

aerofit-case-study-final

April 19, 2024

Business Problem

The market research team at AeroFit wants to identify the characteristics of the target audience for each type of treadmill offered by the company, to provide a better recommendation of the treadmills to the new customers.

```
[ ]: import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
```

```
[ ]: # Loading the dataset and previewing it

df = pd.read_csv("aerofit_treadmill.csv")
df.head()
```

```
[ ]:  Product  Age  Gender  Education  MaritalStatus  Usage  Fitness  Income  Miles
0    KP281   18   Male      14         Single        3        4   29562   112
1    KP281   19   Male      15         Single        2        3   31836    75
2    KP281   19  Female      14     Partnered        4        3   30699    66
3    KP281   19   Male      12         Single        3        3   32973    85
4    KP281   20   Male      13     Partnered        4        2   35247    47
```

```
[ ]: df.shape
```

```
[ ]: (180, 9)
```

```
[ ]: # Checking the structure of the dataset

df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 180 entries, 0 to 179
Data columns (total 9 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Product         180 non-null   object
1   Age             180 non-null   int64
2   Gender          180 non-null   object
3   Education        180 non-null   int64
```

```

4  MaritalStatus  180 non-null  object
5  Usage          180 non-null  int64
6  Fitness        180 non-null  int64
7  Income         180 non-null  int64
8  Miles          180 non-null  int64
dtypes: int64(6), object(3)
memory usage: 12.8+ KB

```

```

[ ]: # Getting a statistical summary of the dataset

df.describe()

```

```

[ ]:
count      Age  Education      Usage      Fitness      Income  \
count  180.000000  180.000000  180.000000  180.000000  180.000000
mean    28.788889  15.572222   3.455556   3.311111  53719.577778
std      6.943498   1.617055   1.084797   0.958869  16506.684226
min     18.000000  12.000000   2.000000   1.000000  29562.000000
25%     24.000000  14.000000   3.000000   3.000000  44058.750000
50%     26.000000  16.000000   3.000000   3.000000  50596.500000
75%     33.000000  16.000000   4.000000   4.000000  58668.000000
max      50.000000  21.000000   7.000000   5.000000 104581.000000

      Miles
count  180.000000
mean   103.194444
std     51.863605
min     21.000000
25%     66.000000
50%     94.000000
75%    114.750000
max     360.000000

```

```

[ ]: # Checking for missing values

missing_values = df.isnull().sum()
print("Missing Values:")
print(missing_values)

```

```

Missing Values:
Product      0
Age          0
Gender       0
Education    0
MaritalStatus 0
Usage        0
Fitness      0
Income       0
Miles        0

```

dtype: int64

```
[ ]: # Checking for duplicate rows

duplicates = df.duplicated()

# Counting the number of duplicate rows
num_duplicates = duplicates.sum()
print("Number of Duplicate Rows:", num_duplicates)
```

Number of Duplicate Rows: 0

```
[ ]: # Check unique values of categorical variables

print("Unique values :", df['Product'].unique())
print("Unique values :", df['Gender'].unique())
print("Unique values :", df['MaritalStatus'].unique())
```

Unique values : ['KP281' 'KP481' 'KP781']

Unique values : ['Male' 'Female']

Unique values : ['Single' 'Partnered']

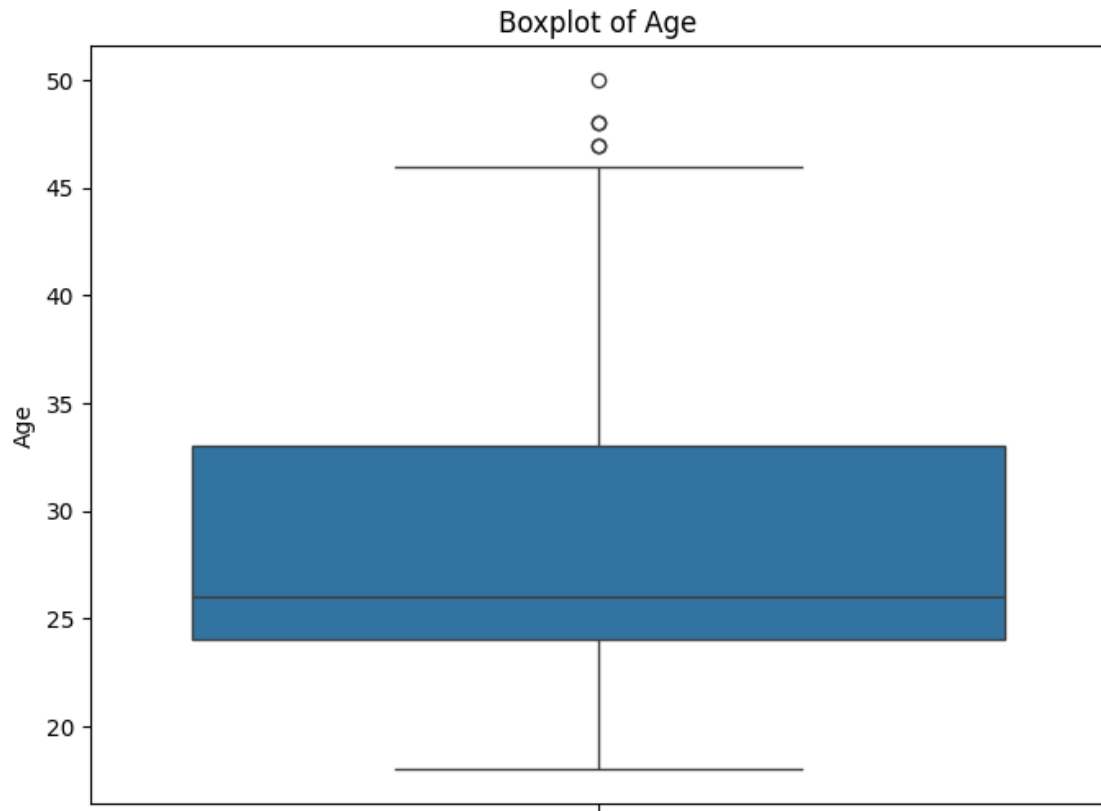
```
[ ]: # Select numerical columns for outlier detection
numerical_columns = df.select_dtypes(include=['int64']).columns

# Plot boxplots for each numerical column
for col in numerical_columns:
    plt.figure(figsize=(8, 6))
    sns.boxplot(y=col, data=df)
    plt.title(f'Boxplot of {col}')
    plt.show()

# Calculate mean and median
mean_val = df[col].mean()
median_val = df[col].median()

print(f"Mean of {col}: {mean_val}")
print(f"Median of {col}: {median_val}")

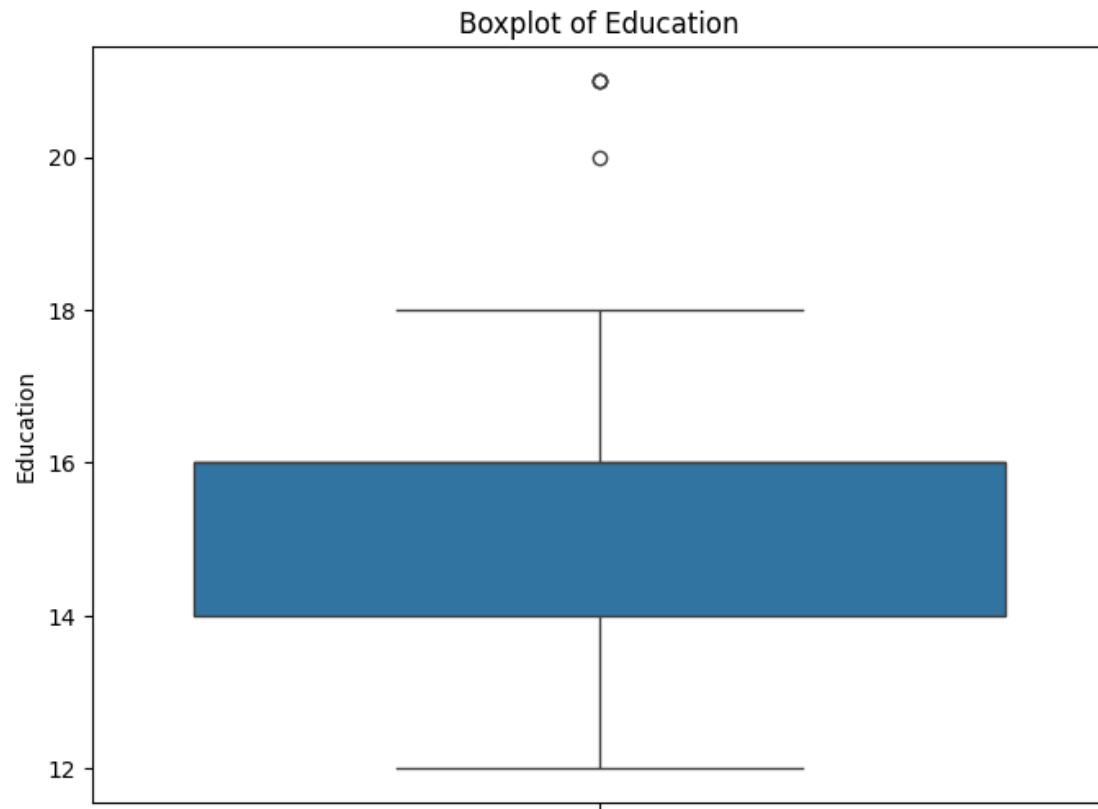
# Calculate the difference between mean and median
diff = mean_val - median_val
print(f"Difference between mean and median of {col}: {diff}")
```



Mean of Age: 28.788888888888888

Median of Age: 26.0

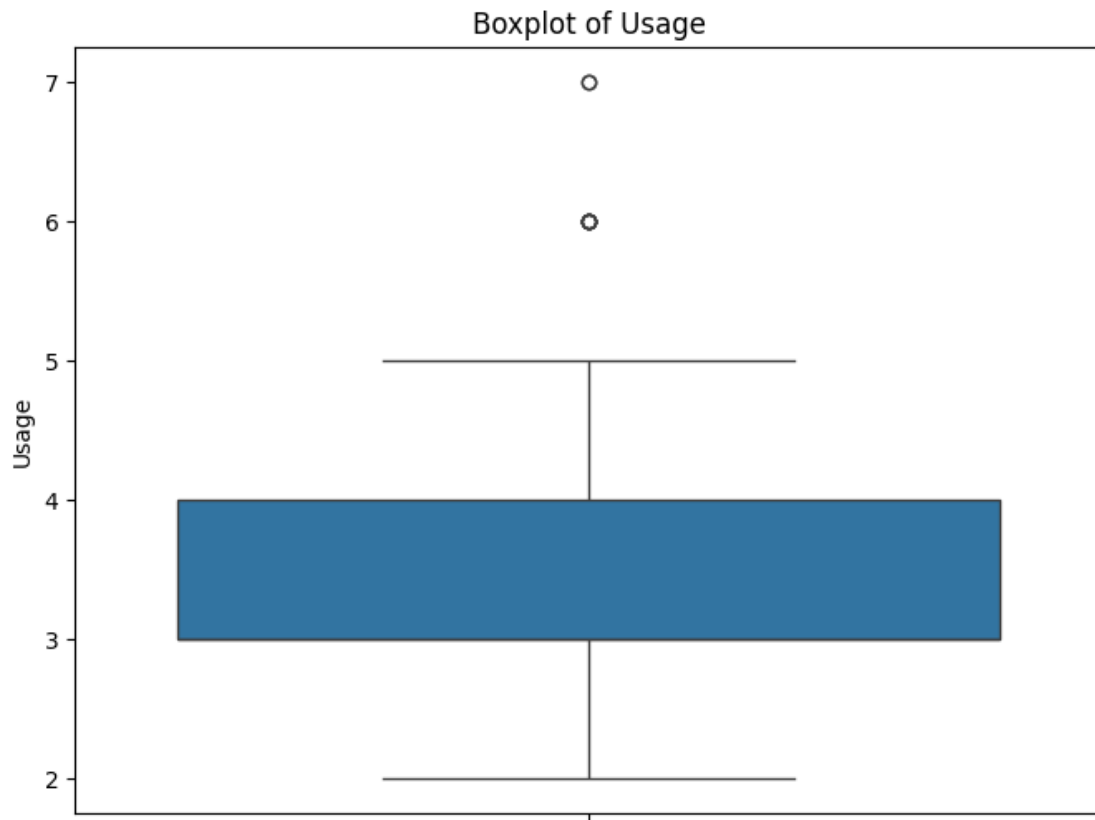
Difference between mean and median of Age: 2.788888888888888



Mean of Education: 15.57222222222223

Median of Education: 16.0

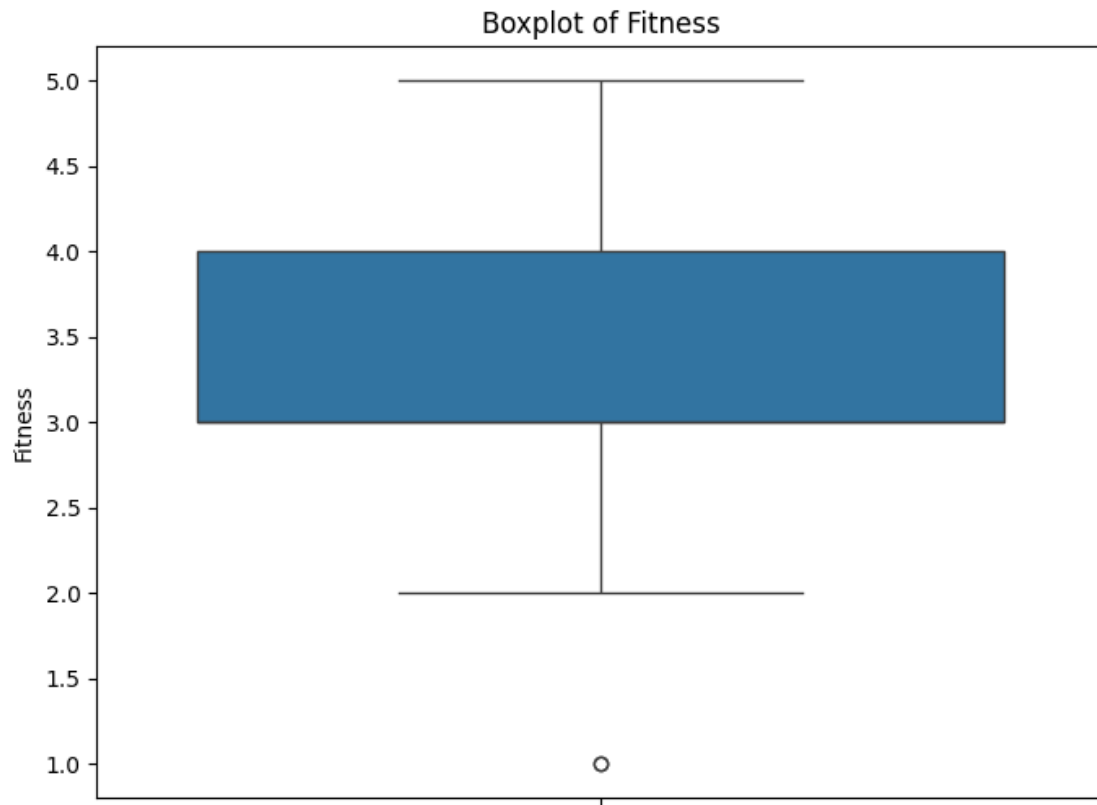
Difference between mean and median of Education: -0.4277777777777715



Mean of Usage: 3.4555555555555557

Median of Usage: 3.0

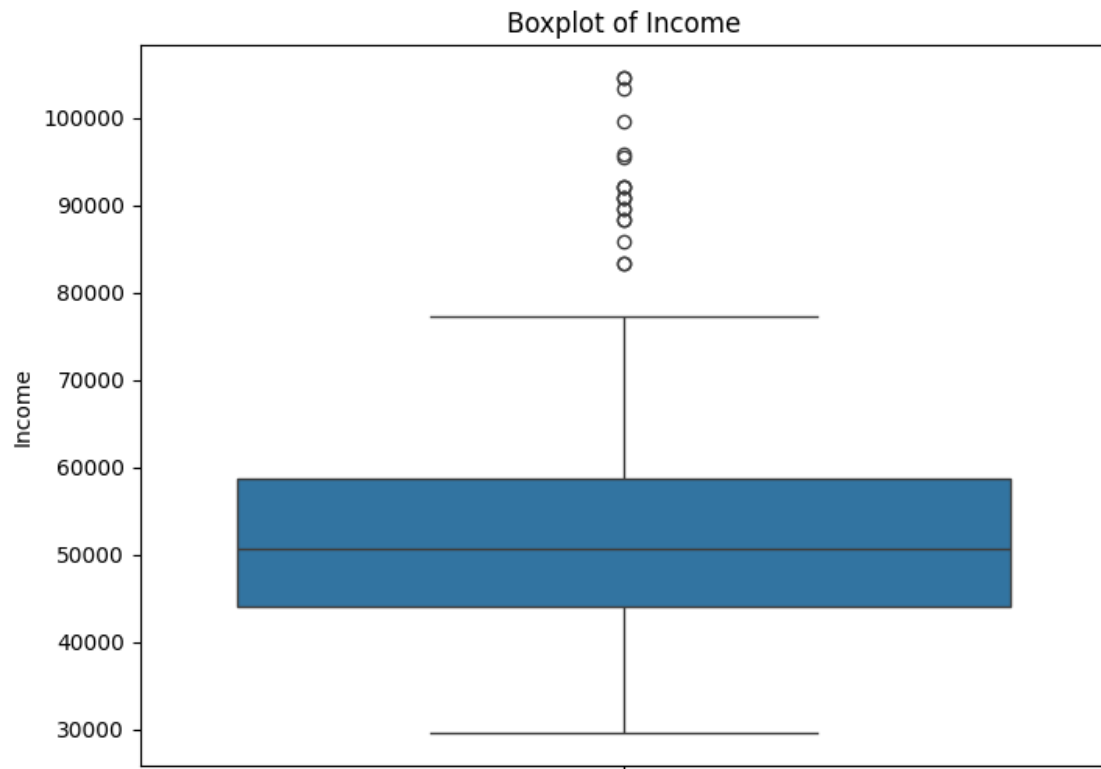
Difference between mean and median of Usage: 0.4555555555555557



Mean of Fitness: 3.311111111111111

Median of Fitness: 3.0

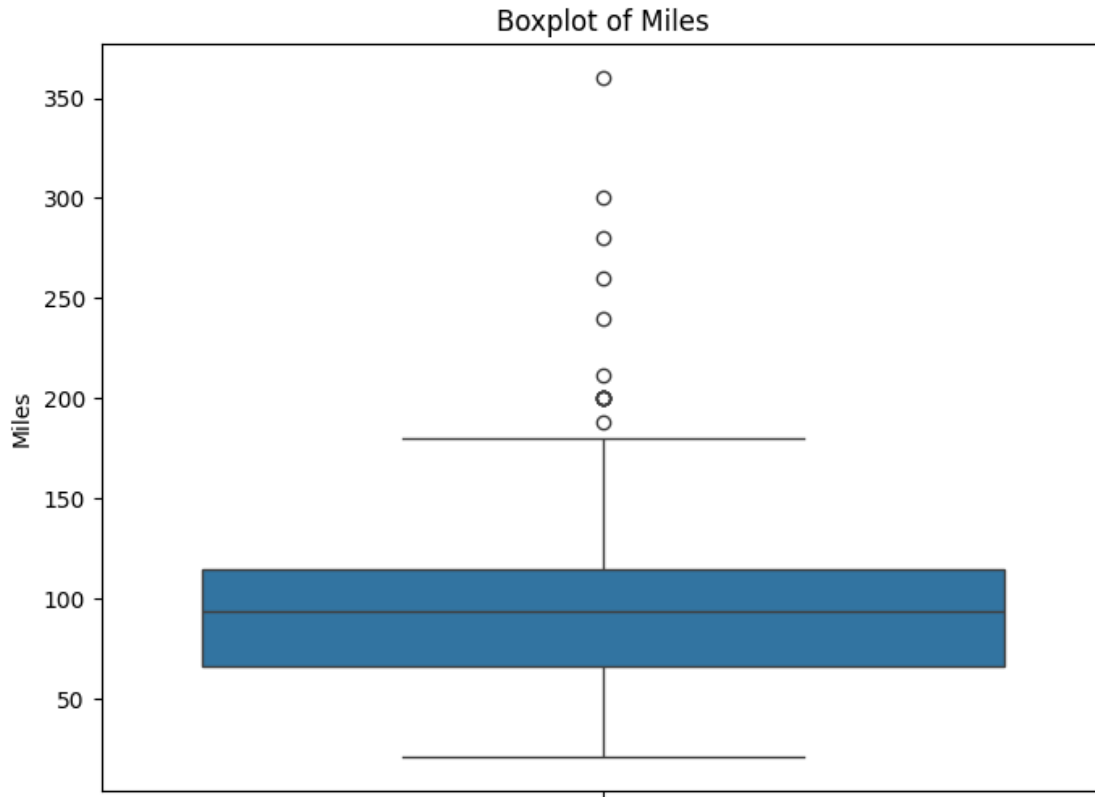
Difference between mean and median of Fitness: 0.311111111111109



Mean of Income: 53719.57777777778

Median of Income: 50596.5

Difference between mean and median of Income: 3123.0777777777766



Mean of Miles: 103.19444444444444

Median of Miles: 94.0

Difference between mean and median of Miles: 9.194444444444443

```
[ ]: # Display the unique values and their counts for each column
for col in df.columns:
    print(f"Column: {col}")
    print(f"Number of unique values: {df[col].nunique()}")
    print(f"Unique values:\n{df[col].unique()}\n")

    # If the column has less than 10 unique values, also display value counts
    if df[col].nunique() <= 10:
        print(f"Value counts:\n{df[col].value_counts()}\n")
```

Column: Product

Number of unique values: 3

Unique values:

['KP281' 'KP481' 'KP781']

Value counts:

Product

KP281 80

```
KP481      60
KP781      40
Name: count, dtype: int64
```

```
Column: Age
Number of unique values: 32
Unique values:
[18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41
 43 44 46 47 50 45 48 42]
```

```
Column: Gender
Number of unique values: 2
Unique values:
['Male' 'Female']
```

```
Value counts:
Gender
Male      104
Female     76
Name: count, dtype: int64
```

```
Column: Education
Number of unique values: 8
Unique values:
[14 15 12 13 16 18 20 21]
```

```
Value counts:
Education
16      85
14      55
18      23
15       5
13       5
12       3
21       3
20       1
Name: count, dtype: int64
```

```
Column: MaritalStatus
Number of unique values: 2
Unique values:
['Single' 'Partnered']
```

```
Value counts:
MaritalStatus
Partnered  107
Single     73
Name: count, dtype: int64
```

Column: Usage
Number of unique values: 6
Unique values:
[3 2 4 5 6 7]

Value counts:
Usage
3 69
4 52
2 33
5 17
6 7
7 2
Name: count, dtype: int64

Column: Fitness
Number of unique values: 5
Unique values:
[4 3 2 1 5]

Value counts:
Fitness
3 97
5 31
2 26
4 24
1 2
Name: count, dtype: int64

Column: Income
Number of unique values: 62
Unique values:
[29562 31836 30699 32973 35247 37521 36384 38658 40932 34110
 39795 42069 44343 45480 46617 48891 53439 43206 52302 51165
 50028 54576 68220 55713 60261 67083 56850 59124 61398 57987
 64809 47754 65220 62535 48658 54781 48556 58516 53536 61006
 57271 52291 49801 62251 64741 70966 75946 74701 69721 83416
 88396 90886 92131 77191 52290 85906 103336 99601 89641 95866
104581 95508]

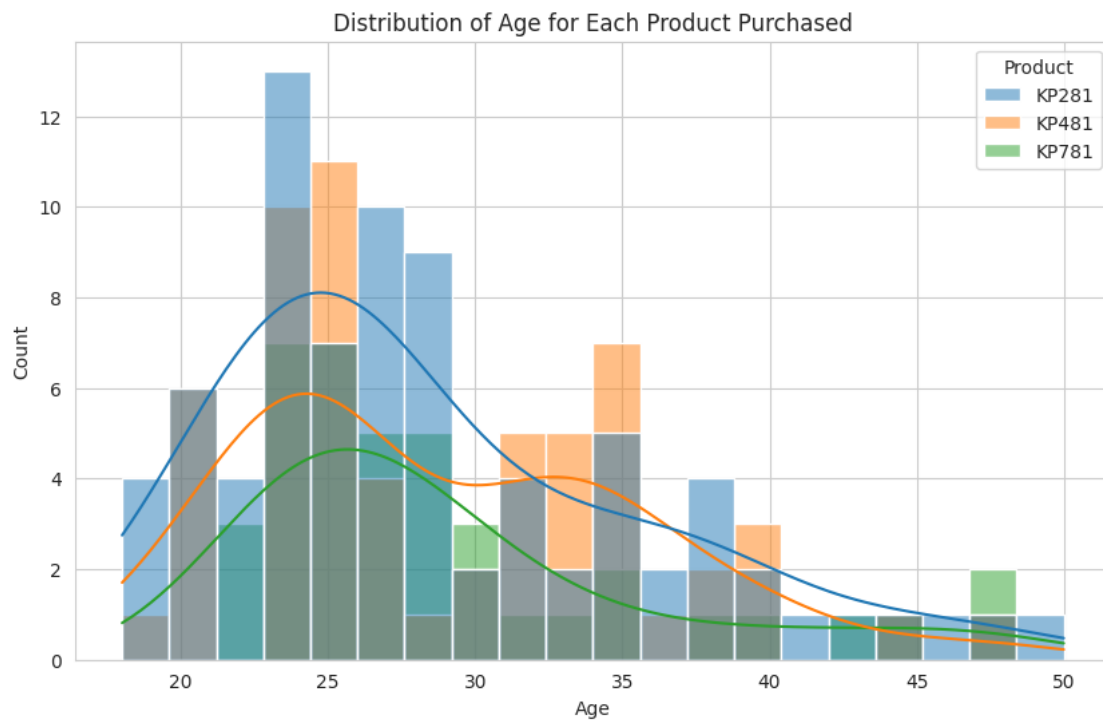
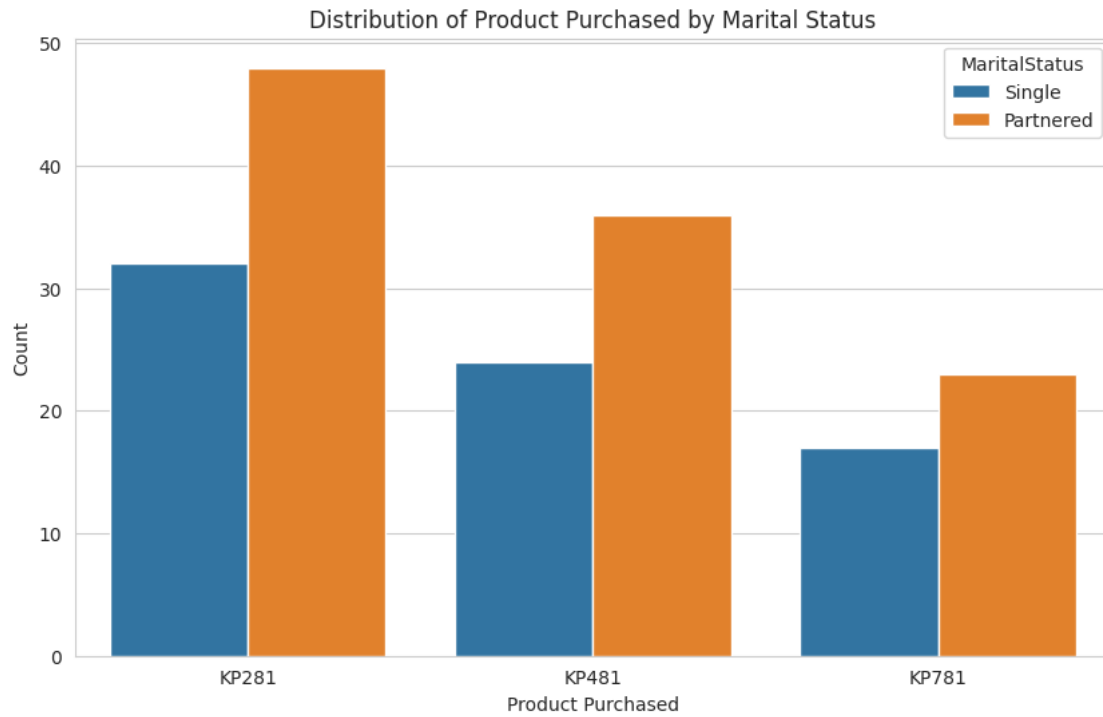
Column: Miles
Number of unique values: 37
Unique values:
[112 75 66 85 47 141 103 94 113 38 188 56 132 169 64 53 106 95
 212 42 127 74 170 21 120 200 140 100 80 160 180 240 150 300 280 260
 360]

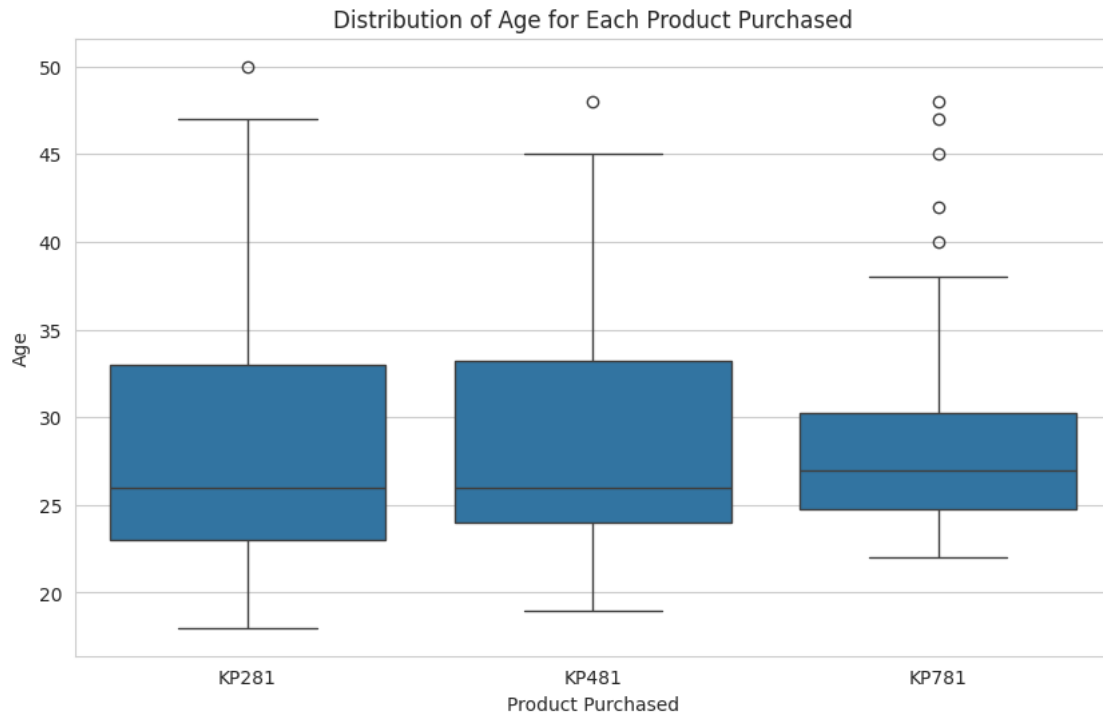
```
[ ]: # Set the style of the plots
sns.set_style("whitegrid")

# Create a countplot to visualize the distribution of product purchased based
↳ on marital status
plt.figure(figsize=(10, 6))
sns.countplot(x="Product", hue="MaritalStatus", data=df)
plt.title("Distribution of Product Purchased by Marital Status")
plt.xlabel("Product Purchased")
plt.ylabel("Count")
plt.show()

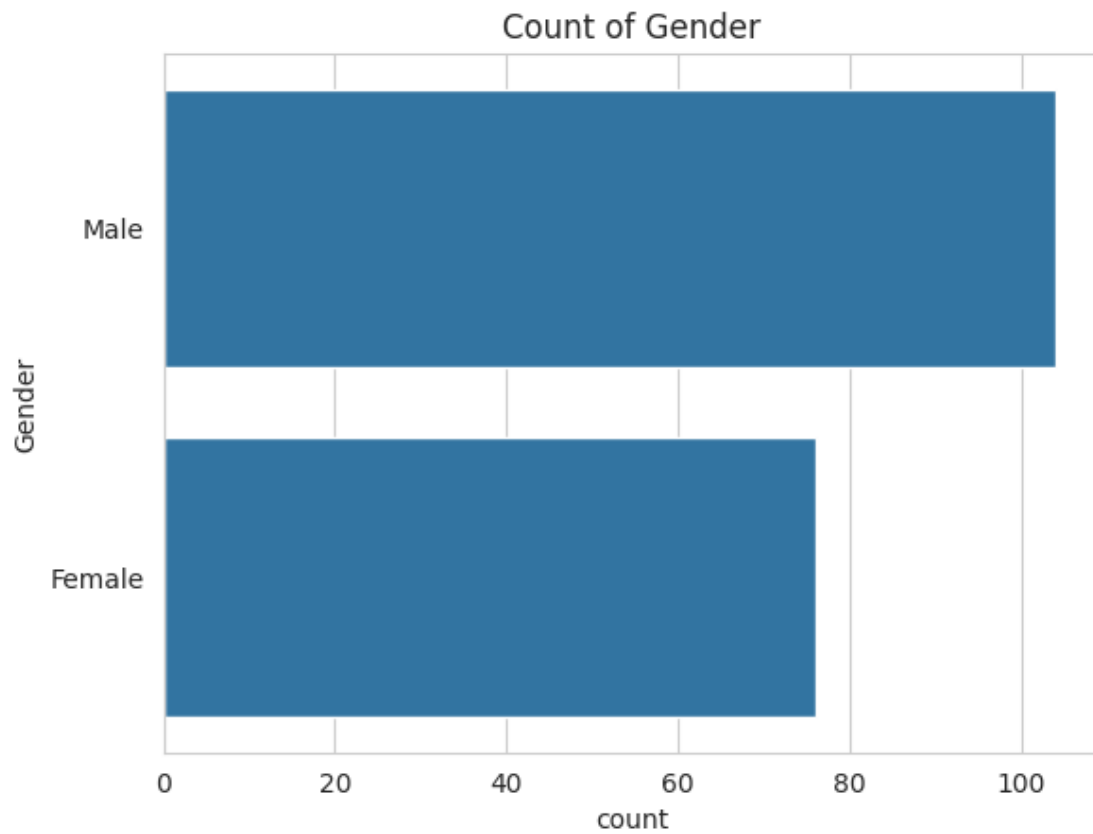
# Create a histogram to visualize the distribution of age for each product
↳ purchased
plt.figure(figsize=(10, 6))
sns.histplot(data=df, x="Age", hue="Product", kde=True, bins=20)
plt.title("Distribution of Age for Each Product Purchased")
plt.xlabel("Age")
plt.ylabel("Count")
plt.show()

# Create a boxplot to visualize the distribution of age for each product
↳ purchased
plt.figure(figsize=(10, 6))
sns.boxplot(x="Product", y="Age", data=df)
plt.title("Distribution of Age for Each Product Purchased")
plt.xlabel("Product Purchased")
plt.ylabel("Age")
plt.show()
```

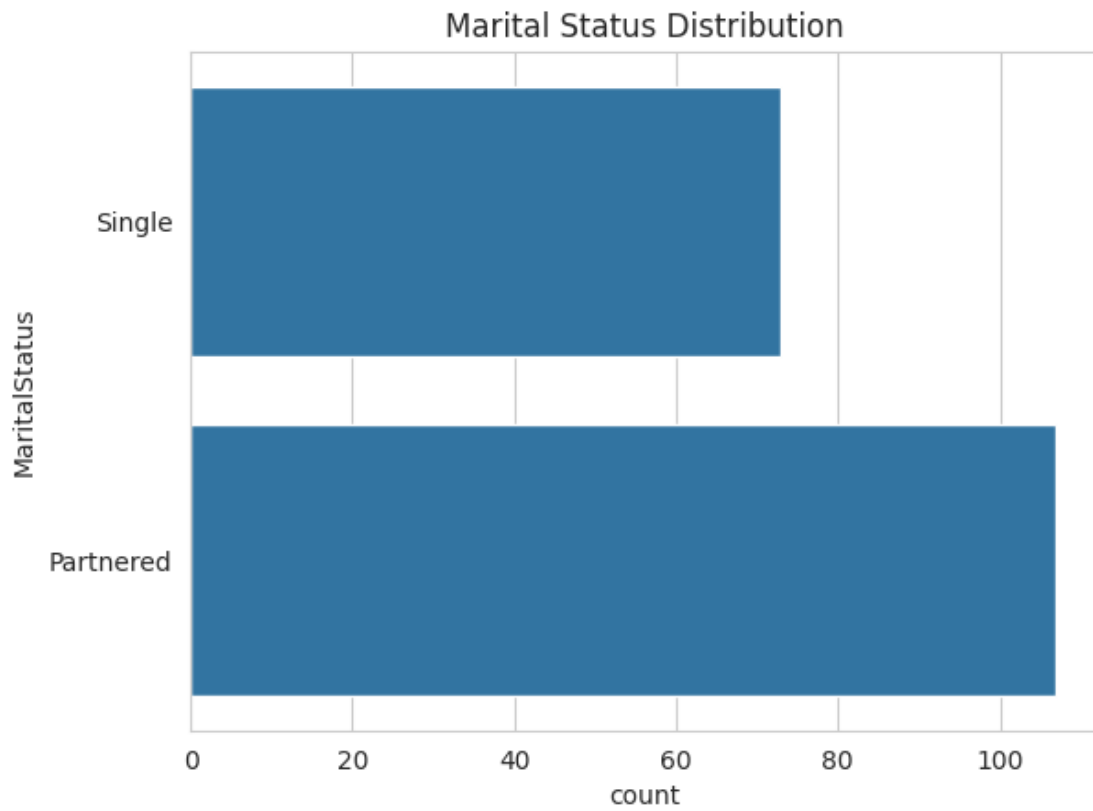




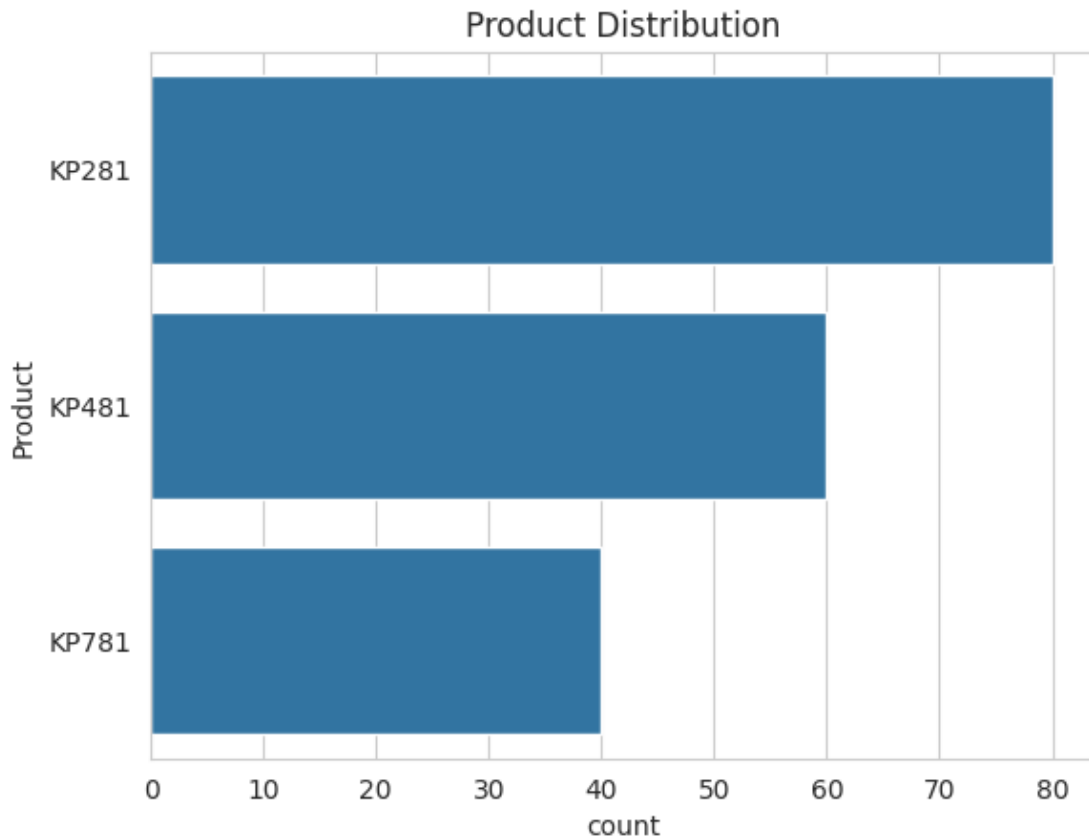
```
[ ]: sns.countplot(df['Gender'])  
plt.title('Count of Gender')  
plt.show()
```



```
[ ]: sns.countplot(df['MaritalStatus'])  
plt.title('Marital Status Distribution')  
plt.show()
```



```
[ ]: sns.countplot(df['Product'])  
plt.title('Product Distribution')  
plt.show()
```

```
[ ]: # Distplot
sns.distplot(df['Age'])
plt.title('Distribution of Age')
plt.show()
```

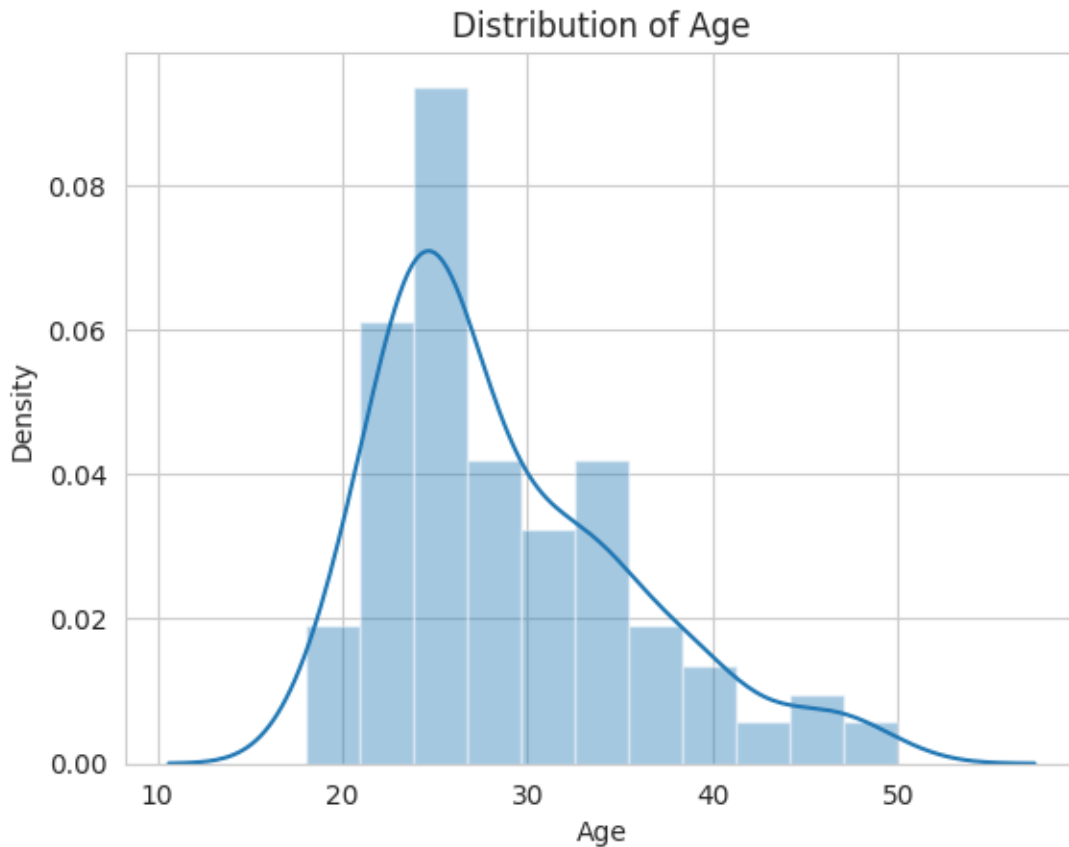
<ipython-input-15-4226616f2e34>:2: UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see <https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751>

```
sns.distplot(df['Age'])
```



```
[ ]: # Distplot
sns.distplot(df['Education'])
plt.title('Distribution of Education')
plt.show()
```

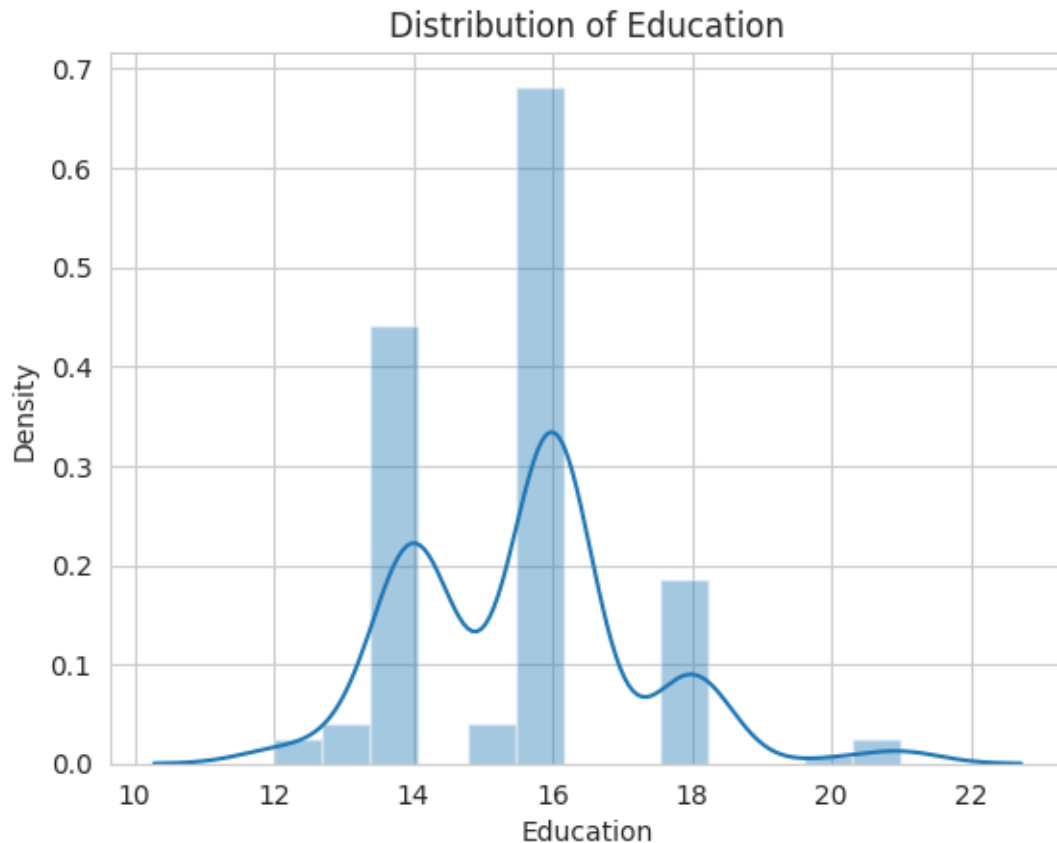
<ipython-input-16-6821fed00a76>:2: UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see <https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751>

```
sns.distplot(df['Education'])
```



```
[ ]: # Distplot
sns.distplot(df['Usage'])
plt.title('Distribution of Usage')
plt.show()
```

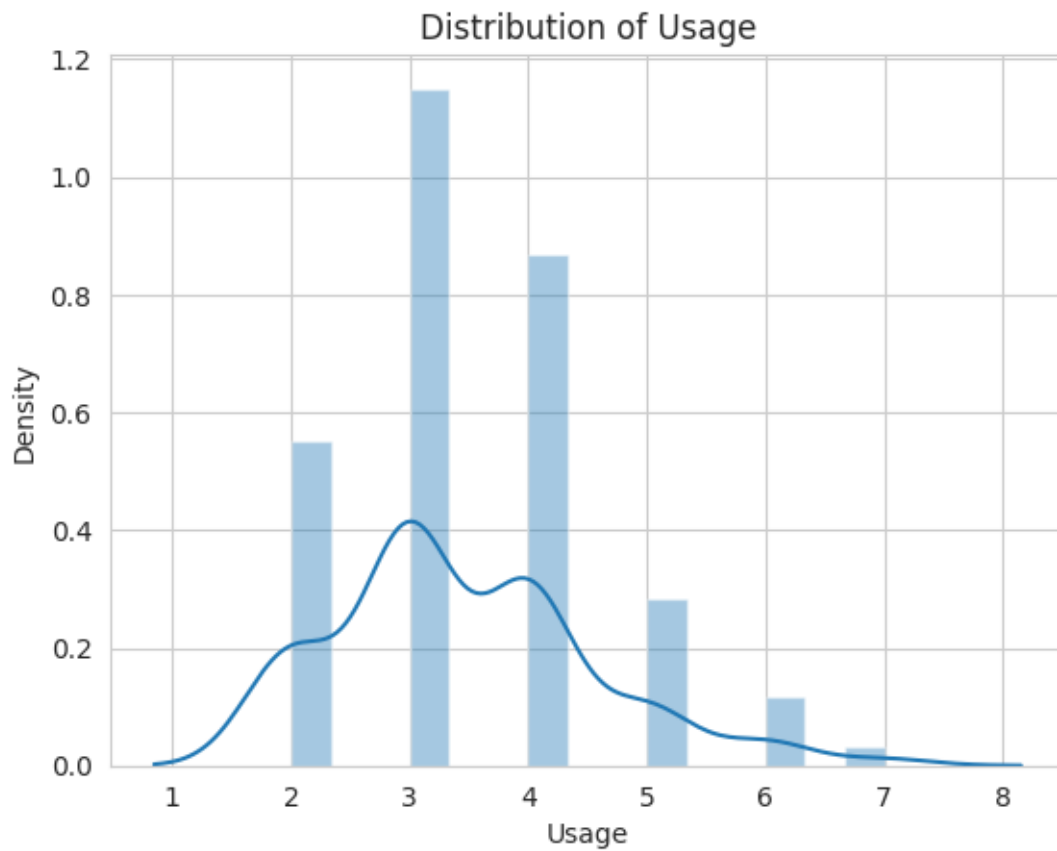
<ipython-input-17-9e284c0404b2>:2: UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

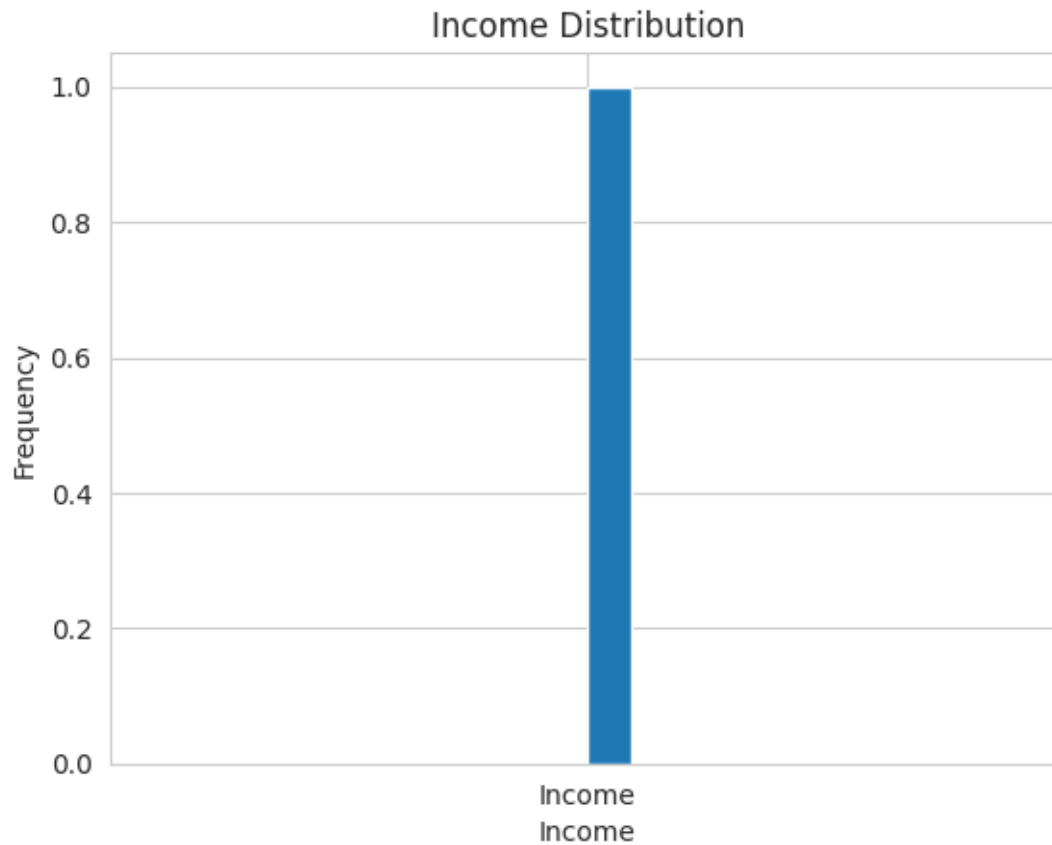
Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see <https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751>

```
sns.distplot(df['Usage'])
```

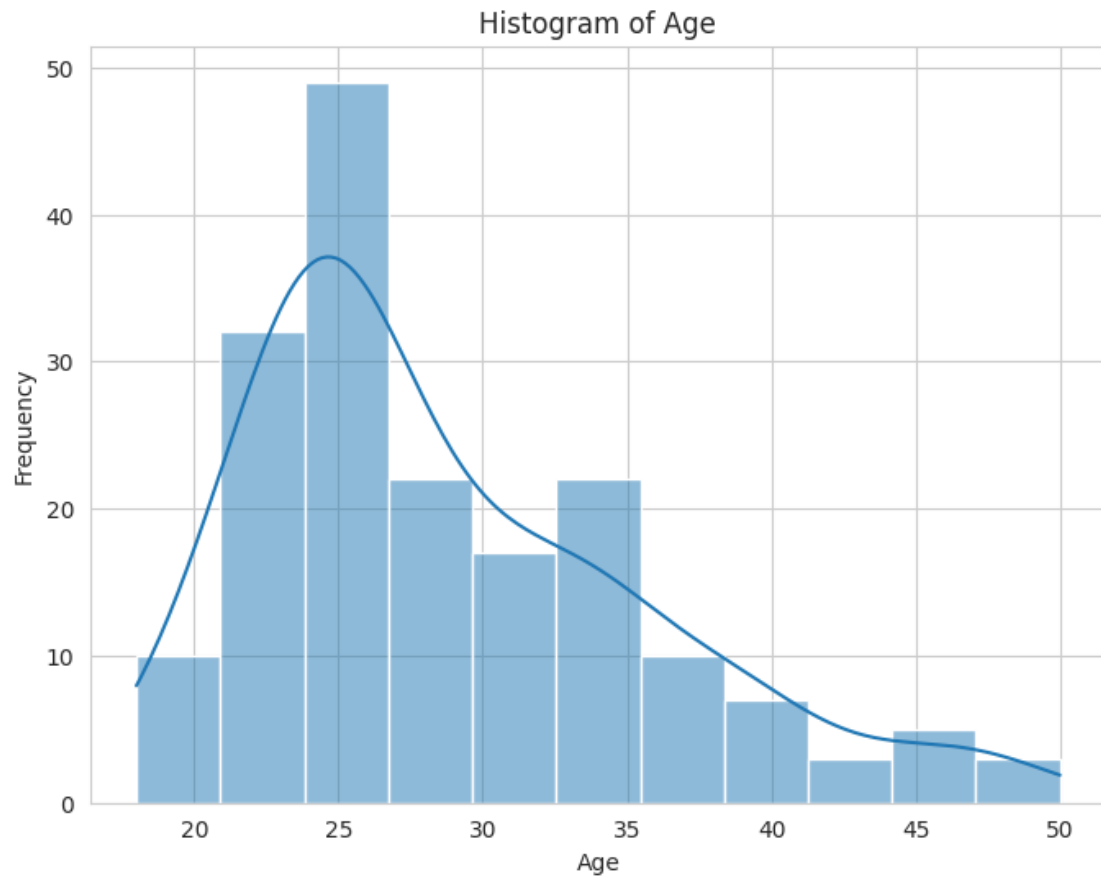


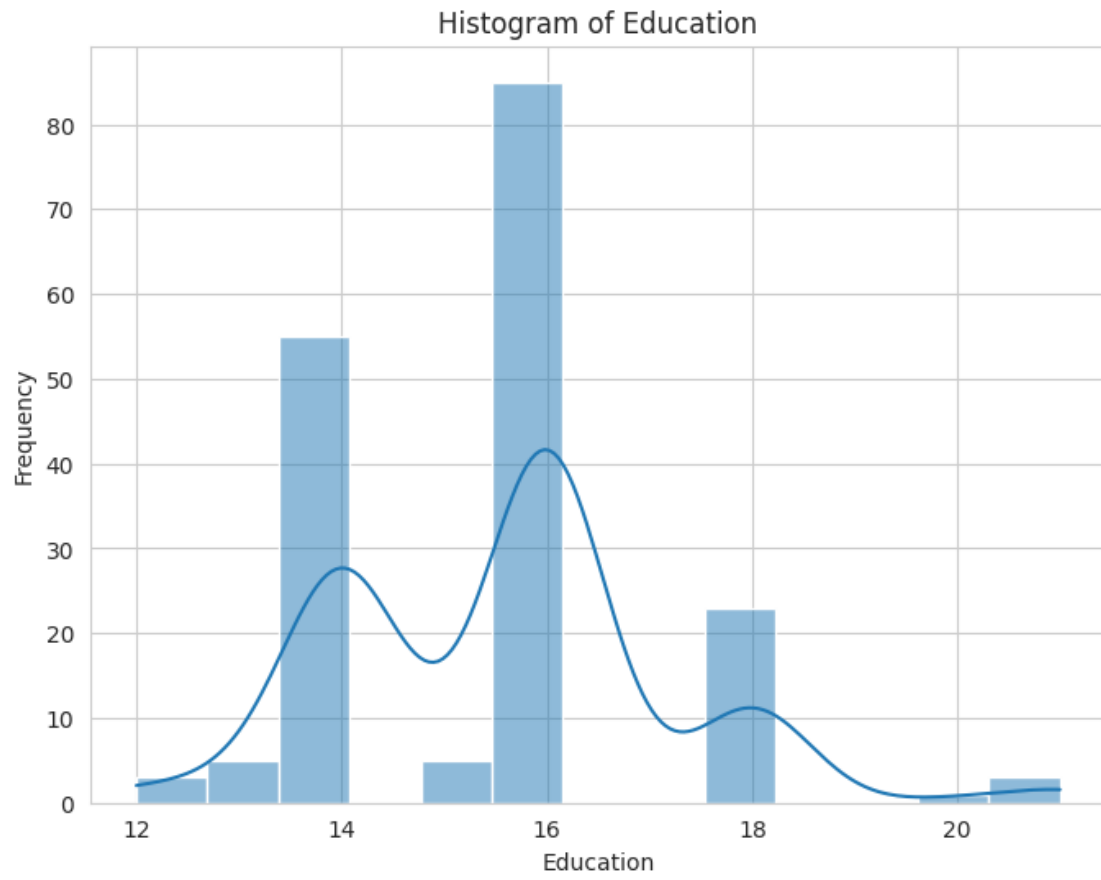
```
[ ]: plt.hist(['Income'], bins=20)
plt.title('Income Distribution')
plt.xlabel('Income')
plt.ylabel('Frequency')
plt.show()
```

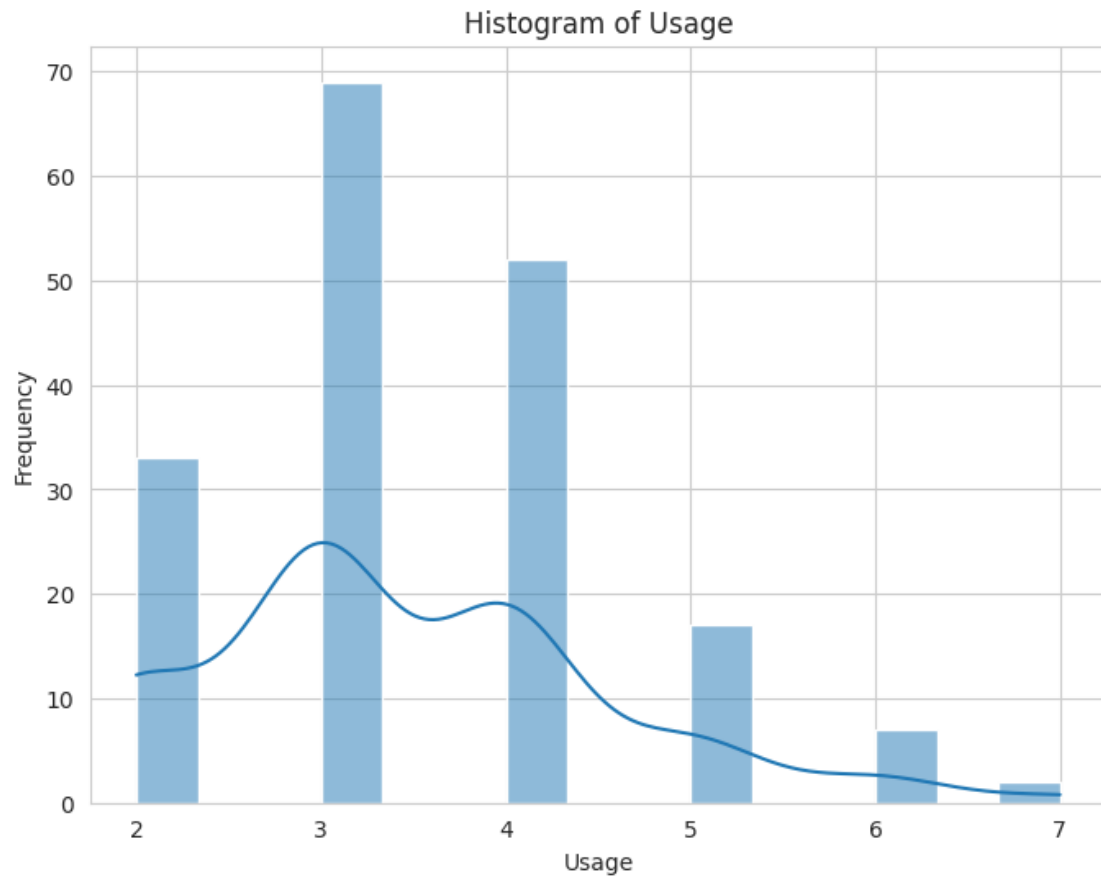


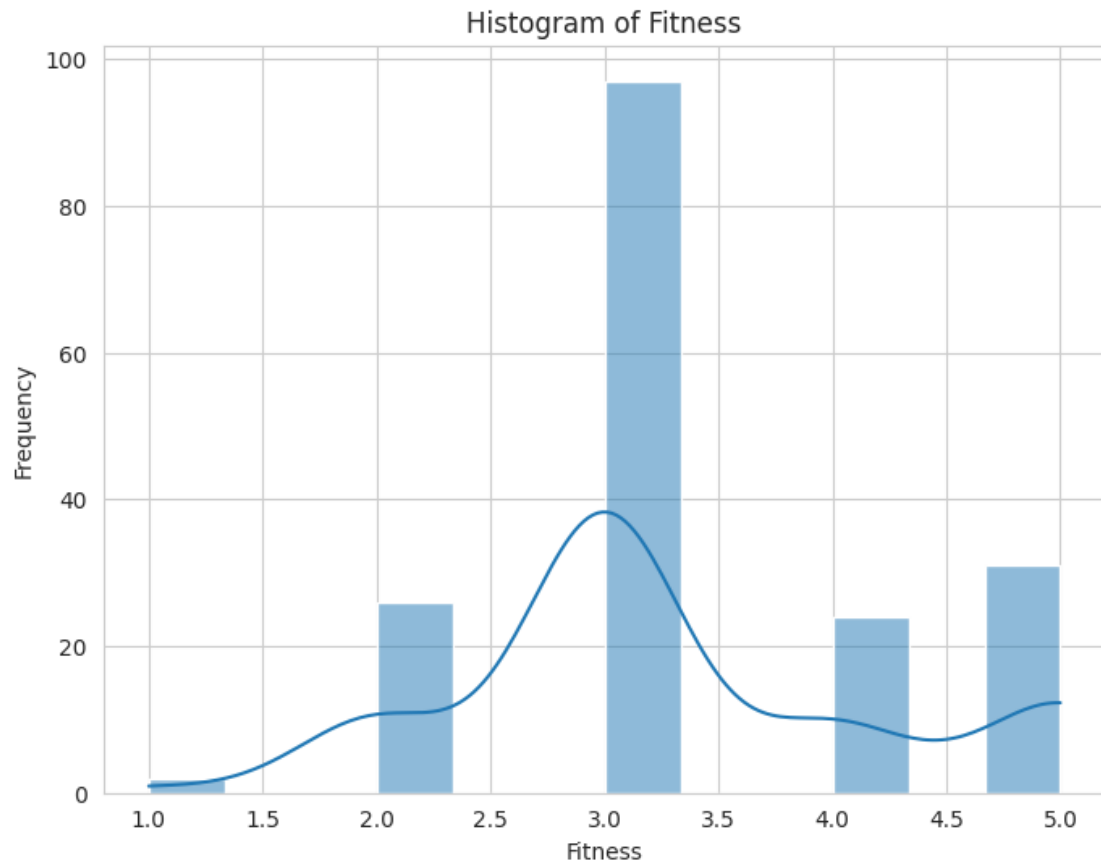
```
[ ]: numerical_columns = df.select_dtypes(include=['int64'])

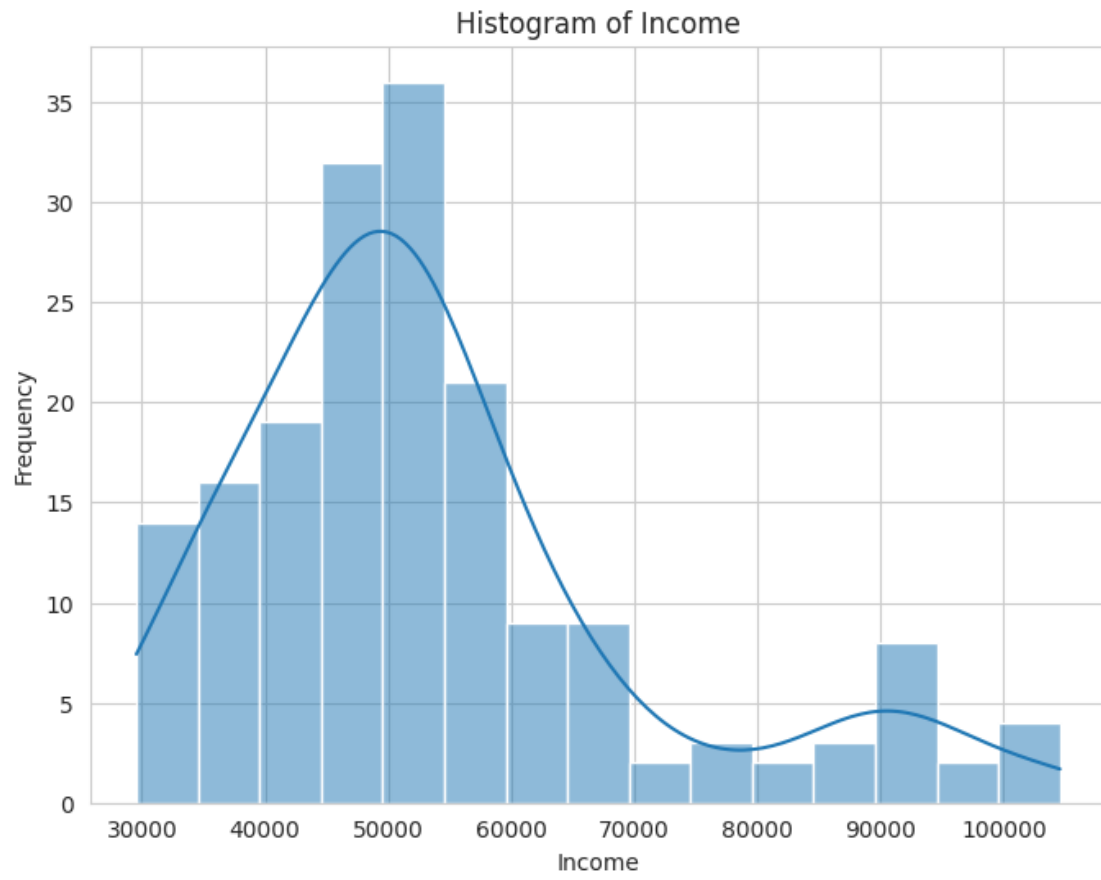
# Plot histograms for each numeric column
for col in numerical_columns.columns:
    plt.figure(figsize=(8, 6))
    sns.histplot(df[col], kde=True)
    plt.title(f'Histogram of {col}')
    plt.xlabel(col)
    plt.ylabel('Frequency')
    plt.show()
```

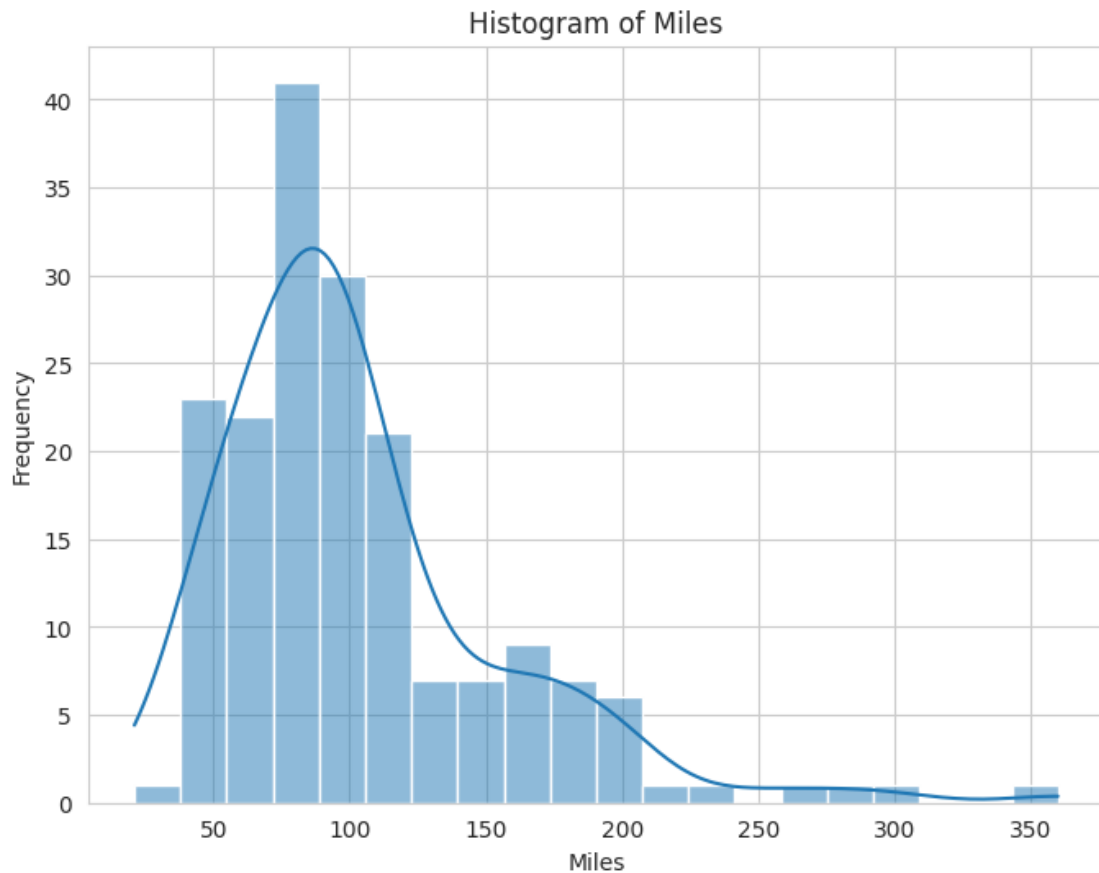






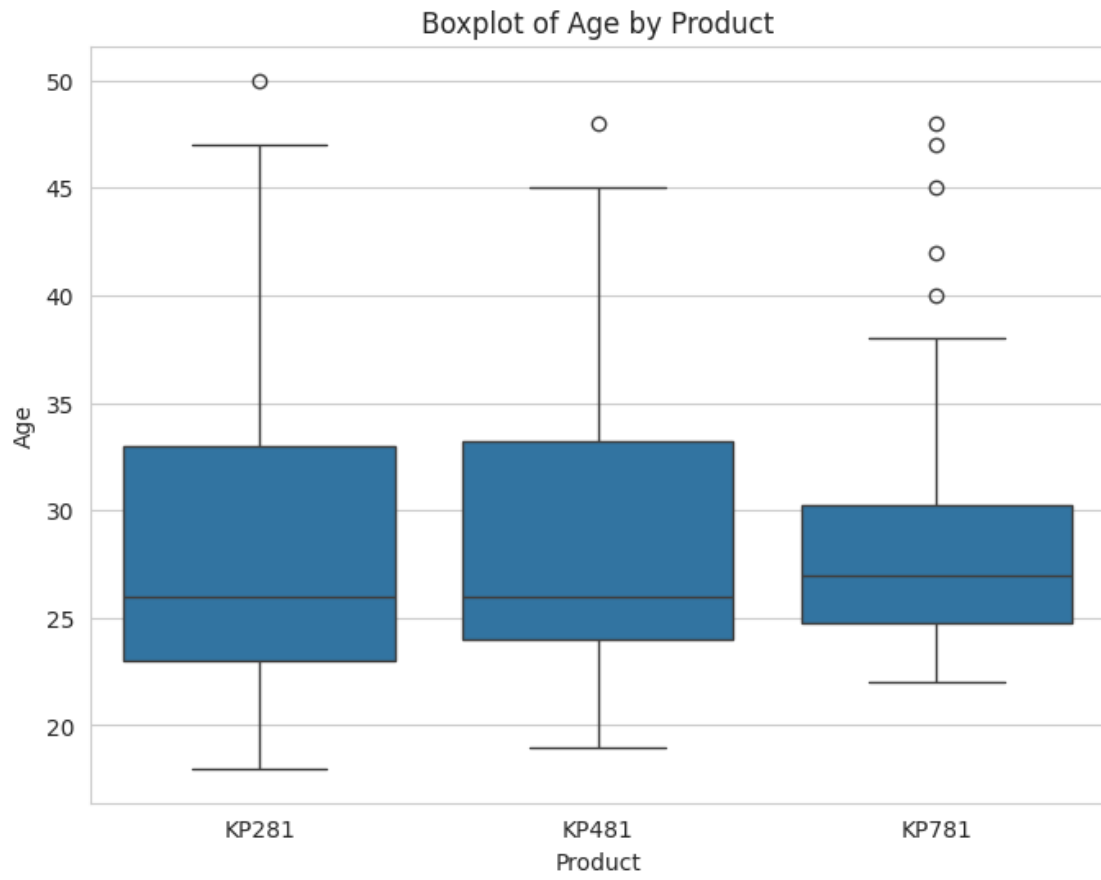


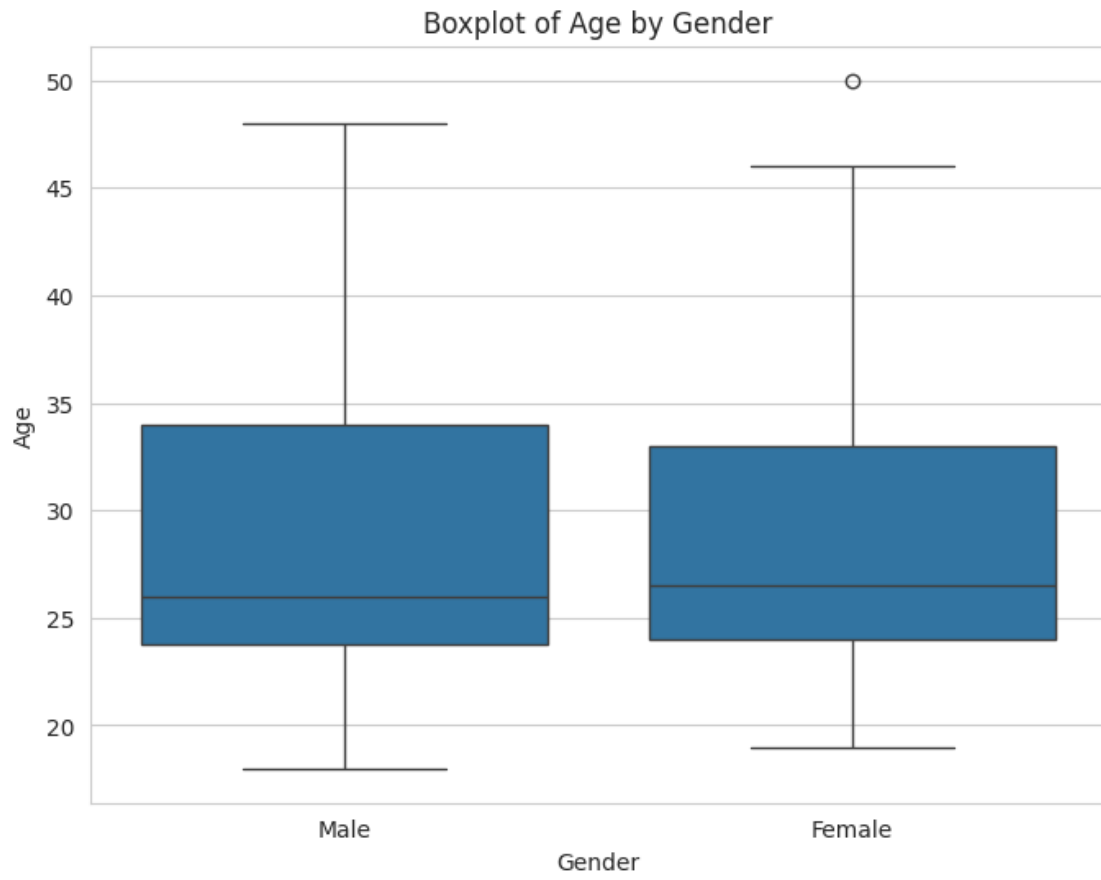


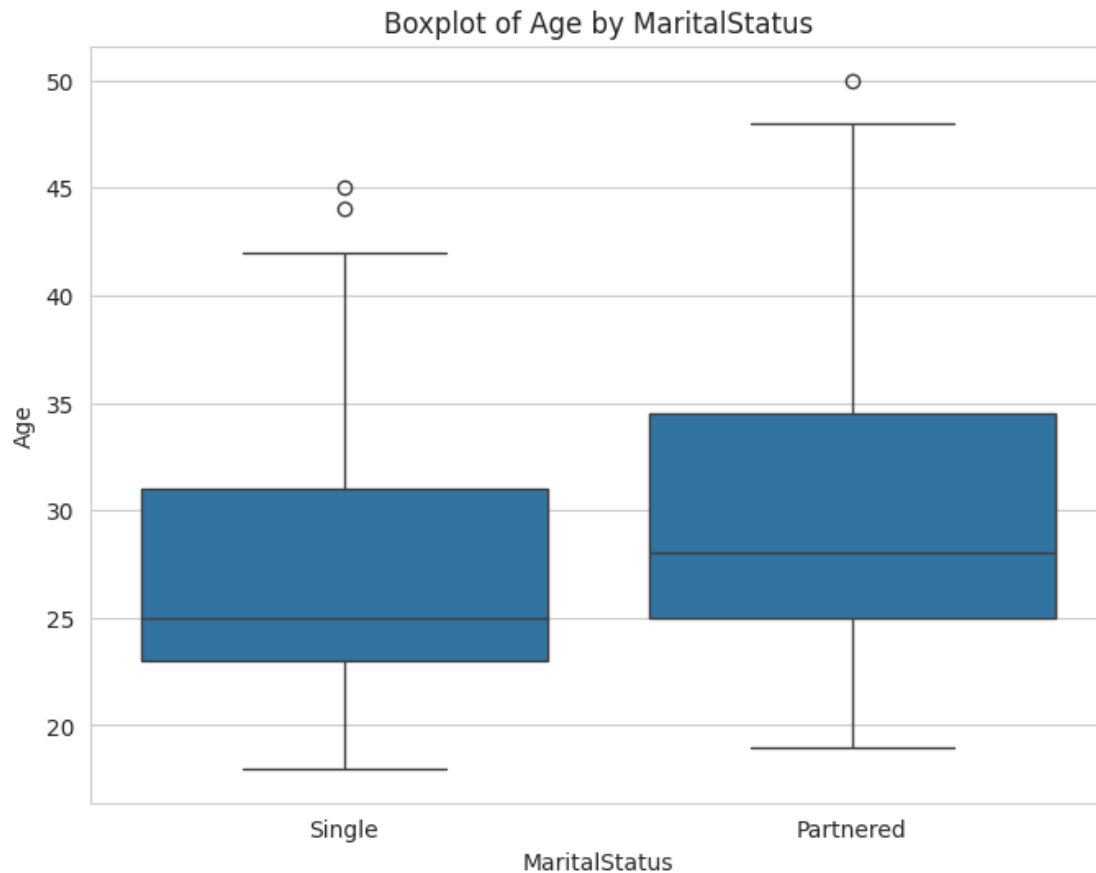


```
[ ]: # Select categorical columns
categorical_columns = df.select_dtypes(include=['object']).columns

for column in categorical_columns:
    plt.figure(figsize=(8, 6))
    sns.boxplot(x=column, y='Age', data=df)
    plt.title(f'Boxplot of Age by {column}')
    plt.xlabel(column)
    plt.ylabel('Age')
    plt.show()
```

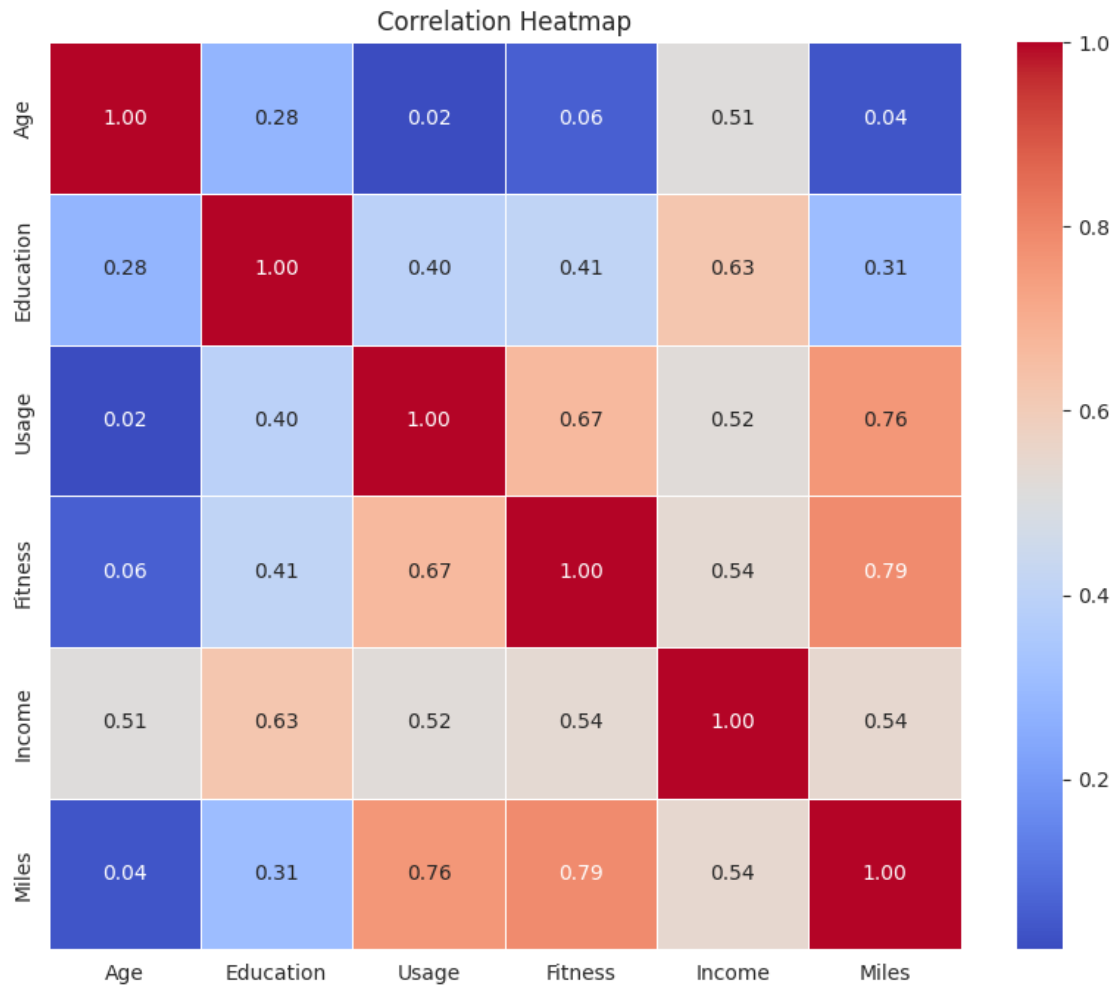




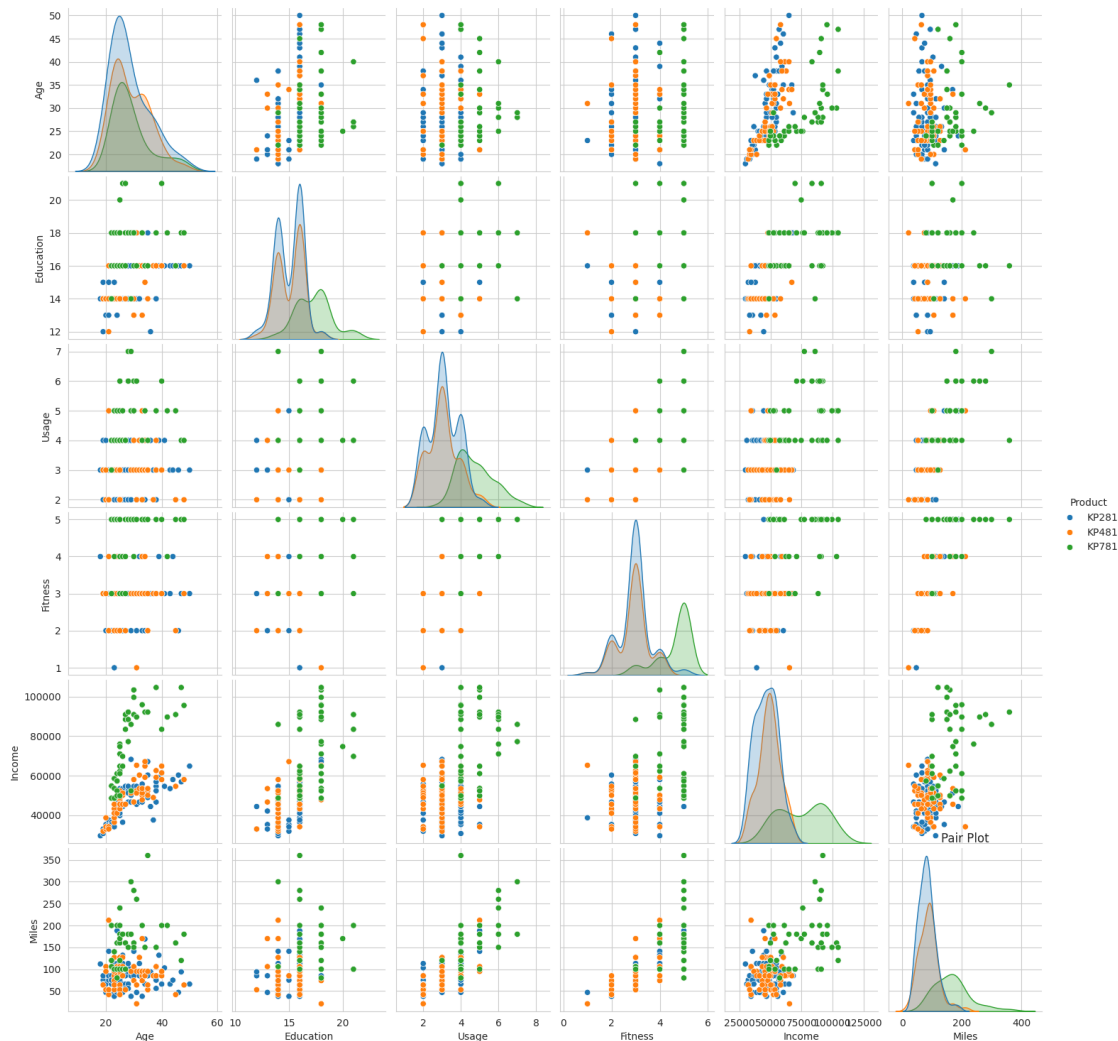


```
[ ]: # Calculate the correlation matrix
numeric_data = df.select_dtypes(include='number')
correlation_matrix = numeric_data.corr()

# Plot the heatmap
plt.figure(figsize=(10, 8))
sns.heatmap(correlation_matrix, annot=True, cmap="coolwarm", fmt=".2f",
            linewidths=0.5)
plt.title("Correlation Heatmap")
plt.show()
```



```
[ ]: # Pair plot
sns.pairplot(df, hue="Product")
plt.title("Pair Plot")
plt.show()
```



```
[ ]: # Create a crosstab to calculate the counts of each product purchased
product_counts = pd.crosstab(index=df["Product"], columns="% Share")

# Calculate the marginal probability (percentage) of each product purchased
marginal_probability = product_counts / product_counts.sum() * 100

print("Marginal Probability of Purchasing Each Product:")

print(marginal_probability)
```

```
Marginal Probability of Purchasing Each Product:
col_0      % Share
Product
KP281      44.444444
KP481      33.333333
```


KP781 22.222222

```
[ ]: # Count the total number of male customers
total_male_customers = len(df[df['Gender'] == 'Male'])

# Count the number of male customers who bought a KP781 treadmill
male_kp781_customers = len(df[(df['Gender'] == 'Male') & (df['Product'] == 'KP781')])

# Calculate the probability
probability_male_kp781 = male_kp781_customers / total_male_customers

print("Probability of a male customer buying a KP781 treadmill:", probability_male_kp781)
```

Probability of a male customer buying a KP781 treadmill: 0.3173076923076923

```
[ ]: # Calculate conditional probability of Product Purchased given Gender is Male

conditional_probability_male = df[df['Gender'] == 'Male']['Product'].
    value_counts() / len(df[df['Gender'] == 'Male'])
conditional_probability_male
```

```
[ ]: Product
KP281      0.384615
KP781      0.317308
KP481      0.298077
Name: count, dtype: float64
```

```
[ ]: # Calculate conditional probability of Product Purchased given Gender is Female

conditional_probability_female = df[df['Gender'] == 'Female']['Product'].
    value_counts() / len(df[df['Gender'] == 'Female'])
conditional_probability_female
```

```
[ ]: Product
KP281      0.526316
KP481      0.381579
KP781      0.092105
Name: count, dtype: float64
```

```
[ ]: #Conditional Probability of Product Purchased given Marital Status is Single:

conditional_probability_single = df[df['MaritalStatus'] == 'Single']['Product'].
    value_counts() / len(df[df['MaritalStatus'] == 'Single'])
conditional_probability_single
```

```
[ ]: Product
      KP281    0.438356
      KP481    0.328767
      KP781    0.232877
      Name: count, dtype: float64
```

```
[ ]: #Conditional Probability of Fitness Rating being 5 given Income is above
      ↪$60,000:
```

```
conditional_probability_fitness_5_given_high_income = df[df['Income'] >
      ↪60000]['Fitness'].value_counts() / len(df[df['Income'] > 60000])
conditional_probability_fitness_5_given_high_income
```

```
[ ]: Fitness
      5    0.476190
      3    0.333333
      4    0.142857
      2    0.023810
      1    0.023810
      Name: count, dtype: float64
```

```
[ ]: # The likelihood of a customer being under 30 years old
```

```
conditional_probability_age_under_30 = df['Age'].value_counts(normalize=True).
      ↪loc[:29].sum()
conditional_probability_age_under_30
```

```
[ ]: 0.8055555555555555
```

```
[ ]: # Calculate the probability of customer being under 30 years old
probability_condition = df['Age'].value_counts(normalize=True).loc[:29].sum()
```

```
# Calculate the probability of each product given the condition
```

```
conditional_probabilities = {}
```

```
for product in df['Product'].unique():
```

```
    probability_product_given_condition = df[df['Age'] <= 29]['Product'].
    ↪value_counts(normalize=True)[product]
```

```
    # Calculate the conditional probability for each product
```

```
    conditional_probability = probability_product_given_condition /
    ↪probability_condition
```

```
    conditional_probabilities[product] = conditional_probability
```

```
# Printing conditional probabilities for all products
```

```
for product, probability in conditional_probabilities.items():
```

```
print(f"Conditional probability of buying {product} for customers under 30_
↳years old: {probability}")
```

Conditional probability of buying KP281 for customers under 30 years old:
0.5822398535245652
Conditional probability of buying KP481 for customers under 30 years old:
0.3625267012511444
Conditional probability of buying KP781 for customers under 30 years old:
0.29661275556911815

```
[ ]: # Construct contingency tables for each product
contingency_tables = {}

for product in df['Product'].unique():
    product_df = df[df['Product'] == product]
    contingency_table = pd.crosstab(product_df['Gender'],
↳product_df['MaritalStatus'])
    contingency_tables[product] = contingency_table

# Display contingency tables
for product, table in contingency_tables.items():
    print(f"\nContingency Table for {product}:")
    print(table)

# Compute marginal probabilities
marginal_probabilities = {}

for product, table in contingency_tables.items():
    marginal_probabilities[product] = table / table.values.sum()

# Display marginal probabilities
for product, probabilities in marginal_probabilities.items():
    print(f"\nMarginal Probabilities for {product}:")
    print(probabilities)

# Compute conditional probabilities
conditional_probabilities = {}

for product, table in contingency_tables.items():
    conditional_probabilities[product] = table.div(table.sum(axis=1), axis=0)

# Display conditional probabilities
for product, probabilities in conditional_probabilities.items():
    print(f"\nConditional Probabilities for {product}:")
    print(probabilities)
```

Contingency Table for KP281:

MaritalStatus	Partnered	Single
Gender		
Female	27	13
Male	21	19

Contingency Table for KP481:

MaritalStatus	Partnered	Single
Gender		
Female	15	14
Male	21	10

Contingency Table for KP781:

MaritalStatus	Partnered	Single
Gender		
Female	4	3
Male	19	14

Marginal Probabilities for KP281:

MaritalStatus	Partnered	Single
Gender		
Female	0.3375	0.1625
Male	0.2625	0.2375

Marginal Probabilities for KP481:

MaritalStatus	Partnered	Single
Gender		
Female	0.25	0.233333
Male	0.35	0.166667

Marginal Probabilities for KP781:

MaritalStatus	Partnered	Single
Gender		
Female	0.100	0.075
Male	0.475	0.350

Conditional Probabilities for KP281:

MaritalStatus	Partnered	Single
Gender		
Female	0.675	0.325
Male	0.525	0.475

Conditional Probabilities for KP481:

MaritalStatus	Partnered	Single
Gender		
Female	0.517241	0.482759
Male	0.677419	0.322581

Conditional Probabilities for KP781:

MaritalStatus	Partnered	Single
Gender		
Female	0.571429	0.428571
Male	0.575758	0.424242

INSIGHTS

KP281 Treadmill:

- There are more partnered females (27) than single females (13) who purchased this treadmill, indicating that partnered females are more likely to buy this entry-level product.
- The marginal probability of partnered females purchasing KP281 is higher (0.3375) compared to single females (0.1625), suggesting that partnered females are the primary customers for this treadmill.
- The conditional probability of partnered females purchasing KP281 (0.675) is higher than single females (0.325), reinforcing that partnered females are more inclined towards this product compared to single females.

KP481 Treadmill:

- Both partnered and single males show a higher count of purchases compared to females for this mid-level treadmill.
- The marginal probability of males purchasing KP481 is higher (0.35 for partnered and 0.1667 for single) compared to females (0.25 for partnered and 0.2333 for single), indicating that males are the primary customers for this treadmill.
- The conditional probabilities suggest that both partnered and single males are more likely to purchase KP481 compared to females.

KP781 Treadmill:

- There is a notable difference in the number of purchases between partnered males (19) and single males (14), indicating that both demographics are interested in this advanced-level treadmill.
- The marginal probability of males purchasing KP781 is significantly higher (0.475 for partnered and 0.350 for single) compared to females (0.100 for partnered and 0.075 for single), suggesting that males are the dominant customers for this treadmill.
- The conditional probabilities for males purchasing KP781 are quite similar regardless of marital status, indicating that males are equally likely to purchase this treadmill regardless of their relationship status.

```
[ ]: education_treadmill_contingency = pd.crosstab(df['Education'], df['Product'])

# Print the contingency table
print("Contingency Table for Education Level vs. Treadmill Product Purchased:")
print(education_treadmill_contingency)

# Compute marginal probabilities
```

```

marginal_prob_education = education_treadmill_contingency.
    ↪div(education_treadmill_contingency.sum(axis=1), axis=0)
marginal_prob_treadmill = education_treadmill_contingency.
    ↪div(education_treadmill_contingency.sum(axis=0), axis=1)

# Compute conditional probabilities
conditional_prob_education_given_product = education_treadmill_contingency.
    ↪div(education_treadmill_contingency.sum(axis=1), axis=0)
conditional_prob_product_given_education = education_treadmill_contingency.
    ↪div(education_treadmill_contingency.sum(axis=0), axis=1)

# Print the contingency table
print("Contingency Table for Education Level vs. Treadmill Product Purchased:")
print(education_treadmill_contingency)
print()

# Print the marginal probabilities
print("Marginal Probabilities for Education Level:")
print(marginal_prob_education)
print()

print("Marginal Probabilities for Treadmill Product Purchased:")
print(marginal_prob_treadmill)
print()

# Print the conditional probabilities
print("Conditional Probabilities for Education Level given Treadmill Product_
    ↪Purchased:")
print(conditional_prob_education_given_product)
print()

print("Conditional Probabilities for Treadmill Product Purchased given_
    ↪Education Level:")
print(conditional_prob_product_given_education)

```

Contingency Table for Education Level vs. Treadmill Product Purchased:

Product	KP281	KP481	KP781
Education			
12	2	1	0
13	3	2	0
14	30	23	2
15	4	1	0
16	39	31	15
18	2	2	19
20	0	0	1
21	0	0	3

Contingency Table for Education Level vs. Treadmill Product Purchased:

Product	KP281	KP481	KP781
Education			
12	2	1	0
13	3	2	0
14	30	23	2
15	4	1	0
16	39	31	15
18	2	2	19
20	0	0	1
21	0	0	3

Marginal Probabilities for Education Level:

Product	KP281	KP481	KP781
Education			
12	0.666667	0.333333	0.000000
13	0.600000	0.400000	0.000000
14	0.545455	0.418182	0.036364
15	0.800000	0.200000	0.000000
16	0.458824	0.364706	0.176471
18	0.086957	0.086957	0.826087
20	0.000000	0.000000	1.000000
21	0.000000	0.000000	1.000000

Marginal Probabilities for Treadmill Product Purchased:

Product	KP281	KP481	KP781
Education			
12	0.0250	0.016667	0.000
13	0.0375	0.033333	0.000
14	0.3750	0.383333	0.050
15	0.0500	0.016667	0.000
16	0.4875	0.516667	0.375
18	0.0250	0.033333	0.475
20	0.0000	0.000000	0.025
21	0.0000	0.000000	0.075

Conditional Probabilities for Education Level given Treadmill Product Purchased:

Product	KP281	KP481	KP781
Education			
12	0.666667	0.333333	0.000000
13	0.600000	0.400000	0.000000
14	0.545455	0.418182	0.036364
15	0.800000	0.200000	0.000000
16	0.458824	0.364706	0.176471
18	0.086957	0.086957	0.826087
20	0.000000	0.000000	1.000000
21	0.000000	0.000000	1.000000

Conditional Probabilities for Treadmill Product Purchased given Education Level:

Product	KP281	KP481	KP781
Education			
12	0.0250	0.016667	0.000
13	0.0375	0.033333	0.000
14	0.3750	0.383333	0.050
15	0.0500	0.016667	0.000
16	0.4875	0.516667	0.375
18	0.0250	0.033333	0.475
20	0.0000	0.000000	0.025
21	0.0000	0.000000	0.075

INSIGHTS:

- Education level seems to have some influence on the choice of treadmill product, particularly for customers with an education level of 18, who show a strong preference for KP781.
- For customers with an education level of 16, there is a relatively even distribution across all treadmill products, suggesting that factors other than education level might play a role in their purchasing decision.
- The marginal and conditional probabilities provide evidence for targeting marketing strategies towards specific education demographics. For instance, advertising campaigns targeting customers with an education level of 18 could focus more on the features and benefits of KP781, while campaigns targeting customers with an education level of 16 could highlight the unique selling points of each treadmill product to appeal to their diverse preferences.

```
[ ]: # Define the income slabs
income_slabs = {
    'Low': (0, 30000),
    'Medium': (30001, 60000),
    'High': (60001, float('inf'))
}

# Create a new column for income category
def categorize_income(income):
    for category, (lower, upper) in income_slabs.items():
        if lower <= income <= upper:
            return category
    return None

df['Income_Category'] = df['Income'].apply(categorize_income)

[ ]: income_treadmill_contingency = pd.crosstab(df['Income_Category'], df['Product'])

# Compute marginal probabilities
marginal_prob_income = income_treadmill_contingency.
    ↪div(income_treadmill_contingency.sum(axis=1), axis=0)
marginal_prob_treadmill = income_treadmill_contingency.
    ↪div(income_treadmill_contingency.sum(axis=0), axis=1)
```



```

# Compute conditional probabilities
conditional_prob_income_given_product = income_treadmill_contingency.
    ↳div(income_treadmill_contingency.sum(axis=1), axis=0)
conditional_prob_product_given_income = income_treadmill_contingency.
    ↳div(income_treadmill_contingency.sum(axis=0), axis=1)

# Print the contingency table
print("Contingency Table for Income Level vs. Treadmill Product Purchased:")
print(income_treadmill_contingency)
print()

# Print the marginal probabilities
print("Marginal Probabilities for Income Level:")
print(marginal_prob_income)
print()

print("Marginal Probabilities for Treadmill Product Purchased:")
print(marginal_prob_treadmill)
print()

# Print the conditional probabilities
print("Conditional Probabilities for Income Level given Treadmill Product_
    ↳Purchased:")
print(conditional_prob_income_given_product)
print()

print("Conditional Probabilities for Treadmill Product Purchased given Income_
    ↳Level:")
print(conditional_prob_product_given_income)

```

Contingency Table for Income Level vs. Treadmill Product Purchased:

Product	KP281	KP481	KP781
Income_Category			
High	6	7	29
Low	1	0	0
Medium	73	53	11

Marginal Probabilities for Income Level:

Product	KP281	KP481	KP781
Income_Category			
High	0.142857	0.166667	0.690476
Low	1.000000	0.000000	0.000000
Medium	0.532847	0.386861	0.080292

Marginal Probabilities for Treadmill Product Purchased:

Product	KP281	KP481	KP781
---------	-------	-------	-------

Income_Category			
High	0.0750	0.116667	0.725
Low	0.0125	0.000000	0.000
Medium	0.9125	0.883333	0.275

Conditional Probabilities for Income Level given Treadmill Product Purchased:

Product	KP281	KP481	KP781
Income_Category			
High	0.142857	0.166667	0.690476
Low	1.000000	0.000000	0.000000
Medium	0.532847	0.386861	0.080292

Conditional Probabilities for Treadmill Product Purchased given Income Level:

Product	KP281	KP481	KP781
Income_Category			
High	0.0750	0.116667	0.725
Low	0.0125	0.000000	0.000
Medium	0.9125	0.883333	0.275

INSIGHTS :

- The evidence shows that among customers with high income, the majority (approximately 69.05%) prefer to purchase KP781.
- The medium-income category, KP281 and KP481 are the dominant choices, constituting approximately 53.28% and 38.69% of purchases, respectively. This indicates that these treadmill models may offer features or pricing that resonate well with customers in this income bracket.
- The data indicates that customers with low income tend not to favour any of the offered treadmill products. This could suggest that the pricing of these products might be prohibitive for individuals in this income segment, leading to minimal adoption.

RECOMMENDATIONS

- **Target High-Income Individuals for KP781:** Focus marketing efforts on high-income demographics, highlighting the premium features and benefits of KP781 to resonate with their preferences for high-end products.
- **Diversify Marketing Strategies for Medium-Income Segment:** Since KP281 and KP481 are preferred choices among medium-income customers, tailor marketing campaigns to highlight the unique selling points of each treadmill model, catering to the specific needs and preferences of this demographic.
- **Explore Pricing Strategies for Low-Income Segment:** Investigate pricing options or promotional strategies to make treadmill products more accessible to customers with low income, potentially introducing entry-level models or flexible payment plans to encourage adoption within this segment.
- **Customized Education-Level Targeting:** Develop targeted advertising campaigns that align with the preferences of different education demographics. For instance, emphasize the advanced features of KP781 to customers with higher education levels through suitable channels, while showcasing the versatility of all treadmill models to appeal to a broader audience.

- **Enhance Product Visibility for Targeted Demographics:** Increase visibility and accessibility of specific treadmill models based on demographic preferences. For example, prioritize showcasing KP281 to partnered females in marketing materials and retail displays to capitalize on their preference for entry-level products, while ensuring ample availability of KP781 for male customers who show a strong interest in advanced features.