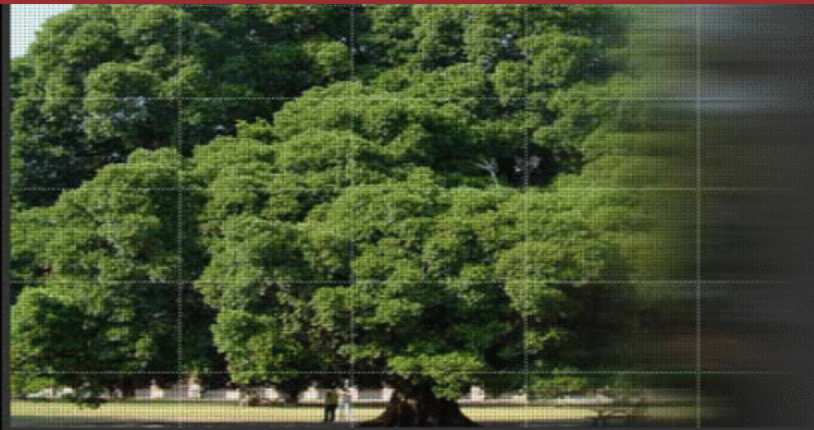




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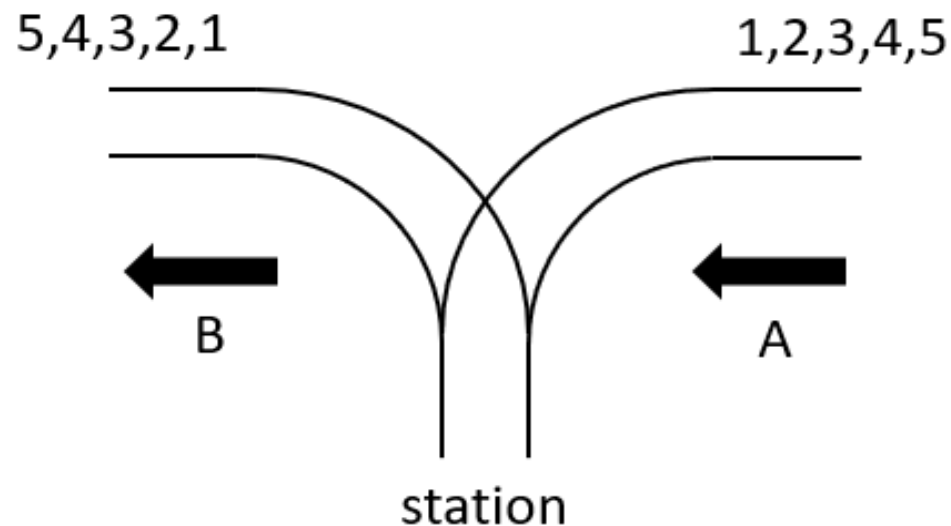
Homework 2 explanation

NCKU CSIE DICLAB

Introduction



- ▶ Every train arrives at the station from direction A, and departs the station from direction B.
- ▶ The arriving trains will be numbered in ascending order from 1 to N . ($3 \leq N \leq 10$)
- ▶ Given a departure order $d1, d2, \dots, dN$, the circuit has to determine if the trains can leave the station in the required order.
- ▶ For any train, there is no limit to its arrival time and staying time at the station.

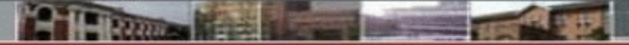


Finite State Machine

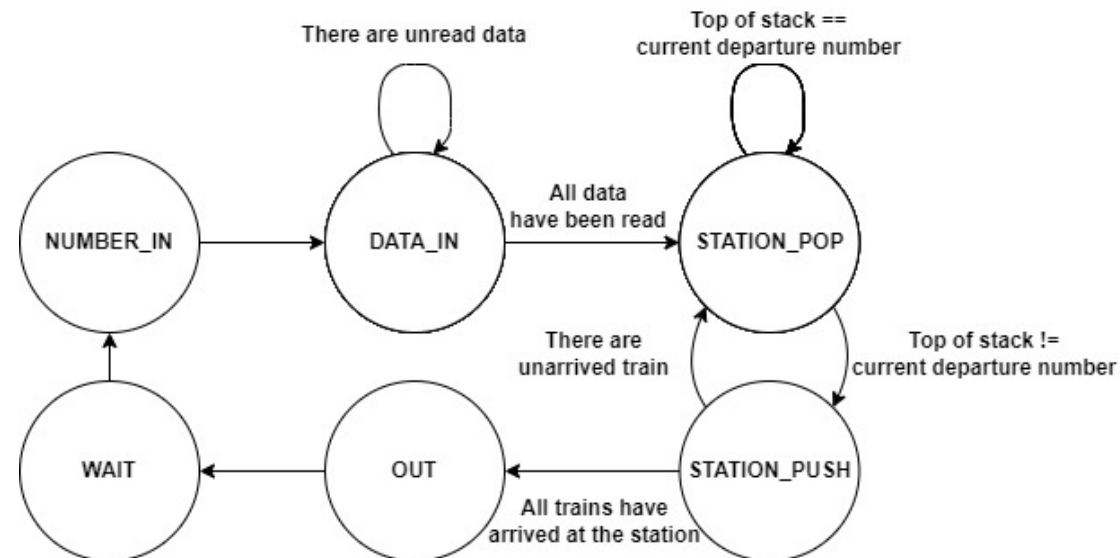


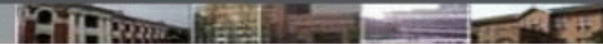
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1. NUMBER_IN : Read the number of coming trains
2. DATA_IN : Read the sequence of departure order
3. STATION_POP : Examine whether the top of stack is equal to current departure number
4. STATION_PUSH : Push number into the stack
5. OUT : Output determination result
6. WAIT : Reset registers and go back to the initial state (NUMBER_IN)





Data Registers

- ▶ num : record the number of coming trains
- ▶ index : index of sequence of departure order
- ▶ order : data array to store departure order
- ▶ station_index : index of the stack
- ▶ station : data array that acts as the stack
- ▶ sequence_index : count of arrived train

order

index	0	1	2	3	4	5	6	7	8	9
data										

stack

index	0	1	2	3	4	5	6	7	8	9
data										

num: 0
sequence_index: 1



NUMBER_IN & DATA_IN

```
70      NUMBER_IN:begin//read number
71          num <= data;
72      end
73      DATA_IN:begin//read data
74          order[index] <= data;
75          if(index == num - 1) index <= 4'd0;
76          else index <= index + 1;
77      end
```

order

index	0	1	2	3	4	5	6	7	8	9
data	4	3	2	5	1					

stack

index	0	1	2	3	4	5	6	7	8	9
data										

num: 5
sequence_index: 1

STATION_POP



```
78      STATION POP:begin//compare top with order
79      if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80          index <= index + 1;
81          station_index <= station_index - 1;
82      end
83  end
```

**station_index == 0 , the stack is empty
go to STATION_PUSH state**

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					

stack	index	0	1	2	3	4	5	6	7	8	9
	data										

num: 5
sequence_index: 1



STATION_PUSH

```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

Train 1 arrives at the station, push 1 into the stack.

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1									

num: 5
sequence_index: 2

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack != current departure number
go to STATION_PUSH state

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1									

num: 5
sequence_index: 2



STATION_PUSH

```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

Train 2 arrives at the station, push 2 into the stack.

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2								

num: 5
sequence_index: 3

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack != current departure number
go to STATION_PUSH state

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2								

num: 5
sequence_index: 3



STATION_PUSH

```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

Train 3 arrives at the station, push 3 into the stack.

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2	3							

num: 5
sequence_index: 4

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack != current departure number
go to STATION_PUSH state

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2	3							

num: 5
sequence_index: 4



STATION_PUSH

```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

Train 4 arrives at the station, push 4 into the stack.

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2	3	4						

num: 5
sequence_index: 5

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack == current departure number

Pop an element from stack and stay at STATION_POP state

Increase the index of order array

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					

stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2	3	4						

num: 5

sequence_index: 5

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack == current departure number

Pop an element from stack and stay at STATION_POP state

Increase the index of order array

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					

stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2	3							

num: 5

sequence_index: 5

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack == current departure number

Pop an element from stack and stay at STATION_POP state

Increase the index of order array

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					

stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	2								

num: 5

sequence_index: 5

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack != current departure number
go to STATION_PUSH state

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1									

num: 5
sequence_index: 5



STATION_PUSH

```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

Train 3 arrives at the station, push 3 into the stack.

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	5								

num: 5
sequence_index: 6

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack == current departure number

Pop an element from stack and stay at STATION_POP state

Increase the index of order array

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	1	5								

num: 5

sequence_index: 6

STATION_POP



```
78      STATION_POP:begin//compare top with order
79          if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80              index <= index + 1;
81              station_index <= station_index - 1;
82          end
83      end
```

The top of stack == current departure number

Pop an element from stack and stay at STATION_POP state

Increase the index of order array

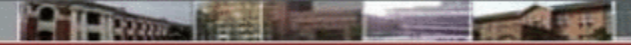
order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					

stack	index	0	1	2	3	4	5	6	7	8	9
	data	1									

num: 5

sequence_index: 6

STATION_POP



```
78      STATION_POP:begin//compare top with order
79      if((station_index > 4'd0) && (station[station_index_minus_one] == order[index]))begin
80          index <= index + 1;
81          station_index <= station_index - 1;
82      end
83  end
```

**station_index == 0 , the stack is empty
go to STATION_PUSH state**

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data										

num: 5
sequence_index: 6

STATION_PUSH



```
84      STATION_PUSH:begin//pop ascending sequence
85          station[station_index] <= sequence_index;
86          station_index <= station_index + 1;
87          sequence_index <= sequence_index + 1;
88      end
```

```
40  ▾  STATION_PUSH:begin
41      if(sequence_index == num + 1) nextState = OUT;
42      else nextState = STATION_POP;
43  end
```

Push 6 into the stack.

sequence_index == num + 1 ,
go to OUT state

order

index	0	1	2	3	4	5	6	7	8	9
data	4	3	2	5	1					

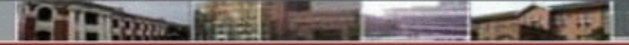
stack

index	0	1	2	3	4	5	6	7	8	9
data	6									

num: 5

sequence_index: 6 + 1

OUT



```
89 ▼      OUT:begin//output result
90          valid <= 1;
91          if(index == num) result <= 1;
92          end
```

Pull up valid to 1

index == 5 , result = 1

order	index	0	1	2	3	4	5	6	7	8	9
	data	4	3	2	5	1					
stack	index	0	1	2	3	4	5	6	7	8	9
	data	6									

num: 5
sequence_index: 7

WAIT



```
93 ▼      WAIT:begin//reset register
94          for(i = 0; i < 10; i = i + 1) station[i] <= 4'b1111;
95          valid <= 0;
96          result <= 0;
97          index <= 0;
98          station_index <= 4'd0;
99          sequence_index <= 4'd1;
100      end
```

Pull down valid to 0

Reset registers

order

index	0	1	2	3	4	5	6	7	8	9
data										

stack

index	0	1	2	3	4	5	6	7	8	9
data										

num: 5

sequence_index: 1