Clustering Problems

- 1. Cluster the following data using k-means clustering algorithm. Consider k=2 . Dataset={2,4,10,12,3,20,30,11,25} **Solution:**
 - Randomly assign means: $m_1 = 3$, $m_2 = 4$ 1.
 - The numbers which are close to mean $m_1 = 3$ are grouped into cluster K_1 an numbers which are close to mean $m_2 = 4$ are grouped into cluster K_2 . 2.
 - Again calculate the new mean for new cluster groups. 3.
 - $K_1 = \{2,3\}, K_2 = \{4,10,12,20,30,11,25\}, m_1 = 2.5, m_2 = 16$ 4.
 - $K_1 = \{2,3,4\}, K_2 = \{10,12,20,30,11,25\}, m_1 = 3, m_2 = 18$ 5.
 - $K_1 = \{2,3,4,10\}, K_2 = \{12,20,30,11,25\}, m_1 = 4.75, m_2 = 19.6$ 6.
 - $K_1 = \{2,3,4,10,11,12\}, K_2 = \{20,30,25\}, m_1 = 7, m_2 = 25$ 7.
 - $K_1 = \{2,3,4,10,11,12\}, K_2 = \{20,30,25\}$ 8.
 - Stop as the clusters with these means (in step 7 and 8) are the same. The clust 9. in the last two groups are identical.
 - So the final answer is $K_1 = \{2,3,4,10,11,12\}, K_2 = \{20,30,25\}$ 10.
- 2. For the following distance matrix, draw single link and complete link dendogram.

	1	2	3	4	5
1	0				
2	2	0			
3	6	3	0		
4	10	9	7	0	
5	9	8	5	4	0

Solution:

Single Link:

$$d_{(1,2)3} = \min \{d_{1,3}, d_{2,3}\} = \min \{6, 3\} = 3$$

$$d_{(1,2)4} = min \{d_{1,4}, d_{2,4}\} = min \{10, 9\} = 9$$

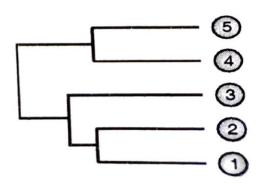
$$d_{(1,2)5} = \min \{d_{1,5}, d_{2,5}\} = \min \{9, 8\} = 8$$

$$d_{(1,2,3),4} = \min \{d_{(1,2),4}, d_{3,4}\} = \min \{9, 7\} = 7$$

$$d_{(1,2,3)5} = \min \{d_{(1,2),5}, d_{3,5}\} = \min \{8, 5\} = 5$$

$$\begin{array}{cccc}
(1,2,3) & 4,5 \\
(1,2,3) & 0 \\
(4,5) & 5 & 0
\end{array}$$

$$d_{(1,2,3),(4,5)} = \min \{d_{(1,2,3),4}, d_{(1,2,3),5}\} = \min \{7, 5\} = 5$$



Complete Link:

Step 1:

$$\begin{aligned} d_{(1,2),3} &= \max \{d_{1,3}, d_{2,3}\} = \max \{6, 3\} = 6 \\ d_{(1,2),4} &= \max \{d_{1,4}, d_{2,4}\} = \max \{10, 9\} = 10 \\ d_{(1,2),5} &= \max \{d_{1,5}, d_{2,5}\} = \max \{9, 8\} = 9 \end{aligned}$$

Step 2:

$$d_{(1,2),(4,5)} = \max \{d_{(1,2),4}, d_{(1,2),5}\} = \max \{10, 9\} = 10$$

$$d_{3,(4,5)} = \max \{d_{3,4}, d_{3,5}\} = \max \{7, 5\} = 7$$

3. Apply DBSCAN clustering algorithm to cluster following dataset. Consider Eps=1.9 and Minpts=4

Point	х	Y
P1	7	4
P2	6	4
Р3	5	6
P4	4	2
P5	6	3
P6	5	2
P7	3	3
P8	4	5
P9	6	5
P10	3	6
P11	4	4
P12	8	2

Solution:

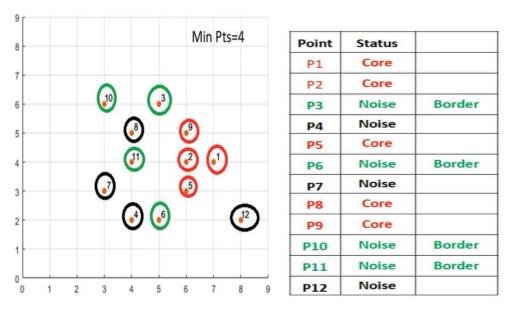
Step1: Find distance matrix using Euclidean distance

	P1	P2	Р3	P4	P5	P6	P7	P8	P9	P10	P11	P12
212	2.24	2.83	5.00	4.00	2.24	3.00	5.10	5.00	3.61	6.40	4.47	0.00
P11	3.00	2.00	2.24	2.00	2.24	2.24	1.41	1.00	2.24	2.24	0.00	
P10	4.47	3.61	2.00	4.12	4.24	4.47	3.00	1.41	3.16	0.00		
P9	1.41	1.00	1.41	3.61	2.00	3.16	3.61	2.00	0.00			
P8	3.16	2.24	1.41	3.00	2.83	3.16	2.24	0.00				
P7	4.12	3.16	3.61	1.41	3.00	2.24	0.00					
P6	2.83	2.24	4.00	1.00	1.41	0.00						
P5	1.41	1.00	3.16	2.24	0.00							
P4	3.61	2.83	4.12	0.00								
Р3	2.83	2.24	0.00									
P2	1.00	0.00										
P1	0.00											

Step 2: Find E-neighborhood of each data point

P1: P2,P5, P9	P2:P1, P5, P9	P3:P8, P9	P4: P6, P7
P5:P1,P2,P6	P6:P4, P5	P7: P4, P11	P8:P3, P10, P11
P9:P1, P2, P3	P10:P8	P11: P7, P8	P12:

Step3: Identify core points, border points and Noise points



https://www.youtube.com/watch?v=S5OvKmWIdZA