

Equivalent & of FA

~~Any set of
Non Equivalent~~

→ Create sets of both FA
make sure (F, NF) → should not
be created

→ If all sets are processed that
means Equivalence is
true

F, NF_X F, P₂, NF, NP₂

Consider the following two DFAs M and M' over $\{0, 1\}$ given in Fig. 5.23.
Determine whether M and M' are equivalent.

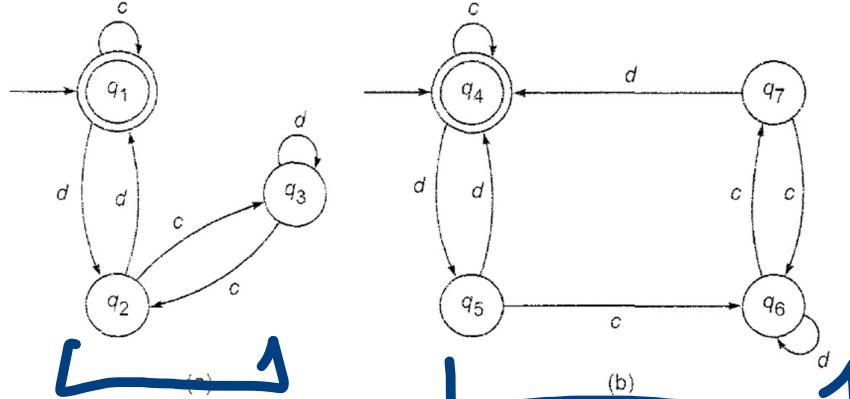


Fig. 5.23 (a) Automaton M and (b) automaton M' .

A B

→ No combination
vs best
every combination
LF or NF, NF

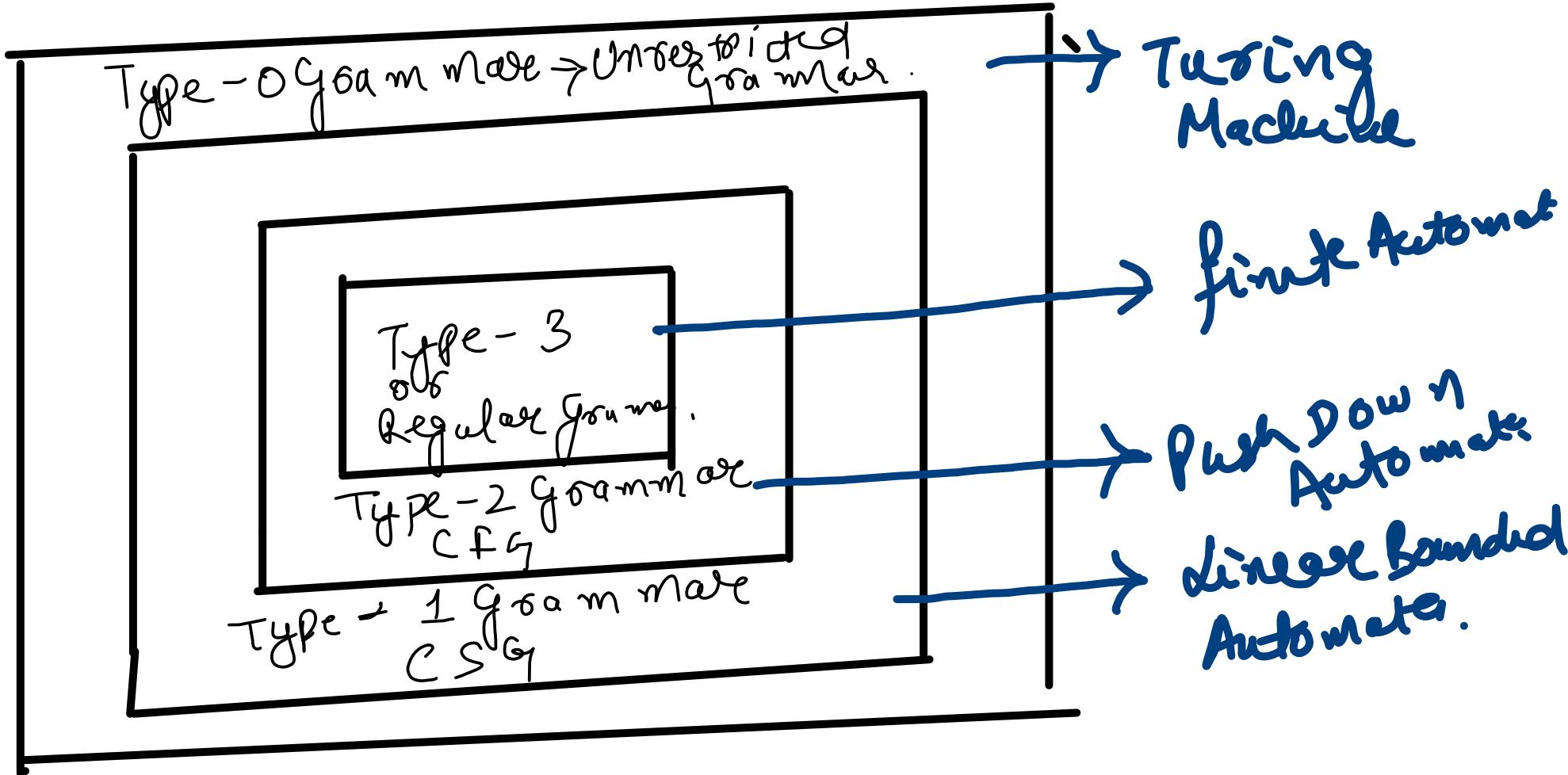
			d
		$\rightarrow q_1, q_2 \{q_1, q_4\}$	$\{q_2, q_5\} \{q_2, q_5\}$
	q_2, q_5	q_3, q_6	$\{q_1, q_4\}$
q_3, q_6	$q_2, q_7 \{q_2, q_7\}$	q_3, q_6	$\{q_3, q_6\}$
q_2, q_7	q_3, q_6	$\{q_3, q_6\}$	$\{q_1, q_4\}$

Both A & B are Equivalent

Tuples of Grammar

- Non Terminals → Variables \Rightarrow Generating Rules
- Terminals + S/P symbols
- Production Rule \Rightarrow Generating strings
- Starting symbol \Rightarrow NonTerminal
 \rightarrow starting of a string

Chomsky Hierarchy of Grammar

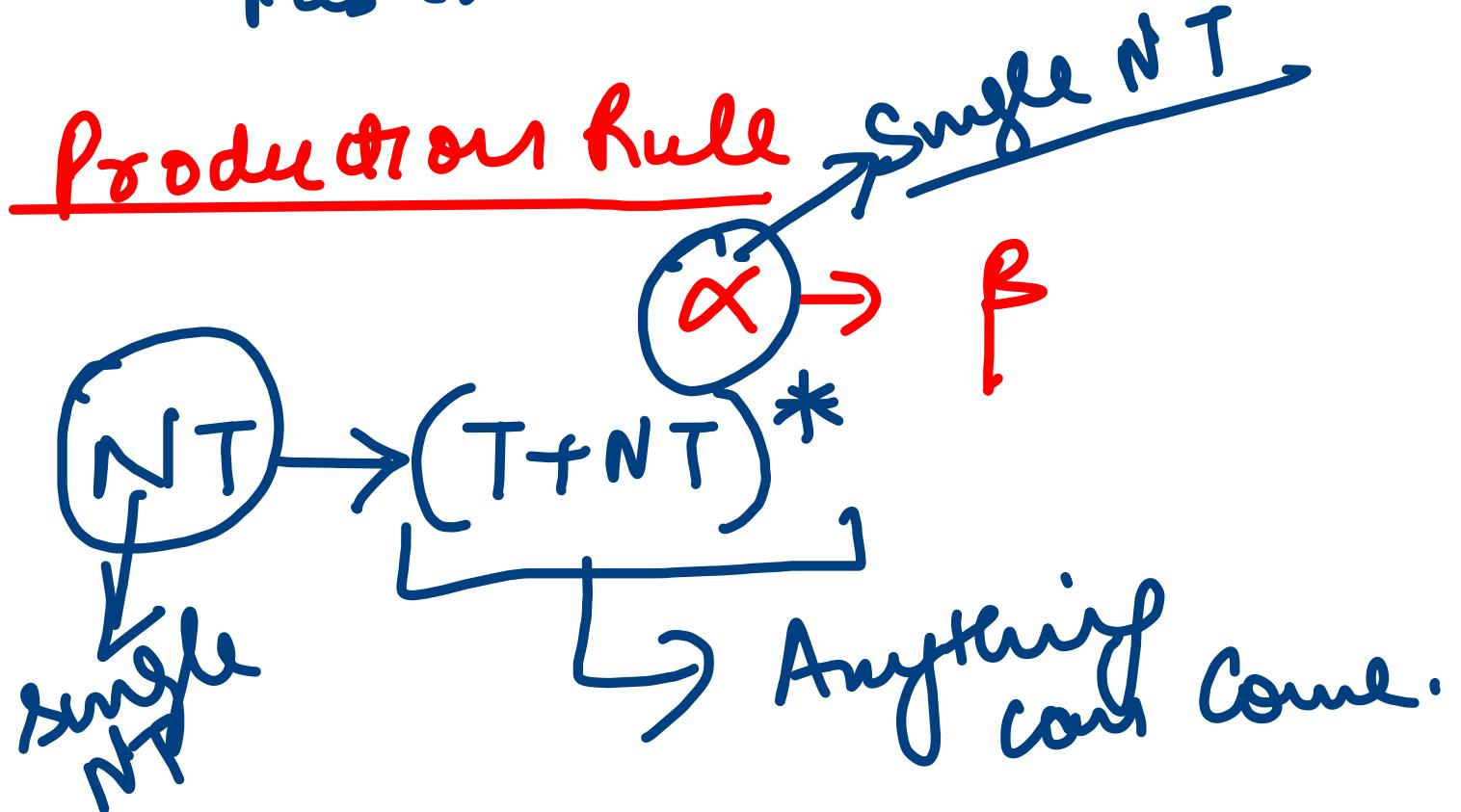


1) Type-3 Grammar (Regular Grammar)

(Finite Automata)

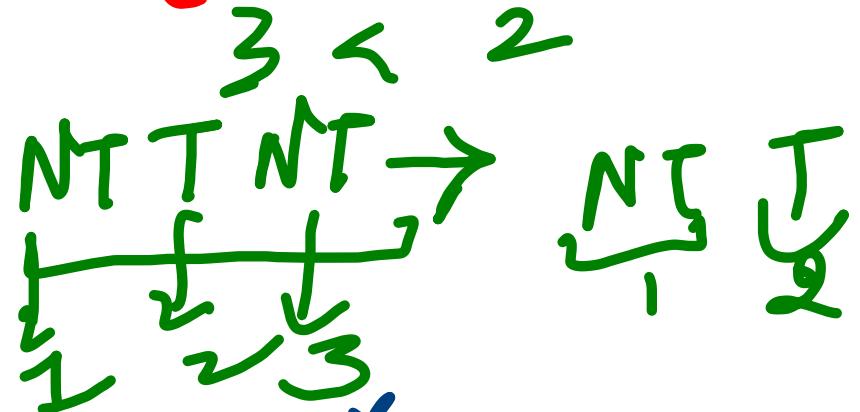
- Most Restricted Part of Grammar
- Production Rules
-
- 1) $NT \rightarrow \underbrace{NT}_{\text{single}} \underbrace{NT}_{\text{single}}$
- 2) $NT \rightarrow \underbrace{NT}_{\text{single}} \underbrace{T}_{\text{single}}$
- $S \rightarrow a \sum \text{ or } S \rightarrow \sum a$

2) Context free Grammar or (Type -2)
Pushdown Automata.



3) Type-1 Grammar or Context Sensitive Grammar \rightarrow ~~direct~~ Bounded Automaton

Restriction (PR)



$$\alpha \Rightarrow \beta$$

$$\alpha \Rightarrow (T + NT)^* \underbrace{NT}_{N}, (T + NC)^*$$

$$\beta = (T + NT)^* \text{ (Anything on } R - R^c S\text{)}$$

Restriction: Depth of $\alpha \leq \beta$. β depth of

4) Unstacked Grammar (Type -0 grammar)

Turing Machine

Producing rule

$$\alpha \rightarrow \beta$$

α must contain a single

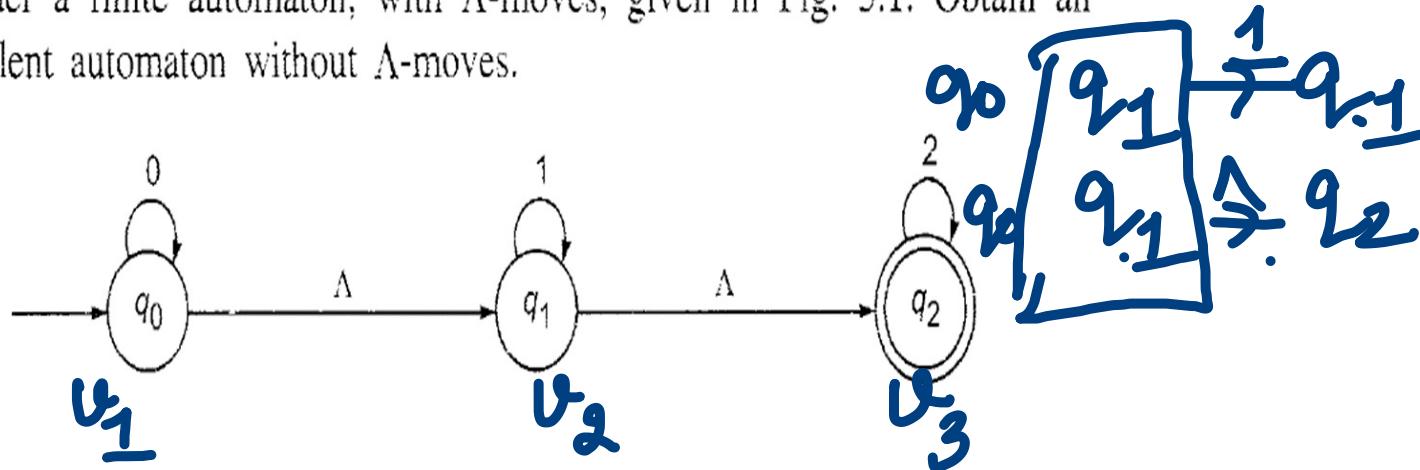
NT

$$\boxed{\alpha \neq \lambda}$$

$\alpha \Rightarrow (T + NT)^*$  $(T + NT)^*$
 $\beta = (T + NT)^*$ single NT must be present

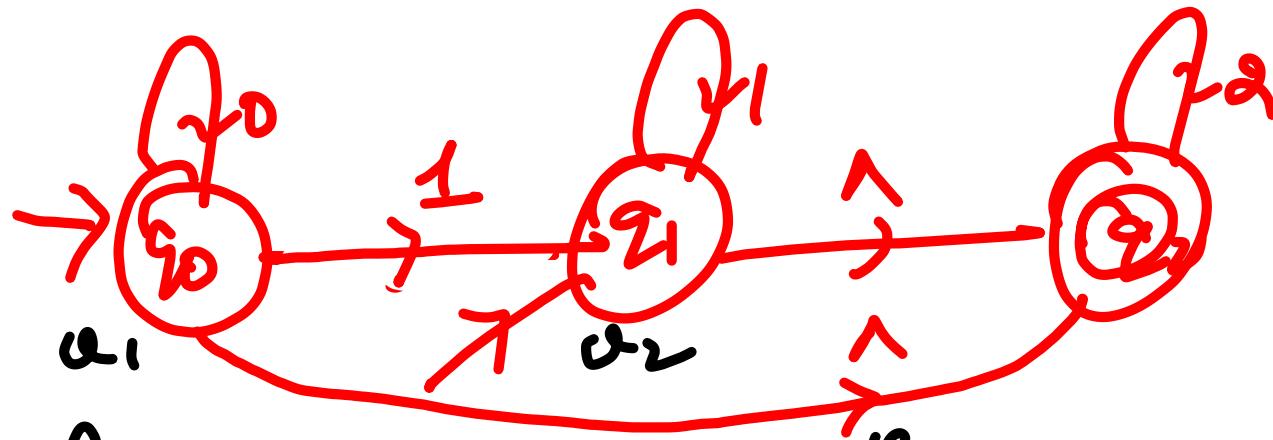
$v_1 \xrightarrow{\lambda} v_2 \quad v_2 \xrightarrow{\lambda} v_3$

Consider a finite automaton, with λ -moves, given in Fig. 5.1. Obtain an equivalent automaton without λ -moves.



4 steps

- Remove the null move ($v_1 \xrightarrow{\lambda} v_2$)
- Copy what v_2 is doing (outgoing transitions of q_2) to v_1 .
- If q_1 is initial state, make v_2 initial
- If v_2 " final state " v_1 final.



1. Remove Null move

2. Copy what q_2 is doing to q_1

$$q_p(1) = q_1$$

$$q_p(\wedge) = q_2$$

$$\begin{array}{c} u_1 q_0 \left| \begin{array}{c} q_1(1) \\ q_1(\wedge) \end{array} \right. \rightarrow q_1 \\ q_0 \left| \begin{array}{c} q_1(1) \\ q_1(\wedge) \end{array} \right. \rightarrow q_2 \end{array}$$

3 - If u_1 is initial, make u_2 also initial
4. If u_2 is final, then u_1 — final.



$$q_1 \xrightarrow{u_1} q_2 \quad \checkmark$$

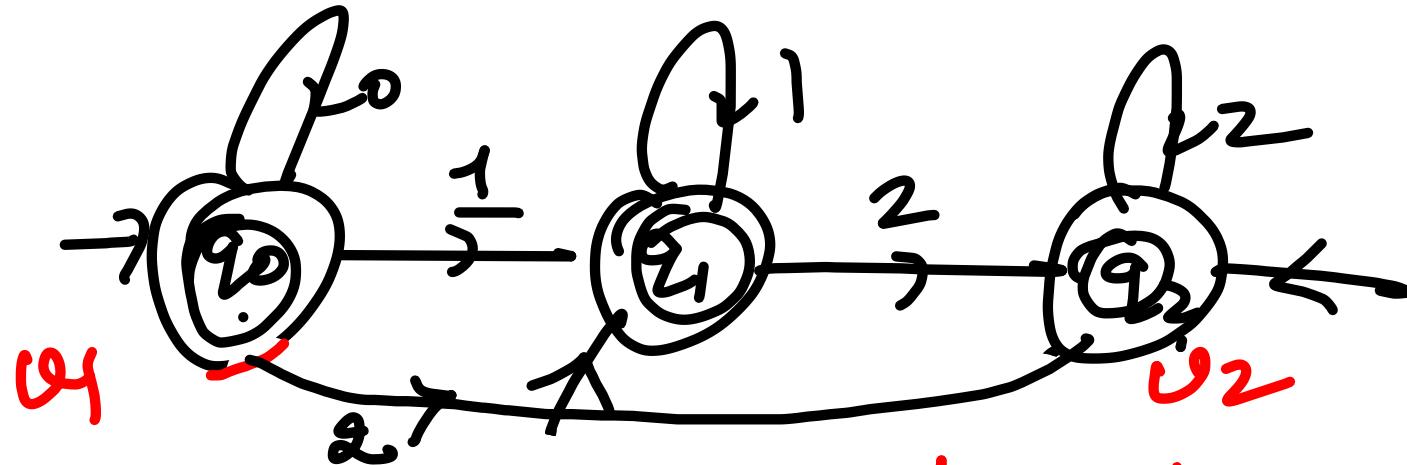
$$\frac{q_1}{q_0} \xrightarrow{u_1} q_2$$

Copy what u_1 is doing to u_1

$$q_1 \boxed{q_2(2)} = q_2$$

$$q_1(2) = q_2$$

If q_1 is initial,
 ~~q_2 — final~~, q_2 becomes initial
 ~~q_1 — final~~.

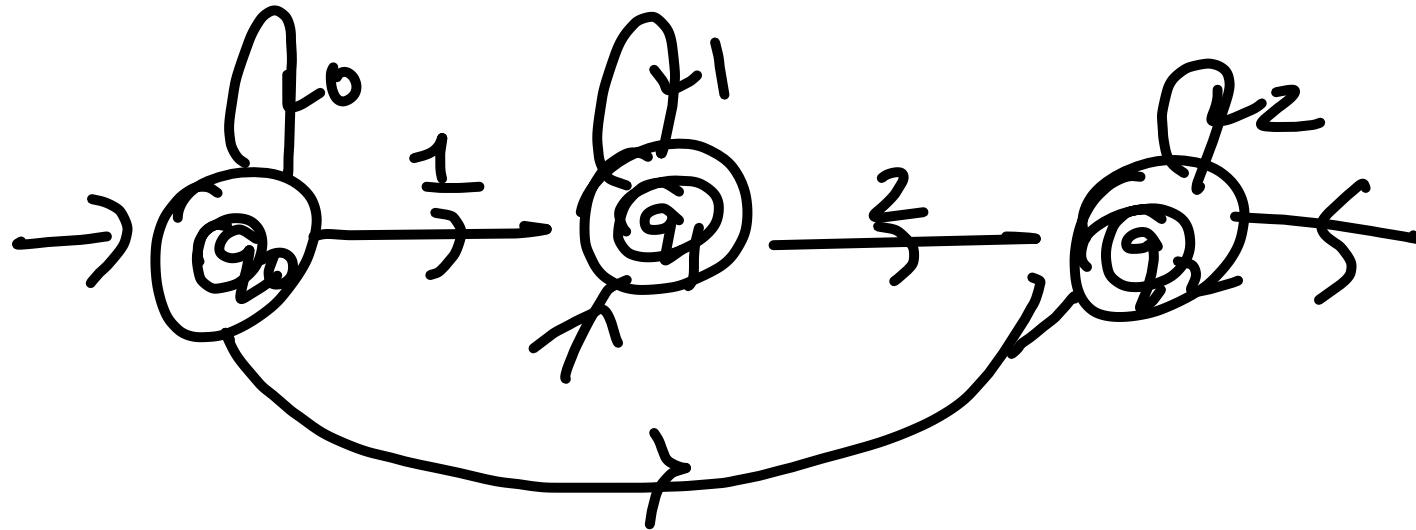


Copy what ϑ_2 is doing to ϑ_1

$$\vartheta_2(2) = \vartheta_2$$

$$\vartheta_0(2) = \vartheta_2$$

If ϑ_2 is final make ϑ_0 free



q

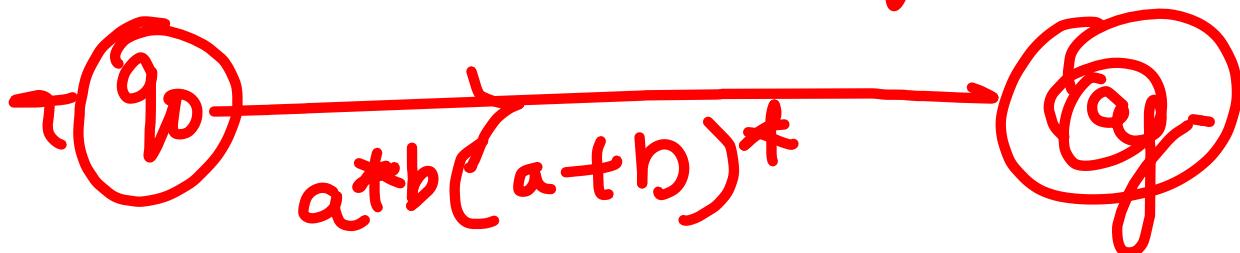
NFA

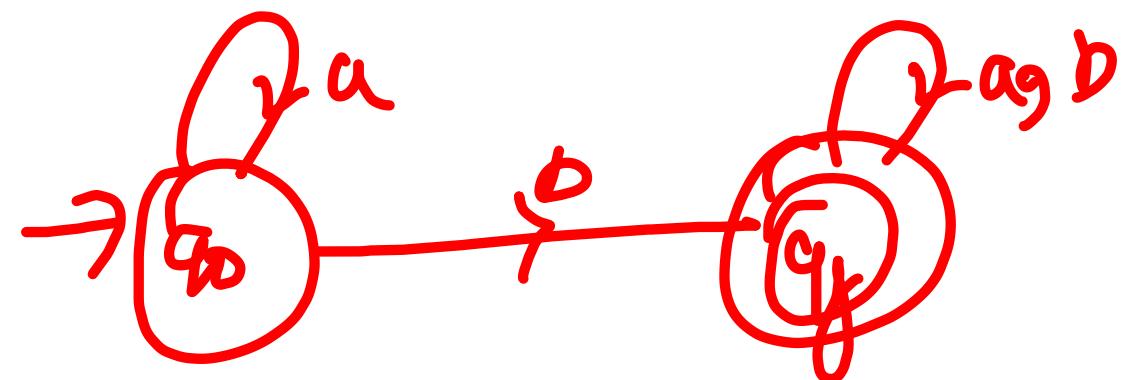
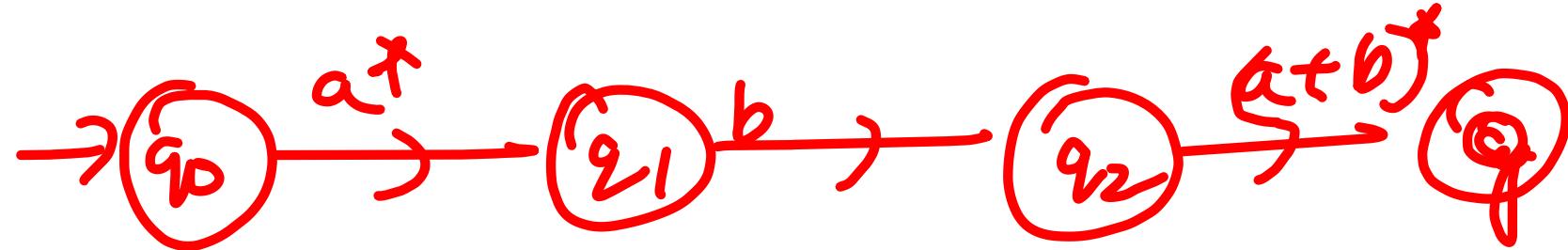
3 initial states

Regular Expressions to Regular Grammar

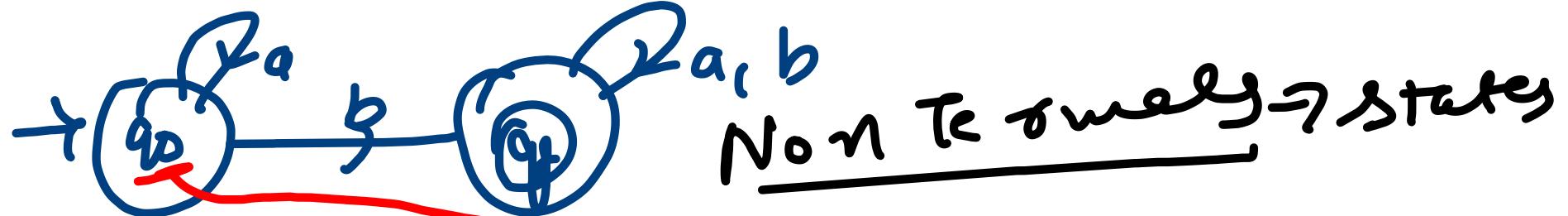
$$RE = a^* b(a+b)^*$$

Convert R-E to finite Automata



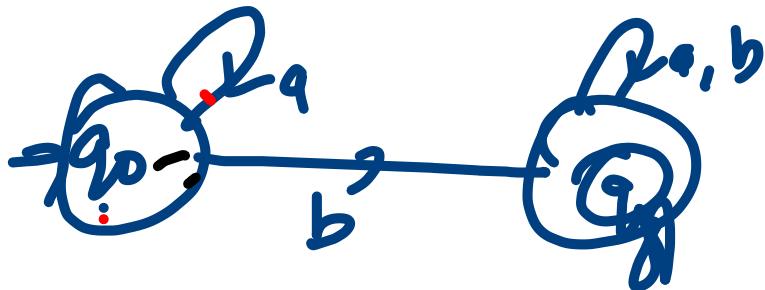


\Rightarrow finite
Automata



R-G has 4 types

- 1) NonTerminals (variables) $\rightarrow \{q_0, q_f\} \rightarrow$ states
- 2) Terminals (I/P symbols) $\rightarrow a, b$
- 3) Production Rules
- 4) Starting Symbol \rightarrow Non Terminal
(Starting State) $\rightarrow q_0$ (Starting symbol)



Production Rules

Transitive
Rules

$$Q_0 \xrightarrow{NT \rightarrow T} Q_0$$

Terminating
Rules

$$\begin{aligned} Q_0 &\xrightarrow{a} Q_0 \\ Q_0 &\xrightarrow{b} Q_f \\ Q_f &\xrightarrow{a} Q_f \\ Q_f &\xrightarrow{b} Q_f \end{aligned}$$

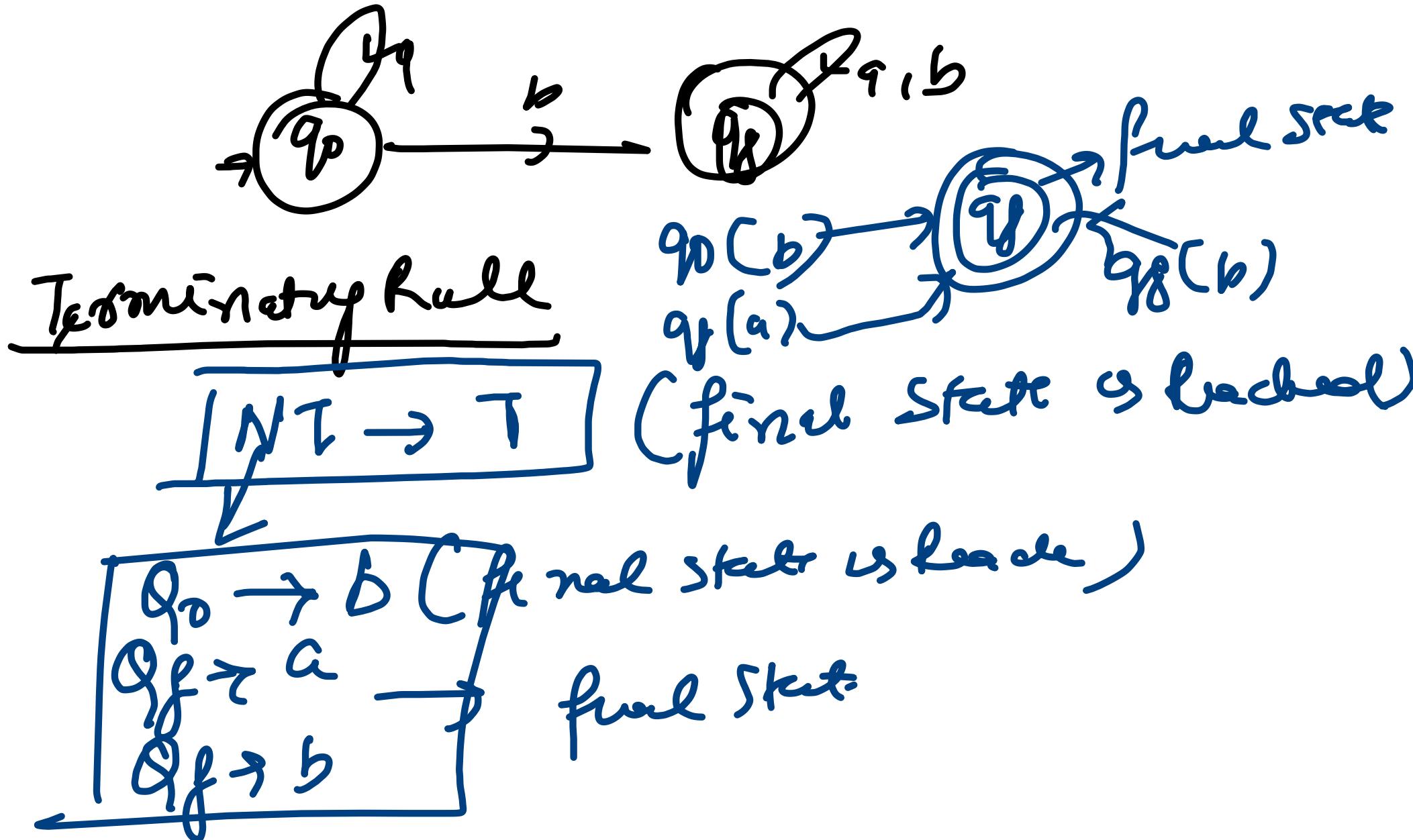
$NT \rightarrow T \quad NT$

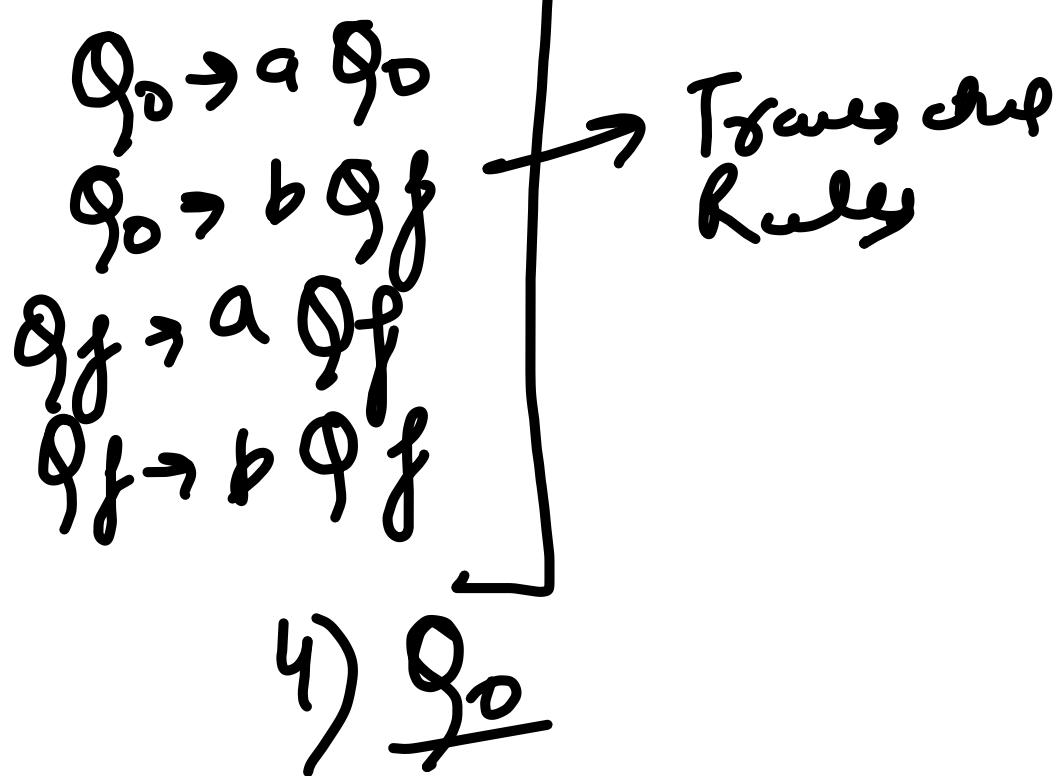
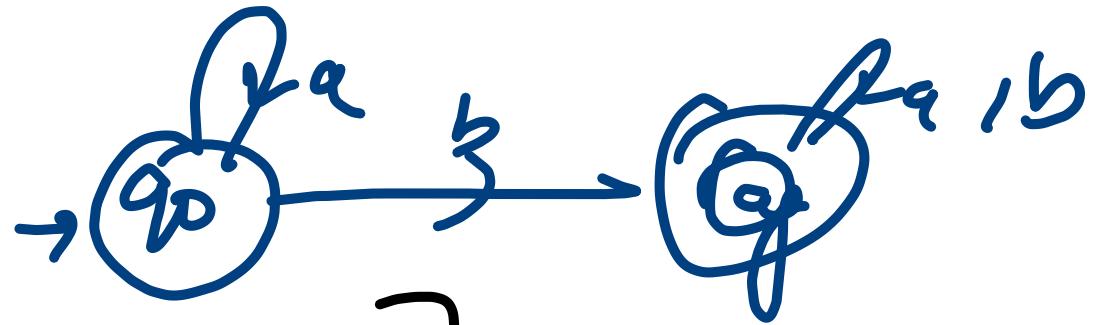
$$\begin{aligned} q_0(a) &\rightarrow q_0 \\ q_0(b) &\rightarrow q_f \\ q_f(a) &\rightarrow q_f \\ q_f(b) &\rightarrow q_f \end{aligned}$$

$\xrightarrow{T \quad NT}$

$$\begin{aligned} q_0 &\xrightarrow{b} Q_f \\ Q_f &\xrightarrow{a} Q_f \end{aligned}$$

\xrightarrow{NT}





- 1) q_0, q_f
- 2) a, b .
- 3)

Terminating rules

- $q_0 \rightarrow B$
- $q_f \rightarrow a$
- $q_f \rightarrow b$
- final state reached