- -> in amortized analysis, we average the time required to ferform a sequence of data structure operations over all the operations performed.
- -> Amortized analysis helps to show that the average cost of an operation is small, if we average over a sequence of operations, even though a single operation within the sequence might to expensive
- -> Amortized analysis is different than average-case analysis
- -> Amortized analysis guarantees the average performance of each operation in the worst case.

It has three most common techniques

- 1 Aggregate analysis
- 2) The accounting method
- 3) The potential method.

By performing amorbized analysis we get insights into a paraicular Data shucture which helps to optimize the Beg design

#] Aggregate analysis: 6-

→ in this method we show for all n

a sequence of n operations takes worst-case time T(n) in total.

- even when there are several types of operations in the sequen

Stack operations:-

Each operation runs in O(1) time, let's consider the cost of each to be 1.

total cost of a sequence of n Push & POP operations 9s therefore n, and the actual running time for n operations is there fore QCn).

lets take into consideration new operation Mutipop (S.K) -> k is positive

- s it removes the k top objects of stack S,
- -> pops the entire stack if the stack contains fewer than k objects.
- -> if k is not positive then multipop operation will not make any change in stack.

Consider the following pseudo code.

MULTIPOP (S, K)

while not STACK-EMPTY (5) and k>0

pop (s)

8: K= K-1

Example:

top-> 23 17 After MULTIPOP(5,4) 06 39 top-> 10 CF, 2) 909 ILLUM 10 47 (S) (5) (S)

running time of MULTIPOP (S, K) on a stack of s objects. ?

- -> actual running time is linear in the number of pop operation actually executed.
- the murroup is applicable in terms of the abstract costs of

- The total cost of MULTIPOP is min (S,K) and actual running time is a linear function of this cost-
- "> for sequence of n. PUSH, POP and MULTIPOP operations on an initially empty stack.

worst-case Multipop is o(n) : size of stack is n.

worst case time of any stack operation is o(n)

and hence a sequence of n operations costs o(n²)

Since p o(n) Multipop operations costing O(n) each is a

we can have.

But this is not right

using aggregate analysis

Better upper bound analysis can be obtained by Considering the entire sequence of n operations.

- -3 though MULTEPOP operation and be expensive any sequence of n push, pop & multepop operations on an initially empty stack is is at most o(n)
- -> Using aggregate analysis

 the number of times that POP can be called on a

 nonempty stack, including calls within MULTIPOP, is at most

 the number of Push operations, it is at most 1.
- -> for any value of n, any sequence of n PUSH
 n POP
 n MULTIPOP

The western (1st of an amonthon is

Accounting method

In the accounting method

- -> we assign differing charges to different operations
- -> Some Operations Charged more or less than they actually cost.
 - -> the amount charged for an operation it is amorbized cost.
- we assign the difference to specific objects in the data sincture as credit
 - -> Erredit can help pay for later operations whose amortized cost is less than their actual cost-