# PH205: Math Method of Physics

# Lecture 2: Math Method of Physics

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# Contents

1	Newton's First Law: The Law of Inertia	2
2	Newton's Second Law: Force and Acceleration	2
3	Newton's Third Law: Action and Reaction	2

## 1 Newton's First Law: The Law of Inertia

Newton's first law states that an object will remain at rest or in uniform motion in a straight line unless acted upon by an external force. This property of an object to resist changes in its state of motion is called **inertia**.

### **Key Point!**

An object's velocity,  $\vec{v}$ , is constant if and only if the net force,  $\sum \vec{F}$ , acting on it is zero. Mathematically:

$$\sum \vec{F} = 0 \iff \frac{d\vec{v}}{dt} = 0$$

## 2 Newton's Second Law: Force and Acceleration

This is the most famous of the three laws. It provides a quantitative relationship between force, mass, and acceleration.

#### **Definition: Force**

In physics, a force is an influence that can change the motion of an object. A force can cause an object with mass to change its velocity (e.g., moving from a state of rest), i.e., to accelerate.

The law is expressed by the formula:

$$\vec{F}_{net} = m\vec{a}$$

Where:

- $\vec{F}_{net}$  is the net force vector.
- m is the mass of the object (a scalar).
- $\vec{a}$  is the acceleration vector.

#### Example

A 10 kg box is pushed on a frictionless surface with a horizontal force of 50 N. What is its acceleration?

Using Newton's second law:

$$a = \frac{F}{m} = \frac{50 \text{ N}}{10 \text{ kg}} = 5 \text{ m/s}^2$$

# 3 Newton's Third Law: Action and Reaction

For every action, there is an equal and opposite reaction.

#### Theorem: Action-Reaction Pairs

If object A exerts a force  $\vec{F}_{AB}$  on object B, then object B simultaneously exerts a force  $\vec{F}_{BA}$  on object A, and the two forces are equal in magnitude and opposite in direction:

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

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