

# Filters

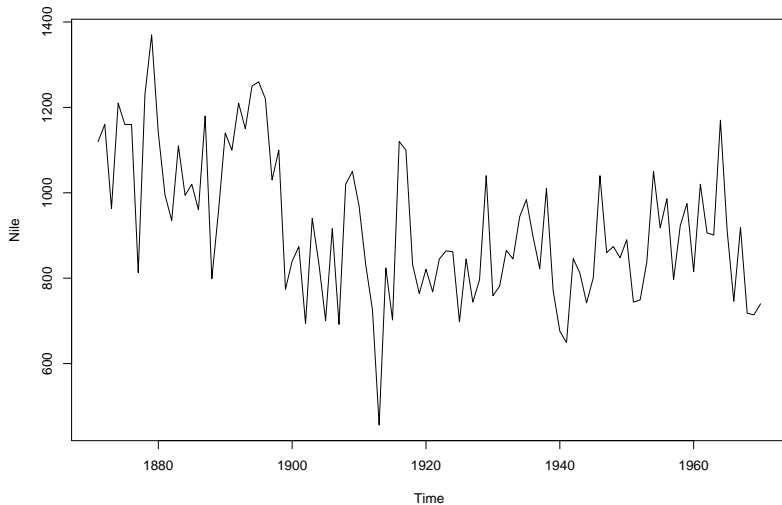
2024-10-07

# Outline

# Data

## Flow of the river Nile

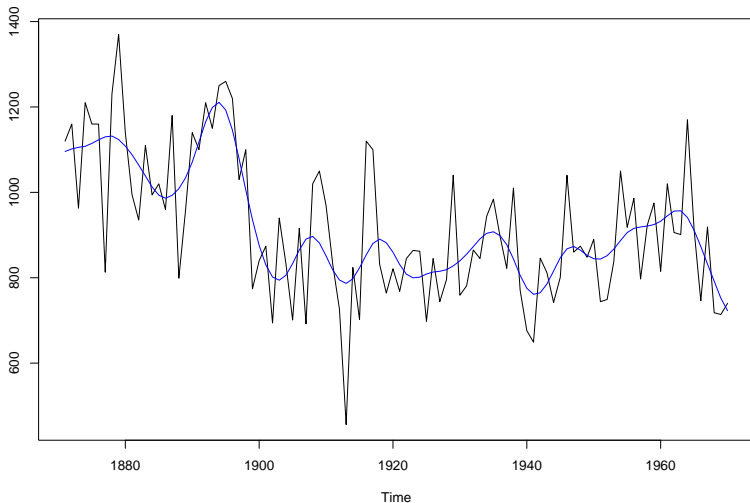
```
plot(Nile)
```



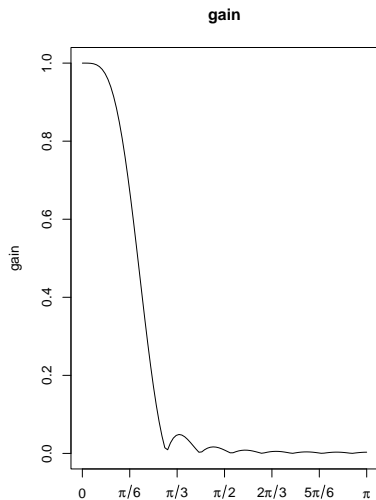
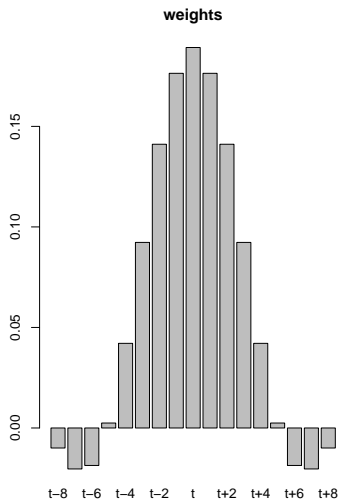
# Pre-specified filters

Filters based on well-defined mathematical properties

## Henderson filters

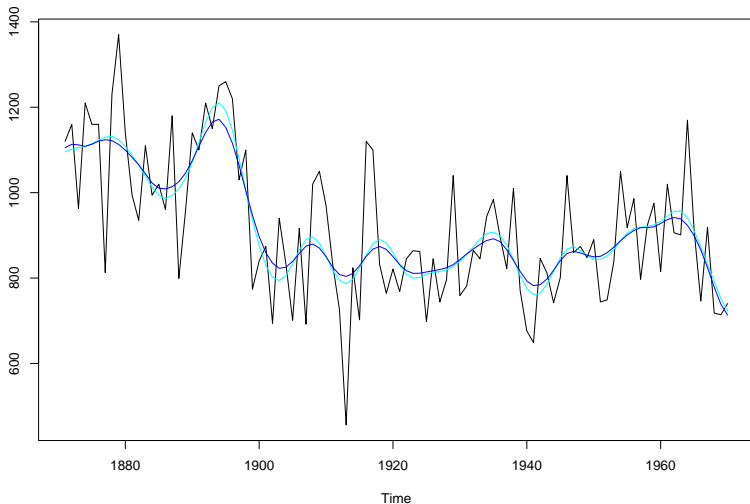


# Henderson filter properties

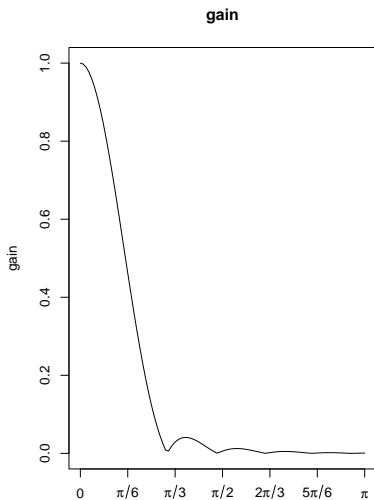
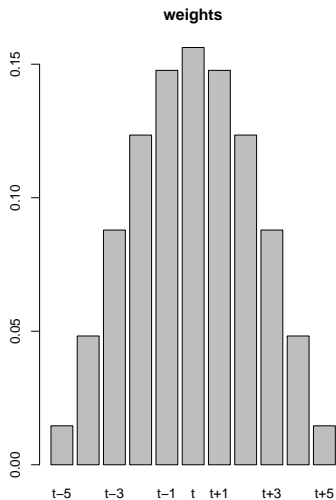


## Local polynomials

Regression with a linear trend on 11 periods, using a bi-weight kernel  $\alpha(1 - x^2)^2$



# Loess filter properties



# Model-based filters (I)

## Structural model (fixed parameters)

$$y(t) = T(t) + N(t)$$

$$\Delta^2 T(t) = \epsilon_T(t) \qquad \epsilon_T \sim N(0, 1)$$

$$N(t) = \epsilon_N(t) \qquad \epsilon_N \sim N(0, \lambda)$$

```
hp_ucm<-function(lambda=25){
  i2<-rjd3toolkit::arima_model("trend", delta = c(1,-2, 1))
  noise<-rjd3toolkit::arima_model(variance=lambda)
  ucm<-rjd3toolkit::ucarima_model(components=list(i2, noise))
}

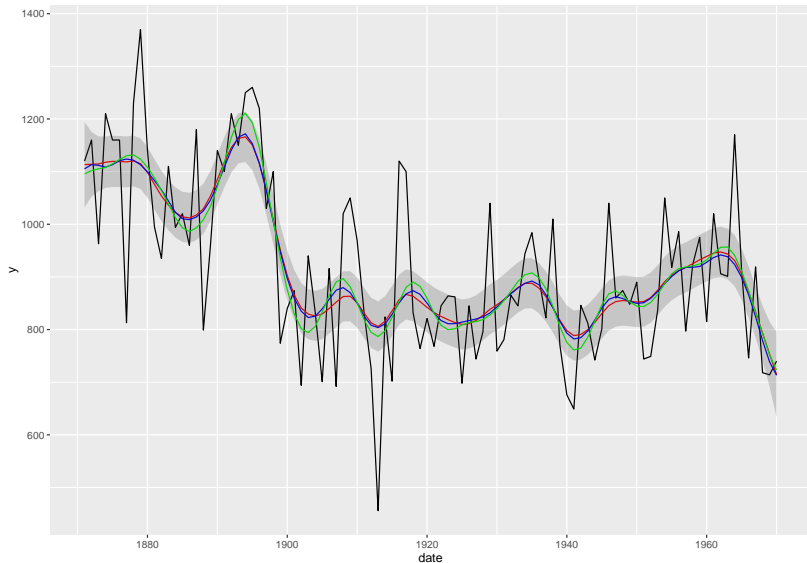
ucm_estimate<-function(x, ucm, stdev=TRUE){
  jucm<-rjd3toolkit:::r2jd_ucarima(ucm)
  jcmps<-rJava::.jcall("jdplus/toolkit/base/r/arima/UcarimaModels",
    "Ljdplus/toolkit/base/api/math/matrices/Matrix;", "estimate",
    as.numeric(x), jucm, as.logical(stdev))
  return(rjd3toolkit:::jd2r_matrix(jcmps))
}

hp_estimate<-function(s, lambda=25){
  ucm<-hp_ucm(lambda = lambda)
  rslt<-ucm_estimate(s, ucm)
}
```



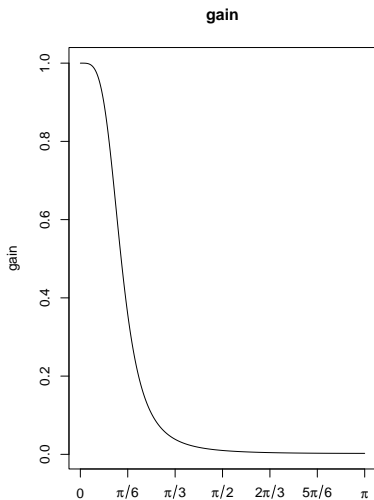
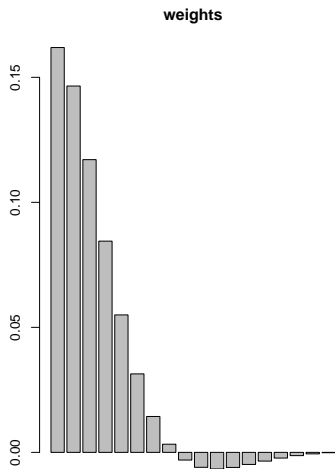
# Model-based filters (I)

## Structural model (fixed parameters)



# Model-based filters properties

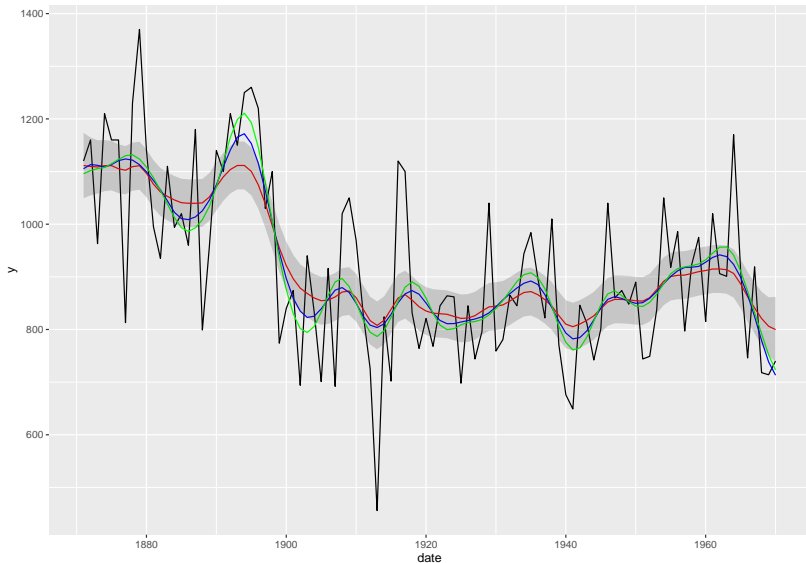
## Structural model (fixed parameters)



## Model-based filters properties

# Model-based filters

## Canonical decomposition



# Model-based filters properties

## Canonical decomposition

