VISVESVARAYA TECHNOLOGICAL UNIVERSITY

"JnanaSangama", Belgaum -590014, Karnataka.

LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING

B.M.S. COLLEGE OF ENGINEERING
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Department of Computer Science and Engineering

CERTIFICATE

This is to certify that the Lab work entitled " Bio Inspired Systems (23CS5BSBIS)" carried out by **Shashidhar B M (1BM22CS257),** who is bonafide student of **B.M.S. College of Engineering.** It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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Github Link:

https://github.com/ShashidharM0118/BIS_Lab-1BM22CS257

<u>Program 1:</u> Genetic Algorithm for Optimization on Problems

Genetic Algorithms (GA) are inspired by the process of natural selection and genetics, where the fittest individuals are selected for reproduction to produce the next generation. GAs are widely used for solving optimization and search problems. Implement a Genetic Algorithm using Python to solve a basic optimization problem, such as finding the maximum value of a mathematical function.

<u>Implementation Steps:</u>

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the population size, mutation rate, crossover rate, and number of generations.
3. Create Initial Population: Generate an initial population of potential solutions.
4. Evaluate Fitness: Evaluate the fitness of each individual in the population.
5. Selection: Select individuals based on their fitness to reproduce.
6. Crossover: Perform crossover between selected individuals to produce offspring.
7. Mutation: Apply mutation to the offspring to maintain genetic diversity.
8. Iteration: Repeat the evaluation, selection, crossover, and mutation processes for a fixed number of generations or until convergence criteria are met.
9. Output the Best Solution: Track and output the best solution found during the generations.

Algorithm:

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Genetic Algorithm:

* Pseudo code:

→ Initialize population of size 'pop-size' with random values in range [x-range-low, x-range-high]

→ For Generation in range (generation):

a. Evaluate fitness of each individual:

for each individual x in population:

fitness(x-i) = x-i**2

b. select 2 parents based on fitness value (roulette wheel selection):

total fitness = sum of all fitness values for each individual x-i in population

probability (x-i) = fitness (x-i) / total-fitness

select 2 parents (p1, p2) based on probability.

c. perform crossover with probability 'crossover-rate':

If random-number < crossover-rate:

alpha = random value between 0 and 1

offspring1 = alpha * p1 + (1-alpha) * p2

else:

offspring1 = p1

offspring = p2

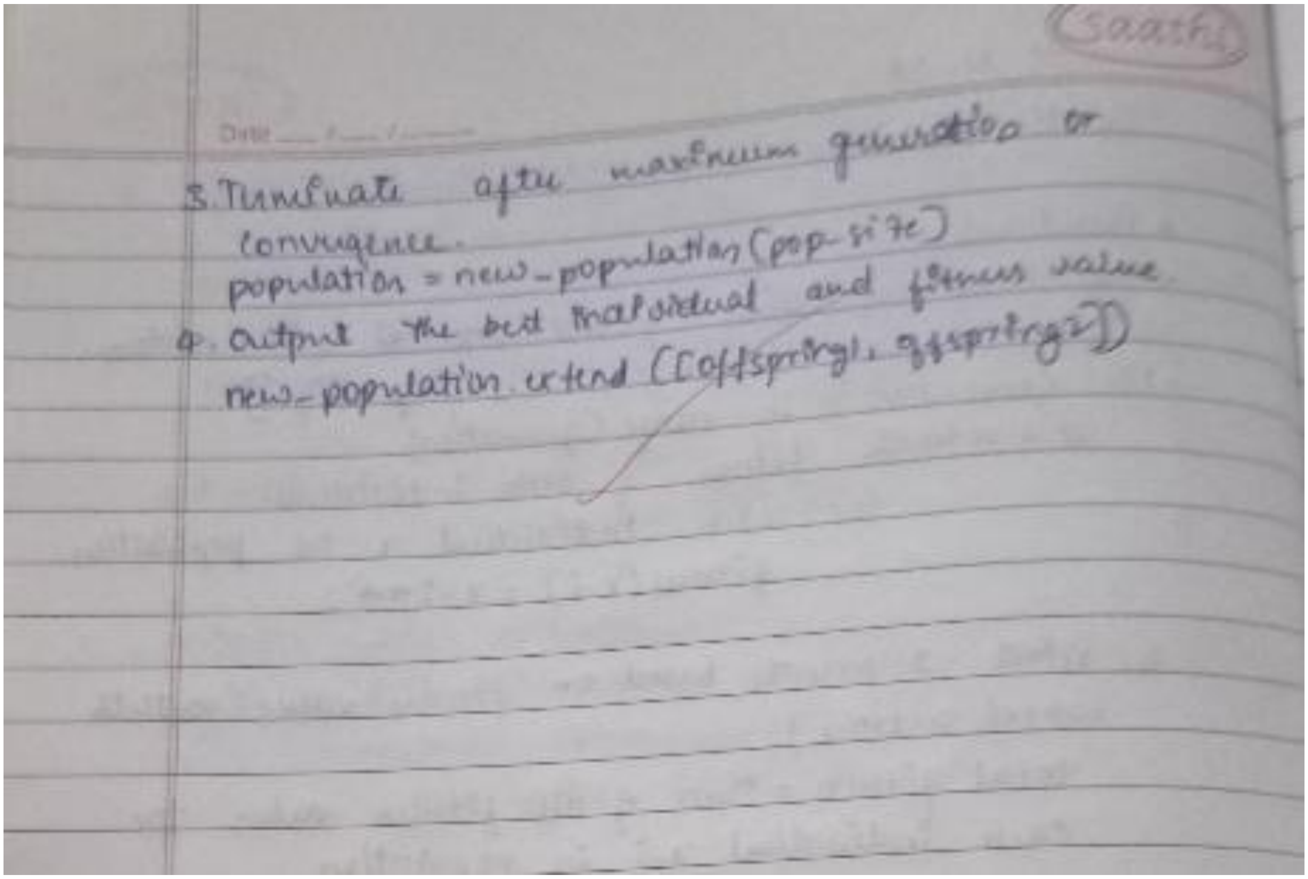
d. Apply mutation with probability 'mutation-rate'

For each offspring:

If random-number < mutation-rate:

offspring = random value in range [x-range-low, x-range-high]

e. update population with new offspring



3. Terminate after maximum generation or convergence.
population = new_population(pop_size)
4. Output the best individual and fitness value
new_population.extend([offspring1, offspring2])

Code:

```
#lab-2: genetic
import numpy as np
import random

# Objective function to maximize
def objective_function(x):
    return x ** 2

# Initialize parameters
population_size = 100
num_generations = 50
mutation_rate = 0.1
crossover_rate = 0.7
range_min = -10
```

```
range_max = 10

# Create initial population
def initialize_population(size, min_val, max_val):
    return np.random.uniform(min_val, max_val, size)

# Evaluate fitness of the population
def evaluate_fitness(population):
    return np.array([objective_function(x) for x in population])

# Selection using roulette-wheel method
def selection(population, fitness):
    total_fitness = np.sum(fitness)
    probabilities = fitness / total_fitness
    return population[np.random.choice(range(len(population)), size=2, p=probabilities)]

# Crossover between two parents
def crossover(parent1, parent2):
    if random.random() < crossover_rate:
        return (parent1 + parent2) / 2  # Simple averaging for crossover
    return parent1  # No crossover

# Mutation of an individual
def mutate(individual):
    if random.random() < mutation_rate:
        return np.random.uniform(range_min, range_max)
    return individual

# Genetic Algorithm function
def genetic_algorithm():
    # Step 1: Initialize population
    population = initialize_population(population_size, range_min, range_max)

    for generation in range(num_generations):
        # Step 2: Evaluate fitness
        fitness = evaluate_fitness(population)

        # Track the best solution
        best_index = np.argmax(fitness)
        best_solution = population[best_index]
        best_fitness = fitness[best_index]

        # print(f"Generation {generation + 1}: Best Solution = {best_solution}, Fitness =
{best_fitness}")

        # Step 3: Create new population
        new_population = []
```

```
        for _ in range(population_size):
            # Select parents
            parent1, parent2 = selection(population, fitness)
            # Crossover to create offspring
            offspring = crossover(parent1, parent2)
            # Mutate offspring
            offspring = mutate(offspring)
            new_population.append(offspring)

        # Step 6: Replace old population with new population
        population = np.array(new_population)

    return best_solution, best_fitness

# Run the Genetic Algorithm
best_solution, best_fitness = genetic_algorithm()
print(f"Best Solution Found: {best_solution}, Fitness: {best_fitness}")
```

OUTPUT:

```
Best Solution Found: -9.290037411642935, Fitness: 86.30479510972536
```

Program 2: Particle Swarm Optimization for Function Optimization

Particle Swarm Optimization (PSO) is inspired by the social behavior of birds flocking or fish schooling. PSO is used to find optimal solutions by iteratively improving a candidate solution with regard to a given measure of quality. Implement the PSO algorithm using Python to optimize a mathematical function.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of particles, inertia weight, cognitive and social coefficients.
3. Initialize Particles: Generate an initial population of particles with random positions and velocities.
4. Evaluate Fitness: Evaluate the fitness of each particle based on the optimization function.
5. Update Velocities and Positions: Update the velocity and position of each particle based on its own best position and the global best position.
6. Iterate: Repeat the evaluation, updating, and position adjustment for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

Saathi

Date __/__/__

Particle Swarm Optimization

1) define problem function

$$f(x) = A.n + \sum_{i=1}^{n} \left[x_i^2 - A\cos(2\pi x_i) \right]$$

where $A = 10$, n = dimensionality of input x

x_i is the value of variable

2 ParticleSwarmOptimizer class is initialized with several key parameters that define optimization problem and behaviours of particle

attributes include num_particles, dimensions, iterations, inertia_weight, cognitive_coeff, global_best position, global best_value

3 Initialize_particle method creates and returns new particles of the swarm

(a) position initialization
self.bounds using np.random.uniform.

(b) velocity = np.random.uniform (-1, 1, self.dimensions)

(c) best position - starting position

(d) Best value - self.function(position)

4 personal Best update : If the particle fitness is better than previous,
update best value and position

Global best :
If particle fitness is better than global fitness then update global value and position

5) Define 2 functions ~~to~~ to update particles velocity and position

~~update velocity~~ :

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class Particle:
    def_init_(self, dim):
        self.position = np.random.uniform(-5.12, 5.12, dim)
        self.velocity = np.random.uniform(-1, 1, dim)

Evaluate Fitness:
    def evaluate_particles(particles)
        for particle in particles:
            fitness = rastrigin_function (particle, position)
        if fitness < particle.best fitness;
            particle.best_fitness = fitness
            particle.best_position = particle.position
                (copy())

update velocity and positions:

def update_particles(particles, global_best_position):
    for particle in particles:
take r_1 and r_2 as random positions.

Initialize particle.velocity using r_1, r_2
inertia_weigh

particle.position += particle.velocity

⇒ In Main loop:

initialize global best position and global fitness position as particles[0]'s best position and best fitness.

Iterate through num_iterations.
    call evaluate_particle (particles)

for every particle in particles
re initialize global best fitness and particle by current particle best fitness and position

call update-particle (particle, global-best-position)

Output:
Best Position: [-9.58601084 e-10 2.6 7937e-09]
Best Fitness: 0.0

Code:

```
#lab-3: pso
import numpy as np
import random

# Define the optimization problem (Rastrigin Function)
def rastrigin(x):
    A = 10
    return A * len(x) + sum([(xi**2 - A * np.cos(2 * np.pi * xi)) for xi in x])

# Particle Swarm Optimization (PSO) implementation
class Particle:
    def _init_(self, dimension, lower_bound, upper_bound):
        # Initialize the particle position and velocity randomly
        self.position = np.random.uniform(lower_bound, upper_bound, dimension)
        self.velocity = np.random.uniform(-1, 1, dimension)
        self.best_position = np.copy(self.position)
        self.best_value = rastrigin(self.position)

    def update_velocity(self, global_best_position, w, c1, c2):
        # Update the velocity of the particle
        r1 = np.random.rand(len(self.position))
        r2 = np.random.rand(len(self.position))

        # Inertia term
        inertia = w * self.velocity

        # Cognitive term (individual best)
        cognitive = c1 * r1 * (self.best_position - self.position)

        # Social term (global best)
        social = c2 * r2 * (global_best_position - self.position)

        # Update velocity
        self.velocity = inertia + cognitive + social

    def update_position(self, lower_bound, upper_bound):
        # Update the position of the particle
        self.position = self.position + self.velocity

        # Ensure the particle stays within the bounds
        self.position = np.clip(self.position, lower_bound, upper_bound)

    def evaluate(self):
        # Evaluate the fitness of the particle
        fitness = rastrigin(self.position)
```

```
        # Update the particle's best position if necessary
        if fitness < self.best_value:
            self.best_value = fitness
            self.best_position = np.copy(self.position)

def particle_swarm_optimization(dim, lower_bound, upper_bound, num_particles=30, max_iter=100,
w=0.5, c1=1.5, c2=1.5):
    # Initialize particles
    particles = [Particle(dim, lower_bound, upper_bound) for _ in range(num_particles)]

    # Initialize the global best position and value
    global_best_position = particles[0].best_position
    global_best_value = particles[0].best_value

    for i in range(max_iter):
        # Update each particle
        for particle in particles:
            particle.update_velocity(global_best_position, w, c1, c2)
            particle.update_position(lower_bound, upper_bound)
            particle.evaluate()

            # Update global best position if needed
            if particle.best_value < global_best_value:
                global_best_value = particle.best_value
                global_best_position = np.copy(particle.best_position)

        # Optionally print the progress
        if (i+1 ) % 10 == 0:
            print(f"Iteration {i+1 }/{max_iter} - Best Fitness: {global_best_value}")

    return global_best_position, global_best_value

# Set the parameters for the PSO algorithm
dim = 2                # Number of dimensions for the function
lower_bound = -5.12    # Lower bound of the search space
upper_bound = 5.12     # Upper bound of the search space
num_particles = 30     # Number of particles in the swarm
max_iter = 100         # Number of iterations

# Run the PSO
best_position, best_value = particle_swarm_optimization(dim, lower_bound, upper_bound,
num_particles, max_iter)

# Output the best solution found
print("\nBest Solution Found:")
print("Position:", best_position)
```

```
print("Fitness:", best_value)
```

OUTPUT:

```
Iteration 10/100 - Best Fitness: 1.1103296669969005
Iteration 20/100 - Best Fitness: 0.020031338560627887
Iteration 30/100 - Best Fitness: 2.788695226740856e-06
Iteration 40/100 - Best Fitness: 1.0778596895022474e-06
Iteration 50/100 - Best Fitness: 6.450946443692374e-10
Iteration 60/100 - Best Fitness: 2.0463630789890885e-11
Iteration 70/100 - Best Fitness: 1.0658141036401503e-14
Iteration 80/100 - Best Fitness: 0.0
Iteration 90/100 - Best Fitness: 0.0
Iteration 100/100 - Best Fitness: 0.0

Best Solution Found:
Position: [-1.63024230e-09  1.14735681e-09]
Fitness: 0.0
```

Program 3: Ant Colony Optimization for the Traveling Salesman Problem

The foraging behavior of ants has inspired the development of optimization algorithms that can solve complex problems such as the Traveling Salesman Problem (TSP). Ant Colony Optimization (ACO) simulates the way ants find the shortest path between food sources and their nest. Implement the ACO algorithm using Python to solve the TSP, where the objective is to find the shortest possible route that visits a list of cities and returns to the origin city.

Implementation Steps:

1. Define the Problem: Create a set of cities with their coordinates.
2. Initialize Parameters: Set the number of ants, the importance of pheromone (alpha), the importance of heuristic information (beta), the evaporation rate (rho), and the initial pheromone value.
3. Construct Solutions: Each ant constructs a solution by probabilistically choosing the next city based on pheromone trails and heuristic information.
4. Update Pheromones: After all ants have constructed their solutions, update the pheromone trails based on the quality of the solutions found.
5. Iterate: Repeat the construction and updating process for a fixed number of iterations or until convergence criteria are met.
6. Output the Best Solution: Keep track of and output the best solution found during the iterations.

Algorithm:

Date 14 / 11 / 2024

Ant Colony Optimization

a) Initialization:

consider parameter num_ants, num_iterations, alpha beta, rho, q.

Initialize pheromone matrix:

pheromone_matrix = np.one_like(dist_matrix)

Initialize distance matrix:

dist_matrix.

b) Ant Solution Generation

Select starting city: start_city = random.randint (0, num_cities-1)

Track visited city:

visited = [False]* num_cities and

visited[start_city] = True.

Select next city: calculate probability.

probabilities [city] = pheromone_matrix[current_city] [city]** alpha * (1 / dist_matrix [current city](city))** beta

c) Solution Evaluation

compute tour length:

tour_length = sum (dist_matrix[tour[i], tour[i+1]) for i in range (num_cities -1))

track best solution:

best_tour, best_length = min(ant_tours, key = lamba x: x['tour_length'])

return tour_length

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d) pheromone update :
phero mone_matrix *= (1-rho)

pheromone_matrix [ant ['tour'][i], ant ['tour'][i+1]] +=
q / ant ['tour_length']

e) Result Evaluation:
Best tour selection :
best_tour, best length = get_best_tour (ant_solution)
return best_tour, best length.

Terminate after num_iterations or when
best_tour no longer improves.

Input :
```
dist_matrix = np.array ([
        [0, 10, 12, 11],
        [10 , 0, 13, 15]
        [12, 13 , 0, 10]
        [11, 15, 10, 0 ]
    ])
```

Sample output :

Best tour : (0, 3, 2, 1)
Best tour length : 36

Code:

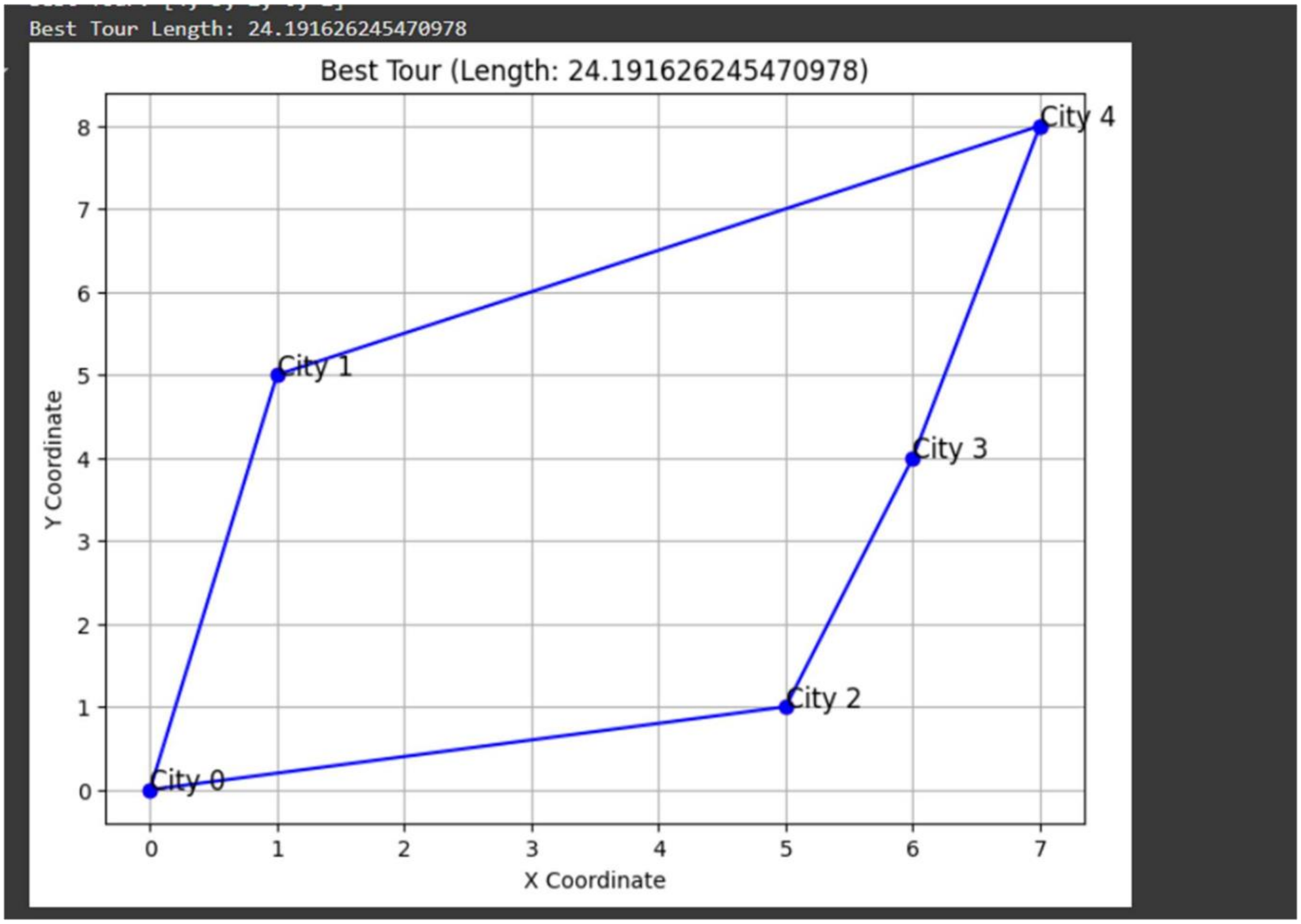
```
#ant colony
import numpy as np
import matplotlib.pyplot as plt

# 1. Define the Problem: Create a set of cities with their coordinates
cities = np.array([
    [0, 0],  # City 0
    [1, 5],  # City 1
    [5, 1],  # City 2
    [6, 4],  # City 3
    [7, 8],  # City 4
])

# Calculate the distance matrix between each pair of cities
def calculate_distances(cities):
    num_cities = len(cities)
    distances = np.zeros((num_cities, num_cities))

    for i in range(num_cities):
        for j in range(num_cities):
            distances[i][j] = np.linalg.norm(cities[i] - cities[j])

    return distances

distances = calculate_distances(cities)

# 2. Initialize Parameters
num_ants = 10
num_cities = len(cities)
alpha = 1.0  # Influence of pheromone
beta = 5.0   # Influence of heuristic (inverse distance)
rho = 0.5    # Evaporation rate
num_iterations = 30
initial_pheromone = 1.0

# Pheromone matrix initialization
pheromone = np.ones((num_cities, num_cities)) * initial_pheromone

# 3. Heuristic information (Inverse of distance)
def heuristic(distances):
    with np.errstate(divide='ignore'):  # Ignore division by zero
        return 1 / distances

eta = heuristic(distances)
```

```
# 4. Choose next city probabilistically based on pheromone and heuristic info
def choose_next_city(pheromone, eta, visited):
    probs = []
    for j in range(num_cities):
        if j not in visited:
            pheromone_ij = pheromone[visited[-1], j] ** alpha
            heuristic_ij = eta[visited[-1], j] ** beta
            probs.append(pheromone_ij * heuristic_ij)
        else:
            probs.append(0)
    probs = np.array(probs)
    return np.random.choice(range(num_cities), p=probs / probs.sum())

# Construct solution for a single ant
def construct_solution(pheromone, eta):
    tour = [np.random.randint(0, num_cities)]
    while len(tour) < num_cities:
        next_city = choose_next_city(pheromone, eta, tour)
        tour.append(next_city)
    return tour

# 5. Update pheromones after all ants have constructed their tours
def update_pheromones(pheromone, all_tours, distances, best_tour):
    pheromone *= (1 - rho)  # Evaporate pheromones

    # Add pheromones for each ant's tour
    for tour in all_tours:
        tour_length = sum([distances[tour[i], tour[i + 1]] for i in range(-1, num_cities - 1)])
        for i in range(-1, num_cities - 1):
            pheromone[tour[i], tour[i + 1]] += 1.0 / tour_length

    # Increase pheromones on the best tour
    best_length = sum([distances[best_tour[i], best_tour[i + 1]] for i in range(-1, num_cities - 1)])
    for i in range(-1, num_cities - 1):
        pheromone[best_tour[i], best_tour[i + 1]] += 1.0 / best_length

# 6. Main ACO Loop: Iterate over multiple iterations to find the best solution
def run_aco(distances, num_iterations):
    pheromone = np.ones((num_cities, num_cities)) * initial_pheromone
    best_tour = None
    best_length = float('inf')

    for iteration in range(num_iterations):
        all_tours = [construct_solution(pheromone, eta) for _ in range(num_ants)]
        all_lengths = [sum([distances[tour[i], tour[i + 1]] for i in range(-1, num_cities - 1)]) for tour in 
all_tours]
```

```
        current_best_length = min(all_lengths)
        current_best_tour = all_tours[all_lengths.index(current_best_length)]

        if current_best_length < best_length:
            best_length = current_best_length
            best_tour = current_best_tour

        update_pheromones(pheromone, all_tours, distances, best_tour)

        print(f"Iteration {iteration + 1}, Best Length: {best_length}")

    return best_tour, best_length

# Run the ACO algorithm
best_tour, best_length = run_aco(distances, num_iterations)

# 7. Output the Best Solution
print(f"Best Tour: {best_tour}")
print(f"Best Tour Length: {best_length}")

# 8. Plot the Best Route
def plot_route(cities, best_tour):
    plt.figure(figsize=(8, 6))
    for i in range(len(cities)):
        plt.scatter(cities[i][0], cities[i][1], color='red')
        plt.text(cities[i][0], cities[i][1], f"City {i}", fontsize=12)

    # Plot the tour as lines connecting the cities
    tour_cities = np.array([cities[i] for i in best_tour] + [cities[best_tour[0]]])  # Complete the loop by
returning to the start
    plt.plot(tour_cities[:, 0], tour_cities[:, 1], linestyle='-', marker='o', color='blue')

    plt.title(f"Best Tour (Length: {best_length})")
    plt.xlabel("X Coordinate")
    plt.ylabel("Y Coordinate")
    plt.grid(True)
    plt.show()

# Call the plot function
plot_route(cities, best_tour)
```

OUTPUT:

```
Iteration 1, Best Length: 24.191626245470978
Iteration 2, Best Length: 24.191626245470978
Iteration 3, Best Length: 24.191626245470978
Iteration 4, Best Length: 24.191626245470978
Iteration 5, Best Length: 24.191626245470978
Iteration 6, Best Length: 24.191626245470978
Iteration 7, Best Length: 24.191626245470978
Iteration 8, Best Length: 24.191626245470978
Iteration 9, Best Length: 24.191626245470978
Iteration 10, Best Length: 24.191626245470978
Iteration 11, Best Length: 24.191626245470978
Iteration 12, Best Length: 24.191626245470978
Iteration 13, Best Length: 24.191626245470978
Iteration 14, Best Length: 24.191626245470978
Iteration 15, Best Length: 24.191626245470978
Iteration 16, Best Length: 24.191626245470978
Iteration 17, Best Length: 24.191626245470978
Iteration 18, Best Length: 24.191626245470978
Iteration 19, Best Length: 24.191626245470978
Iteration 20, Best Length: 24.191626245470978
Iteration 21, Best Length: 24.191626245470978
Iteration 22, Best Length: 24.191626245470978
Iteration 23, Best Length: 24.191626245470978
Iteration 24, Best Length: 24.191626245470978
Iteration 25, Best Length: 24.191626245470978
Iteration 26, Best Length: 24.191626245470978
Iteration 27, Best Length: 24.191626245470978
Iteration 28, Best Length: 24.191626245470978
Iteration 29, Best Length: 24.191626245470978
Iteration 30, Best Length: 24.191626245470978
Best Tour: [4, 3, 2, 0, 1]
Best Tour Length: 24.191626245470978
```



<u>Program 4:</u> Cuckoo Search (CS)

Cuckoo Search (CS) is a nature-inspired optimization algorithm based on the brood parasitism of some cuckoo species. This behavior involves laying eggs in the nests of other birds, leading to the optimization of survival strategies. CS uses Lévy flights to generate new solutions, promoting global search capabilities and avoiding local minima. The algorithm is widely used for solving continuous optimization problems and has applications in various domains, including engineering design, machine learning, and data mining.

<u>Implementation Steps:</u>

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of nests, the probability of discovery, and the number of iterations.
3. Initialize Population: Generate an initial population of nests with random positions.
4. Evaluate Fitness: Evaluate the fitness of each nest based on the optimization function.
5. Generate New Solutions: Create new solutions via Lévy flights.
6. Abandon Worst Nests: Abandon a fraction of the worst nests and replace them with new random positions.
7. Iterate: Repeat the evaluation, updating, and replacement process for a fixed number of iterations or until convergence criteria are met.
8. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

Saathi

Date 21 / 11 / 2024

Cuckoo Search Algorithm.

1) initialization:
Create a population of num_agents cuckoo with random position within search space, where each solution is represented as array of dim variable.
bounds lower_bound and upper_bound.

2) Evaluate Fitness:
This is evaluated using objective function (here sphere function - sphere of variables)

3) Main Loop:
For each iteration (t from 0 to max_iter);
=> Generate New Solution: Each cuckoo randomly moves to new position, moving to better position.

=> Apply boundary Constraints:
Ensure all new solutions lie within the search space by clipping them to boundaries.

=> Evaluate new solution;
Calculate the fitness of new solution using objective function

$$\text{fitness}(x_i') = f(x_i')$$

=> Replace the worst solution:
If the fitness of the new solution $f(x_i')$ is better than old solution $f(x_i)$ replace ~~to~~ old with new solution.
update x_i and its fitness accordingly

Saathi

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⇒ Abandon some nests (Exploration phase)
With probability pa, abandon a fraction of cuckoo's nest and re initialize new random solution.

⇒ Evaluate the fitness of these newly reinitialized cuckoos

Track the best solution:
After each iteration track the best solution so far, based on fitness.

Output:
Best Solution:
Best Fitness: The corresponding fitness of the best solution

Output:
I1: Best Fitness = 1.32193940 76904.
I2: " " = 1.32193940 76904
I3: " " = 1.21794028605 4
I4: " " = 0.179780.

Best Solution: [0.36024327 -0.22361918]
Best Fitness: 0.17978075 22096

Application:
Optimization Engineering design, pattern Recognition
Machine learning models (training)

Sneha SB 21/11/24

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Code:

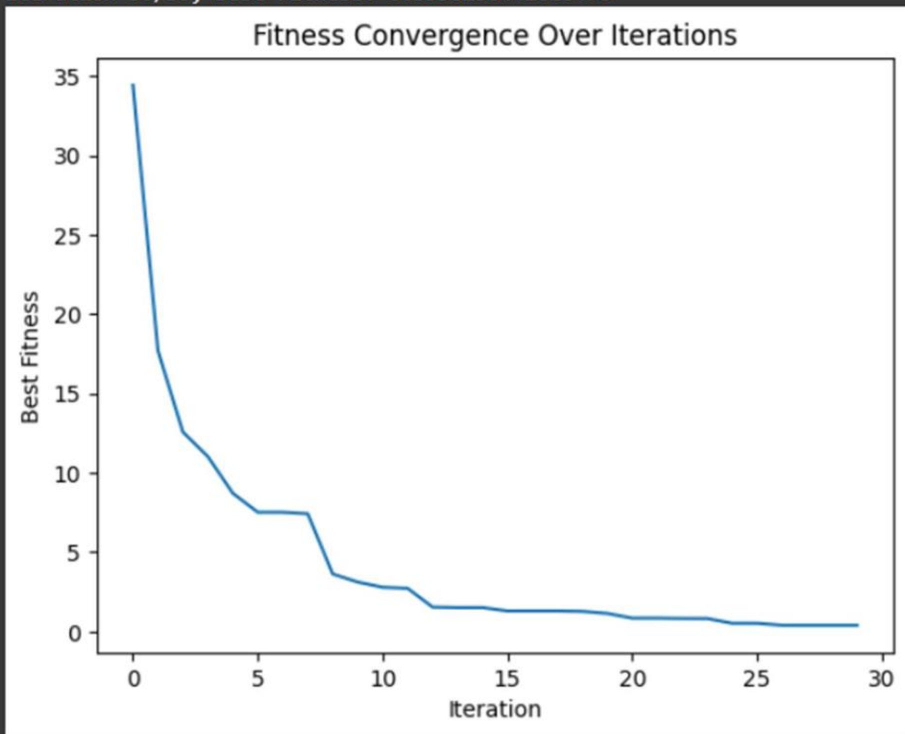
```
#cuckoo search
import numpy as np
import random
import math
import matplotlib.pyplot as plt

# Define a sample function to optimize (Sphere function in this case)
def objective_function(x):
    return np.sum(x ** 2)

#   Lévy   flight   function
def levy_flight(Lambda):
    sigma_u = (math.gamma(1 + Lambda) * np.sin(np.pi * Lambda / 2) /
            (math.gamma((1 + Lambda) / 2) * Lambda * 2 ** ((Lambda - 1) / 2))) ** (1 / Lambda)
    sigma_v = 1
    u = np.random.normal(0, sigma_u, size=1)
    v = np.random.normal(0, sigma_v, size=1)
    step = u / (abs(v) ** (1 / Lambda))
    return step

# Cuckoo Search algorithm
def cuckoo_search(num_nests=25, num_iterations=100, discovery_rate=0.25, dim=5, lower_bound=-
10, upper_bound=10):
    # Initialize nests
    nests = np.random.uniform(lower_bound, upper_bound, (num_nests, dim))
    fitness = np.array([objective_function(nest) for nest in nests])

    # Get the current best nest
    best_nest_idx = np.argmin(fitness)
    best_nest = nests[best_nest_idx].copy()
    best_fitness = fitness[best_nest_idx]

    Lambda = 1.5  # Parameter for Lévy flights
    fitness_history = []  # To track fitness at each iteration

    for iteration in range(num_iterations):
        # Generate new solutions via Lévy flight
        for i in range(num_nests):
            step_size = levy_flight(Lambda)
            new_solution = nests[i] + step_size * (nests[i] - best_nest)
            new_solution = np.clip(new_solution, lower_bound, upper_bound)
            new_fitness = objective_function(new_solution)

            # Replace nest if new solution is better
            if new_fitness < fitness[i]:
```

```
            nests[i] = new_solution
            fitness[i] = new_fitness

        # Discover some nests with probability 'discovery_rate'
        random_nests = np.random.choice(num_nests, int(discovery_rate * num_nests), replace=False)
        for nest_idx in random_nests:
            nests[nest_idx] = np.random.uniform(lower_bound, upper_bound, dim)
            fitness[nest_idx] = objective_function(nests[nest_idx])

        # Update the best nest
        current_best_idx = np.argmin(fitness)
        if fitness[current_best_idx] < best_fitness:
            best_fitness = fitness[current_best_idx]
            best_nest = nests[current_best_idx].copy()

        # Store fitness for plotting
        fitness_history.append(best_fitness)

        # Print the best solution at each iteration (optional)
        print(f"Iteration {iteration+1}/{num_iterations}, Best Fitness: {best_fitness}")

    # Plot fitness convergence graph
    plt.plot(fitness_history)
    plt.title('Fitness Convergence Over Iterations')
    plt.xlabel('Iteration')
    plt.ylabel('Best Fitness')
    plt.show()

    # Return the best solution found
    return best_nest, best_fitness

# Example usage
best_nest, best_fitness = cuckoo_search(num_nests=30, num_iterations=30, dim=10, lower_bound=-
5, upper_bound=5)
print("Best Solution:", best_nest)
print("Best Fitness:", best_fitness)
```

OUTPUT:

```
Iteration 1/30, Best Fitness: 34.421347350368414
Iteration 2/30, Best Fitness: 17.701267864864427
Iteration 3/30, Best Fitness: 12.572246094152595
Iteration 4/30, Best Fitness: 11.025968548544025
Iteration 5/30, Best Fitness: 8.713786692960158
Iteration 6/30, Best Fitness: 7.5206125475077785
Iteration 7/30, Best Fitness: 7.5206125475077785
Iteration 8/30, Best Fitness: 7.426062303628502
Iteration 9/30, Best Fitness: 3.6305424687807872
Iteration 10/30, Best Fitness: 3.122312407680085
Iteration 11/30, Best Fitness: 2.7935374916676268
Iteration 12/30, Best Fitness: 2.7258275326189683
Iteration 13/30, Best Fitness: 1.5451154817432429
Iteration 14/30, Best Fitness: 1.5138101828809285
Iteration 15/30, Best Fitness: 1.5138101828809285
Iteration 16/30, Best Fitness: 1.300269684490209
Iteration 17/30, Best Fitness: 1.300269684490209
Iteration 18/30, Best Fitness: 1.300269684490209
Iteration 19/30, Best Fitness: 1.2738498249584989
Iteration 20/30, Best Fitness: 1.1445834652176474
Iteration 21/30, Best Fitness: 0.8487556087655604
Iteration 22/30, Best Fitness: 0.8487556087655604
Iteration 23/30, Best Fitness: 0.8289231635578032
Iteration 24/30, Best Fitness: 0.8242402471719793
Iteration 25/30, Best Fitness: 0.5258270013075049
Iteration 26/30, Best Fitness: 0.5258270013075049
Iteration 27/30, Best Fitness: 0.3996236442626478
Iteration 28/30, Best Fitness: 0.3996236442626478
Iteration 29/30, Best Fitness: 0.3996236442626478
Iteration 30/30, Best Fitness: 0.3996236442626478
```

```
Iteration 30/30, Best Fitness: 0.3996236442626478
```




```
Best Solution: [ 0.1187463  -0.27226584  0.30789726 -0.04631337 -0.41395998  0.0566571
 -0.05240855 -0.11176247  0.15695263 -0.00202369]
Best Fitness: 0.3996236442626478
```

<u>Program 5:</u> Grey Wolf Optimizer (GWO)

The Grey Wolf Optimizer (GWO) algorithm is a swarm intelligence algorithm inspired by the social hierarchy and hunting behavior of grey wolves. It mimics the leadership structure of alpha, beta, delta, and omega wolves and their collaborative hunting strategies. The GWO algorithm uses these social hierarchies to model the optimization process, where the alpha wolves guide the search process while beta and delta wolves assist in refining the search direction. This algorithm is effective for continuous optimization problems and has applications in engineering, data analysis, and machine learning.

<u>Implementation Steps:</u>
1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of wolves and the number of iterations.
3. Initialize Population: Generate an initial population of wolves with random positions.
4. Evaluate Fitness: Evaluate the fitness of each wolf based on the optimization function.
5. Update Positions: Update the positions of the wolves based on the positions of alpha, beta, and delta wolves.
6. Iterate: Repeat the evaluation and position updating process for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations

Algorithm:

Grey Wolf Optimization

Algorithm:

1) Initialize the parameters:
- N: Number of wolves
- MaxIterations: Maximum no. of iterations.
- D: Dimensionality of problem
- lb, ub: Lower and upper bound of ~~the~~ search space

2) Initialize the positions of the wolves randomly within the bounds.
- $x(i)$ = Position of wolf i
- Evaluate the fitness of each wolf using objective function
  - $Fitness(i) = f(x(i))$

3) Initialize the α, β, and δ wolves.
- α = Best wolf
- β = Second best wolf
- δ = Third best wolf.

4) For $t = 1$ to MaxIteration
a. update the positions of the wolves

For each wolf i:
1. Update the position of the wolf using the formula:

$$x(i) = x(i) + A * D\alpha - x(i)$$
$$x(i) = x(i) + A * D\beta - x(i)$$
$$x(i) = x(i) + A * D\delta - x(i)$$

where
- $A = 2 * r1 - 1$

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- $D\alpha = |C1 * \alpha\text{-position} - X(i)|$
  $D\beta = |C2 * \beta\text{-position} - X(i)|$
  $D\delta = |C3 * \delta\text{-position} - X(i)|$
  $C1, C2, C3 = 2 * r2$

2. update the fitness of each wolf.
   Fitness $(i) = f(X(i))$

b. sort the wolves based on their fitness value and update α, β, δ.

5. Return the best solution found (α wolf) after max iteration.

Application:
- Optimization in Engineering
  structural design.
- Machine learning
  feature selection and extraction.

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Code:

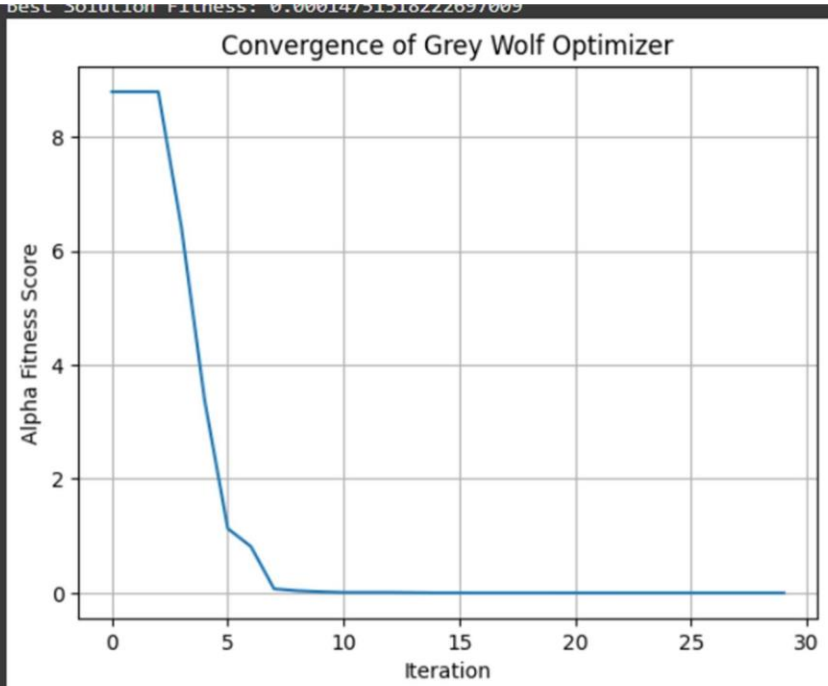
```
#GWO
import numpy as np
import matplotlib.pyplot as plt

# Step 1: Define the Problem (a mathematical function to optimize)
def objective_function(x):
    return np.sum(x**2)  # Example: Sphere function (minimize sum of squares)

# Step 2: Initialize Parameters
num_wolves = 5  # Number of wolves in the pack
num_dimensions = 2  # Number of dimensions (for the optimization problem)
num_iterations = 30  # Number of iterations
lb = -10  # Lower bound of search space
ub = 10  # Upper bound of search space

# Step 3: Initialize Population (Generate initial positions randomly)
wolves = np.random.uniform(lb, ub, (num_wolves, num_dimensions))

# Initialize alpha, beta, delta wolves
alpha_pos = np.zeros(num_dimensions)
beta_pos = np.zeros(num_dimensions)
delta_pos = np.zeros(num_dimensions)

alpha_score = float('inf')  # Best (alpha) score
beta_score = float('inf')   # Second best (beta) score
delta_score = float('inf')  # Third best (delta) score

# To store the alpha score over iterations for graphing
alpha_score_history = []

# Step 4: Evaluate Fitness and assign Alpha, Beta, Delta wolves
def evaluate_fitness():
    global alpha_pos, beta_pos, delta_pos, alpha_score, beta_score, delta_score

    for wolf in wolves:
        fitness = objective_function(wolf)

        # Update Alpha, Beta, Delta wolves based on fitness
        if fitness < alpha_score:
```

```
            delta_score = beta_score
            delta_pos = beta_pos.copy()

            beta_score = alpha_score
            beta_pos = alpha_pos.copy()

            alpha_score = fitness
            alpha_pos = wolf.copy()
        elif fitness < beta_score:
            delta_score = beta_score
            delta_pos = beta_pos.copy()

            beta_score = fitness
            beta_pos = wolf.copy()
        elif fitness < delta_score:
            delta_score = fitness
            delta_pos = wolf.copy()

# Step 5: Update Positions
def update_positions(iteration):
    a = 2 - iteration * (2 / num_iterations)  # a decreases linearly from 2 to 0

    for i in range(num_wolves):
        for j in range(num_dimensions):
            r1 = np.random.random()
            r2 = np.random.random()

            # Position update based on alpha
            A1 = 2 * a * r1 - a
            C1 = 2 * r2
            D_alpha = abs(C1 * alpha_pos[j] - wolves[i, j])
            X1 = alpha_pos[j] - A1 * D_alpha

            # Position update based on beta
            r1 = np.random.random()
            r2 = np.random.random()
            A2 = 2 * a * r1 - a
            C2 = 2 * r2
            D_beta = abs(C2 * beta_pos[j] - wolves[i, j])
            X2 = beta_pos[j] - A2 * D_beta
```

```
            # Position update based on delta
            r1 = np.random.random()
            r2 = np.random.random()
            A3 = 2 * a * r1 - a
            C3 = 2 * r2
            D_delta = abs(C3 * delta_pos[j] - wolves[i, j])
            X3 = delta_pos[j] - A3 * D_delta

            # Update wolf position
            wolves[i, j] = (X1 + X2 + X3) / 3

            # Apply boundary constraints
            wolves[i, j] = np.clip(wolves[i, j], lb, ub)

# Step 6: Iterate (repeat evaluation and position updating)
for iteration in range(num_iterations):
    evaluate_fitness()  # Evaluate fitness of each wolf
    update_positions(iteration)  # Update positions based on alpha, beta, delta

    # Record the alpha score for this iteration
    alpha_score_history.append(alpha_score)

    # Optional: Print current best score
    print(f"Iteration {iteration+1}/{num_iterations}, Alpha Score: {alpha_score}")

# Step 7: Output the Best Solution
print("Best Solution:", alpha_pos)
print("Best Solution Fitness:", alpha_score)

# Plotting the convergence graph
plt.plot(alpha_score_history)
plt.title('Convergence of Grey Wolf Optimizer')
plt.xlabel('Iteration')
plt.ylabel('Alpha Fitness Score')
plt.grid(True)
plt.show()
```

OUTPUT:

```
Iteration 1/30, Alpha Score: 8.789922247101906
Iteration 2/30, Alpha Score: 8.789922247101906
Iteration 3/30, Alpha Score: 8.789922247101906
Iteration 4/30, Alpha Score: 6.409956649485766
Iteration 5/30, Alpha Score: 3.383929841190778
Iteration 6/30, Alpha Score: 1.1292299489236237
Iteration 7/30, Alpha Score: 0.8136628488047792
Iteration 8/30, Alpha Score: 0.07110881373527288
Iteration 9/30, Alpha Score: 0.03823180120070083
Iteration 10/30, Alpha Score: 0.021111314445105462
Iteration 11/30, Alpha Score: 0.00874782100259989
Iteration 12/30, Alpha Score: 0.00874782100259989
Iteration 13/30, Alpha Score: 0.00874782100259989
Iteration 14/30, Alpha Score: 0.005066807028932165
Iteration 15/30, Alpha Score: 0.0011746187200998674
Iteration 16/30, Alpha Score: 0.0011746187200998674
Iteration 17/30, Alpha Score: 0.0008078646351838173
Iteration 18/30, Alpha Score: 0.0008078646351838173
Iteration 19/30, Alpha Score: 0.0006302256737926024
Iteration 20/30, Alpha Score: 0.0005272190797352655
Iteration 21/30, Alpha Score: 0.00035614966782860404
Iteration 22/30, Alpha Score: 0.0003270119398391142
Iteration 23/30, Alpha Score: 0.00022723766847392013
Iteration 24/30, Alpha Score: 0.00022152382849585967
Iteration 25/30, Alpha Score: 0.00022152382849585967
Iteration 26/30, Alpha Score: 0.00020102313789207912
Iteration 27/30, Alpha Score: 0.0001974565833678501
Iteration 28/30, Alpha Score: 0.0001547675581999543
Iteration 29/30, Alpha Score: 0.00014751518222697009
Iteration 30/30, Alpha Score: 0.00014751518222697009
Best Solution: [ 0.00643925 -0.01029812]
Best Solution Fitness: 0.00014751518222697009
```



<u>Program 6:</u> Parallel Cellular Algorithms and Programs

Parallel Cellular Algorithms are inspired by the functioning of biological cells that operate in a highly parallel and distributed manner. These algorithms leverage the principles of cellular automata and parallel computing to solve complex optimization problems efficiently. Each cell represents a potential solution and interacts with its neighbors to update its state based on predefined rules. This interaction models the diffusion of information across the cellular grid, enabling the algorithm to explore the search space effectively. Parallel Cellular Algorithms are particularly suitable for large-scale optimization problems and can be implemented on parallel computing architectures for enhanced performance.

<u>Implementation Steps:</u>

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of cells, grid size, neighborhood structure, and number of iterations.
3. Initialize Population: Generate an initial population of cells with random positions in the solution space.
4. Evaluate Fitness: Evaluate the fitness of each cell based on the optimization function.
5. Update States: Update the state of each cell based on the states of its neighboring cells and predefined update rules.
6. Iterate: Repeat the evaluation and state updating process for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

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Parallel Cellular Algorithm.

Objective Function:

The function is used as sphere function particularly used in the optimization algorithms

def sphere-function (position):
return sum (position_i ^2 for each position_i in position)

Initialize the population Grid:

This function is used to create a grid of shape and fill with random values uniformly distributed between lower-bound and upper-bound

def initialize - population (grid-size solution-frame, lower-bound, upper-bound):
Initialize grid with random values in given bounds
Return Grid

Evaluate Fitness:

This function is used to evaluate the fitness for each cell in grid

def evaluate-fitness (grid):
For each cell in grid:
Calculate fitness using sphere-function

Get Neighbours of a cell:
def get-neighbours (grid, i, j)
Initialize empty list for neighbours
For each (di, dj) in
[(-1, -1), (-1, 0) ..... (1, 1)]

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excluding (0, 0):
n_i = (i + di) % grid-size
n_j = (j + dj) % grid-size
Add grid [ni] (nj) to neighbours list
Return Neighbours

→ Update states of all cells in the grid, the function is used for grid the neighboring cells identify the neighbor with best fitness's position

def update_status(grid, fitness, learning-rate):
Initiate new-grid as a copy of grid.
for each cell (i, j) in grid:
Get neighbours of all (i, j)
Find the best neighbor with minimum fitness
update cell position
new-grid [i, j] = grid [i, j] + learning-rate * best-neighbor-grid(i,j))

Output:
Best Solution:
[-0.00959221 0.3401244]
Best Fitness: 0.00125

Code:

```
#pcap
import numpy as np

# Define the problem: A simple optimization function (e.g., Sphere Function)
def optimization_function(position):
    """Example: Sphere Function for minimization."""
    return sum(x**2 for x in position)

# Initialize Parameters
GRID_SIZE = (10, 10)  # Grid size (rows, columns)
NEIGHBORHOOD_RADIUS = 1  # Moore neighborhood radius
DIMENSIONS = 2  # Number of dimensions in the solution space
ITERATIONS = 30  # Number of iterations

# Initialize Population
def initialize_population(grid_size, dimensions):
    """Initialize a grid with random positions."""
    population = np.random.uniform(-10, 10, size=(grid_size[0], grid_size[1], dimensions))
    return population

# Evaluate Fitness
def evaluate_fitness(population):
    """Calculate the fitness of all cells."""
    fitness = np.zeros((population.shape[0], population.shape[1]))
    for i in range(population.shape[0]):
        for j in range(population.shape[1]):
            fitness[i, j] = optimization_function(population[i, j])
    return fitness

# Get Neighborhood
def get_neighborhood(grid, x, y, radius):
    """Get the neighbors of a cell within the specified radius."""
    neighbors = []
    for i in range(-radius, radius + 1):
        for j in range(-radius, radius + 1):
            if i == 0 and j == 0:
                continue  # Skip the current cell
            ni, nj = x + i, y + j
            if 0 <= ni < grid.shape[0] and 0 <= nj < grid.shape[1]:
                neighbors.append((ni, nj))
    return neighbors

# Update States
def update_states(population, fitness):
    """Update the state of each cell based on its neighbors."""
    new_population = np.copy(population)
```

```
    for i in range(population.shape[0]):
        for j in range(population.shape[1]):
            neighbors = get_neighborhood(population, i, j, NEIGHBORHOOD_RADIUS)
            best_neighbor = population[i, j]
            best_fitness = fitness[i, j]

            # Find the best position among neighbors
            for ni, nj in neighbors:
                if fitness[ni, nj] < best_fitness:
                    best_fitness = fitness[ni, nj]
                    best_neighbor = population[ni, nj]

            # Update the cell state (move towards the best neighbor)
            new_population[i, j] = (population[i, j] + best_neighbor) / 2  # Average position
    return new_population

# Main Algorithm
def parallel_cellular_algorithm():
    """Implementation of the Parallel Cellular Algorithm."""
    population = initialize_population(GRID_SIZE, DIMENSIONS)
    best_solution = None
    best_fitness = float('inf')

    for iteration in range(ITERATIONS):
        # Evaluate fitness
        fitness = evaluate_fitness(population)

        # Track the best solution
        min_fitness = np.min(fitness)
        if min_fitness < best_fitness:
            best_fitness = min_fitness
            best_solution = population[np.unravel_index(np.argmin(fitness), fitness.shape)]

        # Update states based on neighbors
        population = update_states(population, fitness)

        # Print progress
        print(f"Iteration {iteration + 1}: Best Fitness = {best_fitness}")

    print("\nBest Solution Found:")
    print(f"Position: {best_solution}, Fitness: {best_fitness}")

# Run the algorithm
if __name__ == "__main__":
    parallel_cellular_algorithm()
```

OUTPUT:

```
Iteration 1: Best Fitness = 0.43918427791098213
Iteration 2: Best Fitness = 0.43918427791098213
Iteration 3: Best Fitness = 0.062221279350329436
Iteration 4: Best Fitness = 0.030149522005462108
Iteration 5: Best Fitness = 0.015791278460696168
Iteration 6: Best Fitness = 0.0025499667118763104
Iteration 7: Best Fitness = 0.0025499667118763104
Iteration 8: Best Fitness = 0.00019007166980743008
Iteration 9: Best Fitness = 0.00019007166980743008
Iteration 10: Best Fitness = 1.0432171933623911e-05
Iteration 11: Best Fitness = 8.406928148912647e-06
Iteration 12: Best Fitness = 5.511032710180021e-07
Iteration 13: Best Fitness = 4.3084388056725156e-07
Iteration 14: Best Fitness = 2.315054420755622e-07
Iteration 15: Best Fitness = 5.245753459404661e-08
Iteration 16: Best Fitness = 5.245753459404661e-08
Iteration 17: Best Fitness = 4.341357920017173e-08
Iteration 18: Best Fitness = 1.145644119860328e-08
Iteration 19: Best Fitness = 3.147791691706415e-09
Iteration 20: Best Fitness = 2.8192306881167533e-09
Iteration 21: Best Fitness = 9.788374665398935e-11
Iteration 22: Best Fitness = 9.788374665398935e-11
Iteration 23: Best Fitness = 9.788374665398935e-11
Iteration 24: Best Fitness = 9.788374665398935e-11
Iteration 25: Best Fitness = 7.537171686605552e-11
Iteration 26: Best Fitness = 7.234639306921671e-11
Iteration 27: Best Fitness = 7.028872029493468e-11
Iteration 28: Best Fitness = 3.340290444524624e-11
Iteration 29: Best Fitness = 1.4953679944431498e-11
Iteration 30: Best Fitness = 1.0817118995466254e-11

Best Solution Found:
Position: [-2.92599538e-06 -1.50188883e-06], Fitness: 1.0817118995466254e-11
```

<u>Program 7:</u> Optimization via Gene Expression Algorithms

Gene Expression Algorithms (GEA) are inspired by the biological process of gene expression in living organisms. This process involves the translation of genetic information encoded in DNA into functional proteins. In GEA, solutions to optimization problems are encoded in a manner similar to genetic sequences. The algorithm evolves these solutions through selection, crossover, mutation, and gene expression to find optimal or near-optimal solutions. GEA is effective for solving complex optimization problems in various domains, including engineering, data analysis, and machine learning.

<u>Implementation Steps:</u>

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the population size, number of genes, mutation rate, crossover rate, and number of generations.
3. Initialize Population: Generate an initial population of random genetic sequences.
4. Evaluate Fitness: Evaluate the fitness of each genetic sequence based on the optimization function.
5. Selection: Select genetic sequences based on their fitness for reproduction.
6. Crossover: Perform crossover between selected sequences to produce offspring.
7. Mutation: Apply mutation to the offspring to introduce variability.
8. Gene Expression: Translate genetic sequences into functional solutions.
9. Iterate: Repeat the selection, crossover, mutation, and gene expression processes for a fixed number of generations or until convergence criteria are met.
10. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

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Optimization via Gene Expression Algorithm

Objective Function:
This function calculate fitness of a given solution using rastrigin objective function

```
def rasting (x):
    A = 10
    result = A * length (x)
    For each xi in x :
        result += (xi^2 - A* cos (2*pi*xi)
    Return result
```

Initialize population:
Initialize a random population of solutions each solution represented by a set of genes

```
def Initiaze-population(pop-size, num-genes,
                        lower-bound, upper-bound)
    return Population.
```

Evaluate Fitness:

```
def evaluate_fitness (population):
    fitness = list of rastrigin (individual)
    for each individual in population
Return fitness
```

Tournment Selection:

```
def tournment_selection (population, fitness,
                         tournment size)
    Selected = for each individual, Select winner
               of random tournment
    Return Selected
```

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Crossover:

Creates two offspring from two selected parents by combining their genetic material at random crossover point.

def crossover (parent1, parent2)
    crossover_point = Randomly choose a point
    child1 = combine parent1 and parent2 at
        crossover_point
    Return child1, child2

Mutation:

def_mutate (child, mutation_rate, lower_bound, upper_bound):
    for each gene in child, randomly mutate with probability mutation gene.
Return Mutate child

Gene Expression Algorithm:

gene_Expression_algorithm (pop_size, num_gene,
    lower_bound, upper_bound, mutation rate,
    crossover_rate, num_generations)
population = Initialize population
best solution = None, best_fitness = infinity

For generation = 1 to num_generations:
    fitness = Evaluate fitness
    update best solution on if needed
    select population = Tournament Selection
    new_population = For each pair of parents,
        crossover and Mutation
    population = new_population
Return best_solution, best fitness

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Output:

Best Solution: [0.026 0.03131 1.011

0.008 -0.024 0.045

-0.014 0.12 -0.021

-0.018]

Best Fitness : 2.1444198305919713

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Code:

```
import numpy as np
import random

# 1. Define the Problem: Optimization Function (e.g., Sphere Function)
def optimization_function(solution):
    """Sphere Function for minimization (fitness evaluation)."""
    return sum(x**2 for x in solution)

# 2. Initialize Parameters
POPULATION_SIZE = 50  # Number of genetic sequences (solutions)
GENES = 5  # Number of genes per solution
MUTATION_RATE = 0.1  # Probability of mutation
CROSSOVER_RATE = 0.7  # Probability of crossover
GENERATIONS = 30  # Number of generations to evolve

# 3. Initialize Population
def initialize_population(pop_size, genes):
    """Generate initial population of random genetic sequences."""
    return np.random.uniform(-10, 10, (pop_size, genes))

# 4. Evaluate Fitness
def evaluate_fitness(population):
    """Evaluate the fitness of each genetic sequence."""
    fitness = [optimization_function(solution) for solution in population]
    return np.array(fitness)

# 5. Selection: Tournament Selection
def select_parents(population, fitness, num_parents):
    """Select parents using tournament selection."""
    parents = []
    for _ in range(num_parents):
        tournament = random.sample(range(len(population)), 3)  # Randomly select 3 candidates
        best = min(tournament, key=lambda idx: fitness[idx])
        parents.append(population[best])
    return np.array(parents)

# 6. Crossover: Single-Point Crossover
def crossover(parents, crossover_rate):
    """Perform crossover between pairs of parents."""
    offspring = []
    for i in range(0, len(parents), 2):
        if i + 1 >= len(parents):
            break
        parent1, parent2 = parents[i], parents[i + 1]
        if random.random() < crossover_rate:
```

```
        point = random.randint(1, len(parent1) - 1)  # Single crossover point
        child1 = np.concatenate((parent1[:point], parent2[point:]))
        child2 = np.concatenate((parent2[:point], parent1[point:]))
    else:
        child1, child2 = parent1, parent2  # No crossover
    offspring.extend([child1, child2])
  return np.array(offspring)

# 7. Mutation
def mutate(offspring, mutation_rate):
  """Apply mutation to introduce variability."""
  for i in range(len(offspring)):
    for j in range(len(offspring[i])):
      if random.random() < mutation_rate:
        offspring[i][j] += np.random.uniform(-1, 1)  # Random small change
  return offspring

# 8. Gene Expression: Functional Solution (No transformation needed for this case)
def gene_expression(population):
  """Translate genetic sequences into functional solutions."""
  return population  # Genetic sequences directly represent solutions here.

# 9. Main Function: Gene Expression Algorithm
def gene_expression_algorithm():
  """Implementation of Gene Expression Algorithm for optimization."""
  # Initialize population
  population = initialize_population(POPULATION_SIZE, GENES)
  best_solution = None
  best_fitness = float('inf')

  for generation in range(GENERATIONS):
    # Evaluate fitness
    fitness = evaluate_fitness(population)

    # Track the best solution
    min_fitness_idx = np.argmin(fitness)
    if fitness[min_fitness_idx] < best_fitness:
      best_fitness = fitness[min_fitness_idx]
      best_solution = population[min_fitness_idx]

    # Selection
    parents = select_parents(population, fitness, POPULATION_SIZE // 2)

    # Crossover
    offspring = crossover(parents, CROSSOVER_RATE)

    # Mutation
```

```
        offspring = mutate(offspring, MUTATION_RATE)

        # Gene Expression
        population = gene_expression(offspring)

        # Print progress
        print(f"Generation {generation + 1}: Best Fitness = {best_fitness}")

    # Output the best solution
    print("\nBest Solution Found:")
    print(f"Position: {best_solution}, Fitness: {best_fitness}")

# 10. Run the Algorithm
if _name___== "_main_":
    gene_expression_algorithm()
```

OUTPUT:

```
Generation 1: Best Fitness = 55.82997756903893
Generation 2: Best Fitness = 26.410565738143625
Generation 3: Best Fitness = 21.857647823851615
Generation 4: Best Fitness = 20.016914182036285
Generation 5: Best Fitness = 20.016914182036285
Generation 6: Best Fitness = 20.016914182036285
Generation 7: Best Fitness = 13.81760087982789
Generation 8: Best Fitness = 13.81760087982789
Generation 9: Best Fitness = 12.077725051361178
Generation 10: Best Fitness = 10.461698723345474
Generation 11: Best Fitness = 8.933105023570093
Generation 12: Best Fitness = 6.619449963941974
Generation 13: Best Fitness = 3.1567413435369454
Generation 14: Best Fitness = 3.1567413435369454
Generation 15: Best Fitness = 3.1567413435369454
Generation 16: Best Fitness = 2.74585545305795
Generation 17: Best Fitness = 2.7031453676198964
Generation 18: Best Fitness = 2.078188177116774
Generation 19: Best Fitness = 1.5193087227027497
Generation 20: Best Fitness = 1.4413606561895607
Generation 21: Best Fitness = 0.8501569187378994
Generation 22: Best Fitness = 0.4209372164676112
Generation 23: Best Fitness = 0.3893761873774093
Generation 24: Best Fitness = 0.3893761873774093
Generation 25: Best Fitness = 0.3893761873774093
Generation 26: Best Fitness = 0.3741053651316379
Generation 27: Best Fitness = 0.1381555631914642
Generation 28: Best Fitness = 0.12238160343023853
Generation 29: Best Fitness = 0.12238160343023853
Generation 30: Best Fitness = 0.12238160343023853

Best Solution Found:
Position: [-0.03614343 -0.00257499  0.02260677  0.31412563  0.14792784], Fitness: 0.12238160343023853
```