

# Statistics Demonstrations-Updated

September 23, 2024

## 0.1 Statistics Demonstrations

- Distributions (Binomial and Normal)
- Random Numbers
- Combinations

```
[4]: #Importing the libraries
import numpy as np
#Introducing the scipy.stats library
import scipy.stats as ss # Scipy is scientific python , stats is statistics
```

### 0.1.1 Distributions

**1. Binomial Distribution** A binomial distribution is utilised when the following conditions are met - Total number of trials is fixed at **n**

- Each trial is binary, i.e., has only two possible outcomes - success or failure
- Probability of success is same in all trials, denoted by **p** Now if you want to find the probability of **k** successes or  $P(X = k)$ , then you can use the following formula:

$$P(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$$

Where:

- $P(X = k)$  is the probability of getting exactly  $k$  successes in  $n$  trials.
- $\binom{n}{k}$  is the binomial coefficient, calculated as  $\frac{n!}{k!(n-k)!}$ , representing the number of ways to choose  $k$  successes from  $n$  trials.
- $p$  is the probability of success on a single trial.
- $1 - p$  is the probability of failure.
- $n$  is the number of trials.
- $k$  is the number of successes.

```
[6]: n = 10      # number of times i tossed a coin , that is 10 times i tossed
     p = 0.4     # probability if 4%
     k = 4       # 4 times in got head , this the measure of success
```

```
[7]: ?ss.binom.pmf
```

**Signature:** `ss.binom.pmf(k, *args, **kwds)`

**Docstring:**

Probability mass function at k of the given RV.

Parameters

-----

k : array\_like

Quantiles.

arg1, arg2, arg3,... : array\_like

The shape parameter(s) for the distribution (see docstring of the instance object for more information)

loc : array\_like, optional

Location parameter (default=0).

Returns

-----

pmf : array\_like

Probability mass function evaluated at k

**File:** /opt/conda/envs/anaconda-panel-2023.05-py310/lib/python3.11/

site-packages/scipy/stats/\_distn\_infrastructure.py

**Type:** method

```
[8]: ss.binom.pmf(k,n,p)
```

```
[8]: 0.25082265599999987
```

```
[9]: np.round(ss.binom.pmf(k,n,p),3)
```

```
[9]: 0.251
```

## 1 Normal Distribution

Let's say you're given a normal distribution with

- mean = M
- standard deviation = sd

Now you are given a value **x** and you want to compute  $P(X \leq x)$

```
[11]: M = 60
      sd = 10
      x = 40
```

```
[12]: ?ss.norm.cdf
```

**Signature:** `ss.norm.cdf(x, *args, **kwargs)`

**Docstring:**

Cumulative distribution function of the given RV.

Parameters

-----

`x` : array\_like

quantiles

`arg1, arg2, arg3,...` : array\_like

The shape parameter(s) for the distribution (see docstring of the instance object for more information)

`loc` : array\_like, optional

location parameter (default=0)

`scale` : array\_like, optional

scale parameter (default=1)

Returns

-----

`cdf` : ndarray

Cumulative distribution function evaluated at `x`

**File:** /opt/conda/envs/anaconda-panel-2023.05-py310/lib/python3.11/site-packages/scipy/stats/\_distn\_infrastructure.py

**Type:** method

```
[13]: ss.norm.cdf(x,M,sd)
```

```
[13]: 0.022750131948179195
```

```
[14]: ss.norm(60,10).cdf(40)
```

```
[14]: 0.022750131948179195
```

```
[15]: ss.norm.cdf(80,60,10)
```

```
[15]: 0.9772498680518208
```

```
[16]: ss.norm.cdf(40,60,10)
```

```
[16]: 0.022750131948179195
```

```
[17]: ss.norm.cdf(80,60,10) - ss.norm.cdf(40,60,10)
```

```
[17]: 0.9544997361036416
```

```
[18]: # Generate random numbers for a given distribution
```

```
[19]: ?np.random
```

```
Type:      module
String form: <module 'numpy.random' from '/opt/conda/envs/anaconda-panel-2023.05-py310/lib/python3.11/site-packages/numpy/random/__init__.py'>
File:      /opt/conda/envs/anaconda-panel-2023.05-py310/lib/python3.11/site-packages/numpy/random/__init__.py
```

```
Docstring:
```

```
=====
Random Number Generation
=====
```

Use ``default\_rng()`` to create a `Generator` and call its methods.

```
=====
Generator
-----
Generator      Class implementing all of the random number distributions
default_rng    Default constructor for ``Generator``
=====
```

```
=====
BitGenerator Streams that work with Generator
-----
MT19937
PCG64
PCG64DXSM
Philox
SFC64
=====
```

```
=====
Getting entropy to initialize a BitGenerator
-----
SeedSequence
=====
```

```
Legacy
-----
```

For backwards compatibility with previous versions of numpy before 1.17, the various aliases to the global `RandomState` methods are left alone and do not use the new `Generator` API.

```
=====
Utility functions
```

random	Uniformly distributed floats over ``[0, 1)``
bytes	Uniformly distributed random bytes.
permutation	Randomly permute a sequence / generate a random sequence.
shuffle	Randomly permute a sequence in place.
choice	Random sample from 1-D array.
=====	
Compatibility	
functions - removed	
in the new API	
-----	
rand	Uniformly distributed values.
randn	Normally distributed values.
ranf	Uniformly distributed floating point numbers.
random_integers	Uniformly distributed integers in a given range. (deprecated, use ``integers(..., closed=True)`` instead)
random_sample	Alias for `random_sample`
randint	Uniformly distributed integers in a given range
seed	Seed the legacy random number generator.
=====	
Univariate	
distributions	
-----	
beta	Beta distribution over ``[0, 1]``.
binomial	Binomial distribution.
chisquare	:math:`\chi^2` distribution.
exponential	Exponential distribution.
f	F (Fisher-Snedecor) distribution.
gamma	Gamma distribution.
geometric	Geometric distribution.
gumbel	Gumbel distribution.
hypergeometric	Hypergeometric distribution.
laplace	Laplace distribution.
logistic	Logistic distribution.
lognormal	Log-normal distribution.
logseries	Logarithmic series distribution.
negative_binomial	Negative binomial distribution.
noncentral_chisquare	Non-central chi-square distribution.
noncentral_f	Non-central F distribution.
normal	Normal / Gaussian distribution.
pareto	Pareto distribution.
poisson	Poisson distribution.
power	Power distribution.
rayleigh	Rayleigh distribution.

triangular	Triangular distribution.
uniform	Uniform distribution.
vonmises	Von Mises circular distribution.
wald	Wald (inverse Gaussian) distribution.
weibull	Weibull distribution.
zipf	Zipf's distribution over ranked data.

=====

Multivariate  
distributions

-----

dirichlet	Multivariate generalization of Beta distribution.
multinomial	Multivariate generalization of the binomial distribution.
multivariate_normal	Multivariate generalization of the normal distribution.

=====

Standard  
distributions

-----

standard_cauchy	Standard Cauchy-Lorentz distribution.
standard_exponential	Standard exponential distribution.
standard_gamma	Standard Gamma distribution.
standard_normal	Standard normal distribution.
standard_t	Standard Student's t-distribution.

=====

Internal functions

-----

get_state	Get tuple representing internal state of generator.
set_state	Set state of generator.

=====

### 1.0.1 Binomial Distribution

For binomial distribution, given the value of **n** (the number of trials) and **p** ( the probability of success for each trial) we can generate random sequence of possible number of successes **r** when we run this experiment multiple times.

```
[21]: ?np.random.binomial
```

**Docstring:**

```
binomial(n, p, size=None)
```

Draw samples from a binomial distribution.

Samples are drawn from a binomial distribution with specified parameters,  $n$  trials and  $p$  probability of success where  $n$  an integer  $\geq 0$  and  $p$  is in the interval  $[0,1]$ . ( $n$  may be input as a float, but it is truncated to an integer in use)

.. note::

New code should use the `~numpy.random.Generator.binomial` method of a `~numpy.random.Generator` instance instead; please see the :ref:`random-quick-start`.

#### Parameters

-----  
`n` : int or array\_like of ints

Parameter of the distribution,  $\geq 0$ . Floats are also accepted, but they will be truncated to integers.

`p` : float or array\_like of floats

Parameter of the distribution,  $\geq 0$  and  $\leq 1$ .

`size` : int or tuple of ints, optional

Output shape. If the given shape is, e.g., `((m, n, k))`, then `m * n * k` samples are drawn. If size is `None` (default), a single value is returned if `n` and `p` are both scalars. Otherwise, `np.broadcast(n, p).size` samples are drawn.

#### Returns

-----  
`out` : ndarray or scalar

Drawn samples from the parameterized binomial distribution, where each sample is equal to the number of successes over the  $n$  trials.

#### See Also

-----  
`scipy.stats.binom` : probability density function, distribution or cumulative density function, etc.

`random.Generator.binomial`: which should be used for new code.

#### Notes

-----  
The probability density for the binomial distribution is

.. math:: P(N) = \binom{n}{N} p^N (1-p)^{n-N},

where  $n$  is the number of trials,  $p$  is the probability of success, and  $N$  is the number of successes.

When estimating the standard error of a proportion in a population by using a random sample, the normal distribution works well unless the product  $p \cdot n \leq 5$ , where  $p$  = population proportion estimate, and  $n$  = number of samples, in which case the binomial distribution is used

instead. For example, a sample of 15 people shows 4 who are left handed, and 11 who are right handed. Then  $p = 4/15 = 27\%$ .  $0.27 \cdot 15 = 4$ , so the binomial distribution should be used in this case.

## References

- .. [1] Dalgaard, Peter, "Introductory Statistics with R", Springer-Verlag, 2002.
- .. [2] Glantz, Stanton A. "Primer of Biostatistics.", McGraw-Hill, Fifth Edition, 2002.
- .. [3] Lentner, Marvin, "Elementary Applied Statistics", Bogden and Quigley, 1972.
- .. [4] Weisstein, Eric W. "Binomial Distribution." From MathWorld--A Wolfram Web Resource.  
<http://mathworld.wolfram.com/BinomialDistribution.html>
- .. [5] Wikipedia, "Binomial distribution",  
[https://en.wikipedia.org/wiki/Binomial\\_distribution](https://en.wikipedia.org/wiki/Binomial_distribution)

## Examples

Draw samples from the distribution:

```
>>> n, p = 10, .5 # number of trials, probability of each trial
>>> s = np.random.binomial(n, p, 1000)
# result of flipping a coin 10 times, tested 1000 times.
```

A real world example. A company drills 9 wild-cat oil exploration wells, each with an estimated probability of success of 0.1. All nine wells fail. What is the probability of that happening?

Let's do 20,000 trials of the model, and count the number that generate zero positive results.

```
>>> sum(np.random.binomial(9, 0.1, 20000) == 0)/20000.
# answer = 0.38885, or 38%.
Type:          builtin_function_or_method
```

```
[22]: # Let us generate 10 random numbers from Binomial
```

```
[23]: n = 10
      p = 0.4
      size = 10
      np.random.binomial(n,p,size)
```

```
[23]: array([7, 4, 3, 3, 6, 0, 4, 4, 3, 4])
```



### 1.0.2 Normal Distribution

For normal distribution, given the value of mean (**M**) and standard deviation (**sd**) we can generate random sequence of values belonging to this distribution

```
[25]: ?np.random.normal # ? is the help function (What is np.random.normal?)
```

```
Object `np.random.normal # ? is the help function (What is np.random.normal?)`  
not found.
```

```
[26]: M = 60  
      sd = 10  
      np.random.normal(M,sd,10)
```

```
[26]: array([65.42709854, 71.05547796, 72.81903122, 64.88387427, 47.88066188,  
            56.43691405, 54.52811441, 60.78701889, 69.74555022, 63.47721017])
```

### 1.0.3 In order to fix the output we can set the seed value

```
[28]: ?np.random.seed
```

```
Docstring:  
seed(seed=None)
```

Reseed the singleton RandomState instance.

Notes

-----

This is a convenience, legacy function that exists to support older code that uses the singleton RandomState. Best practice is to use a dedicated ``Generator`` instance rather than the random variate generation methods exposed directly in the random module.

See Also

-----

numpy.random.Generator

Type: builtin\_function\_or\_method

```
[29]: seed = 100  
      np.random.seed(seed)
```

```
[30]: np.random.normal(M,sd,10)
```

```
[30]: array([42.50234527, 63.42680403, 71.53035803, 57.47563963, 69.81320787,  
            65.14218841, 62.21179669, 49.29956669, 58.10504169, 62.55001444])
```

```
[31]: np.random.normal(M,sd,10)
```

```
[31]: array([55.41973014, 64.35163488, 54.1640495 , 68.16847072, 66.72720806,
          58.95588857, 54.68719623, 70.29732685, 55.61864377, 48.81681754])
```

The seed has to be initialised each time you run the code to get the same output

#### 1.0.4 Combinations

Given a list containing **n** number of objects, we can find all the combinations of size **r**

```
[34]: from itertools import combinations
```

```
[35]: ?combinations
```

Init signature: combinations(iterable, r)

Docstring:

Return successive r-length combinations of elements in the iterable.

combinations(range(4), 3) --> (0,1,2), (0,1,3), (0,2,3), (1,2,3)

Type: type

Subclasses:

```
[36]: alpha = 'ABCD'
      p = combinations(alpha, 2)
      p
```

```
[36]: <itertools.combinations at 0x7fac1baf380>
```

```
[37]: list(p)
```

```
[37]: [('A', 'B'), ('A', 'C'), ('A', 'D'), ('B', 'C'), ('B', 'D'), ('C', 'D')]
```

```
[38]: alpha = ['A','B','C','D']
      p = combinations(alpha, 2)
      list(p)
```

```
[38]: [('A', 'B'), ('A', 'C'), ('A', 'D'), ('B', 'C'), ('B', 'D'), ('C', 'D')]
```

```
[39]: num = [1,2,3]
      num
```

```
[39]: [1, 2, 3]
```

```
[40]: list(combinations(num, 2))
```

```
[40]: [(1, 2), (1, 3), (2, 3)]
```

```
[41]: for c in combinations(num, 2):
      if 2 in c:
```

```
print(c)
```

```
(1, 2)
```

```
(2, 3)
```

```
[42]: for c in combinations(alpha, 2):  
      if 'A' in c:  
          print(c)
```

```
('A', 'B')
```

```
('A', 'C')
```

```
('A', 'D')
```

### 1.0.5 Working on BeautifulSoup library to fetch data from webpages

```
[44]: pip install requests beautifulsoup4
```

```
Defaulting to user installation because normal site-packages is not writeable  
Looking in links: /usr/share/pip-wheels  
Requirement already satisfied: requests in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (2.31.0)  
Requirement already satisfied: beautifulsoup4 in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (4.12.2)  
Requirement already satisfied: charset-normalizer<4,>=2 in  
/opt/conda/envs/anaconda-panel-2023.05-py310/lib/python3.11/site-packages (from  
requests) (2.0.4)  
Requirement already satisfied: idna<4,>=2.5 in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (from requests) (3.4)  
Requirement already satisfied: urllib3<3,>=1.21.1 in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (from requests) (1.26.16)  
Requirement already satisfied: certifi>=2017.4.17 in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (from requests) (2023.7.22)  
Requirement already satisfied: soupsieve>1.2 in /opt/conda/envs/anaconda-  
panel-2023.05-py310/lib/python3.11/site-packages (from beautifulsoup4) (2.4)  
Note: you may need to restart the kernel to use updated packages.
```

```
[45]: import requests  
      from bs4 import BeautifulSoup
```

```
[46]: url = "https://www.bing.com/images/search?q=Archana+Hebbar&form=RESTAB&first=1"  
      response = requests.get(url)  
      soup = BeautifulSoup(response.content, 'html.parser')
```

```
[47]: print(soup.title.string)
```

```
Archana Hebbar - Search Images
```

```
[ ]:
```