

Appendix 2: Finding which initial conditions and model parameters lead to which IPM strategies

It is unlikely a given IPM strategy will perform well in all scenarios, for example strategy that works well in cases where the yield penalty (Y_D) of the weed is very low is unlikely to be good in cases where the yield penalty is very high. To find the parameters and initial conditions (n_0) that most influence what makes a good IPM strategy we extend the meta-modelling approach outlined in (Coutts & Yokomizo, 2014) to complex multivariate time series outputs (i.e. the sequences of the four sub actions). The meta-modelling approach to global sensitivity analysis is very flexible, and only requires building a function that predicts a models output given a set of parameters. The complication in this case is that the model output is a time series of actions, rather than a single number. To address this we use multi-variate boosted regression trees (Miller *et al.*, 2016) as follows:

1. We use latin hypercube sampling to generate 15000 parameter combinations, see Table S1 for upper and lower limits of each parameter. We treat the initial conditions as parameters (Rr_{int} , Qq_{int} and N_{int}).
2. For each parameter combination we run the genetic algorithm (Appendix 1) for 100 iterations, experience showed that improvements to the best solution found dramatically slowed down after 60 iterations with a solution set size of 1000 and mutation rate of 0.03. After 100 iterations we choose the action sequence with the highest reward as the best action sequence.
3. This resulted in 15000 action sequences. We only use the first 10 time steps of each action sequence, although the reward was calculated over 25 time steps. This ensured that the action chosen at each time step was done so considering rewards from at least 15 time steps in to the future.
4. To make sense of this mass of data we built a dissimilarity matrix of each action sequence to all the other action sequences, to represent how all the action sequences related to each other. We use a distance metric from text analysis, longest common sub-sequence, calculated with the 'SimilarityMeasures' (Toohey, 2015) package in R. We allow a positional displacement of one time step, that is actions in sequence A are allowed to be matched to actions in sequence B that are separated in time by at most one time step. This allows out of phase cycles to have very high similarity. Two action sequences where the same combinations of actions are used, but at times more than one time step apart will have low similarity.
5. We use non-metric multi-dimensional scaling (NMDS), implemented with the 'ecodist' package (Goslee & Urban, 2007), to project this very high dimensional dissimilarity matrix into a lower dimensional space. We call this the solution space and we found that we could project the dissimilarity matrix into an eight dimensional solution space, with a stress of 0.09. Stress measures the difference between the relative location of each solution in the solution space, and the dissimilarity matrix. Lower values are better. We found that 8 dimensions was a good trade-off between low stress and a manageable number of dimensions. Figure S1 shows how the solution space matches up to a separate hierarchical clustering (using the wardD2 method) we carried out to confirm and aid visualization of the NMDS.

6. We recorded the eight co-ordinates of each solution in the solution space, along with the parameter set that generated that solution. This built a data-set 15000 rows long, where each row was a parameter set and a location in the solution space.
7. We use multi-variate boosted regression trees (mvBRT) as our meta-model. mvBRTs were fit using the 'mvtboost' package (Miller *et al.*, 2016). mvBRTs fit a separate boosted regression tree to each dimension of the response, in our case a position in the eight dimensional solution space. At each iteration in each tree the split that most reduced the co-variance between the eight responses is chosen. For further details see (Miller *et al.*, 2016). We used a learning rate of 0.01, maximum interaction depth of 5. These tuning parameters lead to a optimum of 12229 trees in the mvBRT.
8. We interrogate the mvBRT to find the most influential parameters. We also calculate partial dependence plots of the mvBRT to predict where in the solution space a given set of parameters leads to, and use the closest solution to that location to estimate what a solution in the predicted location would look like. We use this as guide to help us explore and and interrogate the complex solution space. However, we have access to the data generating process and so do not need to rely on this estimate. For the actual plots in the results we re-run the genetic algorithm with the desired parameter combinations.

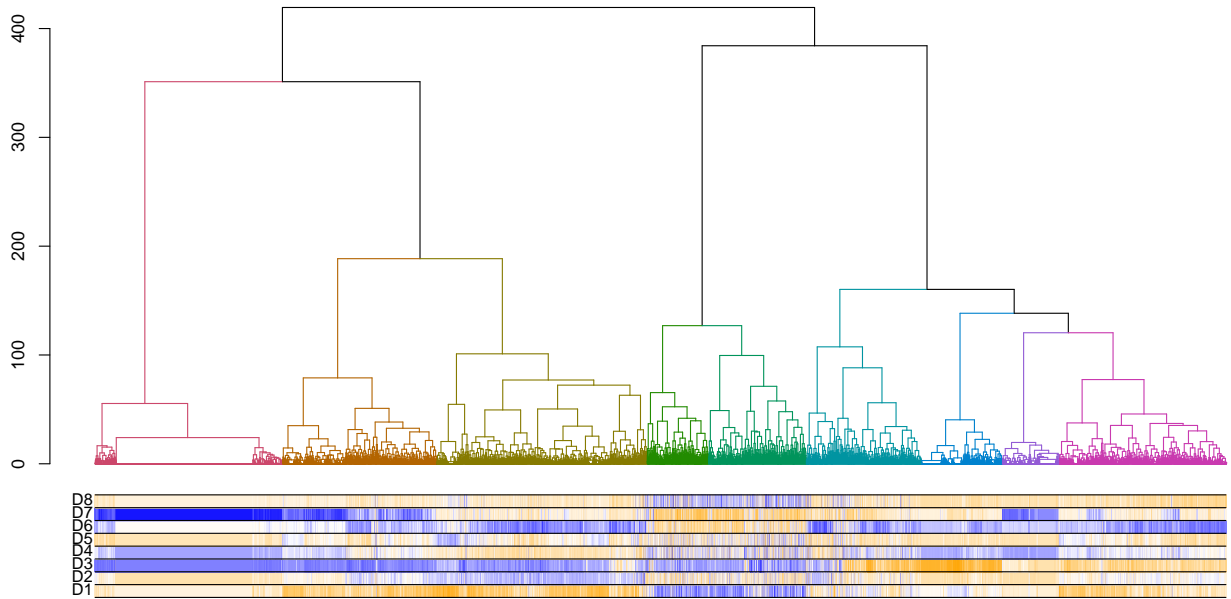


Figure S1: Position of all 15000 IPM strategies found by the genetic algorithm in the eight dimensional solution space and dendrogram built using the wardD2 method. Different colors in the dendrogram highlight the 9 most distinct clusters. Colors in the bars show each solutions position in the solution space. All dimensions are centered on 0 (white), with dark blues being at one extreme and dark oranges the other (only relative position is meaningful).

Table S1: Parameter descriptions and the range each parameter was tested over

Parameter	Units	Range	Description	Source
<i>Population Model see Appendix 5</i>				
ϕ_e	prob.	0.45–0.6	germination probability	Colbach <i>et al.</i> (2006)
ϕ_b	prob.	0.2–0.86	Probability a seed survives one year	Colbach <i>et al.</i> (2006), Thompson <i>et al.</i> (1997), Cavan <i>et al.</i> (1999)
s_0	prob.	fixed 0.99	Survival probability without herbicide	Assumed fixed and high so density effects only expressed through fecundity.
θ	prob.	0.7–1	Proportion of <i>A. myosuroides</i> population exposed to herbicide under sub-action a_h = herb R, herb Q or both. plants may be missed spatially or temporally, or spraying may be affected by rain. Tested over wide range.	
s_h	prob.	0.01	Survival of susceptible <i>A. myosuroides</i> exposed to herbicide (a_h)	herbicide assumed to be effective.
α	prob.	0.22–0.04	Survival probability under the alternative crop (a_k = alt), spring barley.	Lutman <i>et al.</i> (2013)
β	prob.	0.05–0.2	Survival under spot control (sub-action a_s), for example because plants are missed	tested over wide range.
f_m	seeds·plant ⁻¹	30–300	Number of seeds produced when density is 0 (f_m)	
f_d	$\frac{1}{plants \cdot ha^{-1}}$	0.001–0.0001	The effect of density on seed production (f_d) interact to determine maximum population size. Values chosen to keep the max population close to the maximum population seen in Queenborough <i>et al.</i> (2011) so yield is not extrapolated outside the observed range.	
I	prob.	0.5–0.9	The proportion of seed moved between seed bank levels by ploughing (sub-action a_b)	Grundy <i>et al.</i> (1999)
<i>Reward function see Appendix 3</i>				
γ		0.75–1	discount rate on future returns	tested over wide range

Table S1: Parameter descriptions and the range each parameter was tested over

Parameter	Units	Range	Description	Source
Y_0	$\text{£}\cdot\text{ha}^{-1}$	968–1758	Yield from winter wheat when <i>A. myosuroides</i> is absent.	Upper limit upper 95% confidence interval from fitted yield function (Appendix 3). Lower limit from low production scenario Redman (2016, pp. 9).
Y_D	$\text{£}\cdot\text{plant}\cdot\text{ha}^{-1}$	0.0002–0.006	reduction in yield caused by each <i>A. myosuroides</i> .	95% confidence interval from fitted yield function, see Appendix 3.
ϑ	$\text{£}\cdot\text{ha}^{-1}$	672–920	Yield of spring barley, an alternative crop commonly used to control <i>A. myosuroides</i> .	Redman (2016, pp. 12)
ϖ	prop.	0.85–1	proportion of yield achieved if crop a_k is repeated	Redman (2016, pp. 9)
η_h	$\text{£}\cdot\text{ha}^{-1}$	50–100	Cost of a single herbicide application	Redman (2016, pp. 9)
η_b	$\text{£}\cdot\text{ha}^{-1}$	55–92	Cost of ploughing	Redman (2016, pp. 202)
η_s^0	$\text{£}\cdot\text{ha}^{-1}$	10–100	Cost of spot control even when <i>A. myosuroides</i> density is 0	tested over wide range
η_s	$\text{£}\cdot\text{plant}\cdot\text{ha}^{-1}$	10–100	Increase in spot control cost for each <i>A. myosuroides</i>	tested over wide range
η_{wheat}	$\text{£}\cdot\text{ha}^{-1}$	383	Cost of growing winter wheat not associated with <i>A. myosuroides</i> control	Redman (2016, pp. 9)
η_{alt}	$\text{£}\cdot\text{ha}^{-1}$	273	Cost of growing the alternative crop, spring barley.	Redman (2016, pp. 12)
η_{fal}	$\text{£}\cdot\text{ha}^{-1}$	36	Cost of a fallow rotation. Based on two applications of glyphosate to control any germinating <i>A. myosuroides</i> .	Redman (2016, pp. 202 and 284)
<i>Initial Conditions</i>				
R_{int}		0–1	Initial frequency of R alleles	
Q_{int}		0–1	Initial frequency of Q alleles	
N_{int}		100–100000	Initial number of seeds in each level of the seed bank	

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