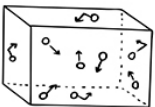
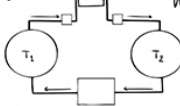
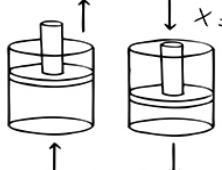


# Thermal Physics Notes

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$U_i(n_i, P_i, V_i, \dots)$   $\rightarrow$   $U_f(n_f, P_f, V_f, \dots)$   $W = -nRT \int_{V_i}^{V_f} \frac{dV}{V} = -nRT \ln\left(\frac{V_f}{V_i}\right)$   $H = U + pV$   $T(K) = T(^{\circ}C) + 273.15$   
 $dH = dU + d(pV)$   $dH = dU + p dV + V dp$   $C_p = (\Delta H / \Delta T)_p$   $\Delta U = Q - W$   $\Delta S = nRT \ln\left(\frac{V_f}{V_i}\right)$   
 $dU = dq + dw$   $C_p = \left(\frac{\partial H}{\partial T}\right)_p$   $W = P \Delta U$   $W = \int_{V_i}^{V_f} P dV$   
 $dH = dq - p dV + V dp$   $dH = C_p dT$   $dS \geq \frac{dq}{T}$   
 $H = U + pV$   $\Delta S = \frac{\Delta_{\text{rev}} H}{T}$   $\Delta H = q_p = C_p \times \Delta T$   $C_v = (\Delta U / \Delta T)_v$   
 $dw = -p dV$   $C_v = \left(\frac{\partial U}{\partial T}\right)_v$   $dS = \frac{dq_{\text{rev}}}{T}$   $\Delta S = \int_1^f \frac{dq_{\text{rev}}}{T}$   
  
 $\Delta U = m(u_2 - u_1) \Delta KE$   
 $= \frac{1}{2} m (v_2^2 - v_1^2) \Delta PE$   
 $= mg(z_2 - z_1)$   
  
 $W_b = \frac{P_2 V_2 - P_1 V_1}{1 - \gamma}$   $\eta_{\text{th}} = \frac{W_{\text{net}}}{Q_{\text{in}}} = 1 - \frac{Q_{\text{out}}}{Q_{\text{in}}}$   $Q = \Delta U + P \Delta V$   
 $dH = dq + V dp$   $\Delta H = \Delta U + V \Delta p$   $T_R = \frac{T}{T_{\text{cr}}}$   $dU = C_v dT$   $\Delta U = q_v = C_v \times \Delta T$   
 $dH = (dq)_p$   $\Delta H = q_p$   $\Delta U = U_f - U_i = q(\text{heat}) + w(\text{work})$   
 $dU = (dq)_v$   $\Delta U = q_v$   $W_b = P_1 V_1 \ln \frac{V_2}{V_1}$   $= P_1 V_1 \ln \frac{P_1}{P_2}$   $= RT_1 \ln \frac{P_1}{P_2}$   
 $P_R = \frac{P}{P_{\text{cr}}}$   $x = \frac{m_g}{m_f + m_g}$   $\gamma_R = \frac{\gamma_{\text{cr}}}{RT_{\text{cr}}}$   


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# 1 | Introduction

**Reference book:** Herbert B. Callen - Thermodynamics and Thermostatistics - [https://drive.google.com/file/d/11ygKC1ITZgF4yU05\\_UyhQ4CKt7QYX9wQ/view?usp=sharing](https://drive.google.com/file/d/11ygKC1ITZgF4yU05_UyhQ4CKt7QYX9wQ/view?usp=sharing)  
Let's get started!

- Laws of thermodynamics apply to macroscopic objects/collections of particles  $\rightarrow$  systems with many interactions
- For Newton's Laws, you need the positions, velocities and the model/type of interparticle forces present in order to predict the evolution of the system.
- Macroscopic systems  $\rightarrow$  General Laws  $\rightarrow$  Universal in nature (applicable to a wide variety of systems)
- These laws are not fundamental  $\rightarrow$  Emerge from microscopic laws  $\rightarrow$  But they make the analysis of macroscopic properties simple
- Example: Consider a box with  $N$  ideal gas particles  $\rightarrow$  We need  $6N$  coordinates, i.e., 3-spatial coordinates and 3-velocity components for each particle  $\rightarrow$  Law:  $\vec{F}_i = m_i \vec{a}_i$  (3 second-order differential equations).

Let's try to find what *coordinates* describe macroscopic systems  $\rightarrow$  Thermodynamic variable

Consider a 1-D lattice (say a metal rod) with separation between adjacent particles  $= a$ . The particles are held together so they are vibrating about their mean position. Plot the displacement of  $i^{th}$  particle  $\Delta x_i$  against  $i$ . As  $N$  (total number of particle) is very large we can look at the scenario wherein  $N \rightarrow \infty$ , i.e., the particle number-axis becomes

approximately continuous. We will see "collective behaviour" because there motions are connected. At a later time, the curve shifts forward  $\rightarrow$  analogy: wave that is propagating forward.

$$k = \frac{2\pi}{\lambda}$$

$\omega(k)$ : dispersion relation

Modes:

1. Slow mode:

- (a) Small  $k$  modes
- (b) Large  $\lambda$  modes
- (c) Small  $\omega$  modes

"Long distance modes"  $\rightarrow \lambda \gg a$

2. Fast mode:

- (a) Large  $k$  modes
- (b) Small  $\lambda$  modes
- (c) Large  $\omega$  modes - oscillate rapidly

"Short distance modes"  $\rightarrow \lambda \approx a$

# When we observe time average, the high frequency modes are un-observable  $\rightarrow$  "Things that don't change over long time interval are macroscopic observables". Take the limits  $\lambda \rightarrow \infty$  and  $T \rightarrow \infty$ , the states that emerge are called "Thermodynamic States"/ "Static States".

# When we take into account the extremely large wavelength modes, we see that particles on one side move in a certain direction (say left) and particles on the other side move in the opposite direction (right). Overall effect: Length of the rod appears to be increasing  $\rightarrow$  Macroscopic effect  $\rightarrow$  Length of rod: macroscopic variable  $\rightarrow$  Volume of solid: thermodynamic coordinate

- Some examples of macroscopic variables:

- 1. Electrostatics: Macroscopic variable  $\rightarrow$  Net charge ( $Q$ )
- 2. Magnetostatics: Macroscopic value  $\rightarrow$  net magnetic dipole moment ( $\vec{\mu}$ )

- Speciality of thermodynamics → Takes into account "hidden coordinates". Tells us energy is distributed among the modes which are invisible to us at a macroscopic level!