

COURSE
NUCLEUS

JEE-MAIN MOCK TEST-6
XII

TEST CODE
1 1 2 7 8

Q.No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	4	2	4	1	4	3	2	3	3	1	2	3	4	4	3
Q.No.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans	2	3	3	2	3	3	3	1	1	1	3	2	3	2	3
Q.No.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans	2	4	2	2	1	3	1	1	3	1	4	4	4	1	3
Q.No.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans	3	3	3	2	4	2	3	2	4	2	3	1	2	3	3
	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC
Q.No.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75
Ans	1	2	3	1	3	3	4	4	4	1	1	2	3	3	4
	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC	IOP	OC	PC
Q.No.	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90
Ans	3	4	2	1	2	2	2	4	2	1	3	3	2	2	4

HINTS & SOLUTIONS**PHYSICS**

Q.1 $A = 2 + |T - 2|$
 for $t \leq 2$
 $a = 2 - t + 2$
 $a = 4 - t$
 $dv = (4 - t) dt$
 $v = 4t - t^2/2$
 at $t = 2$, $v = 6$ m/s
 for $t > 2$
 $a = 2 + t - 2 = t$
 $\int_6^v dv = \int_2^t t dv$
 $v - 6 = \left[t^2/2 \right]_2^t$
 $v = \frac{t^2}{2} + 4$
 at $t = 4$, $v = 12$ m/s

Q.3 Friction force on upper block is $f = ma$
 So work done $= ma \times 5$

Q.4 $T = \frac{2\pi R_2}{\sqrt{\frac{GM}{R_2}}}$

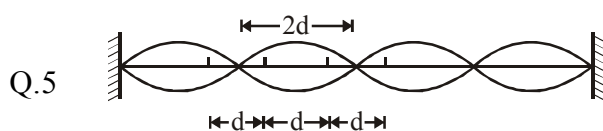
$$\Rightarrow \frac{GM}{R_2^3} = \frac{4\pi^2}{T^2}$$

$$g = \frac{GM}{R_1^2} = \frac{4\pi^2 R_2^3}{T^2 R_1^2}$$

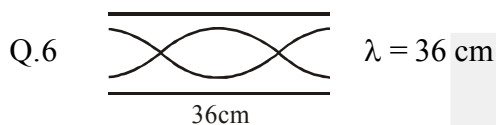
$$\frac{1}{4\pi\epsilon_0} \left(\frac{-2Q}{PA} \right) + \frac{1}{4\pi\epsilon_0} \frac{Q}{PB} = 0$$

$$\frac{2}{PA} = \frac{1}{PB} \Rightarrow 4PB^2 - 4PB^2 = PA^2$$

$$(x - 5a)^2 + y^2 = (4a)^2$$



length of string is $8d$.



frequency remains same

$$\text{now } C = \sqrt{\frac{rRT}{M}} = f\lambda$$

$$\Rightarrow \frac{\lambda}{\sqrt{T}} = \text{constant}$$

Q.7 Say speed of boat is v w.r.t. water and speed of river is C . Then, distance travelled in ground frame

$$= (c + v) \times \frac{1}{2} \text{ hour} + (v - c) \times \frac{1}{2} \text{ hour}$$

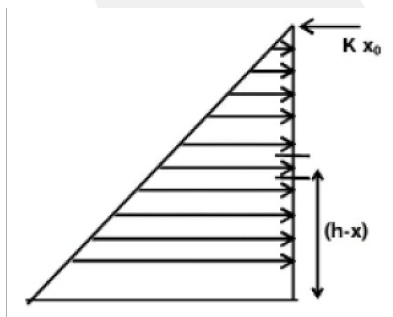
$$= v \times 1 \text{ hour}$$

= distance travelled by boat w.r.t. river.

Q.8
$$kx_0 h = \int_0^h (b dx) \rho g x (h - x)$$

$$\Rightarrow kx_0 h$$

$$= b \rho g \int_0^h (hx - x^2) dx = b \rho g \left[h \frac{h^2}{2} - \frac{h^3}{3} \right]$$



$$\Rightarrow kx_0 h = b \rho g \frac{h^3}{6} \Rightarrow x_0 = \frac{b \rho g h^2}{6k}$$

$$PE = \frac{1}{2} kx_0^2 = \frac{1}{2} k \frac{b^2 \rho^2 g^2 h^4}{36k^2} = \frac{b^2 \rho^2 g^2 h^4}{72k}$$

Q.9
$$T = 2\pi\sqrt{LC}$$

In SHM time from A to $\frac{A}{2}$ is $\frac{T}{6}$ so here also

it is $\frac{T}{6}$.

Q.10 Spring time period is always

$$T = 2\pi\sqrt{\frac{m}{k}}$$

Q.11 Initial extension is $x = \frac{mg}{k}$

at mean position

$$F + mg = k \left(\frac{mg}{k} + y \right)$$

$$y = \frac{F}{m} = A \text{ (amplitude of SHM)}$$

maximum displacement is $2A$.

Q.12
$$\frac{dT}{dx} = -\frac{l}{kA}$$

Q.13
$$\omega = F \times \frac{\pi R}{2} = \mu mg \times \frac{\pi l}{2}$$

Q.14 The cylinder will step so
 $f = \mu mg \cos \theta$

Q.15 Centre of mass falls vertically down so that mass m falls at origin.

Q.16
$$H_{\max} = \frac{(20)^2 \sin^2 \theta}{2g} \leq 5$$

$$\Rightarrow \sin \theta \leq \frac{1}{2} \Rightarrow \theta \leq 30^\circ$$

$$\therefore R = \frac{(20)^2 \sin 2\theta}{g} \rightarrow \text{max. for } \theta = 30^\circ$$

$$\Rightarrow R_{\max} = 20\sqrt{3} \text{ m.}$$

Q.17 $T_A = T_B = T(\text{say})$

$$\text{Now } V_A = \frac{nRT}{16P_0} = V$$

$$\Rightarrow V_B = V_C = \frac{nRT}{2P_0} = 8V$$

Now in A $\rightarrow C$, $16 P_0 V^\gamma = P_0 (8V)^\gamma$

$$\Rightarrow \gamma = \frac{4}{3} \Rightarrow C_V = \frac{R}{\gamma - 1} = 3R$$

- Q.18 Both waves at M from P and Q are in same phase as originated.

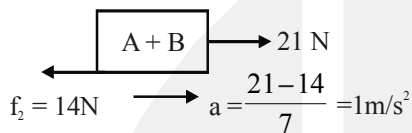
\therefore Constructive interference

$$\Rightarrow I = \left(\sqrt{I_0} + \sqrt{\frac{I_0}{4}} \right)^2 = \frac{9I_0}{4}$$

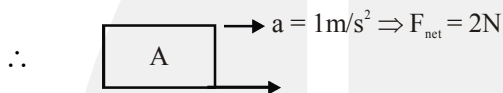
- Q.19 $f_{1\max}$ (between A and B) = $0.4 \times 20 = 8 \text{ N}$

$$f_{2\max} \text{ (between B and ground)} = 0.2 \times 70 = 14 \text{ N}$$

Assuming system,



$$f_2 = 14 \text{ N} \quad \rightarrow a = \frac{21 - 14}{7} = 1 \text{ m/s}^2$$



$$\therefore \quad \rightarrow a = 1 \text{ m/s}^2 \Rightarrow F_{\text{net}} = 2 \text{ N}$$

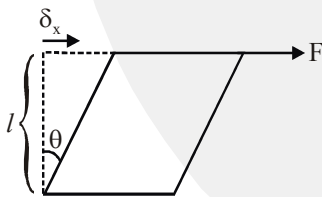
$$\therefore f_1 = 2 \text{ N} < f_{1\max} \Rightarrow \text{Assumption correct}$$

$$\therefore f_1 - f_2 = 2 \text{ N.}$$

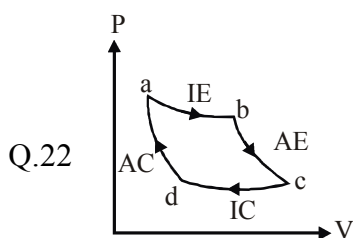
- Q.20 $2Sl = 1.8 \times 10^{-2} \text{ N}$

$$\Rightarrow S = \frac{1.8 \times 10^{-2}}{2 \times 0.1} = 0.09 \text{ N/m}$$

- Q.21 $\theta \approx \frac{\delta x}{l} = \frac{1.2 \times 10^{-4}}{5 \times 10^{-2}}$



$$\therefore \eta = \frac{F/A}{\theta} = 1.67 \times 10^{10} \text{ N/m}^2$$



- Q.22

- Q.23 By equation of continuity, 'A' in horizontal pipe \rightarrow constant $\Rightarrow v \rightarrow$ constant \Rightarrow same 'P' at all points.

Q.24 $\alpha = -\omega \frac{d\omega}{d\theta} \propto \theta = -k\theta$

$$E = \frac{1}{2} I \omega^2 \Rightarrow \frac{dE}{d\theta} = \frac{1}{2} I \cdot 2\omega \frac{d\omega}{d\theta} = -k I \theta$$

$$\therefore \int dE = -k I \int \theta d\theta \Rightarrow \Delta E \propto \theta^2$$

- Q.25 On earth's surface, $\sigma = \frac{x \text{prg}}{2}$

In the mine, $\sigma = \frac{y \text{prg}_d}{2}$

Dividing, we get $\frac{x}{y} = \frac{g_d}{g}$

$$= \frac{g \left(1 - \frac{d}{R} \right)}{g} = 1 - \frac{d}{R}$$

Hence the correct choice is (1)

- Q.26 $f = M \Rightarrow M = \frac{\text{Tesla} - \text{m}^2}{\text{Ampere}}$

$$F = qVB$$

$$\Rightarrow \text{Tesla} = \frac{\text{N}}{\text{coulomb} \times (\text{meter} / \text{second})}$$

$$\frac{\text{kg} - \text{ms}^2}{\text{Ampere} \times \text{meter}} = \frac{\text{kg} - \text{s}^{-2}}{\text{Ampere}}$$

$$M = \frac{\text{kg} - \text{m}^2 \text{s}^{-2}}{\text{Ampere}^2} \Rightarrow \text{ML}^2 \text{T}^{-2} \text{A}^{-2} = [\text{M}]$$

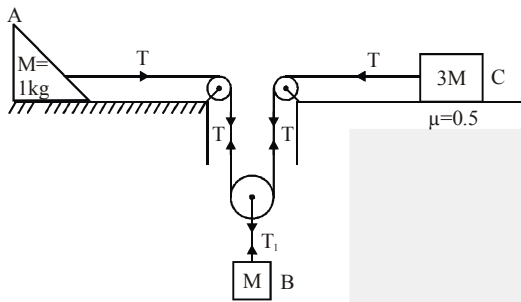
Also, $\frac{L}{R} = T$

$$CR = T \Rightarrow LC = T^2$$

$$\therefore C = \frac{T^2}{L} = \frac{T^2}{M}$$

$$\Rightarrow [C] = \text{M}^{-1} \text{T}^{-2} \text{A}^2$$

- Q.27 Clearly the block on the right hand side will not move



$$\begin{aligned} Mg - 2T &= Ma_B \\ T &= Ma_A = 2Ma_B \quad (\text{constraint}) \\ 2T &= 4M a_B \\ Mg &= 5M a_B \end{aligned}$$

$$a_B = \frac{g}{5} = 2 \text{ m/s}^2$$

$$T_1 = 2T = 4M \times 2 = 8 \text{ N}$$

$$W = 8 \times \left(-\frac{1}{2} \times 2 \times 1^2 \right) = -8 \text{ J}$$

- Q.28 $1 \times 0.6 = v_B \times 0.3$, $v_B = 2 \text{ m/s}$
 Force = $\rho A V^2 = 10^3 (0.3)(2 \times 2) = 1.2 \times 10^3$

Q.29 $B = 10 \log_{10} \left(\frac{I}{I_0} \right)$

$$\Rightarrow \frac{I}{I_0} = 10^{B/10}$$

$$\Rightarrow I = \frac{P}{4\pi r^2} = I_0 10^{0.1B}$$

$$\Rightarrow P = 4\pi r^2 I_0 10^{0.1B}$$

$$I_R = \frac{4\pi r^2 I_0 10^{0.1B}}{4\pi R^2} = \frac{r^2}{R^2} [I_0] 10^{0.1B}$$

- Q.30 Before collision $v_0 = \vec{u}$; $\vec{v}_m = 0$

$$v_3 = -\vec{u}$$

After collision

$$v_0 = 0; v_m = \vec{u}$$

$$v_3 = 3\vec{u}$$

MATHEMATICS

Q.31 $\log_4 \left(\frac{3-x}{3+x} \right) = \log_4 \left(\frac{1-x}{2x+1} \right)$

$$\Rightarrow \frac{3-x}{3+x} = \frac{1-x}{2x+1}$$

$$(3-x)(2x+1) = (1-x)(3+x)$$

$$5x - 2x^2 + 3 = 3 - 2x - x^2$$

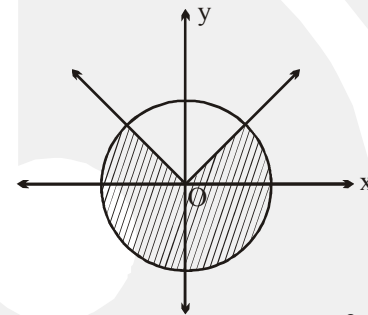
$$x^2 - 7x = 0 \Rightarrow x = 0 \text{ or } x = 7.$$

Reject $x = 7$; as domain $= x \in \left(\frac{-1}{2}, 1 \right)$.

\therefore Only solution is $x = 0$.

- Q.32 From the first radical sign $x^2 + y^2 \leq 16$ i.e. interior of a circle with circle $(0, 0)$ and radius 4.
 From the 2nd radical sign $y \leq |x|$

i.e. $\frac{3}{4}$ th of the circle



$$\therefore \text{Required area} = (\pi \cdot 16) \frac{3}{4} = 12\pi. \text{ Ans.}$$

- Q.33 $D = 0$ gives $m = 6, \frac{2}{3}$

Q.34 Seperable $\int_0^y e^y dy = \int_0^x (2 + \cos x) dx$

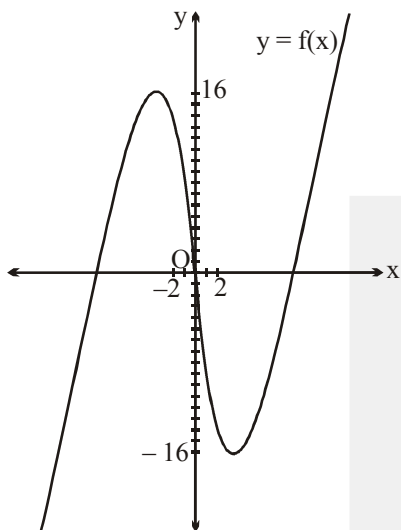
$$\Rightarrow e^y - 1 = 2x + \sin x$$

For $x = \frac{\pi}{2}$, we find $y = \ln(2 + \pi)$. **Ans.**

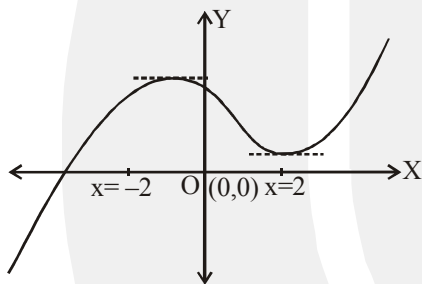
- Q.35 Let $y = f(x) = x^3 - 12x$ and $y = -a$
 For $f(x) = -a$ to have exactly one real root, we must have

$$-a > 16 \text{ or } -a < -16$$

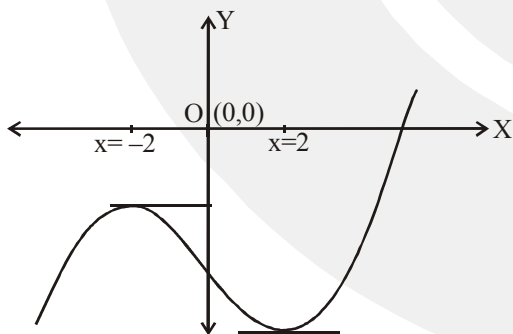
$$\Rightarrow a \in (-\infty, -16) \cup (16, \infty)$$

**Ans.**

Alternate: Let $f(x) = x^3 - 12x + a$
 $f'(x) = 3x^2 - 12 = 3(x+2)(x-2)$
 \therefore The equation $f(x) = 0$
 has exactly one real root, if
 $f(-2)f(2) > 0 \Rightarrow (16+a)(-16+a) > 0$
 $\Rightarrow (a-16)(a+16) > 0$
 $\therefore a \in (-\infty, -16) \cup (16, \infty)$



OR

Two possible graph of $f(x)$. **Ans.**

$$\begin{aligned} \text{Q.36} \quad \sum_{r=1}^{15} r \cdot \frac{a_r}{a_{r-1}} &= \sum_{r=1}^{15} r \cdot \frac{{}^{15}C_r}{{}^{15}C_{r-1}} \\ &= \sum_{r=1}^{15} r \cdot \frac{(15)!}{(15-r)!r!} \times \frac{(r-1)!(15-r+1)!}{(15)!} \\ &= \sum_{r=1}^{15} (16-r) = (1+2+3+\dots+15) \\ &= \frac{15 \times 16}{2} = 120. \end{aligned}$$

Q.37 Using LMVT, \forall some $c \in (1, 8)$ s. t.

$$\begin{aligned} f'(c) &= \frac{f(8)-f(1)}{7} = \frac{f(8)-3}{7} \leq 1.4 \\ f(8) &= 9 \cdot 8 + 3 = 12.8 \text{ Ans.} \end{aligned}$$

$$\begin{aligned} \text{Q.38} \quad \therefore \int (x^9 + x^6 + x^3)(2x^6 + 3x^3 + 6)^{\frac{1}{3}} dx \\ &= \int (x^8 + x^5 + x^2)(2x^9 + 3x^6 + 6x^3)^{\frac{1}{3}} dx \\ \text{Let } 2x^9 + 3x^6 + 6x^3 &= t \\ \Rightarrow 18(x^8 + x^5 + x^2)dx &= dt \\ \therefore I &= \int \frac{t^{1/3}}{18} dt = \frac{1}{18} \cdot \frac{t^{4/3}}{4/3} + C = \frac{1}{24} t^{4/3} + C \\ \therefore AB &= 24 \times \frac{4}{3} = 32 \text{ Ans.} \end{aligned}$$

$$\begin{aligned} \text{Q.39} \quad \cos \theta + \sqrt{3} \sin \theta &= 2 \sin \theta \\ \Rightarrow \cot \theta &= 2 - \sqrt{3} \text{ and } \tan \theta = 2 + \sqrt{3} \\ \frac{\sin \theta - \sqrt{3} \cos \theta}{\cos \theta} &= \tan \theta - \sqrt{3} \\ &= 2 + \sqrt{3} - \sqrt{3} = 2 \text{ Ans.} \end{aligned}$$

Q.40 Use L'Hospital's rule

$$\begin{aligned} \lim_{x \rightarrow \infty} \frac{(\tan^{-1} x) \sqrt{x^2 + 1}}{x} ; \frac{\pi}{2} \lim_{x \rightarrow \infty} \frac{\sqrt{x^2 + 1}}{x} \\ = \frac{\pi}{2} \text{ Ans.} \end{aligned}$$

Q.41 We know that

$\frac{\sin \theta}{\theta}$ and $\frac{\theta}{\tan \theta}$ both are decreasing functions

of θ in $\left(0, \frac{\pi}{2}\right)$. So maximum value, when

$\theta \rightarrow 0$ is $1 + 1 = 2$ and minimum value, when

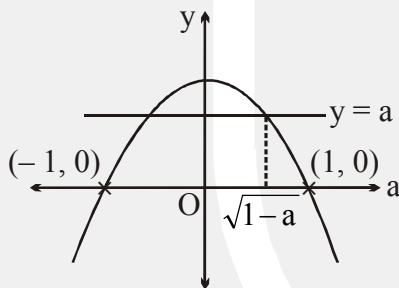
$\theta \rightarrow \frac{\pi}{2}$ is $\frac{2}{\pi}$.

$$Q.42 \quad T_n = \frac{(n+1)^2 - n}{n(n+1)} = 1 + \left(\frac{1}{n} - \frac{1}{n+1}\right)$$

$$\therefore S_{10} = 10 + \left(1 - \frac{1}{11}\right) = \frac{120}{11} \text{ Ans.}$$

$$Q.43 \quad A(a) = 2 \int_0^{\sqrt{1-a}} \left((1-x^2) - a\right) dx = \frac{4}{3} (1-a)^{3/2}$$

$$\therefore A(0) = \frac{4}{3}$$



$$\text{and } A\left(\frac{1}{2}\right) = \frac{4}{3} \left(\frac{1}{2}\right)^{3/2} \Rightarrow \frac{A(0)}{A\left(\frac{1}{2}\right)} = 2\sqrt{2}.$$

Q.44 Use expansion.

Q.45 Replace x by $(1-x)$, we get

$$\frac{f^2(1-x)}{f(x)} = (1-x)^3$$

$$\therefore f^3(x) = x^6(1-x)^3 \Rightarrow f(x) = x^2(1-x)$$

$$\Rightarrow f\left(\frac{1}{2}\right) = \frac{1}{2} \text{ Ans.}$$

$$Q.46 \quad \text{Let } u = \frac{c}{x}, \text{ so } du = \frac{-c}{x^2} dx, \text{ so } \int_1^{\sqrt{c}} \frac{f(x)}{x} dx$$

$$= \int_c^{\sqrt{c}} \frac{u f(u)}{c} \left(\frac{-x^2}{c}\right) du = \int_{\sqrt{c}}^c \frac{f(u)}{u} du$$

$$\text{Therefore, } \int_1^c \frac{f(x)}{x} dx$$

$$= \int_1^{\sqrt{c}} \frac{f(x)}{x} dx + \int_{\sqrt{c}}^c \frac{f(u)}{u} du = 3 + 3 = 6 \text{ Ans.}$$

$$Q.47 \quad 2\alpha^3 = \alpha - 1 \Rightarrow \alpha^3 = \frac{\alpha - 1}{2}$$

$$\therefore \alpha^3 + \beta^3 + \gamma^3 = \frac{1}{2}(\alpha - 1 + \beta - 1 + \gamma - 1)$$

$$= \frac{1}{2}(\alpha + \beta + \gamma - 3) = -\frac{3}{2} \text{ Ans.}$$

$$Q.48 \quad \int e^x (\tan x - x + \tan^2 x - \tan^2 x - 2 \tan x \sec^2 x) dx$$

$$= \int e^x (\tan x - x + \tan^2 x) dx - \int e^x (\tan^2 x + 2 \tan x \sec^2 x) dx$$

$$= e^x (\tan x - x - \tan^2 x) + C$$

$$f(x) = \tan x - x - \tan^2 x$$

$$f\left(\frac{\pi}{4}\right) = \frac{-\pi}{4}.$$

$$Q.49 \quad (e-1)e^{xy} + x^2 = e^{x^2+y^2} + y^2$$

$$(e-1)e^{xy}(xy' + y) + 2x = e^{x^2+y^2}(2x + 2yy')$$

$$\text{Put } x = 1 \text{ and } y = 0 \text{ to get } \left.\frac{dy}{dx}\right|_{(1,0)} = 2.$$

$$Q.50 \quad y = \left(5 - x^{2/3}\right)^{3/2}$$

$$\frac{dy}{dx} = \frac{-3}{2} \sqrt{5 - x^{2/3}} \left(\frac{2}{3}, \frac{1}{x^{1/3}}\right)$$

$$\left.\frac{dy}{dx}\right|_{M(1,8)} = \sqrt{5-1} = -2$$

When $x = 1, y = 8$

tangent is $y - 8 = -2(x - 1)$

$$2x + y = 10$$

$$\text{length of intercept} = \sqrt{100 + 25} = \sqrt{125}$$

$$\Rightarrow N = 125 \text{ Ans.}$$

Q.51 $\sin\left(\frac{5x}{6}\right) + \cos\left(\frac{10x}{9}\right) = 2$

$$\sin\left(\frac{5x}{6}\right) = 1$$

$$\Rightarrow \frac{5x}{6} = 2n\pi + \frac{\pi}{2} \Rightarrow x = (4n+1)\frac{3\pi}{5}, n \in \mathbb{I}$$

and $\cos\left(\frac{10x}{9}\right) = 1$

$$\Rightarrow \frac{10x}{9} = 2m\pi$$

$$\Rightarrow x = \frac{9m\pi}{5}, m \in \mathbb{I}$$

\therefore least common value of x is $\frac{27\pi}{5}$.

Q.52 $l = \lim_{x \rightarrow 1} k \left(\frac{x-1-\ln x}{(x-1)\ln x} \right)$

$$x = 1 + h$$

$$l = k \lim_{h \rightarrow 0} \frac{h - \ln(1+h)}{h^2} = \frac{k}{2}$$

\therefore For $\sin^{-1}\left(\frac{k}{2}\right)$ to exist

$$-1 \leq \frac{k}{2} \leq 1 \Rightarrow k \in [-2, 2]$$

Number of integers is 5. **Ans.**

Q.53 $\log_{\pi} x > 0 \Rightarrow x > 1$

For $x > 1$, $\sin^{-1} \frac{2x}{1+x^2} = \pi - 2 \tan^{-1} x$

$$\log_{\frac{1}{\pi}} (\pi - 2 \tan^{-1} x + 2 \tan^{-1} x) = \log_{\frac{1}{\pi}} (\pi)$$

$$= -1 \text{ **Ans.**}$$

Q.54 $y_1 = e^{2\sin^{-1} x} \cdot \frac{2}{\sqrt{1-x^2}} = \frac{2y}{\sqrt{1-x^2}}$

$$y_1^2 (1-x^2) = 4y^2$$

$$y_1^2 (-2x) + (1-x^2) 2y_1 y_2 = 8yy_1$$

$$(1-x^2)y_2 = xy_1 + 4y$$

$$\therefore \lambda = 4. \text{ **Ans.**}$$

Q.55 Put $x^2 - 1 = t$

$$I = \frac{1}{2} \int_0^1 \tan^{-1} t \, dt = \frac{1}{2} \left[\tan^{-1} t \cdot t \Big|_0^1 - \int_0^1 \frac{t}{1+t^2} dt \right]$$

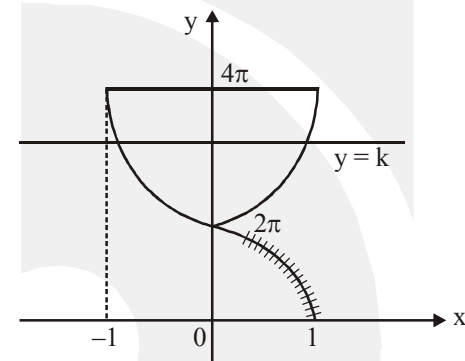
$$I = \frac{\pi}{8} - \frac{1}{2} \cdot \frac{1}{2} \ln(2) = \frac{\pi}{8} - \frac{\ln 2}{4}. \text{ **Ans.**}$$

Q.56 Graph of $y = 4 \cos^{-1}(-|x|)$

From the graph it is

Clear that $k \in (2\pi, 4\pi]$

\therefore integral values of k are 7, 8, 9, 10, 11, 12



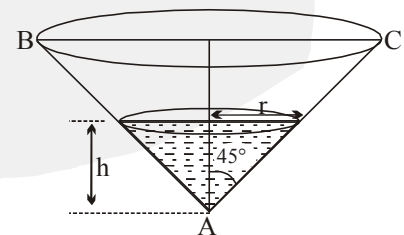
Q.57 We have

$$\frac{dV}{dt} = 2 \Rightarrow \frac{d}{dt} \left(\frac{1}{3} \pi r^3 \right) = 2$$

[Here $r = h$, as $\theta = 45^\circ$]

$$\Rightarrow \pi r^2 \frac{dr}{dt} = 2 \Rightarrow \frac{dr}{dt} = \frac{2}{\pi r^2} \dots (1)$$

Now, perimeter $= 2\pi r = p$ (let)



$$\Rightarrow \frac{d}{dt} (2\pi r) = 2\pi \left(\frac{2}{\pi r^2} \right) = \frac{4}{r^2} \dots (2)$$

(Using equation (1))

When $h = 2$ meters $\Rightarrow r = 2$ meters

Hence $\frac{dp}{dt} = \frac{4}{4} = 1$ m/sec. **Ans.**

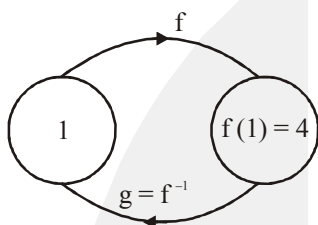
Q.58 Here, $T_n = n(2n)^2 = 4n^3$

$$\therefore S_{10} = \sum_{n=1}^{10} T_n = 4 \sum_{n=1}^{10} n^3$$

$$= 4 \left(\frac{10 \times 11}{2} \right)^2 = 4 \times (55)^2 = (2 \times 55)^2$$

$$= (110)^2 = 12100. \text{ Ans.}$$

Q.59 $g'(4) = \frac{1}{f'(1)} = \frac{1}{13} \equiv \frac{a}{b}$



So, $a = 1$ and $b = 13$
Hence, $(a + b) = 14$ **Ans.**

Q.60 $g(x) =$

$$f(|x|) = \begin{cases} -\sin(x^3) + x^3 + 1; & -\infty < x \leq -1 \\ -\sin(x^3) - x^3 - 1; & -1 \leq x < 0 \\ \sin(x^3) + x^3 - 1; & 0 \leq x < 1 \\ \sin(x^3) - x^3 + 1; & 1 \leq x < \infty \end{cases}$$

$\therefore g(x)$ is non-derivable at $x = -1, 1$.

CHEMISTRY

Q.61 $[\text{Pt}(\text{NH}_3)_2\text{Cl}_2]$
 $x + 0 + (-2) = 0$
 $x = +2$

NH_3 (Ammine)–Neutral ligand
 Cl^- (Chloride) \rightarrow Anionic ligand

* Oxidation state of Pt = +2

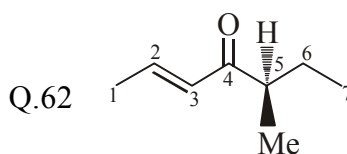
* It is a neutral complex \rightarrow

CMI name – Platinum

* Ligands are named alphabetically

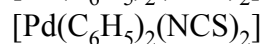
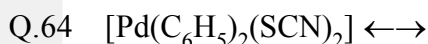
* Naming of complex \rightarrow

Diamminedichloridoplatinum(II)



(2E, 5R)-5-methylhept-2-en-4-one.

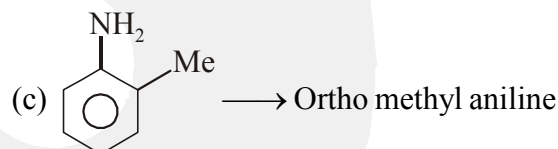
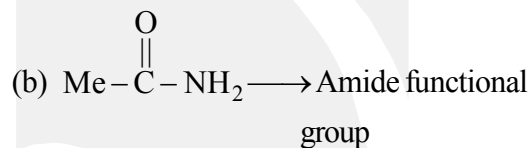
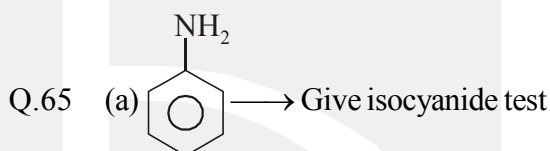
Q.63 Theory based



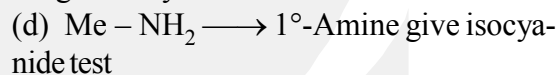
$\text{SCN} \rightarrow$ Thiocyanato

$\text{NCS} \rightarrow$ Isothiocyanato

In both complexes Pd is co-ordinated by ambidentate ligands it shows linkage isomerism.

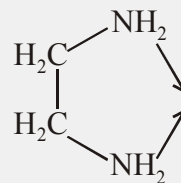


not give isocyanide test



Q.66 Theory based

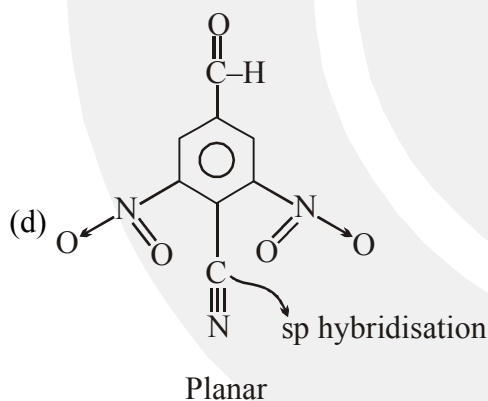
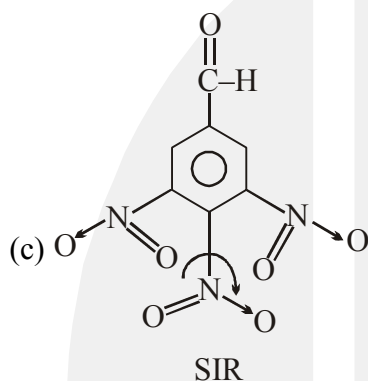
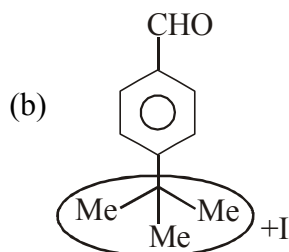
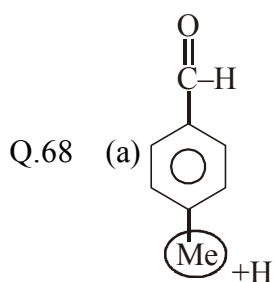
Q.67 Ethane-1, 2-diamine



* It is a neutral ligand

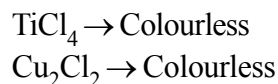
* Bidentate ligand

* Chelating ligand



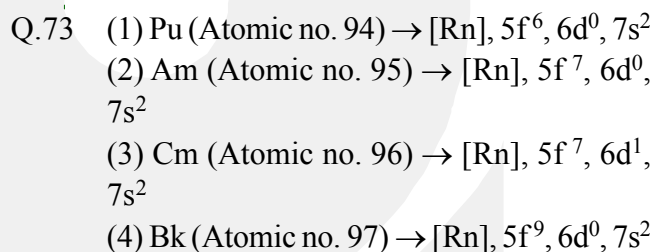
Q.69 $2d \sin \theta = n\lambda$
 $2d \sin 30^\circ = 227 \times 1$

$$d = \frac{227}{2 \times \sin 30^\circ} = \frac{227}{2 \times \frac{1}{2}} = 227 \text{ pm}$$

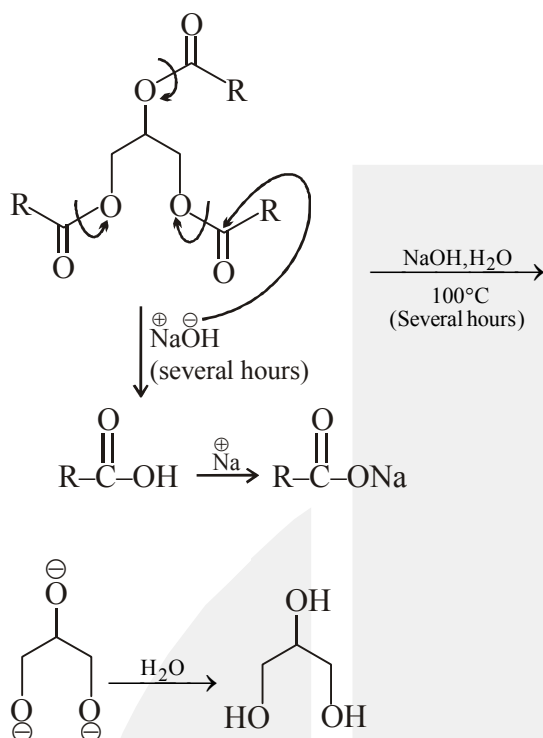


Q.71 Glucose and Fructose are monosaccharides than show mutarotation

Q.72 $K_{\text{saturated solution}} = 2.06 \times 10^{-6} \text{ ohm}^{-1} \text{ cm}^{-1}$
 $K_{\text{water}} = 4.1 \times 10^{-7} \text{ ohm}^{-1} \text{ cm}^{-1}$
 $K_{\text{CO}_2[\text{Fe}(\text{CN})_6]} = K_{\text{sol}} - K_{\text{H}_2\text{O}}$
 $= 2.06 \times 10^{-6} - 0.41 \times 10^{-6}$
 $= 1.65 \times 10^{-6} \text{ ohm}^{-1} \text{ cm}^{-1}$
 $\Lambda_m^0 [\text{Co}_2(\text{Fe}(\text{CN})_6)] = 2\Lambda_m^0 (\text{Co}^{2+}) +$
 $\Lambda_m^0 [\text{Fe}(\text{CN})_6]^{-4}$
 $= 2 \times 86 + 444$
 $= 616 \text{ ohm}^{-1} \text{ cm}^{-1} \text{ mol}^{-1}$
 For SSS
 $\Lambda_m^0 = \Lambda_m$
 $\Lambda_m = \frac{K \times 1000}{M}$
 $611 = \frac{1.65 \times 10^{-6} \times 1000}{M}$
 $M = 0.267 \times 10^{-5}$
 $S \text{ or } M = 2.67 \times 10^{-6}$



Q.74



Q.75 $k_{\text{obs}} = \left(\frac{k_1}{k_2} \right)^{1/2} \cdot k_3$

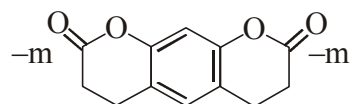
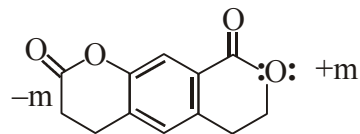
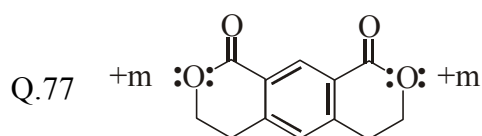
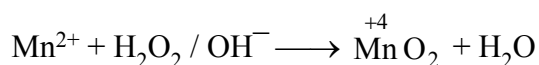
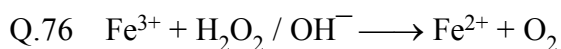
$$= \left(\frac{A_1 e^{-E_1/RT_1}}{A_2 e^{-E_2/RT_2}} \right) (A_3 e^{-E_3/RT})$$

$$= \left(\frac{A_1}{A_2} \right)^{1/2} \cdot A_3 \left[e^{\frac{-E_1+E_2}{RT}} \right]^{1/2} e^{-E_3/RT}$$

$$= \left(\frac{A_1}{A_2} \right)^{1/2} \cdot A_3 \left[e^{\frac{-\left(\frac{1}{2}(E_1-E_2)+E_3\right)}{RT}} \right]$$

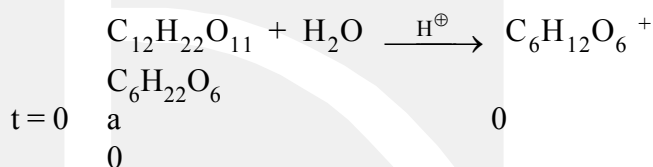
Comparing with $Ae^{-E_a/RT}$

$$E_a = E_3 + \frac{1}{2}(E_1 - E_2)$$



Increasing rate of reaction with HNO_3 / H_2SO_4 is (i) < (ii) < (iii)

Q.78 Let α , β and γ be the angle of rotation of sucrose, glucose and fructose per mol respectively.



$$\Rightarrow a \cdot \alpha = r_0 \dots (1)$$

$t = 50\%$ $a - \frac{a}{2} = \frac{a}{2}$ $\frac{a}{2}$ $\frac{a}{2}$

$$\Rightarrow \frac{a}{2}(\alpha + \beta + \gamma) = r_1 \dots (2)$$

$t = \infty$ 0 a a

$$\Rightarrow a(\beta + \gamma) = r_\infty$$

$$\frac{a}{2}(\alpha + \beta + \gamma) = r_1$$

$$a\alpha + a(\beta + \gamma) = 2r_1$$

$$r_0 + r_\infty = 2r_1$$

$$r_0 = 2r_1 - r_\infty$$

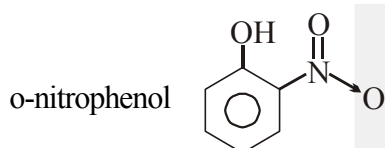
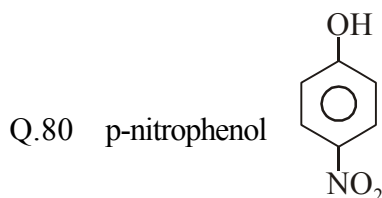
Q.79

(1) Haematite(Fe_2O_3)

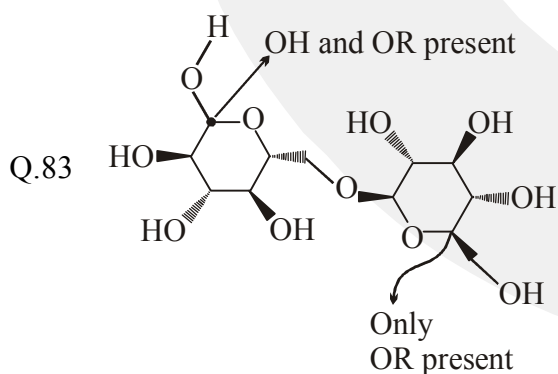
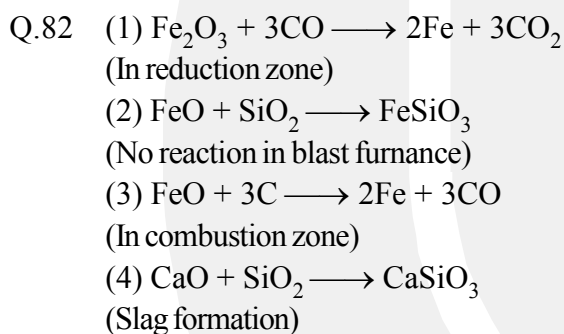
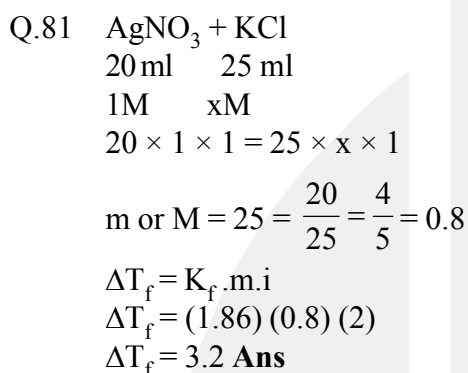
→ Oxides ore is directly reduced by carbon

(2) Chalcocite(Cu_2S)(3) Iron pyrites (FeS_2)(4) Sphalerite (ZnS)

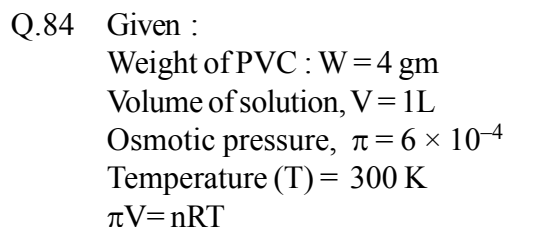
Sulphide ores are roasted first converted to oxide and then reduced by coke.



p-nitrophenol and o-nitrophenol are separated by Steam distillation



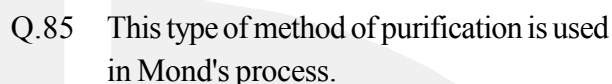
If one C have OH and OR than hemiacetals.
 If one C have OR and OR than acetal.



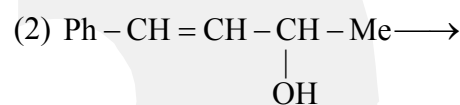
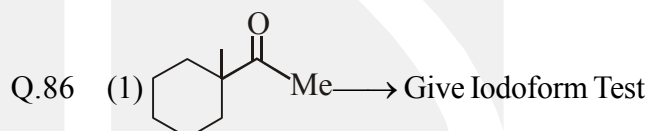
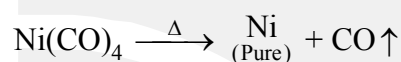
$$(6 \times 10^{-4}) \times 1 = \frac{4}{M} \times 0.0821 \times 300$$

$$M = \frac{4}{6 \times 10^{-4}} \times 0.0821 \times 300$$

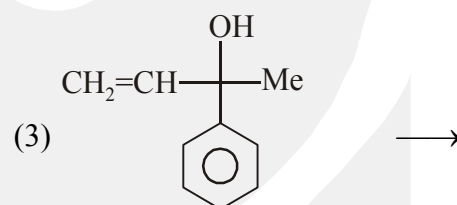
$$M = 1.6 \times 10^5$$



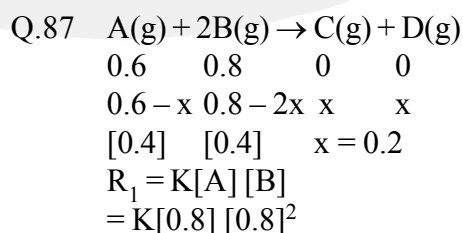
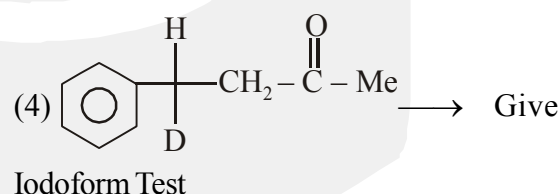
For - Ni ; Reagent - CO



Give Iodoform Test

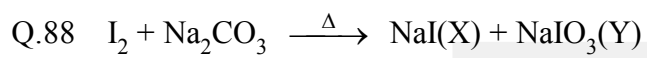


In capable to show Iodoform Test



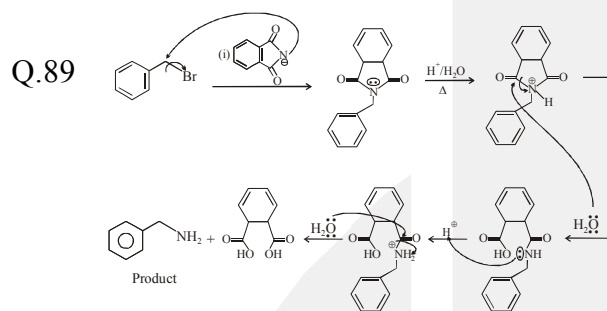
$$R_2 = K [0.6] [0.4]^2$$

$$\frac{R_2}{R_1} = \frac{K[0.6][0.4]^2}{K[0.8][0.8]^2} = \frac{3}{16} \text{ Ans.}$$



$Y = NaIO_3$ (Oxidising agent)

It will not oxidise $Cr_2O_7^{2-}$ in basic medium.



Q.90 Theory based