = 50;`.  
int a = ri + 1; // Same as `int a = ival + 1;`.
```

When we define a reference, instead of copying the initializer's value, we **bind** the reference to its initializer.

After a reference has been defined, **all** operations on that reference are actually operations on the object to which the reference is bound.

```
ri = a;
```

- This is the same as `ival = a;`. It is not rebinding `ri` to refer to `a`.

A reference must be initialized

```
ri = a;
```

- This is the same as `ival = a;`. It is not rebinding `ri` to refer to `a`.

Once initialized, a reference remains bound to its initial object. **There is no way to rebind a reference to refer to a different object.**

Therefore, references must be initialized.

References must be bound to *existing objects* ("lvalues")

It is not allowed to bind a reference to temporary objects or literals:

```
int &r1 = 42;    // Error: binding a reference to a literal
int &r2 = 2 + 3; // Error: binding a reference to a temporary object
int a = 10, b = 15;
int &r3 = a + b; // Error: binding a reference to a temporary object
```

In fact, the references we learn today are "lvalue references", which must be bound to *lvalues*. We will talk about *value categories* in later lectures.

References are not objects

A reference is an alias. It is only an alternative name of another object, but the reference itself is **not an object**.

Therefore, there are no "references to references".

```
int ival = 42;  
int &ri = ival; // binding `ri` to `ival`.  
int & &rr = ri; // Error! No such thing!
```

What is the meaning of this code? Does it compile?

```
int &ri2 = ri; // Same as `int &ri2 = ival;`.
```

- `ri2` is a reference that is bound to `ival`.
- Any use of a reference is actually using the object that it is bound to!

References are not objects

A reference is an alias. It is only an alternative name of another object, but the reference itself is **not an object**.

Pointers must also point to objects. Therefore, there are no "pointers to references".

```
int ival = 42;  
int &ri = ival; // binding `ri` to `ival`.  
int &*pr = ri; // Error! No such thing!
```

What is the meaning of this code? Does it compile?

```
int *pi = &ri; // Same as `int *pi = &ival;`.
```

Reference declaration

Similar to pointers, the ampersand `&` only applies to one identifier.

```
int ival = 42, &ri = ival, *pi = &ival;  
// `ri` is a reference of type `int &`, which is bound to `ival`.  
// `pi` is a pointer of type `int *`, which points to `ival`.
```

Placing the ampersand near the referred type does not make a difference:

```
int& x = ival, y = ival, z = ival;  
// Only `x` is a reference. `y` and `z` are of type `int`.
```

* and &

Both symbols have many identities!

- In a **declaration** like `Type *x = expr`, `*` is a part of the pointer type `Type *`.
- In a **declaration** like `Type &r = expr`, `&` is a part of the reference type `Type &`.
- In an **expression** like `*opnd` where there is only one operand, `*` is the **dereference operator**.
- In an **expression** like `&opnd` where there is only one operand, `&` is the **address-of operator**.
- In an **expression** like `a * b` where there are two operands, `*` is the **multiplication operator**.
- In an **expression** like `a & b` where there are two operands, `&` is the **bitwise-and operator**.

Example: Use references in range-**for**

```
std::string str;
std::cin >> str;
int lower_cnt = 0;
for (char c : str)
    if (std::islower(c))
        ++lower_cnt;
std::cout << "There are " << lower_cnt << " lowercase letters in total.\n";
```

The range-**for** loop in the code above traverses the string, and declares and initializes the variable **c** in each iteration as if

```
for (std::size_t i = 0; i != str.size(); ++i) {
    char c = str[i]; // Look at this!
    if (std::islower(c))
        ++lower_cnt;}
```

Example: Use references in range-`for`

```
for (char c : str)
    // ...
```

The range-`for` loop in the code above traverses the string, and declares and initializes the variable `c` in each iteration as if

```
for (std::size_t i = 0; i != str.size(); ++i) {
    char c = str[i];
    // ...
}
```

Here `c` is a copy of `str[i]`. Therefore, modification on `c` does not affect the contents in `str`.

Example: Use references in range-**for**

What if we want to change all lowercase letters to their uppercase forms?

```
for (char c : str)
    c = std::toupper(c); // This has no effect.
```

We need to declare **c** as a reference.

```
for (char &c : str)
    c = std::toupper(c);
```

This is the same as

```
for (std::size_t i = 0; i != str.size(); ++i) {
    char &c = str[i];
    c = std::toupper(c); // Same as `str[i] = std::toupper(str[i]);`.
}
```

Example: Pass by reference-to-const

Write a function that accepts a string and returns the number of lowercase letters in it:

```
int count_lowercase(std::string str) {  
    int cnt = 0;  
    for (char c : str)  
        if (std::islower(c))  
            ++cnt;  
    return cnt;  
}
```

To call this function:

```
int result = count_lowercase(my_string);
```

Example: Pass by reference-to-const

```
int count_lowercase(std::string str) {  
    int cnt = 0;  
    for (char c : str)  
        if (std::islower(c))  
            ++cnt;  
    return cnt;  
}
```

```
int result = count_lowercase(my_string);
```

When passing `my_string` to `count_lowercase`, the parameter `str` is initialized as if

```
std::string str = my_string;
```

The contents of the entire string `my_string` are copied!

Example: Pass by reference-to-`const`

```
int result = count_lowercase(my_string);
```

When passing `my_string` to `count_lowercase`, the parameter `str` is initialized as if

```
std::string str = my_string;
```

The contents of the entire string `my_string` are copied! This copy is unnecessary, because `count_lowercase` is a read-only operation on `str`.

How can we avoid this copy?

Example: Pass by reference-to-`const`

```
int count_lowercase(std::string &str) { // `str` is a reference.  
    int cnt = 0;  
    for (char c : str)  
        if (std::islower(c))  
            ++cnt;  
    return cnt;  
}
```

```
int result = count_lowercase(my_string);
```

When passing `my_string` to `count_lowercase`, the parameter `str` is initialized as if

```
std::string &str = my_string;
```

Which is just a reference initialization. No copy is performed.

Example: Pass by reference-to-`const`

```
int count_lowercase(std::string &str) { // `str` is a reference.  
    int cnt = 0;  
    for (char c : str)  
        if (std::islower(c))  
            ++cnt;  
    return cnt;  
}
```

However, this has a problem:

```
std::string s1 = something(), s2 = some_other_thing();  
int result = count_lowercase(s1 + s2); // Error: binding reference to  
                                     // a temporary object.
```

`a + b` is a temporary object, which `str` cannot be bound to.

Example: Pass by reference-to-const

References must be bound to existing objects, not literals or temporaries.

There is an exception to this rule: References-to-const can be bound to anything.

```
const int &rci = 42; // OK.  
const std::string &rscs = a + b; // OK.
```

rscs is bound to the temporary object returned by a + b as if

```
std::string tmp = a + b;  
const std::string &rscs = tmp;
```

⇒ We will talk more about references-to-const in recitations.

Example: Pass by reference-to-`const`

The answer:

```
int count_lowercase(const std::string &str) { // `str` is a reference-to-`const`.
    int cnt = 0;
    for (char c : str)
        if (std::islower(c))
            ++cnt;
    return cnt;
}
```

```
std::string a = something(), b = some_other_thing();
int res1 = count_lowercase(a);           // OK.
int res2 = count_lowercase(a + b);       // OK.
int res3 = count_lowercase("hello");     // OK.
```

Benefits of passing by reference-to-const

Apart from the fact that it avoids copy, declaring the parameter as a reference-to-const also prevents some potential mistakes:

```
int some_kind_of_counting(const std::string &str, char value) {  
    int cnt = 0;  
    for (std::size_t i = 0; i != str.size(); ++i) {  
        if (str[i] = value) // Ooops! It should be `==`.  
            ++cnt;  
        else {  
            // do something ...  
            // ...  
        }  
    }  
    return cnt;  
}
```

`str[i] = value` will trigger a compile-error, because `str` is a reference-to-const. 99/115

Benefits of passing by reference-to-`const`

1. Avoids copy.
2. Accepts temporaries and literals (*rvalues*).
3. The `const` qualification prevents accidental modifications to it.

[Best practice] Pass by reference-to-`const` if copy is not necessary and the parameter should not be modified.

References vs pointers

A reference

- is not itself an object. It is an alias of the object that it is bound to.
- cannot be rebound to another object after initialization.
- has no "default" or "zero" value. It must be bound to an object.

A pointer

- is an object that stores the address of the object it points to.
- can switch to point to another object at any time.
- can be set to a null pointer value `nullptr`.

Both a reference and a pointer can be used to refer to an object, but references are more convenient - no need to write the annoying `*` and `&`.

`std::vector`

Defined in the standard library file `<vector>` .

A "dynamic array".

Class template

`std::vector` is a **class template**.

Class templates are not themselves classes. Instead, they can be thought of as instructions to the compiler for *generating* classes.

- The process that the compiler uses to create classes from the templates is called **instantiation**.

For `std::vector`, what kind of class is generated depends on the type of elements we want to store, often called **value type**. We supply this information inside a pair of angle brackets following the template's name:

```
std::vector<int> v; // `v` is of type `std::vector<int>`
```

Create a `std::vector`

`std::vector` is not a type itself. It must be combined with some `<T>` to form a type.

```
std::vector v;           // Error: missing template argument.
std::vector<int> vi;      // An empty vector of `int`s.
std::vector<std::string> vs; // An empty vector of strings.
std::vector<double> vd;   // An empty vector of `double`s.
std::vector<std::vector<int>> vvi; // An empty vector of vector of `int`s.
                                // "2-d" vector.
```

What are the types of `vi`, `vs` and `vvi` ?

Create a `std::vector`

`std::vector` is not a type itself. It must be combined with some `<T>` to form a type.

```
std::vector v;           // Error: missing template argument.
std::vector<int> vi;      // An empty vector of `int`s.
std::vector<std::string> vs; // An empty vector of strings.
std::vector<double> vd;   // An empty vector of `double`s.
std::vector<std::vector<int>> vvi; // An empty vector of vector of `int`s.
                                // "2-d" vector.
```

What are the types of `vi`, `vs` and `vvi`?

- `std::vector<int>`, `std::vector<std::string>`, `std::vector<std::vector<int>>`.

Create a `std::vector`

There are several common ways of creating a `std::vector` :

```
std::vector<int> v{2, 3, 5, 7};           // A vector of `int`s,  
                                           // whose elements are {2, 3, 5, 7}.  
std::vector<int> v2 = {2, 3, 5, 7};      // Equivalent to ↑  
  
std::vector<std::string> vs{"hello", "world"}; // A vector of strings,  
                                           // whose elements are {"hello", "world"}.  
std::vector<std::string> vs2 = {"hello", "world"}; // Equivalent to ↑  
  
std::vector<int> v3(10);                  // A vector of ten `int`s, all initialized to 0.  
std::vector<int> v4(10, 42);              // A vector of ten `int`s, all initialized to 42.
```

Note that all the elements in `v3` are initialized to `0`.

- We hate uninitialized values, so does the standard library.

Create a `std::vector`

Create a `std::vector` as a copy of another one: **No need to write a loop!**

```
std::vector<int> v{2, 3, 5, 7};  
std::vector<int> v2 = v; // `v2` is a copy of `v`  
std::vector<int> v3(v);  // Equivalent  
std::vector<int> v4{v};  // Equivalent
```

Copy assignment is also enabled:

```
std::vector<int> v1 = something(), v2 = something_else();  
v1 = v2;
```

- Element-wise copy is performed automatically.
- Memory is allocated automatically. The memory used to store the old data of `v1` is deallocated automatically.

C++17 CTAD

"Class Template **A**rgument **D**eduction": As long as enough information is supplied in the initializer, **the value type can be deduced automatically by the compiler.**

```
std::vector v1{2, 3, 5, 7}; // vector<int>
std::vector v2{3.14, 6.28}; // vector<double>
std::vector v3(10, 42);      // vector<int>, deduced from 42 (int)
std::vector v4(10);          // Error: cannot deduce template argument type
```

Size of a `std::vector`

`v.size()` and `v.empty()` : same as those on `std::string` .

```
std::vector v{2, 3, 5, 7};  
std::cout << v.size() << '\n';  
if (v.empty()) {  
    // ...  
}
```

`v.clear()` : Remove all the elements.

Append an element to the end of a `std::vector`

```
v.push_back(x)
```

```
int n;  
std::cin >> n;  
std::vector<int> v;  
for (int i = 0; i != n; ++i) {  
    int x;  
    std::cin >> x;  
    v.push_back(x);  
}  
std::cout << v.size() << '\n'; // n
```

Remove the last element of a `std::vector`

```
v.pop_back()
```

Exercise: Given `v` of type `std::vector<int>`, remove all the consecutive even numbers in the end.

```
while (!v.empty() && v.back() % 2 == 0)
    v.pop_back();
```

`v.back()` : returns the *reference* to the last element.

- How is it different from "returning the *value* of the last element"?

`v.back()` and `v.front()`

Return the references to the last and the first elements, respectively.

It is a **reference**, through which we can modify the corresponding element.

```
v.front() = 42;  
++v.back();
```

For `v.back()`, `v.front()` and `v.pop_back()`, the behavior is undefined if `v` is empty. They do not perform any bounds checking.

Range-based `for` loops

A `std::vector` can also be traversed using a range-based `for` loop.

```
std::vector<int> vi = some_values();  
for (int x : vi)  
    std::cout << x << std::endl;  
std::vector<std::string> vs = some_strings();  
for (const std::string &s : vs) // use reference-to-const to avoid copy  
    std::cout << s << std::endl;
```

Access through subscripts

`v[i]` returns the **reference** to the element indexed `i`.

- `i` $\in [0, N)$, where $N = \text{v.size()}$.
- Subscript out of range is **undefined behavior**. `v[i]` performs no bounds checking.
 - In pursuit of efficiency, most operations on standard library containers do not perform bounds checking.
- A kind of "subscript" that has bounds checking: `v.at(i)`.
 - If `i` is out of range, a `std::out_of_range` exception is thrown.

Feel the style of STL

Basic and low-level operations are performed automatically:

- Default initialization of `std::string` and `std::vector` results in an empty string / container, not indeterminate values.
- Copy of `std::string` and `std::vector` is done automatically, which performs member-wise copy.
- Memory management is done automatically.

Interfaces are consistent:

- `std::string` also has member functions like `.push_back(x)`, `.pop_back()`, `.at(i)`, `.size()`, `.clear()`, etc. which do the same things as on `std::vector`.
- Both can be traversed by range-`for`.