



# North South University

Department of Electrical & Computer Engineering

## LAB REPORT- 04

Course Code: **EEE141L**

Course Title: **Electrical Circuits Lab**

Section: **07**

Lab Number: **04**

Experiment Name:

### Delta-Wye Conversion

Experiment Date: **28<sup>th</sup> March, 2024**

Date of Submission: **4<sup>th</sup> April, 2024**

Submitted by Group Number: **02**

Group members:

Serial	Name	ID	Marks
01	Md Tamim Ahamed	2014286642 (W)	
02	Sudipto Roy	2222756042	
03	Rezuan Islam Samir	2021092642	
04	Abrar Tazwar Aziz	1813399642	
05	Sadman Sakib Prodhan	1510748642	

Course Instructor: **Dr. Mahdy Rahman Chowdhury (Mdy)**

Submitted To Lab Instructor: **Md. Masud Rana**

### Objective:

- ① To Perform Delta-Wye Conversion.
- ② To verify the results with measured Data.
- ③ Solve the complex circuit using Delta-Wye conversion.

### Equipment:

- ① Trainer Board
- ② Software
- ③ DMM
- ④  $5 \times (5 \text{ k}\Omega)$
- ⑤  $3 \times (5 \text{ k}\Omega)$

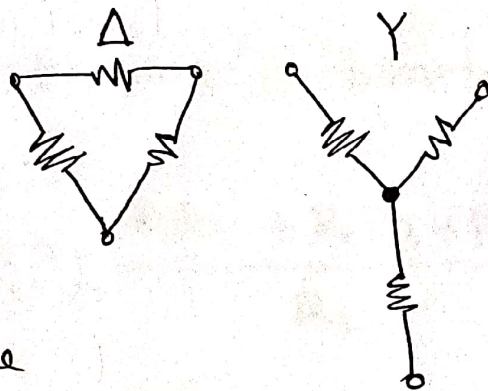
### Theory:

In many circuits, the components of resistors are connected to a certain way that looks like the "delta" ( $\nabla$ ) and " $\gamma$ " format that is known as Delta-Wye.

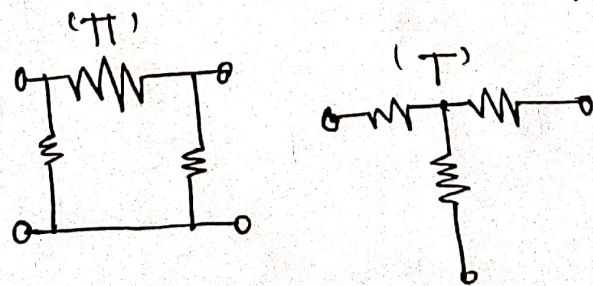
[P.T.O.]



Sometimes it is hard to identify the resistors connections if those were connected parallel or series. At that time, we use delta-wye conversion to calculate the total resistor in an easier way. With this conversion, we can change the  $\Delta$  for  $Y$  as vice-versa. This is also called  $\pi$ - $T$  transformation when the connection of resistor looks like  $\pi$  or  $T$ .



Here in the drawing, we can see the formation of both  $\Delta$  and  $Y$ . The difference between these two formations is one has three and other has four nodes.



These resistor connection look like  $\pi$  and  $T$ , is called  $\pi$ - $T$  configuration. But that is same as  $\Delta$ - $Y$  configuration.



To convert a Delta ( $\Delta$ ) to a Wye ( $Y$ ):

$$R_A = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_B = \frac{R_A R_c}{R_a + R_b + R_c}$$

$$R_C = \frac{R_a R_b}{R_a + R_b + R_c}$$

To convert  $Y \rightarrow \Delta$  transformation:

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

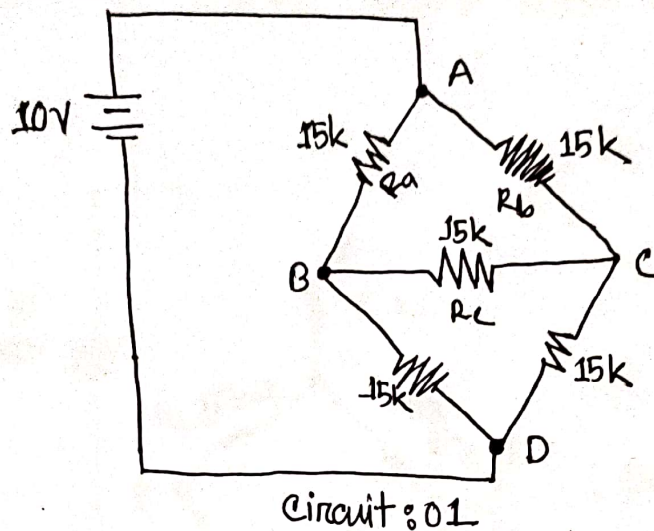
$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

#### Procedure :

- ① Measure the resistor values with DMM and noted down in table 1.
- ② Then setup the circuit as shown in the circuit 1.
- ③ After that we measure voltage to AD, BD and CD, and noted down table 2
- ④ Then, measure  $V_{AB}$ ,  $V_{BC}$  and  $V_{AC}$  and note down table 2.
- ⑤ Then we setup circuit 2
- ⑥ After that, the voltage  $V_{AD}$ ,  $V_{BD}$  and  $V_{CD}$  (D is the reference node) and note down in table 2)
- ⑦ Measure the voltage  $V_{AB}$ ,  $V_{BC}$ ,  $V_{AC}$  and note down in table 2.



① Solution:



The resistors in circuit 1 are in vague to identify that it's in series or parallel combination.

② Solution:

Here we used Delta-wye conversion to find the equivalent resistance.

③ Solution:

Circuit 1 is in  $\nabla$  form.  $R_A$ ,  $R_B$ ,  $R_C$  all these resistors values are  $15k\Omega$ . From  $\nabla$  to Y

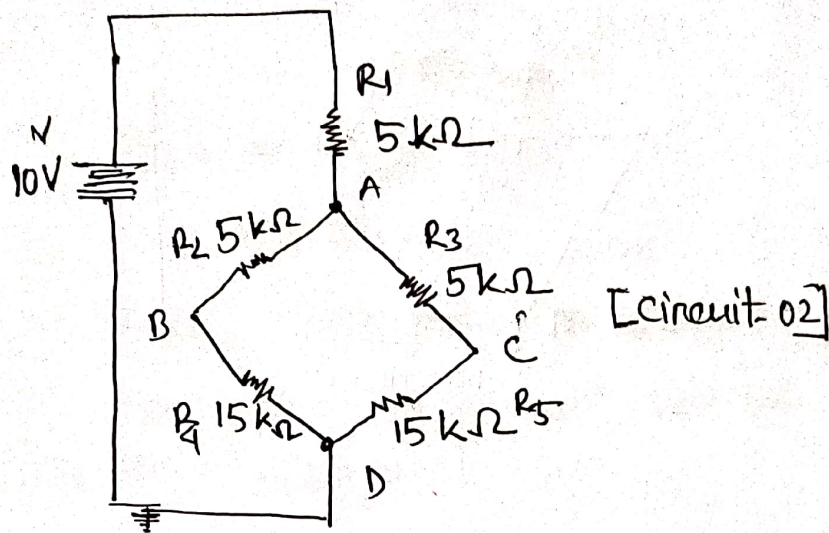
conversion -

$$\begin{aligned} R_1 = R_2 = R_3 &= R_B \times R_C / R_A + R_B + R_C \\ &= 15 \times 15 / 45 \\ &= 5k\Omega \end{aligned}$$



④ Solution:

The equivalent circuit after delta-wye conversion



Yes,  $\Delta ABC$  is the same as circuit 2. Because circuit 2 itself is a formatted circuit.

⑤ Calculating  $R_{eq}$ .

= from circuit 2

$$R_2 \text{ series } R_4 = (5 + 15) = 20 \text{ k}\Omega$$

$$R_3 \text{ series } R_5 = (5 + 15) = 20 \text{ k}\Omega$$

Now, these are connected

$$\text{parallel } R_P = (20 \parallel 20) \\ = 10 \text{ k}\Omega$$

Therefore,

$$R_{eq} \text{ is } = 5 + R_P \\ = 5 + 10 \\ = 15 \text{ k}\Omega$$



⑥ Calculating the voltage of  $R_1, R_2, R_3$

= From Q5, the req. is  $15 \text{ k}\Omega$

Therefore,  $I = 10/15$

$$= .67 \text{ mA}$$

$$V_{R_1} = 5 \times .67$$

$$= 3.35 \text{ V}$$

$R_2 \text{ \& } R_4 \parallel R_3 \text{ \& } R_5$  with equal resistors in both side of parallel connection. So, current will be equally divided in this node.

$$V_{R_2} = 5 \times .335$$

$$= 1.67 \text{ V}$$

$$V_{R_3} = 5 \times .335$$

$$= 1.67 \text{ V}$$

⑦

From circuit 2,

$$V_{ae} = V_{ab} = V_{R_1} + V_{R_2}$$

$$= 3.35 + 1.67$$

$$= 5.02 \text{ V}$$

$$\text{ERROR} = \left( \frac{5 - 5.02}{5.02} \right) \times 100$$

$$= .398 \%$$



### Discussion :

In this lab session we focused on Delta-Wye transformation, the fundamental technique used in analyzing electrical circuits. In this lab, we have explored the concept, conversion formula's and its practical application. We got ~~a~~ right data similar to experimental and theoretical data.

We came to a conclusion that, Delta-wye conversion is a valuable tool for simplifying and analyzing electrical circuits, that allows a impactful technique in various complex circuits.

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Group: 02

SECTION: 07

## NORTH SOUTH UNIVERSITY

DEPARTMENT OF ELECTRICAL &amp; COMPUTER ENGINEERING



EEE41L/ETE141L

Instructor's Signature

02

For, 15k :

$$\frac{14.92 + 14.98 + 14.94 + 14.81 + 14.87}{5} = 14.904$$

Table 1:

Theoretical R	Measured R	% Error
15k	14.92 k $\Omega$ , 14.98 k $\Omega$ , 14.94 k $\Omega$ , 14.81 k $\Omega$ , 14.87 k $\Omega$	0.64 %
5k	4.85 k $\Omega$ , 5.14 k $\Omega$ , 4.95 k $\Omega$	0.4 %

$$\text{For, 5k: } \frac{4.85 + 5.14 + 4.95}{3} = 4.98$$

Table 2:

Readings	Rt= 15 K		Rt= 15 K		% Error
$V_{AD}$	10 V	10.09 V	10 V	10.09 V	0 %
$V_{BD}$	5 V	5.05 V	5 V	5.11 V	1.19 %
$V_{CD}$	5 V	5.05 V	5 V	5.06 V	0.19 %
$V_{AB}$	5 V	5.03 V	5 V	4.98 V	0.99 %
$V_{BC}$	0 V	0.11 V	0 V	0.113 V	2.73 %
$V_{AC}$	5 V	5.03 V	5 V	5.02 V	0.198 %

\* MD Tamim

## Report:

1. The resistors in Circuit 1 are in series or in parallel combination?
2. What technique would you use to find the equivalent resistance?
3. Perform Delta-Wye conversion for  $\Delta ABC$  (upper portion) of circuit 1. Show all your steps to find the equivalent resistance  $R_1$ ,  $R_2$ ,  $R_3$  from  $R_a$ ,  $R_b$ ,  $R_c$ .
4. Redraw the equivalent the circuit after applying the Delta-Wye conversion for  $\Delta ABC$ . Is it same as circuit 2?
5. Calculate  $R_{eq}$ .
6. Calculate the voltage of  $R_1$ ,  $R_2$ ,  $R_3$ .
7. Calculate  $V_{AB}$ ,  $V_{BC}$ ,  $V_{AC}$  and  $V_{AD}$ ,  $V_{BD}$ ,  $V_{CD}$ . Do your calculated values match the measured values for circuit 2? Find the % Error.
8. Using Table 2, analyze whether Circuit 2 is equivalent to Circuit 1? Was Delta-Wye conversion successful?