Optimal control in the face of evolving resistance is an economic problem not a biological one.

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Evolved resistance to xenobiotics (i.e. antibiotics, herbicides, pesticides, fungicides) is a global threat to public health and food security. In agricultural systems non-chemical control methods can be combined with xenobiotics (Integrated Pest Management; IPM) to prolong the useful life of compounds and manage pest populations after resistance has evolved. We find IPM strategies with the highest economic returns for an arable cropping system, and perform a global sensitivity analysis to find the factors that shape those strategies. The key uncertainties we find are economic in nature, and farmers have an economic incentive to be responsive to changes in weed the shape of the yield loss function. Doing so will require estimating, at a minimum, what yields would be in the absence of the pest, and how yields change with increasing pest density, with enough detail to say how much control (if any) is justified.

Integrated Pest Management | herbicide resistance | *Alopecurus myosuroides* | combinatorial optimisation

Controlling populations in the face evolving resistance to xenobiotics (i.e. antibiotics, herbicides, pesticides, fungicides) is one of the biggest challenges facing public health (1, 2) and food security (3–5). Evolved resistance also costs billions of dollars globally (5–7). In response, strategies to manage resistance focus on delaying the initial evolution of resistance by reducing the population (reducing the potential for *de nova* resistance mutations), and killing any resistant mutants by using a second compound (3, 8). Multiple compounds are either stacked (used at the same time) or cycled in sequence. While these strategies can be effective in delaying the initial evolution of resistance they may be counter-productive if xenobiotic resistance is already present, which is true of important pests in food production systems (3, 5) and threats to human health (2). Strategies like stacking and cycling involve the continuous (and even increased) use of xenobiotics, which can help drive existing resistance through an entire population (3, 5).

In agricultural systems chemical control can be used in combination with non-chemical control such as crop rotation, cultivation and spot control (e.g. hand-weeding), known as integrated pest management (IPM). IPM can be used both pro-actively to delay the evolution of resistance, and reactively to control pest populations as chemical control becomes less effective. While the concept of IPM is well established (9), finding cost effective IPM strategies is challenging (10, 11). Management tools need to be used in the correct combination and sequence to be most effective. This results in a very large number of potential IPM strategies (i.e. different combinations and sequences), even when considering only a handful of management tools and short time horizons (11). As a result, there have been few attempts to rigorously search for good IPM strategies (see 11 for an exception). More commonly optimal strategies have looked for the best allocation between a few management options (12–15), and none have been developed where resistance could evolve to one of the primary management tools. These are important omissions for food production systems where resistance to xenobiotics has evolved numerous times (3, 4) and multiple non-chemical control options can be used in combination to deliver cost effective control (11).

Further, little is known about how robust good IPM strategies are to changes in factors such as crop yield and pest population dynamics (12). Thus, even when effective IPM strategies are found, we do not know how generally we should expect them to apply.

We used *Alopecurus myosuroides* as a test case. *A. myosuroides* is Europe's most economically burdensome weed (16) and one of the worlds most serious herbicide resistant grass weeds (17). Herbicide-resistant *A. myosuroides* costs up to £320·ha^{-1} in yield loss and extra herbicide use (5), and imposes a total cost of £0.5bn across England (Varah et al, in press).

We found economically beneficial IPM strategies, which factors shaped those strategies and how. We framed IPM as a combinatorial optimisation problem with the goal of finding good combinations of management tools, used in sequence. To model IPM strategies we built a population model for *Alopecurus myosuroides* where target site resistance to evolve to two herbicides, and crop rotation, cultivation and spot control were management options alongside herbicide. We used a genetic algorithm (Appendix 1) to solve this combinatorial problem (18, 19) for 15000 parameter combinations that incorporate a wide range of economic, biological and psychological factors.

Significance Statement

Integrated pest management (IPM) applies chemical and non-chemical control methods to pest populations to manage evolved resistance. However, we have a poor understanding of when different IPM strategies are incentivised. We find IPM strategies with the highest economic returns in an arable cropping system where high levels of herbicide resistance has evolved repeatedly. The best IPM strategies were dependent crop yields, yield loss caused by the weed, land tenure and levels of herbicide resistance. With the exception of herbicide resistance, all these factors are economic in nature. Knowing which IPM strategy to apply where will require, at a minimum, knowing the yield loss function for the major weeds of a farm, an economic problem rather than biological one.

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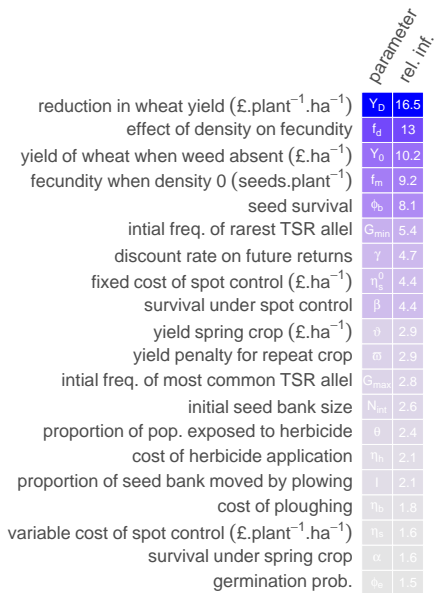| parameter		rel. inf.
reduction in wheat yield (£.plant^{-1}.ha^{-1})	Y_D	16.5
effect of density on fecundity	f_d	13
yield of wheat when weed absent (£.ha^{-1})	Y_0	10.2
fecundity when density 0 (seeds.plant^{-1})	f_m	9.2
seed survival	ϕ_b	8.1
intial freq. of rarest TSR allel	G_{min}	5.4
discount rate on future returns	γ	4.7
fixed cost of spot control (£.ha^{-1})	η_a^0	4.4
survival under spot control	β	4.4
yield spring crop (£.ha^{-1})	$\bar{\sigma}$	2.9
yield penalty for repeat crop	ϖ	2.9
intial freq. of most common TSR allel	G_{max}	2.8
initial seed bank size	N_{int}	2.6
proportion of pop. exposed to herbicide	θ	2.4
cost of herbicide application	η_h	2.1
proportion of seed bank moved by plowing	l	2.1
cost of ploughing	η_p	1.8
variable cost of spot control (£.plant^{-1}.ha^{-1})	η_a	1.6
survival under spring crop	α	1.6
germination prob.	ϕ_g	1.5

Fig. 1. Relative influence (relative reduction in squared error; 20) of each parameter on IPM strategy (Appendix 2). Values are scaled 0 to 100, with higher values indicating parameters with more influence on the structure of incentivized IPM strategies.

We applied a global sensitivity analysis to this set of IPM solutions to find parameters that were important in changing those IPM strategies (Appendix 2). We used multi-variate boosted regression trees (20) as a meta-model (21). This allowed us to find important parameters accounting for high-level interactions and non-linear responses (using the relative influence metric), and describe the effect of each parameter over a wide range of values (using partial dependence plots). Relative influence is the mean reduction in mean squared error attributable to each parameter, re-scaled to sum to one across al parameters (20, 22). Partial dependence plots show the marginal effect of a parameter of interest on IPM strategy (20, 22).

Results and Discussion

Across a wide range of parameter combinations the key uncertainties were economic, despite much research on IPM focusing on biological factors (23). In particular parameters defining the yield loss function (Fig. 1) had the most influence on shaping incentivized IPM strategies. The yield loss function describes the relationship between weed density and crop yield. Yield when the weed was absent (Y_0) and the effect of weed density on yield (Y_D) were two of the most important parameters (Fig. 1). Another set of parameters that control how large the seed bank can become (f_m, f_d and ϕ_b; Fig. 1) were also important. The potential size of the seed bank set the scale the x-axis of the yield function. Although yield functions have been estimated for major weeds (24–26), there is evidence that yield functions vary substantially between fields (5, 26), and little attention has been paid this variation and understanding its causes.

The yield loss function determines how much control is justified (27). While the shape of the yield loss function is important, knowing how much management is justified may only require an estimate of yield in the absence of the
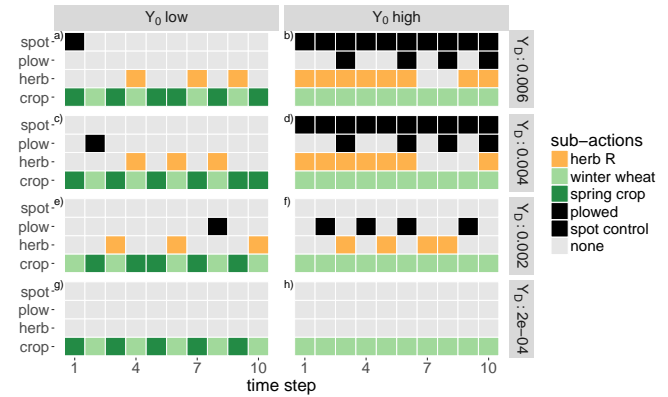

Fig. 2. IPM strategies under high (£1668·ha^{-1}) and low (£986·ha^{-1}) values of Y_0 (yield of winter wheat with no *A. myosuroides*), under increasing values (rows) of Y_D (in £·plant^{-1}·ha^{-1}). At the lower limit of Y_D very high *A. myosuroides* densities result in a 1% yield loss under the high Y_0 scenario, and the upper limit implies a yield loss of 35%. There is initially one effective herbicide ($R_{int} = 0.0001$, $Q_{int} = 0.9$). We used partial dependence plots to explore how different parameter combinations change IPM strategy, then re-ran the genetic algorithm for those parameter combinations to generate these plots.

weed (Y_0), and one or two thresholds values of weed density where a new IPM strategy becomes advantageous. When the yield of winter wheat with no *A. myosuroides* (Y_0) was low, management intensity was lower and relied on crop rotation and tactical use of herbicide (Fig. 2, 'Y_0 low'). The strategy changed little when the effect of weed density on yield (Y_D) increased. Although, more herbicide was used when the value of Y_D increased from a very low value to a slightly higher value (1% to 12% losses at high densities of *A. myosuroides*; Fig. 2g,e). When Y_0 was high, Y_D showed two thresholds where IPM strategy changed. When Y_D was very low the best strategy was to do noting and live with high populations of *A. myosuroides* (Fig. 2h), since yield losses were never high enough to justify expenditure on control. Increasing Y_D slightly meant some herbicide use and cultivation to rotate the seed bank became advantageous (Fig. 2f). Once Y_D increased enough to justify intensive control, further increases did not change the IPM strategy (Fig. 2b,d). Thus,

Intensive management can be costly, and so require returns over several years to justify. As a result valuing returns further into the future (in our model controlled by the discount rate γ) encourages more intensive management (12). Intensive management to reduce the seed bank was only selected by the genetic algorithm when future returns were valued at a similar rate to current returns (Figure 3). In agricultural systems land tenure have a crucial effect on how investments in weed control are valued. Those who own fields can benefit from long-term investments like weed control campaigns and soil conservation, whereas those who rent fields do not (28, 29). The amount of rented farm land can be considerable. In 2014 54% of crop land in the USA was rented (30), and 35% of all agricultural land in England and Wales is rented (31). This has important implications for the level of control managers are incentivised to provide, and thus its spread and the evolution of resistance (32).

Resistance increased quickly with herbicide use. Even starting at low frequencies, high levels of resistance evolved after just seven herbicide applications (Fig. 4b). The best IPM strategies found were responsive to increasing resistance, dras-
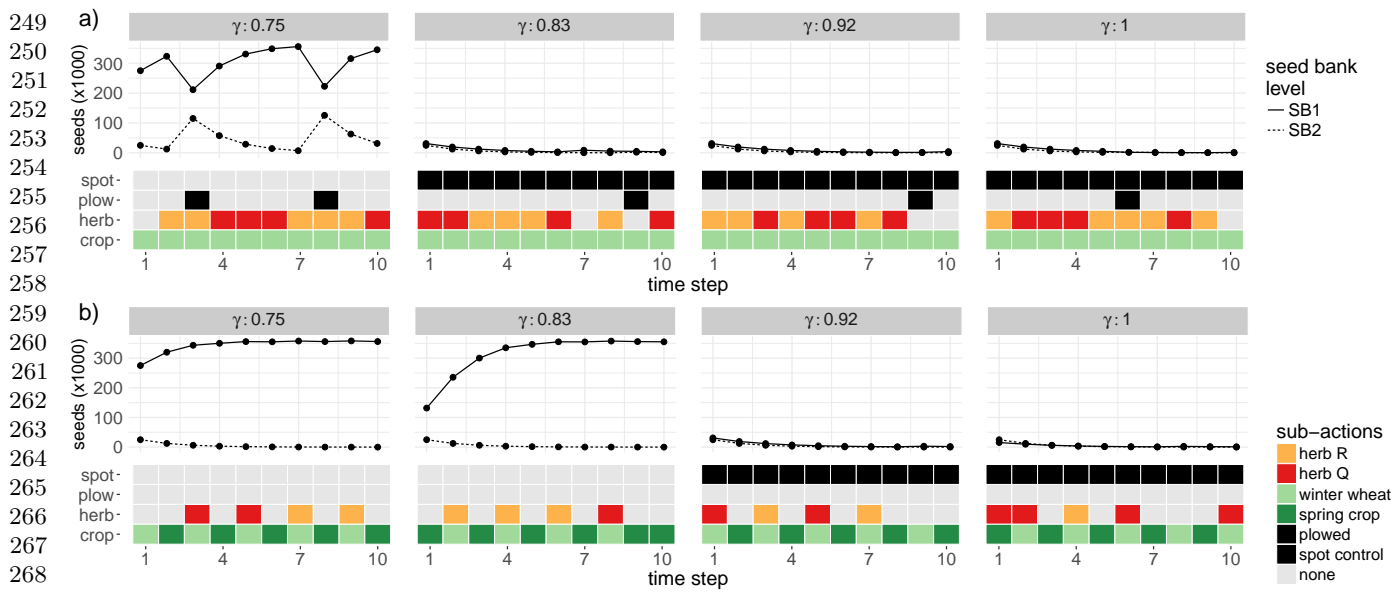
Fig. 3. The effect of discount rate (γ) on the seed bank and IPM strategy (tile plots) when yields from winter wheat are high (a; £1668·ha^{-1}) and low (b; £986·ha^{-1}). When $\gamma = 0.75$ rewards 5 years in the future are valued at 23% of current returns and when $\gamma = 1$ present and future rewards are valued equally. In both cases the slope of the yield function (Y_D) is high (£0.006·plant^{-1}·ha^{-1}). Initial resistance was low for both herbicides. Although we only show the first 10 years of IPM strategy, the discounted returns over 25 years are considered by the genetic algorithm.

tically reducing herbicide use as higher levels of resistance evolved (Fig. 4b–d). In contrast, multiple herbicide applications per year are the norm in this cropping system, despite high levels of resistance (5). This disparity could arise from a number of contributing factors. Some managers may believe that even a little control (mortality of a few susceptible individuals) is better than no control and inaction is seen as the worst approach to weed management (33). In addition, IPM strategies are often seen as complex in comparison to routine application of chemicals, and having a steep learning curve (34). Resistance tends to be partial and build up slowly (35, 36), so farmers may be victims of a shifting baseline, lowering their expectations of efficacy of weed control. There may be a belief that new herbicides will become available, despite no new modes of action being marketed for over 20 years (37). Thus, current strategies are viewed as a bridging strategy until a new product is found (38). Finally, Our population model was deterministic, so IPM strategies could not be risk averse to variability in *A. myosuroides* populations and economics factors like crop prices. Uncertainty in when herbicide resistance will emerge and the efficacy of non-chemical control can be a major impediment to adopting IPM (38).

In our system herbicide resistance incurred a high cost, and even the best IPM strategies found saw their gross margin (reward) reduced by upto a quarter once high levels of resistance had evolved (Fig. 4c,d). These losses had different sources depending on the initial resistance. When initial resistance was low the weed population could be initially reduced with herbicide, but required more expensive non-chemical control to keep the weed population low so that spot control remained feasible (Fig. 4c). When resistance was high there were few effective control options and high weed populations reduced the yield (Fig. 4c). It should be noted this result depends on the yield loss function. If high densities of the weed do not cause large yield loses then high levels of resistance are less

of a concern, and high expenditure on non-chemical control is not justified.

Much work on managing resistance focuses on delaying its establishment in the population, and in such cases both stacking and cycling compounds can be effective (8). In contrast we modelled reactive management, where resistance is already established in the population (5). Over a wide range of parameters, when both herbicides were effective the preference was to cycle between them (e.g. Fig. 3 and 4a). Cycling was favoured over stacking because the application of each herbicide was spread out, prolonging their life.

We present the best case that can be hoped for in reactive management, as we assume that herbicide resistance was conferred by target site mutations. However, there is growing evidence that non-target site resistance, which confers cross resistance, is widespread (5). If generalized, non-target site resistance mechanisms are present, the total amount of herbicide exposure predicts resistance level (5), and cycling will not help.

We assume that herbicide is the only action that drives the evolution of resistance. Any effective management tool will impose selection pressure, and so drive resistance to that tool. In reality, the spring cropping and spot control sub-actions make heavy use of glyphosate to control *A. myosuroides*. Glyphosate resistance has evolved on many separate occasions in response to prolonged, heavy use (39). As glyphosate becomes a more important part of weed management (5) resistance is likely.

Conclusion

Combating xenobiotic resistance is ultimately a problem of behaviour change, and thus how individuals are incentivized to act (38). Our results show that farmers have an economic incentive to be responsive to changes in weed the shape of the yield loss function. Doing so will require estimating, at a minimum, what yields would be in the absence of the pest, and
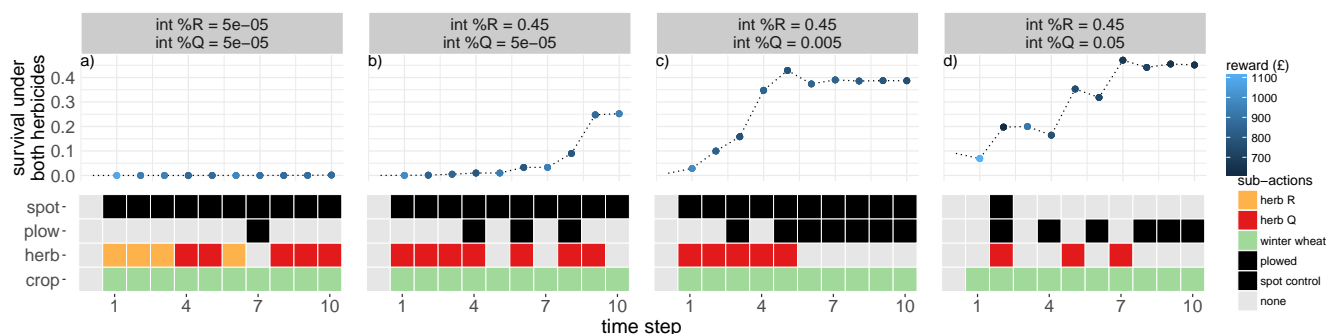
Fig. 4. The effect of initial resistance on the selected IPM strategy (tile plots) and the evolution of herbicide resistance (% survival to under both herbicides). Lighter coloured points indicate higher reward (gross margin) obtained in that time step. In this case $Y_0 = 1668$ (high winter wheat yield) and $Y_D = 0.0062$ (high yield penalty).

how yields change with increasing pest density, with enough detail to say how much control (if any) is justified. The most salient piece of data on the weed population is its maximum density, as this sets the maximum possible yield loss.

[ALEXA: would be nice to conclude with a nice summary statement on what a failure to be responsive will cost farmers, the economy as whole and the environment, are at least as much as we can say at this point. Also be a good place to flag your up coming work for any things that are still unresolved. If it is all unresolved that is an important message as well I think.]

Data Archival. PNAS must be able to archive the data essential to a published article. Where such archiving is not possible, deposition of data in public databases, such as GenBank, ArrayExpress, Protein Data Bank, Unidata, and others outlined in the Information for Authors, is acceptable.

Supporting Information (SI).

Appendices. Appendix 1: Genetic Algorithm
Appendix 2: Finding Which Initial Conditions and Model Parameters Lead to Which IPM Strategies
Appendix 3: Action Space
Appendix 4: Population Model
Appendix 5: Reward Function

Materials and Methods

We frame IPM as a combinatorial optimisation problem where the goal is to find a good combination of management tools, used in sequence. We use a genetic algorithm to solve this combinatorial problem (18, 19). Genetic algorithms cannot be checked to have found the globally optimal solution, as this would require already knowing the solution; however, genetic algorithms are efficient at selecting out comparatively poor solutions, so that over successive iterations the regions of the solution space being explored gets progressively better, resulting in a set of good (often near optimal) solutions.

Our goal is to find good IPM strategies in the face of rapidly evolving resistance, and how those strategies change in response to biological and management parameters. This problem has fours parts: i) a reward function that measures how good a given IPM strategy is based on how much that strategy costs and its effectiveness, we use net present economic value; ii) a population model that translates a given IPM strategy into a population, and thus a reward; iii) an algorithm that finds IPM strategies with higher rewards, the genetic algorithm (Appendix 1); iv) finally we need to relate changes in the best IPM strategy found to changes in

initial conditions and model parameters. For this we use a meta-modelling global sensitivity analysis (40) based on multi-variate boosted regression trees (20).

Population model. The population model links management actions to the response of the *A. myosuroides* population, and thus wheat yields. Each action a_j is a tuple of four sub-actions $a_j = \langle a_h, a_b, a_k, a_s \rangle$. See Appendix 3 for a description of the sub-actions and all eligible combinations of these sub-actions (i.e. the full actions space, $\mathbf{A}$).

The processes included in the population model limit the scope of the IPM strategies found. We use a deterministic model, and so our IPM strategies can only deal with average expected population responses, ignoring demographic uncertainty, and environmental and market variability. Also, we only model herbicide resistance that is already present in the population because *de nova* mutation is a fundamentally stochastic process.

A commonly recommended (8) and applied (5) strategy to combat resistance is to apply xenobiotics that impair different cellar pathways (i.e. modes of action), either sequentially (cycling) or concurrently (stacking). To allow this behaviour we use a discrete time, spatially implicit model, where two independent alleles (R and Q), each confer target site resistance to a separate herbicide. The model must also be flexible enough to accommodate non-chemical control. We include a two level seed bank (to allow plowing to take seeds out of the germinating population) and model survival as a function of resistance, herbicide choice, crop choice and spot control (where the cost increases with *A. myosuroides* density). The model tracks the number of seeds in each level of the seed bank in each of nine genotypes G, starting at the beginning of the growing season before any seeds have emerged. See Appendix 4 for a full description of the model and how each sub-action affects the population.

Reward function. The reward function measures how good an IPM strategy is, given an initial starting condition and parameter set that the model is run under. The reward function encodes the goals of a manager. We assume farmers are primarily driven by economic returns. The economic return consists of two parts: the income made from the crop, and the costs of producing that crop. We assume that usual farm costs, such as buildings and machinery are constant from year to year, so we focus on gross margin, i.e. income - variable costs (41, pp. 3–4).

To explicitly link the above ground population to the reward function we define $N''(\mathbf{a}, n_0, t)$, the total above ground population after all control actions, at time t given an initial population n_0 and a sequence of actions

$$\mathbf{a} = \{a_j^0, a_j^1, \cdots, a_j^T\} \quad [1]$$

where a_j^t is the action $a_j \in \mathbf{A}$ taken at time t and T is the time horizon over which management is run. We assume all returns after T are ignored. The reward function is

$$R(\mathbf{a}, n_0) = \sum_{t=0}^{T} \gamma^t \left(Y(N''(\mathbf{a}, n_0, t)) - C(a_j^t) \right) \quad [2]$$

where $R(\mathbf{a}, n_0)$ is the time-discounted reward for action sequence $\mathbf{a}$ given starting population n_0, $\gamma \in [0,1]$ is the discount rate. When $\gamma = 0$ only the reward in the first time step is considered; when $\gamma = 1$ returns in all future time steps up to T are valued equally. $Y(N''(\mathbf{a}, n_0, t))$ is the income (in £·ha^{-1}) from the crop chosen at time t given initial state n_0 and following action sequence $\mathbf{a}$. $C(a_j)$ is the cost of taking action a_j, and is composed of the cost of controlling *A. myosuroides* plus other costs that depend on the crop being grown (a_k).

See Appendix 5 for the yield and cost models for each sub-action and parameter estimation.

Finding good IPM strategies. Our goal is to find good strategies to manage *A. myosuroides* in the face of evolving resistance. However, it is not feasible to test every combination of management options over more than a handful of years. Genetic algorithms have been used to find good solutions to this class of problem (18, 19). The genetic algorithm starts with an randomly generated set of action sequences. These action sequences are then iteratively improved to find a set of action sequences with a high gross margin. Genetic algorithms rely on the fact that even though the number of possible action sequences is large, many perform very poorly. The genetic algorithm explores better performing regions of the solution space more intensely. While genetic algorithms are not guaranteed to find the optimal action sequence they will find a set of actions sequences that perform well, often close to the optimal solution.

To find good action sequences we use a genetic algorithm with knock-out tournament selection, where each action sequence in a set of 1000 actions sequences is randomly paired with another, and the action sequence with the highest $R(\mathbf{a}, n_0)$ survives to help generate new action sequences. We used pair mating between survivors and N-point cross-over to produce new action sequences. After new action sequences are created there is a process of random mutation where each a_j^t is changed to another $a_j^t \in \mathbf{A}$ with probability $m = 0.03$. The algorithm used is given in Appendix 1.

Finding which initial conditions and model parameters lead to which IPM strategies. It is unlikely a given IPM strategy will perform well in all scenarios. To find the parameters and initial conditions (n_0) that shaped the IPM strategy with the highest reward, we extend the meta-modelling approach to global sensitivity analysis (outlined in (40)), to multivariate time series outputs (i.e. the sequences of the four sub actions). We: i) ran the genetic algorithm under 15000 different parameter sets and initial conditions, generated with Latin hyper-cube sampling (see Table S1 in Appendix 2 for upper and lower limits of each parameter); ii) used Longest Common Sub-Sequence (42) as a measure of distance between these action sequences; iii) projected the resulting distance matrix into an 8D solution space using non-metric multi-dimensional scaling, implemented in the 'ecodist' R package (43); and iv) predicted where each IPM solution sat in the solution space using multi-variate boosted regression trees (20), where the model parameters and initial conditions were predictors. See Appendix 2 for details.

We interrogated this multi-variate boosted regression tree to find which parameters and initial conditions were important for changing the best IPM strategy found. We used two tools, relative influence and partial dependence plots (20).

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