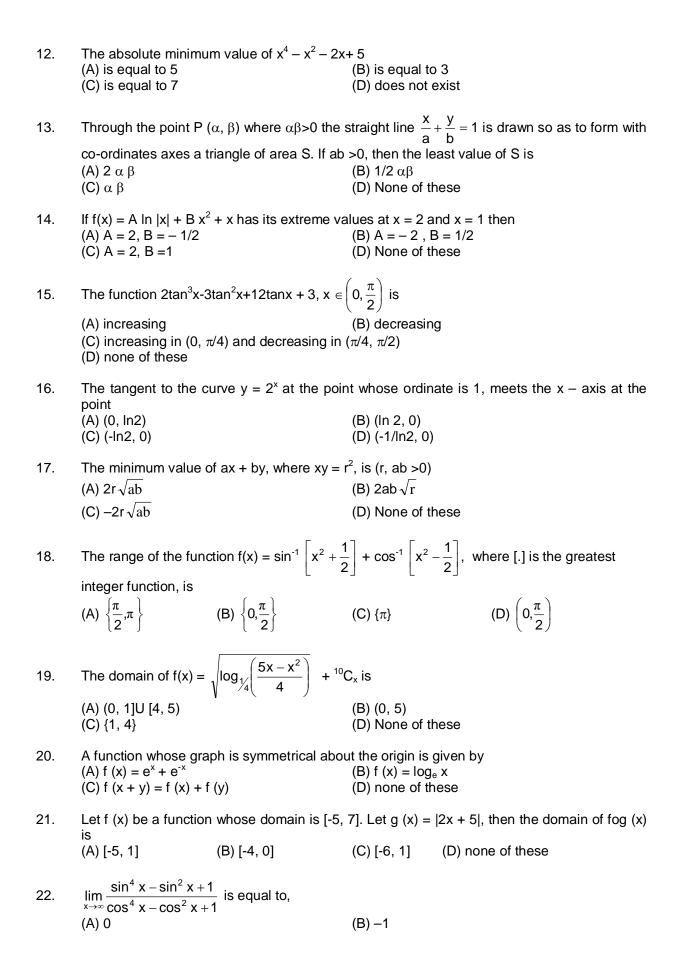
LEVEL-I

	$\lfloor v^2 \rfloor / 1 \rfloor$		
1.	Number of critical points of f (x) = $\frac{ x^2 - 4 }{x^2 - 1}$	are	
	(A) 1 (C) 3	(B) 2 (D) no	ne of these
2.	If the function f (x) = $\cos  x  - 2ax + b$ increa (A) $a \le b$ (C) $a < -1/2$	ses for (B) a = (D) a ≥	= b/2
3.	Area of the triangle formed by the posit $x^2 + y^2 = 4$ at $(1, \sqrt{3})$ is	ive x-a	xis and the normal and the tangent to
	(A) $2\sqrt{3}$ sq. units (C) $4\sqrt{3}$ sq. units	` '	sq. units ne of these
4.	A tangent to the curve $y = \frac{x^2}{2}$ which is para	allel to t	he line y = x cuts off an intercept from the
	y-axis is (A) 1 (C) 1/2	(B) -1. (D) -1.	
5.	A particle moves on a co-ordinate line so Then distance travelled by the particle durin (A) 4/3 (C) 16/3		me interval $0 \le t \le 4$ is
6.	The derivative of f (x) = $ x $ at x = 0 is (A) 1 (C) -1	(B) 0 (D) do	es not exist
7.	$f(x) = -[x^2 + 3x^4 + 5x^6 + 5]$ have only	· val	ue in $(-\infty,\infty)$ at $x =$
8.	If $y = a \log  x  + bx^2 + x$ has its extremum $y$	alues a	t x = -1 and x =2 then a=
	b =		
9.	The value of b for which the function $f(x) = $ is given by	sin x –b	ox + c is decreasing in the interval $(-\infty,\infty)$
	(A) b < 1 (C) b > 1	(B) b ≥ (D) b ≤	
10.	Equation of the tangent to the curve $y = e^{- x }$ (A) is $ey + x = 2$ (C) is $ex + y = 1$	at the	point where it cuts the line x=1 (B) is x + y = e (D) does not exist
11.	The greatest and least values of the functio the interval [0,1] are	n f(x) =	$ax + b \sqrt{x + c}$ , when $a > 0$ , $b > 0$ , $c > 0$ in
	(A) a+b+c and c	(B)	a/2 b√2+c, c
	(C) $\frac{a+b+c}{\sqrt{2}}$ , c	(D)	None of these



	(C) 1	(D) does not exist
23.	Pick up the correct statement of the followir (A) If $f(x)$ is continuous at $x = a$ then $[f(x)]$ (B) If $f(x)$ is continuous at $x = a$ then $[f(x)]$ (C) If $ f(x) $ is continuous at $x = a$ then $f(x)$ (D) None of these	is differentiable at $x = a$ .
24.	The greatest value of f (x) = $\cos (xe^{[x]} + 7x^2)$ (A) -1 (C) 0	-3x), x ∈ [-1, ∞) is (B) 1 (D) none of these.
25.	The equation of the tangent to the curv y = 2 is (A) $x + 2y = 2$ (C) $x - 2y = 1$	The f (x) = 1 + $e^{-2x}$ where it cuts the line (B) 2x + y = 2 (D) x - 2y + 2 = 0
26.	The angle of intersection of curves $y = 4 - x$	$^{2}$ and y = $x^{2}$ is
27.		$\frac{\sin 2x}{\ln \left(x + \frac{\pi}{4}\right)}$ on the interval $\left[0, \frac{\pi}{2}\right]$ is
28.	Let $f(x) = x - \sin x$ and $g(x) = x - \tan x$ , when	Te $x \in \left(0, \frac{\pi}{2}\right)$ . Then for these value of x.
	(A) $f(x)$ , $g(x) > 0$	(B) $f(x) \cdot g(x) < 0$
	(C) $\frac{f(x)}{g(x)} > 0$	(D) none of these
29.	Suppose that $f(x) \ge 0$ for all $x \in [0, 1]$ an $\forall x \in [0, 1]$ , f is	d f is continuous in [0, 1] and $\int_{0}^{1} f(x)dx = 0$ , then
	(A) entirely increasing (B) (C) constant (D)	entirely decreasing None of these

#### LEVEL-II

- 1. Let h (x) = f (x) +  $\ln\{f(x)\}$  +  $\{f(x)\}^2$  for every real number x, then
  - (A) h (x) is increasing whenever f (x) is increasing
  - (B) h (x) is increasing whenever f (x) is decreasing
  - (C) h (x) is decreasing whenever f (x) is increasing
  - (D) nothing can be said in general
- 2. Let  $f(x) = a_0 + a_1x^2 + a_2x^4 + \dots + a_nx^{2n}$ , where  $0 < a_0 < a_1 < a_2 < \dots < a_n$ , then f(x) has
  - (A) no minimum

(B) only one minimum

(C) no maximum

- (D) neither a maximum nor a minimum
- 3. The maximum value of  $\frac{\sin x \cos x}{\sin x + \cos x}$  in the interval  $\left[0, \frac{\pi}{2}\right]$  is
  - (A) 1/2

(B) 1/4

(C)  $\frac{1}{2\sqrt{2}}$ 

- (D) 1/3
- 4. If  $y = \sqrt{\sin x + \sqrt{\sin x + \sqrt{\sin x + \dots + \infty}}}$ , then the value of  $\frac{dy}{dx}$  is
  - (A)  $\sqrt{\frac{\sin x}{y+1}}$

(B)  $\frac{\sin x}{v+1}$ 

(C)  $\frac{\cos x}{2y+1}$ 

- (D)  $\frac{\cos x}{2y-1}$
- 5. The curve  $y e^{xy} + x = 0$  has a vertical tangent at the point
  - (A) (1, 1)

(B) at no point

(C)(0,1)

- (D) (1, 0)
- 6. A differentiable function f(x) has a relative minimum at x = 0 then the function y = f(x) + ax + b has a relative minimum at x = 0 for
  - (A) all a and all b

(B) all b if a = 0

(C) all b > 0

- (D) all  $a \ge 0$
- 7. Let  $f(x) = \begin{cases} 1 + \sin x, & x < 0 \\ x^2 x + 1, & x \ge 0 \end{cases}$ . Then
  - (A) f has a local maximum at x = 0
- (B) f has a local minimum at x = 0
- (C) f is increasing every where
- (D) f is decreasing everywhere
- 8. Let  $f(x) = x^{n+1} + a$ .  $x^n$ , where 'a' is a positive real number,  $n \in I^+$ . Then x = 0 is a point of
  - (A) local minimum for any integer n
- (B) local maximum for any integer n
- (C) local minimum if n is an even integer
- (D) local minimum if n is an odd integer
- 9.  $f(x) = max (sinx, cosx) \forall x \in R$ . Then number of critical points  $\in [-2\pi, 2\pi]$  is /are;
  - (A) 5

(B) 7

(C) 9

- (D) none of these
- 10. Let  $\phi(x) = (f(x))^3 3(f(x))^2 + 4f(x) + 5x + 3 \sin x + 4 \cos x$   $\forall x \in R$ , then
  - (A) φ is increasing whenever f is increasing
  - (B) φ is increasing when ever f is decreasing
  - (C)  $\phi$  is decreasing whenever f is decreasing

- (D) Nothing can be said
- 11. A function  $f(x) = \frac{x^2 3x + 2}{x^2 + 2x 3}$  is:
  - (A) Maximum at x = -3

- (B) Minimum at x = -3 and maximum at x = 1
- (C) No point of maxima or minima
- (D) Function is decreasing in it's domain.
- 12. Let  $f(x) = \begin{cases} \sin(x^2 3x) & x \le 0 \\ 5x^2 + 6x & x > 0 \end{cases}$ . Then f(x) has
  - (A) local maxima at x = 0

- (B) Local minima at x = 0
- (C) Global maxima at x = 0
- (D) Global minima at x = 0
- 13. If a, b, c, d are four positive real numbers such that abcd =1, then minimum value of (1+a) (1+b) (1+c) (1+d) is
  - (A) 8

(B) 12

(C) 16

- (D) 20
- 14. If  $f(x) + 2f(1-x) = x^2 + 2 \forall x \in \mathbb{R}$ , then f(x) is given as
  - (A)  $\frac{(x-2)^2}{3}$

(B)  $x^2 - 2$ 

(C) 1

- (D) None of these
- 15.  $\lim_{x\to 5\pi/4} [\sin x + \cos x]$ , where [ . ] denotes the Integral part of x.
  - (A) is equal to -1

(B) is equal to -2

(C) is equal to -3

- (D) Does not exist
- 16. If  $f(x) = \frac{\ln(1+x)^{1+x}}{x^2} \frac{1}{x}$ , then the value of f(0) so that f(x) is continuous at x = 0, is;
  - (A) 2

(B)

(C)1/2

(D) None of these

- 17. If f (x) =  $\frac{x}{1+|x|}$ , then
  - (A) f (x) is differentiable  $\forall x \in R$
- (B) f (x) is no where differentiable
- (C) f (x) is not differentiable at finite no. of point
- (D) None of these
- 18. If  $f_1(x) = \sin x + \tan x$ ,  $f_2(x) = 2x$  then
  - (A)  $f_1(x) > f_2(x) \forall x \in (0, \pi/2)$
  - (B)  $f_1(x) < f_2(x) \forall x \in (0, \pi/2)$
  - (C)  $f_1(x) f_2(x) = 0$  has exactly one root  $\forall x \in (0, \pi/2)$
  - (D) None of these
- 19. Let  $f(x) = \begin{cases} |x-1| + a, & x \le 1 \\ 2x + 3, & x > 1 \end{cases}$ . If f(x) has a local minima at x = 1. Then exhaustive set of
  - values of 'a' is;
  - (A)  $a \le 4$

(B)  $a \le 5$ 

(C)  $a \le 6$ 

- (D)  $a \le 7$
- 20. A differentiable function f(x) has a relative minimum at x = 0 then the function y = f(x) + ax + b has a relative minimum at x = 0 for

	(B) all a and all b (D) all b > 0	(B) all b if $a = 0$ (D) all $a \ge 0$
21.	The maximum value of $f(x) =  x \ln x $ in $x \in (0)$	,1) is;
	(A) 1/e (C) 1	(B) e (D) none of these
22.	If f (x) = $\int_{0}^{x} (t+1) (e^{t}-1) (t-2) (t+4) dt$ then f	(x) would assume the local minima at;
	(A) $x = -4$ (C) $x = 1$	(B) $x = 0$ (D) $x = 2$ .
23.	$f(x) = tan^{-1} (sinx + cosx)$ is an increasing fun (A) $(0, \pi/4)$ (C) $(-\pi/4, \pi/4)$	ction in (B) $(0, \pi/2)$ (D) none of these.
24.	Let f: $R \rightarrow R$ , where $f(x) = x^3$ - ax, $a \in R$ . Then its entire domain is;	set of values of 'a' so that f(x) is increasing in
	(A) (-∞, 0) (C) (-∞, ∞)	(B) $(0, \infty)$ (D) none of these
25.	The curves $y = 4x^2 + 2x - 8$ and $y = x^3 - x +$	10 touch each other at the point
26.	Let f be differentiable for all x. if f (1) = -2 a (A) f (6) < 8 (C) f (6) $\geq$ 5	and f' $(x) \ge 2$ for all $x \in [1, 6]$ , then $(B) f (6) \ge 8$ $(D) f (6) \le 5$
27.	The function f (x) = $\frac{2x^2 - 1}{x^4}$ decreases in the	ne interval
28.	The function $f(x) = (x + 2) e^{-x}$ increases in decreases in	and
29.	The function $y = x - \cot^{-1} x - \log (x + \sqrt{x^2 + \cos x})$ (A) $(-\infty, 0)$ (C) $(0, \infty)$	-1) is increasing on (B) $(-\infty,\infty)$ (D) R $-\{0\}$
30.	Let f: $(0, \infty) \to R$ defined by $f(x) = x + \frac{9\pi^2}{x}$	+ cos x . Then minimum value of f(x) is
	(A) 10π – 1 (C) 3π – 1	(B) $6\pi - 1$ (D) none of these
31.	Let $a, n \in \mathbb{N}$ such that $a \ge n^3$ then $\sqrt[3]{a+1}$	- <sup>3</sup> √a is always
	(A) less than $\frac{1}{3n^2}$	(B) less than $\frac{1}{2n^3}$
	(C) more than $\frac{1}{n^3}$	(D) more than $\frac{1}{4n^2}$
32.	The global minimum value of function $f(x) = (A)$	$= x^3 + 3x^2 + 10x + \cos \pi x$ in [-2,3] is (B) 3-2 $\pi$

	(C)	16-2π		(D)	-15	5		
33.	The m (A) (C)	inimum value of the function do 0 1	efined t (B) (D)	oy f(x) = 1/2 3/2	= Ma	aximum {x, x+	-1, 2-x} is	
LEVE	L-III							
1.				(B) 144	4	and $a \in [1, 3]$ , of these	then differe	ence between
2.		$\beta$ and $\gamma$ be the roots of f(x) = eatest integer function, is equa		-5x -1 (B) - 2 (D) - 3		). Then $[lpha]$ + $[$	$eta]$ +[ $\gamma$ ], whe	ere [.] denotes
3.	The nu (A) 0 (C) 2	umber of solutions of the equat	ion x <sup>3</sup> +	+2x <sup>2</sup> +5 (B) 1 (D) 3	x +	2cosx = 0 in [	[0, 2π] is	
4.	f(x)=2	•	ralues actly on	of pa e local (B) (-3 (D) (-0	max , 3)	ximum and ex	r which t cactly one lo	the equation ocal minimum.
5.	functio (A) Dif (C) not	der a function y = f (x) defined price of the first state of the first		(B) nor	n-di	x = 2t +  t , y		∈ R. then
6.	If the lin	ne $ax + by + c = 0$ is normal to	the cur	ve x y +	+ 5 =	= 0 then		
	(A) a >	0 , b > 0		(B) b	> 0	, a < 0		
	(C) a <	< 0 , b < 0		(D) b	< 0	, a > 0		
7.	The nui (A) One (C) Thre		[1,2] is	(B) Tw		of these		
8.		c f(x) vanishes at $x = -2$ and h $(x) = \dots$	as extr	ema at	x =	$x = -1 \text{ and } x = \frac{1}{3}$	such that	$\int_{1}^{-1} f(x) dx = \frac{14}{3}$
9.	If g(x)	= f(x) + f(1-x) and $f''(x) < 0, 0$	$\leq x \leq 1$ ,					
	(A) g(	x) is decreasing in (0, 1)		(B) g(x	k) is	decreasing ir	$1\left(0,\frac{1}{2}\right)$	

	(C) g(x) is decreasing in $\left(\frac{1}{2}, 1\right)$	(D) g(x) is increasing in (0, 1)
10.	Let $g'(x) > 0$ and $f'(x) < 0 \ \forall \ x \in R$ then (A) $g(f(x + 1)) > g(f(x - 1))$ (C) $g(f(x + 1) < g(f(x - 1))$	(B) $f(g(x-1)) < f(g(x+1))$ (D) $g(g'(x+1)) < g(g(x+1))$
11.	The function $f(x) = \frac{ax+b}{(x-1)(x-4)}$ has a loc	cal maxima at (2, -1) then
40	(A) $b = 1$ , $a = 0$ (C) $b = -1$ , $a = 0$	(B) a = 1, b = 0 (D) None of these
12.	$f_1(x) = 2x$ , $f_2(x) = 3\sin x - x - \cos x$ , then (A) $f_1(x) < f_2(x)$	for $x \in (0, \pi/2)$ : (B) $f_1  x  < f_2  x $
	(C) $f_1(x) > f_2(x)$	(D) $f_1  x  > f_2  x $
13.	y = f(x) is a parabola, having its axis paralle at $x = 1$ then	I to $y - axis$ . If the line $y = x$ touches this parabola
	(A) $f''(1) - f'(0) = 1$ (C) $f''(1) + f'(0) = 1$	(B) $f''(0) - f'(1) = 1$ (D) $f''(0) + f'(1) = 1$
14.	If $f(x) = 2e^x - ae^{-x} + (2a+1)x - 3$ is increasing (A) $a \in (-\infty, \infty) - \{0\}$ (C) $a \in (0, \infty)$	ng for all values of 'x' then (B) $a \in (-\infty, 0]$ (D) $a \in [0, \infty)$
15.	If $2a + 3b + 6c = 0$ , then equation $ax^2 + bx + (A)(0, 1)$ (C) (1, 2)	c=0 has roots in the interval (B) (2, 3) (D) (0, 2)
16.	The equation $3x^2 + 4ax + b = 0$ has at least (A) $4a + b + 3 = 0$ (C) $b = 0$ , $a = -4/3$	one root in $(0, 1)$ if (B) $2a + b + 1 = 0$ (D) None of these
17.	If f(x) satisfies the conditions of Rolle's theo	rem in [1, 2] then $\int_{-\infty}^{2} f'(x) dx$ is equal to
	(A) 3 (C) 1	(B) 0 (D) -1
18.	If $f(x) = x^2 e^{-x^2/a^2}$ is a non-decreasing function (A) $x \in [a, 2a)$ (C) $x \in (-a, 0)$	on then for $a > 0$ ; (B) $x \in (-\infty, -a] \cup [0, a]$ (D) None of these
19.	The function $f(x) = \frac{x}{1 + x \tan x}$ has	
	<ul> <li>(A) One point of minimum in the interval (0,</li> <li>(B) One point of maximum in the interval (0,</li> <li>(C) No point of maximum, no point of minim</li> <li>(D) Two points of maximum in (0, π/2)</li> </ul>	, π/2)
20.		$g(x) + g(x) = 0$ , where a > 0, $g(x) \neq 0$ and has
	(A) 1 (C) 4	(B) 2 (D) 0

### **ANSWERS**

#### LEVEL -I

1.	Α	2.	С	3.	Α	4.	D
5.	С	6.	D	7.	0	8.	2, -1/2
9.	С	10.	Α	11.	Α	12.	В
13.	С	14.	D	15.	Α	16.	D
17.	Α	18.	С	19.	С	20.	D
21.	С	22.	С	23.	С	24.	В
25.	В	26.	$2\sqrt{2}$	27.	$\sqrt{2}$	28.	В
29.	С						

#### LEVEL -II

1.	Α	2.	В	3.	С		D
5.	D	6.	В	7.	Α	8.	С
9.	В	10.	Α	11.	С	12.	В
13.	С	14.		15.	В	16.	С
17.	С	18.	Α	19.	В	20.	В
21.	Α		D	23.	С	24.	Α
25.	3, 34; $-\frac{1}{3}$ ,	$-\frac{74}{9}$		26.	В	27.	$\left(-\frac{1}{2},0\right)\cup\left(\frac{1}{2},\infty\right)$
28.	(0, 1); R -	(0, 1)		29.	В	30.	В
31.	À	32.	D	33.	С		

#### LEVEL -III

1. 5.	C A	2. 6. A, C	3. 7.		4. 8.	D $-x^3 - x^2 + x - 2$
9. 13. 17.	C C B	10. C 14. D 18. B	11. 15. 19.	Α	12. 16. 20.	В