

### 1.) Initialize Population [Current Iteration (t) = 0]

Population Size = 4;

$x_i$  : (i = 1,2,3,4) and (t = 0)

$x_1 = 1.3$ ;

$x_2 = 4.3$ ;

$x_3 = 0.4$ ;

$x_4 = -1.2$

### 2.) Fitness Function used:

$$f(x) = \sum_{l=1}^n x_l^2$$

Compute Fitness Values for Each Particle using fitness function.

$f_1 = 1.69$ ;

$f_2 = 18.49$ ;

$f_3 = 0.16$ ;

$f_4 = 1.44$ ;

### 3.) Initialize Velocity for each particle in the current Population.

$v_1 = 0$ ;

$v_2 = 0$ ;

$v_3 = 0$ ;

$v_4 = 0$ ;

### 4.) Find Personal Best & Global Best ( $G\_Best = 0.4$ ;) for each Particle.

$G\_Best = 0.4$ ;

$$\begin{aligned} \circ P_{Best,1}^1 &= 1.3; \\ \circ P_{Best,2}^1 &= 4.3; \\ \circ P_{Best,3}^1 &= 0.4; \\ \circ P_{Best,4}^1 &= -1.2 \end{aligned}$$

### 5.) Calculate Velocity for each Particle.

Calculate Velocity by:

$$v_i^{t+1} = wv_i^t + c_1r_1(P_{Best,i}^t - x_i^t) + c_2r_2(G_{Best}^t - x_i^t)$$

$$v_1^{(0+1)} = 1*0 + 1*0.233(1.3 - 1.3) + 1*0.801(0.4 - 1.3) ;$$

$$v_1^1 = 0.7209;$$

$$v_2^1 = -3.1229;$$

$$v_3^1 = 0;$$

$$v_4^1 = 1.2816;$$

### 6.) Calculate Position for each Particle.

Calculate Particles Position by :

$$x_i^{t+1} = x_i^t + v_i^t$$

$$x_1^{(0+1)} = 1.3 + 0.7209 = 2.0209 ;$$

$$x_2^{(0+1)} = 4.3 - 3.1229 = 1.1771;$$

$$x_3^{(0+1)} = 0.4 + 0 = 0.4;$$

$$x_4^{(0+1)} = -1.2 + 1.2816 = 0.0819 ;$$

### 7.) Calculate Fitness Values for each Particle (t = 1).

$$f_1^1 = 4.084;$$

$$f_2^1 = 1.3855;$$

$$f_3^1 = 0.16;$$

$$f_4^1 = 0.0067;$$

### 8.) Repeat Until Stopping Criteria is met.

```

Iteration 87: Best Cost = 0.20362
Iteration 88: Best Cost = 0.14245
Iteration 89: Best Cost = 0.14245
Iteration 90: Best Cost = 0.12074
Iteration 91: Best Cost = 0.10434
Iteration 92: Best Cost = 0.10298
Iteration 93: Best Cost = 0.084605
Iteration 94: Best Cost = 0.070687
Iteration 95: Best Cost = 0.063776
Iteration 96: Best Cost = 0.055252
Iteration 97: Best Cost = 0.055252
Iteration 98: Best Cost = 0.055252
Iteration 99: Best Cost = 0.035831
Iteration 100: Best Cost = 0.030934

```

(Output after 100 iterations )

For More details watch this video:

Link: <https://youtu.be/Dds5CQGwxIM>

**PARTICLE SWARM OPTIMIZATION ALGORITHM**

Particle Swarm Optimization (P.S.O.) Algorithm Step-by-Step with Numerical Example.

- STEP 03:** Calculate Velocity for each Particle.
- Calculate Velocity by:**  $v_i^{t+1} = wv_i^t + c_1r_1(P_{Best,i}^t - x_i^t) + c_2r_2(G_{Best}^t - x_i^t)$
- $v_1^{0+1} = 1 * 0 + 1 * 0.233(1.3 - 1.3) + 1 * 0.801(0.4 - 1.3);$
- $v_1^1 = 0.7209;$
- $v_2^1 = -3.1229;$
- $v_3^1 = 0;$
- $v_4^1 = 1.2816;$

Best values:

- $P_{Best,1}^1 = 1.3;$
- $P_{Best,2}^1 = 4.3;$
- $P_{Best,y}^1 = 0.4;$
- $P_{Best,x}^1 = -1.2$

Particle Swarm Optimization (PSO) [Part - 2] with Numerical Example and Source Code ~xRay Pixy