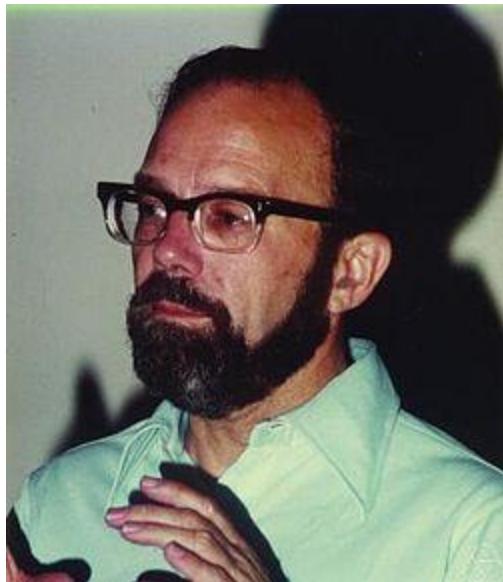


Who's Guarding the Louvre?! The Art Gallery Problem Explained

Shayan Shahrabi – Fall 2025
shayanshahrabi.github.io



Problem Statement

20TH Century

American

Audubon

American

Ancient American

North Courtyard

Ancient Egyptian



Thematic
Gallery

African

Rodin Garden

Rodin Court

Sculpture Court

20TH-21ST
Century

Art
Conservation

European

European

Judaic

European

Ancient Greek,
Italian, and Roman

EXIT

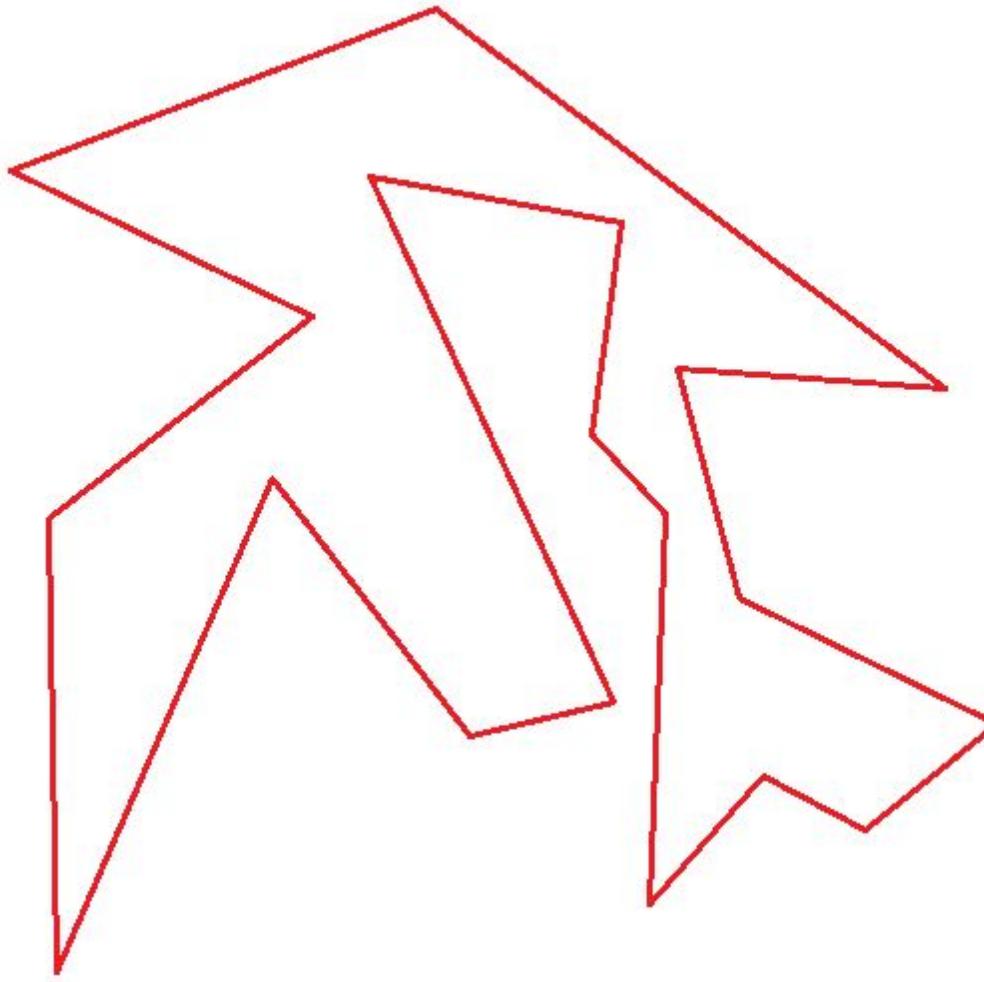
ENTRY

NCMA Café

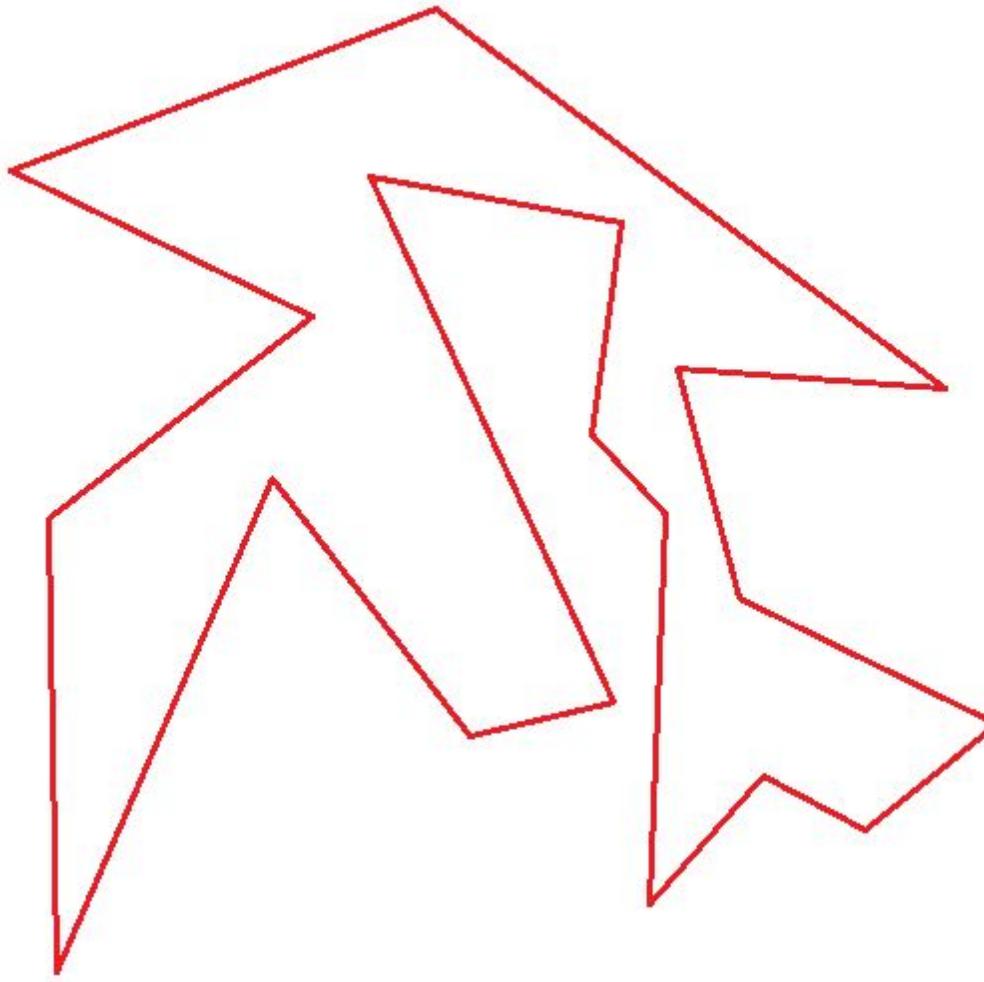
Museum Store

Assumptions

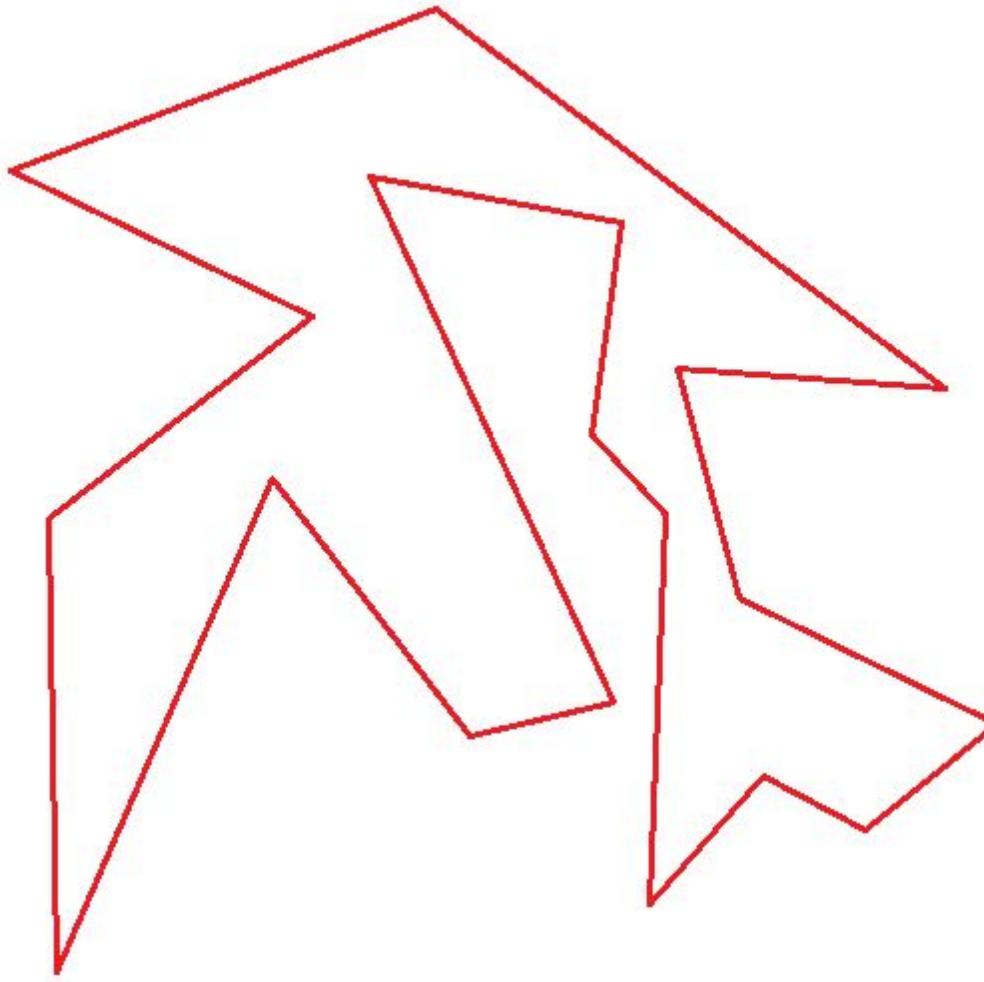
1. 360-degree FOV



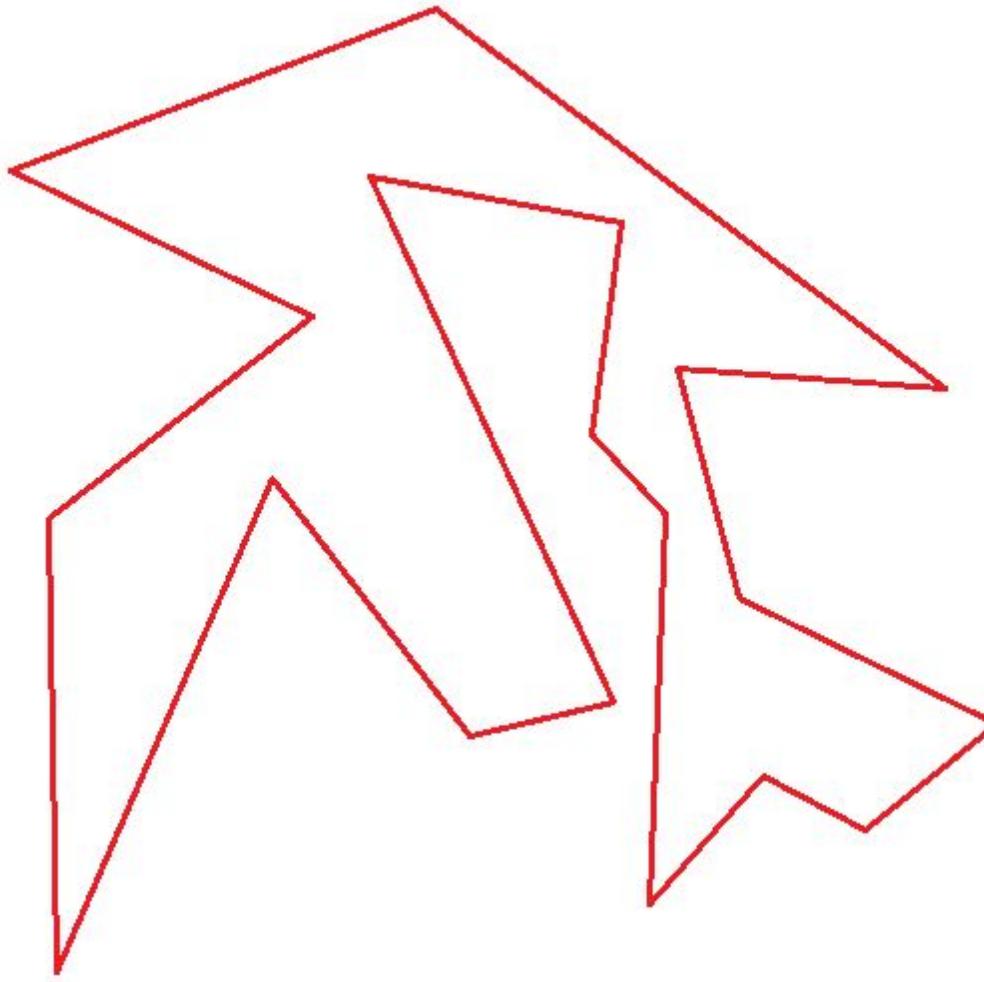
2. Unbounded visibility dist.



3. For guard G & point P ...

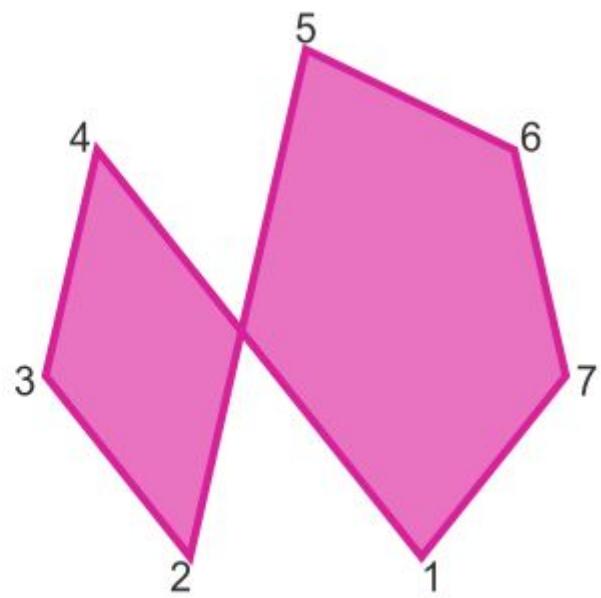
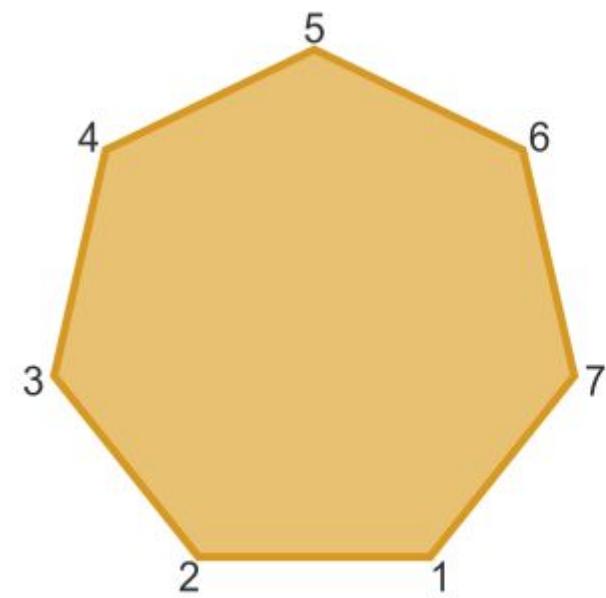


Problem Statement?!

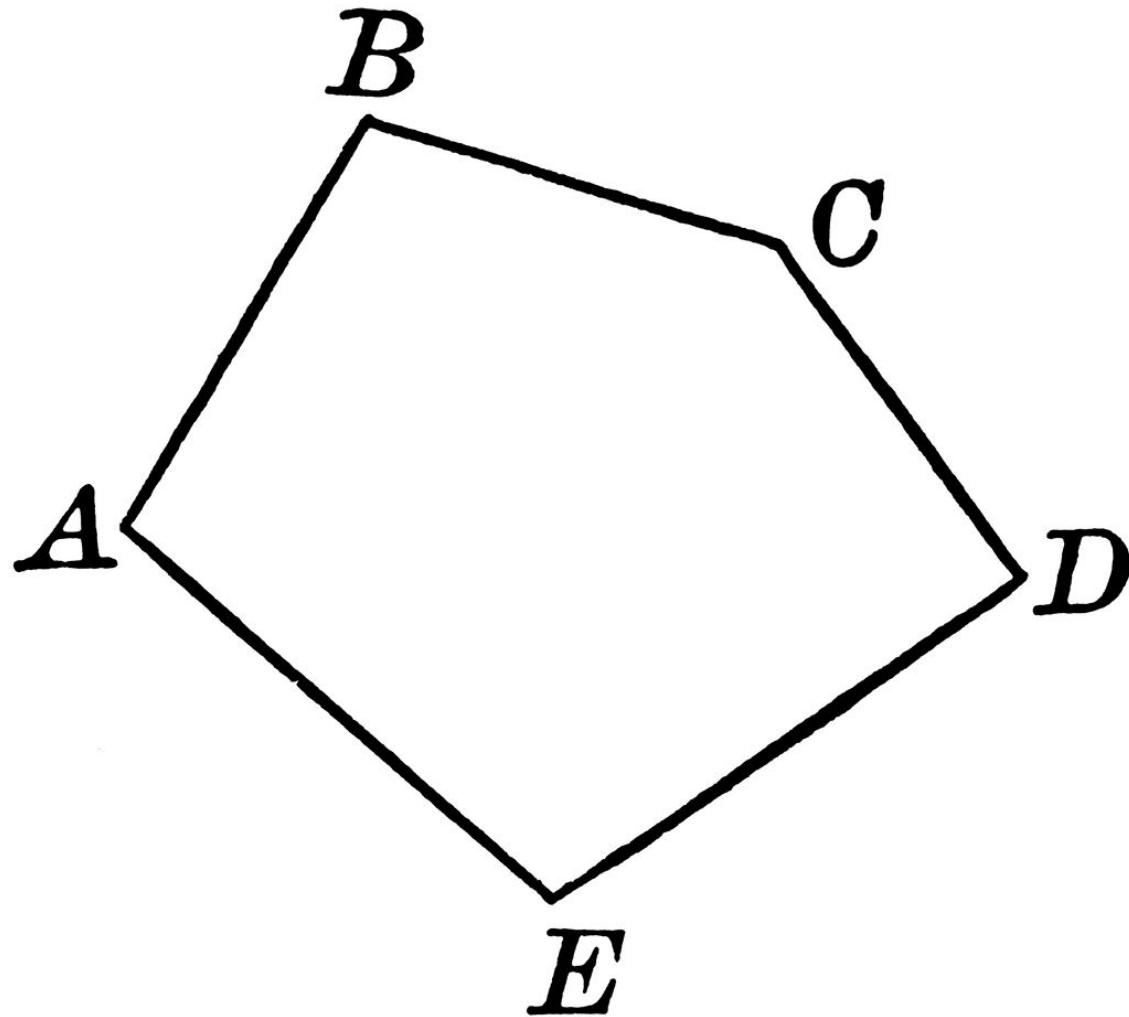


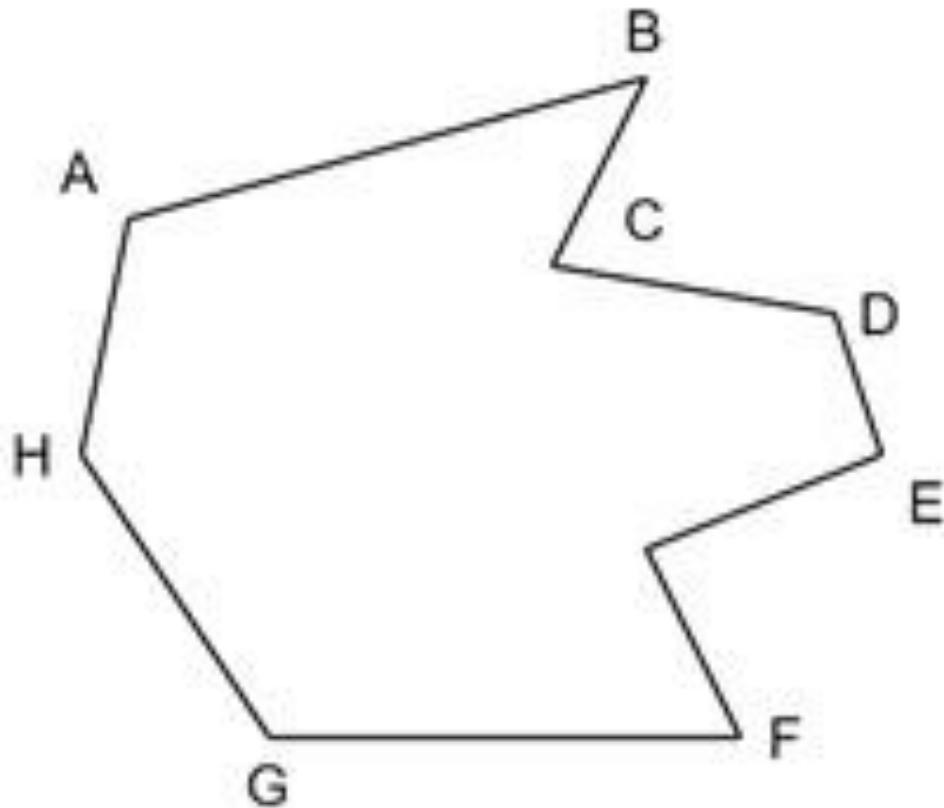
Some Examples

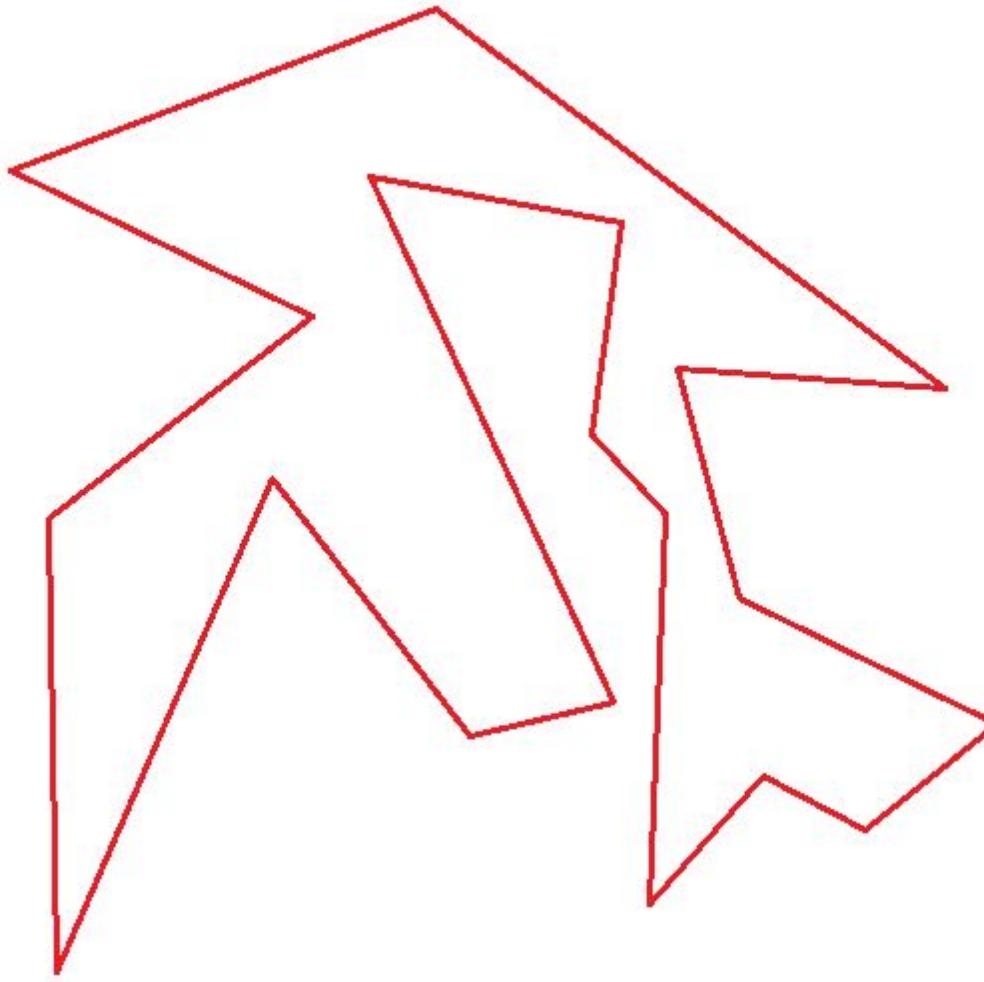
But Before That...



Now Some Examples!







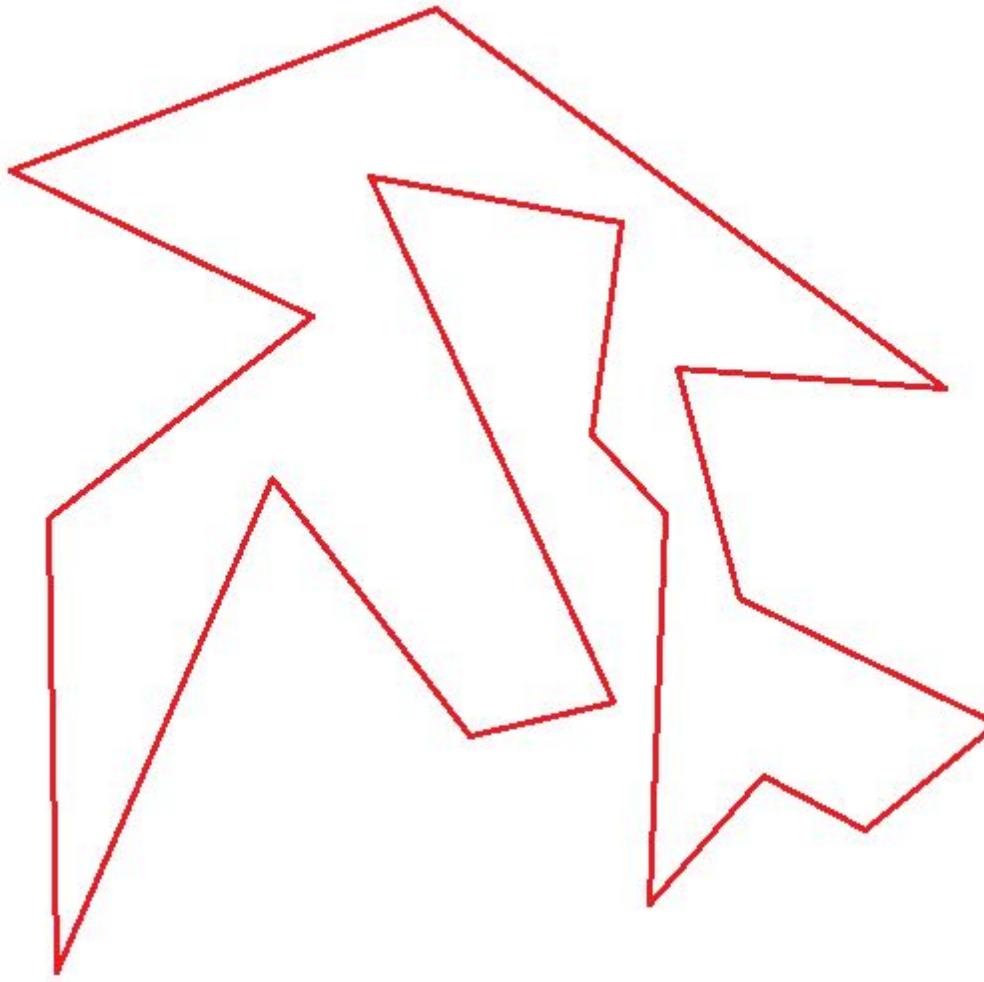
There are 2 parts to the problem

Part I : # Sufficient Guards

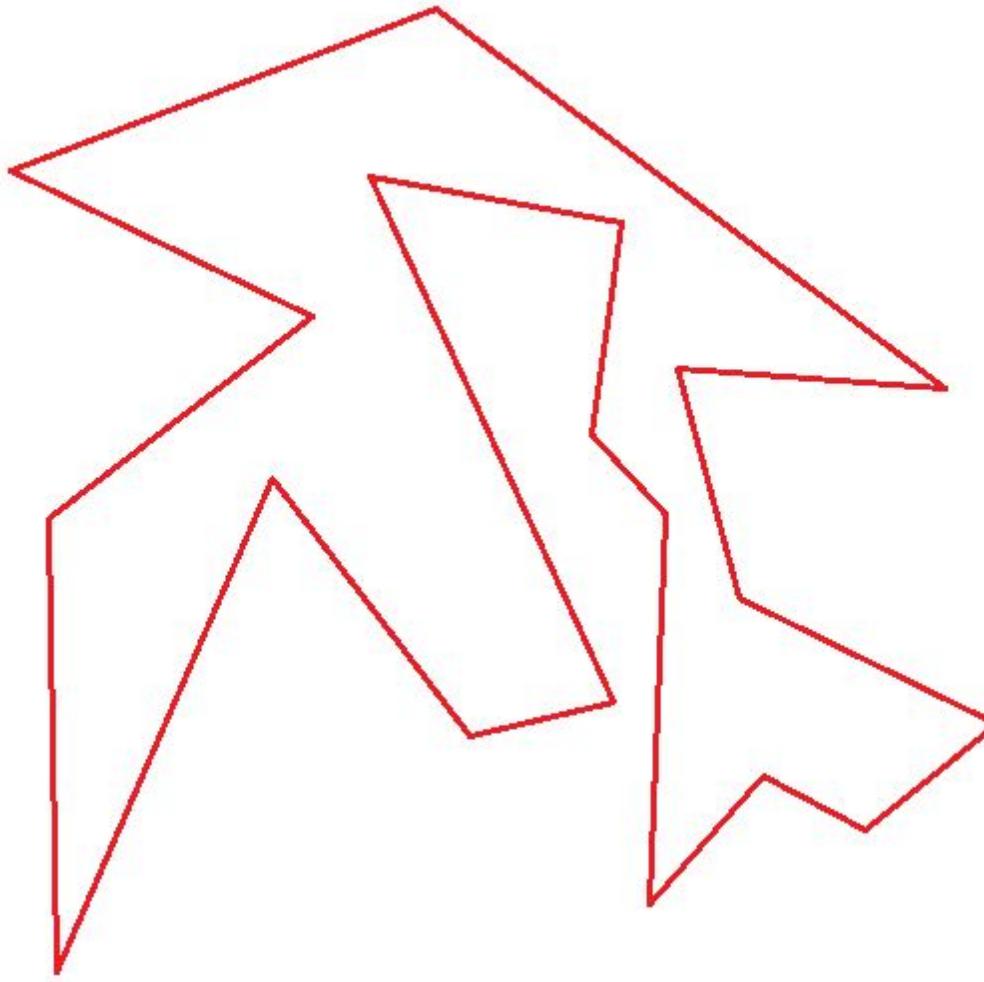
Part II : Minimal # Guards

Part I Vs. Part II ?

Note: We do NOT Consider Polygons with Holes



Guards Can Be Placed ANYWHERE!

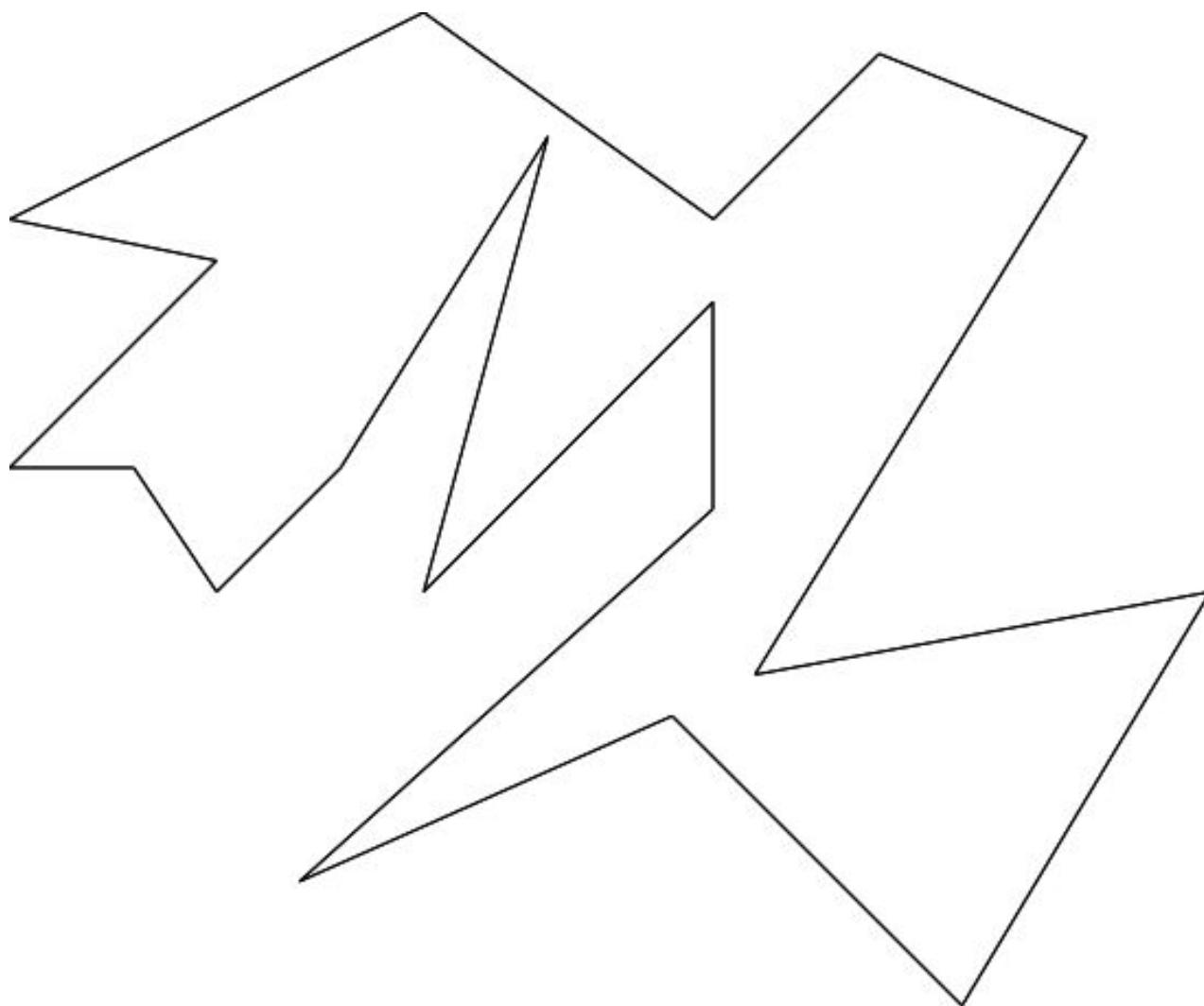


Let's Solve Part I

Sufficient Guards

Our Thinking Procedure?

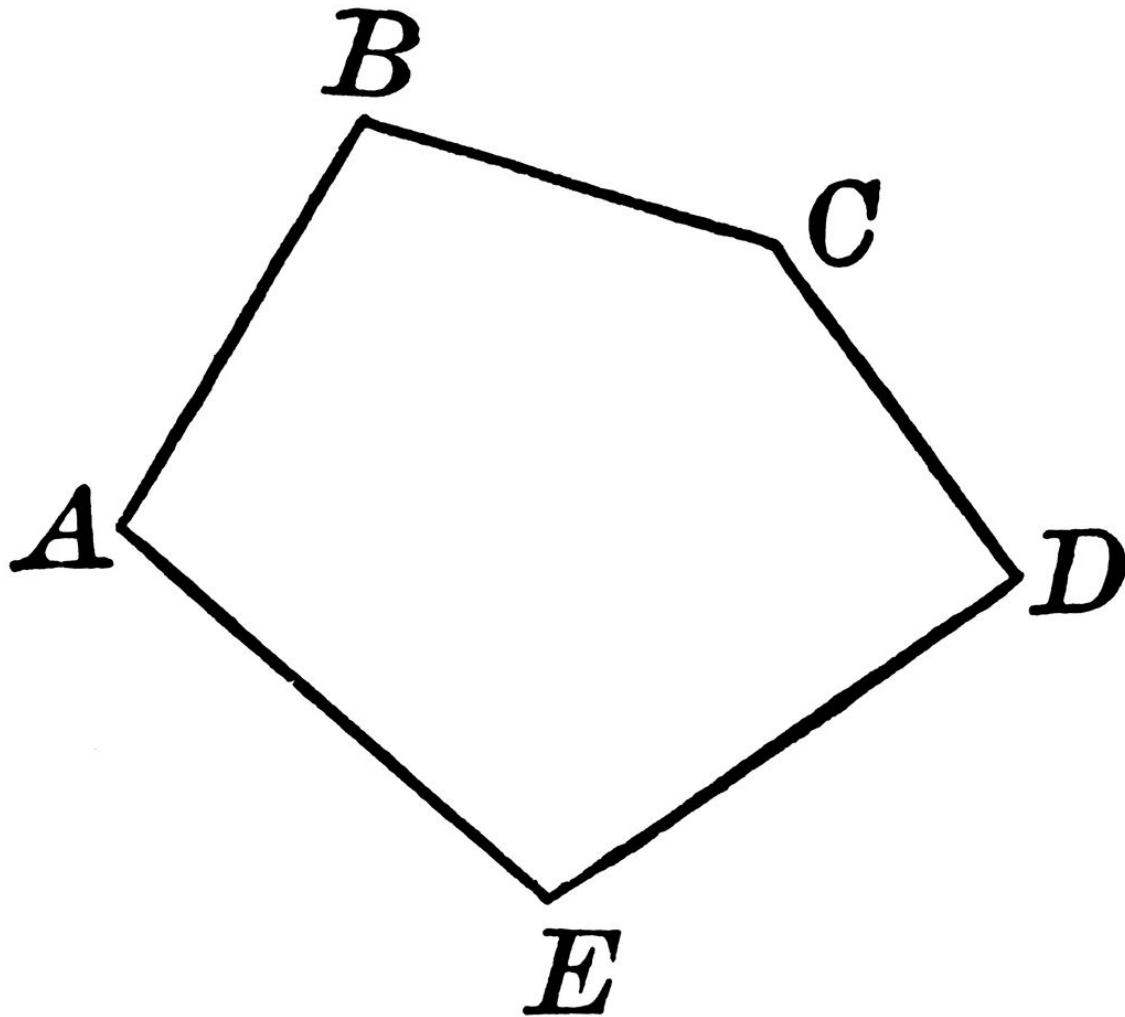
A Naive Approach (g_1 Func.)

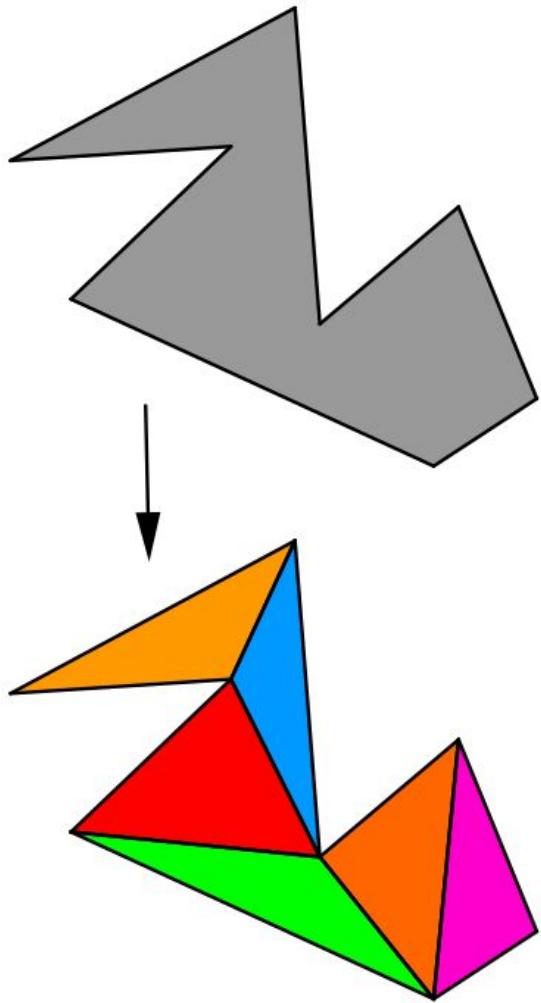


A Better Upper Bound?

The Concept of Triangulation

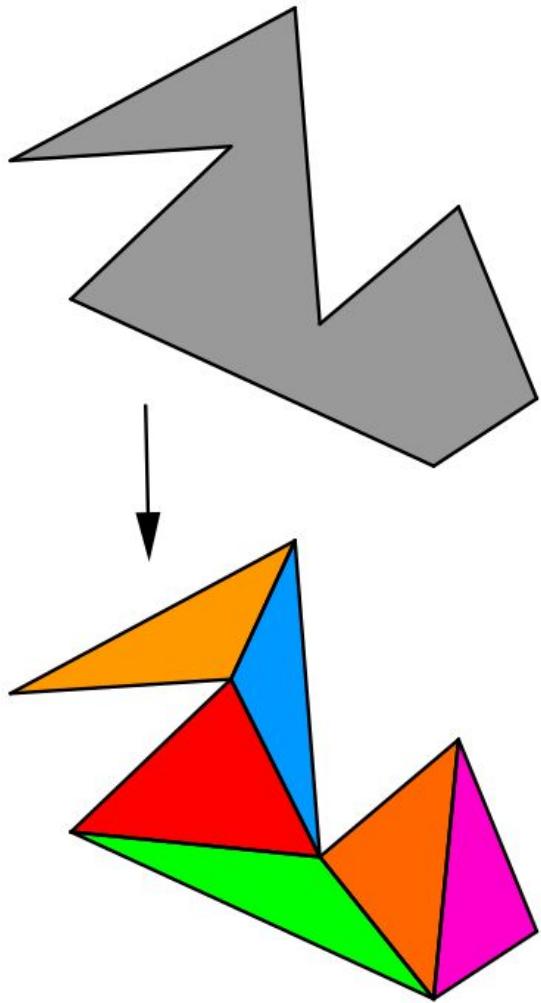
Definition





Is It Unique?

NO!



Always Feasible?

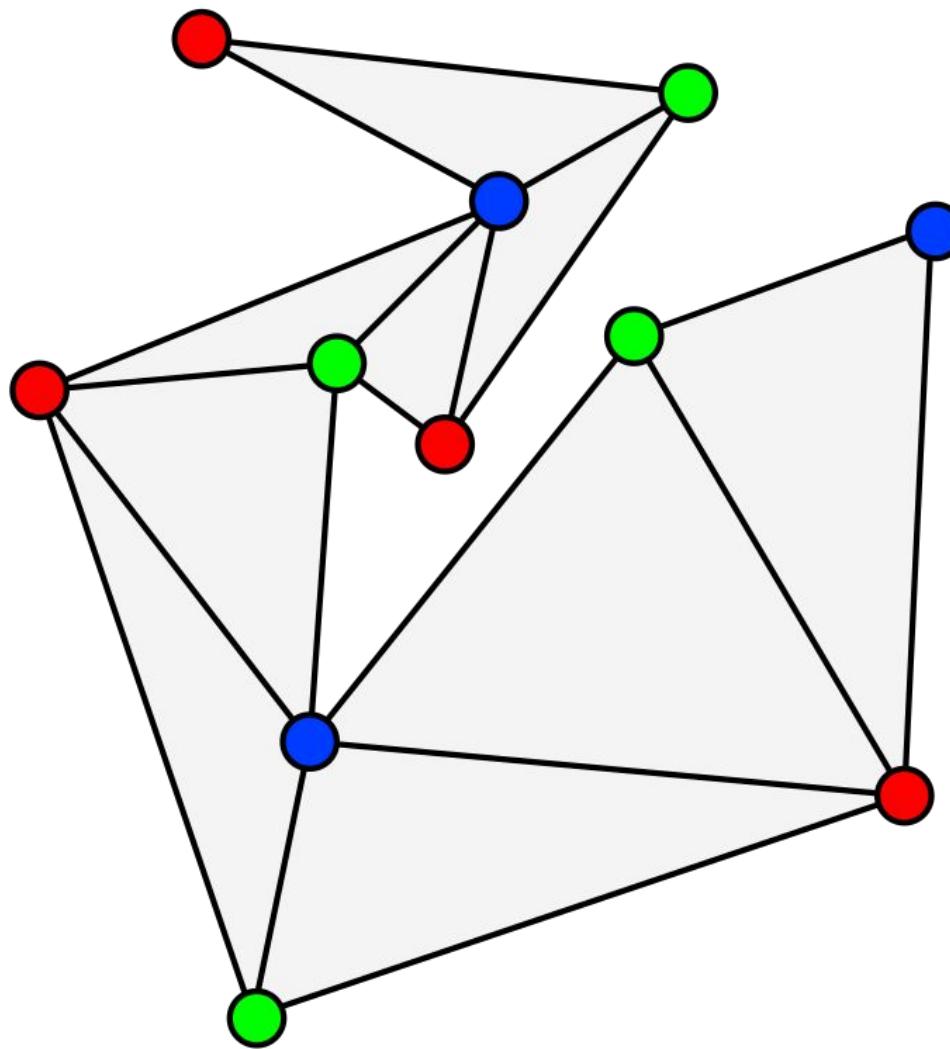
YES!
(Triangulation Theorem)

HOW?

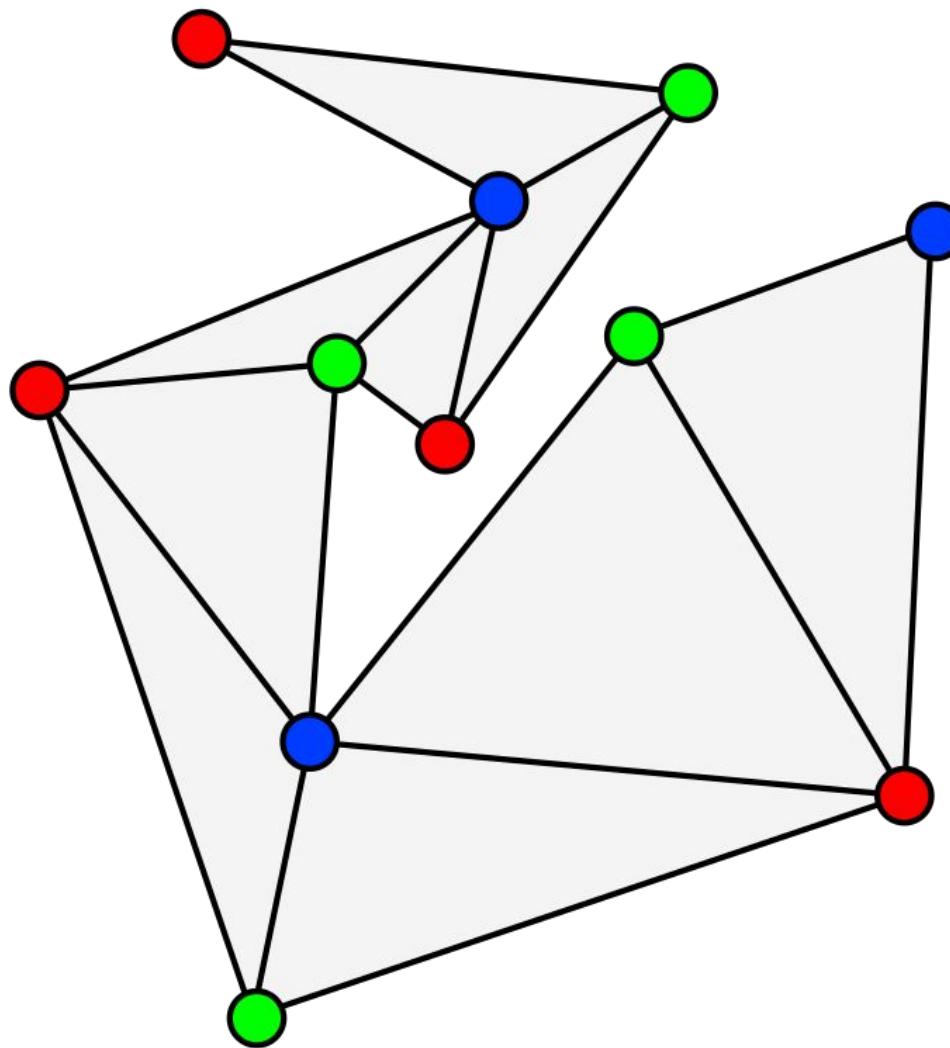
The Ear Clipping Algorithm

[Triangulation by Ear Clipping, David Eberly](#)

[Polygon Triangulation Wikipedia Page](#)

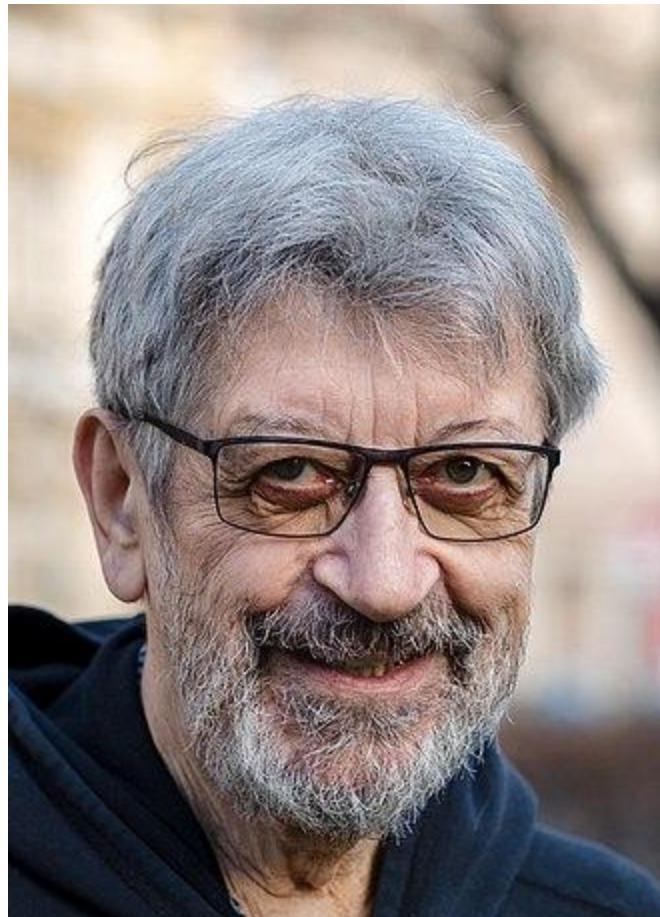


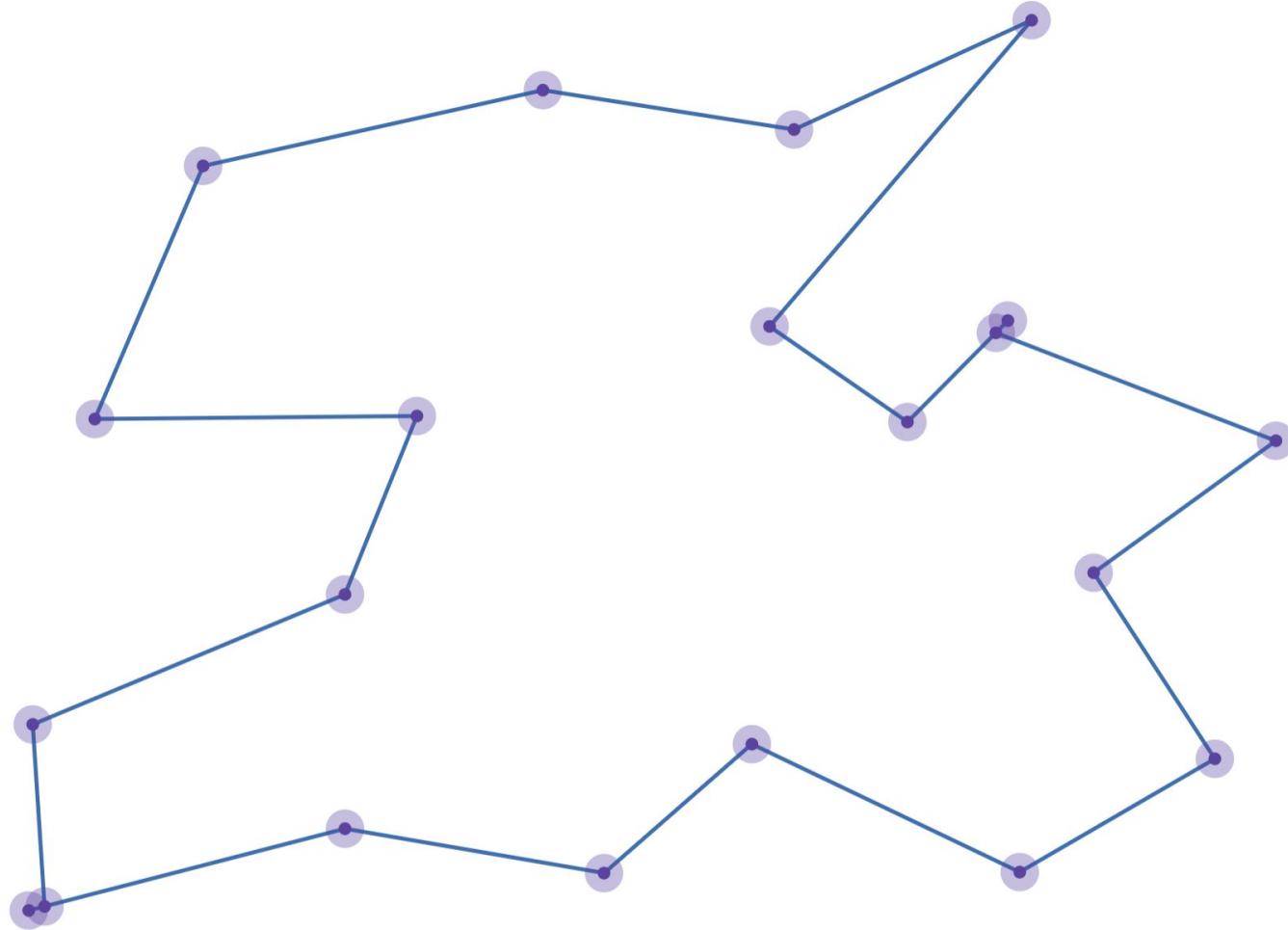
Maybe a Better Bound?
(g_2 Func.)

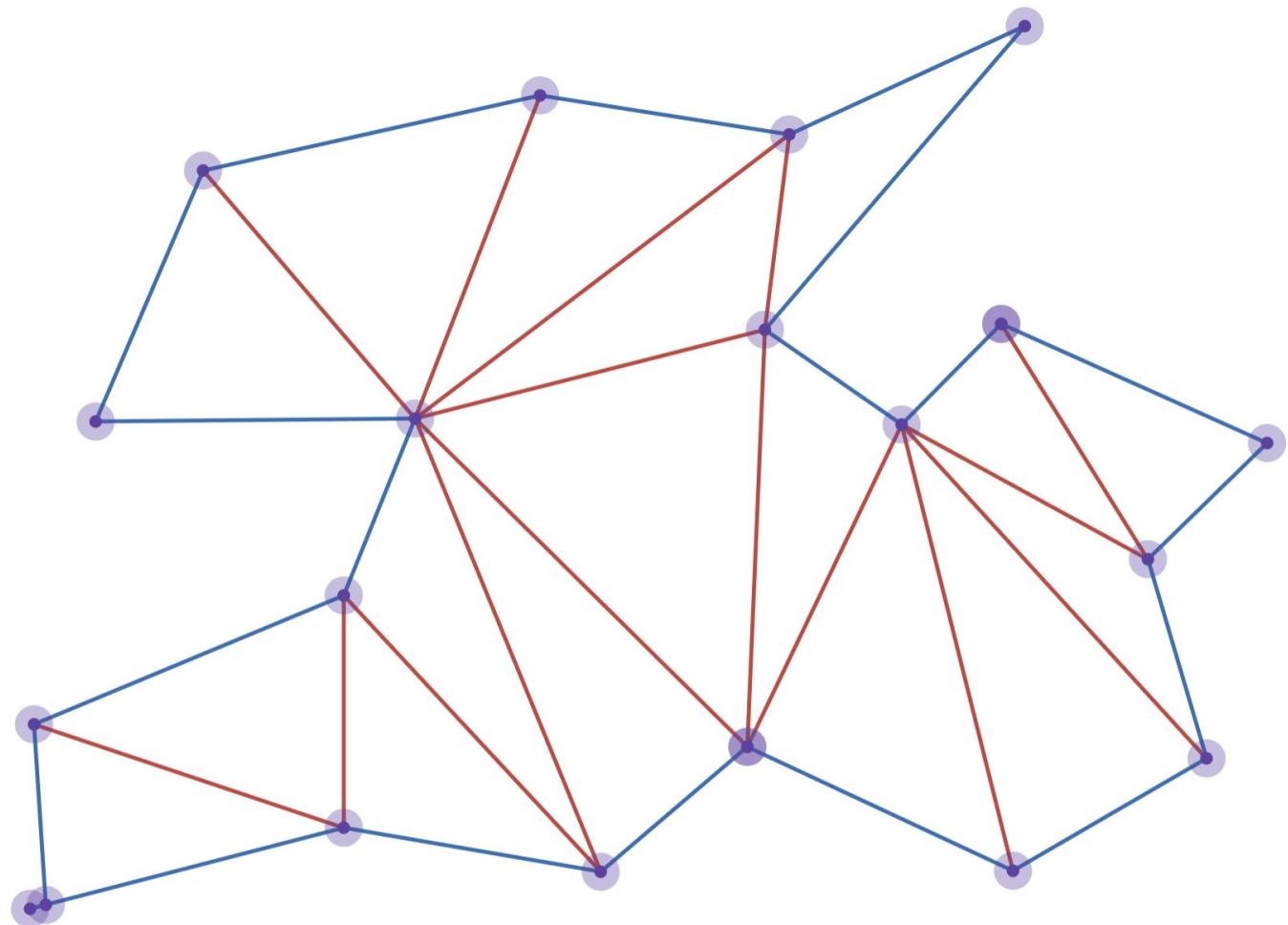


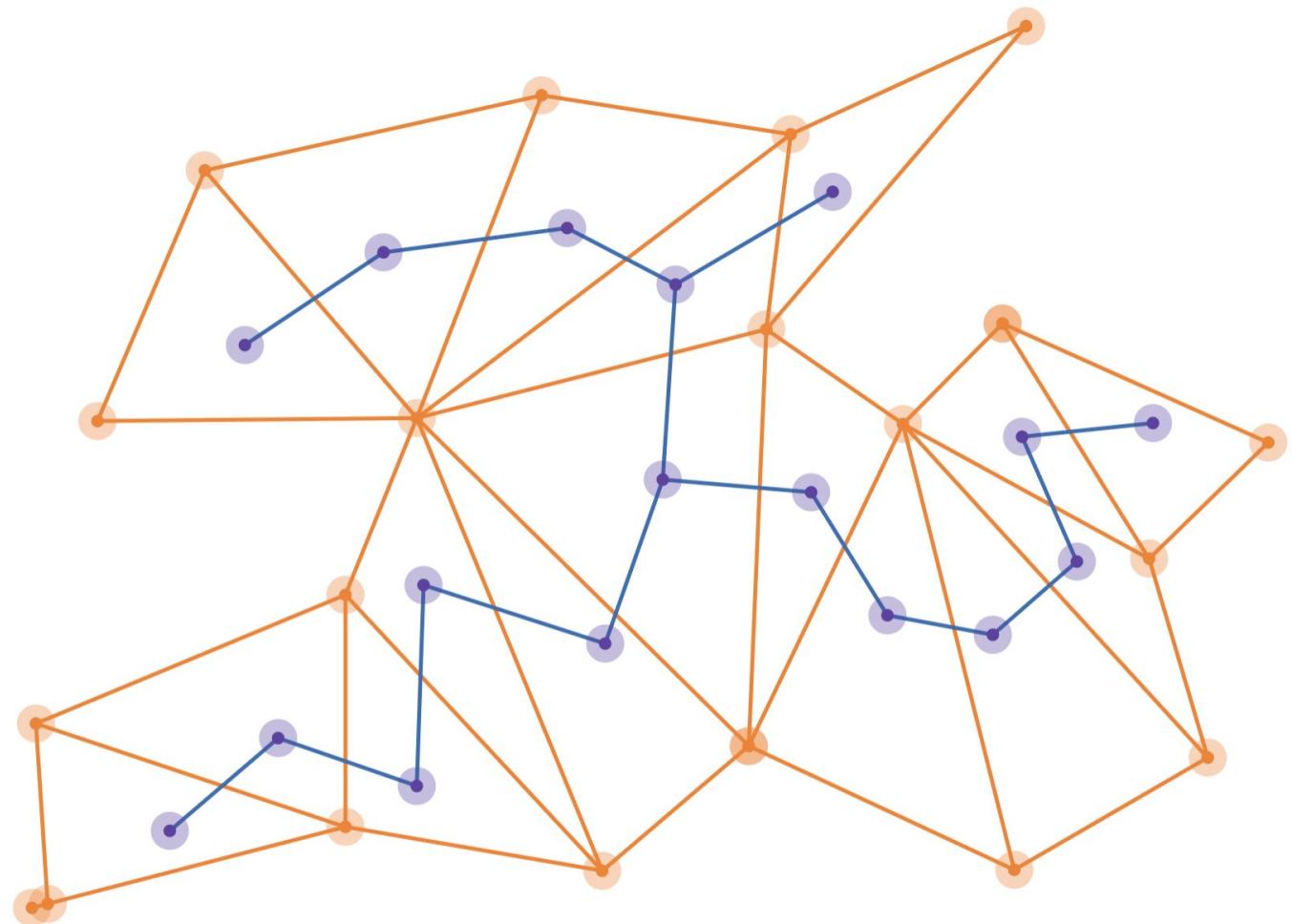
Are We Close to the Answer?

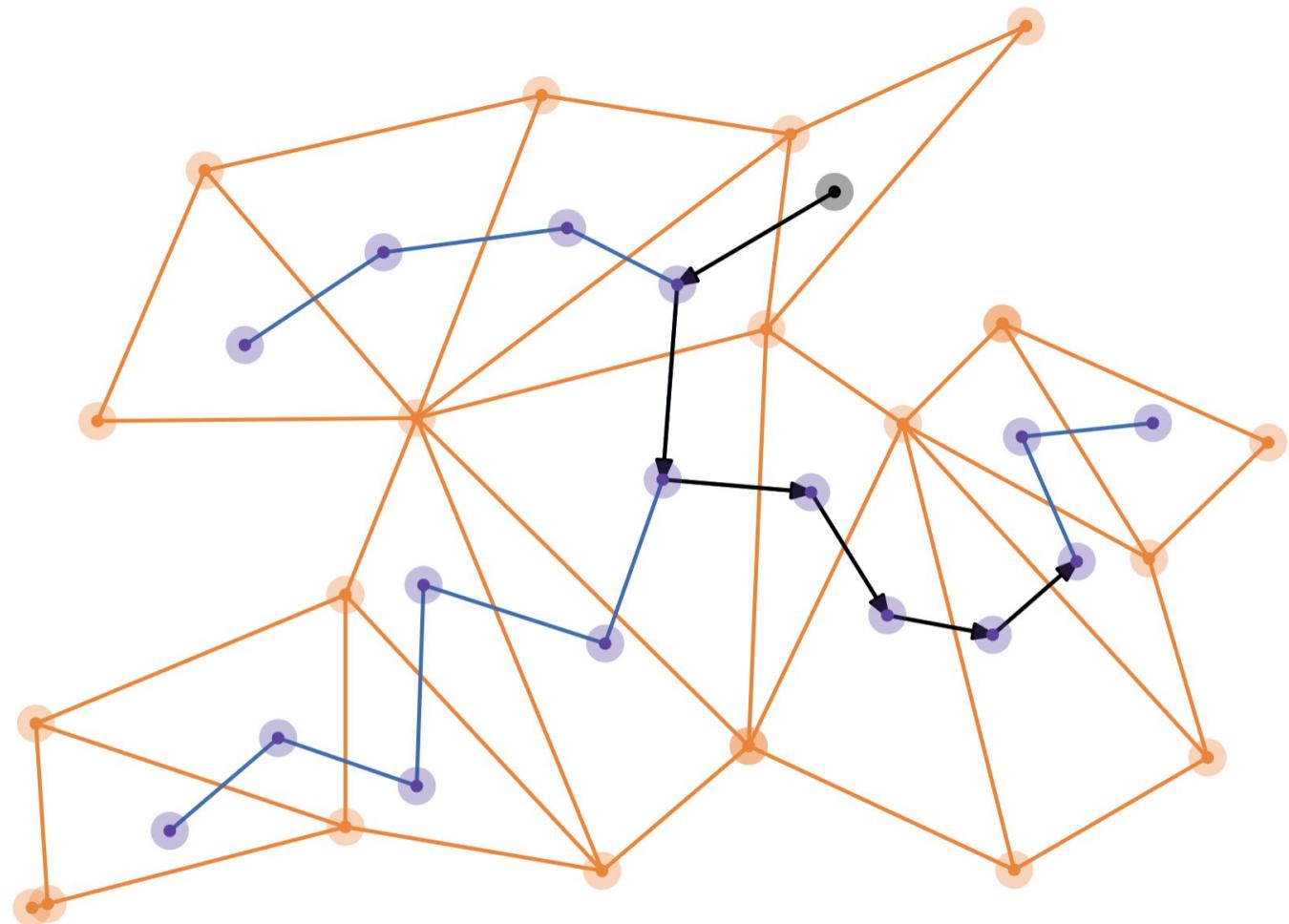
Chvátal's Art Gallery Theorem (g₃ Func.)

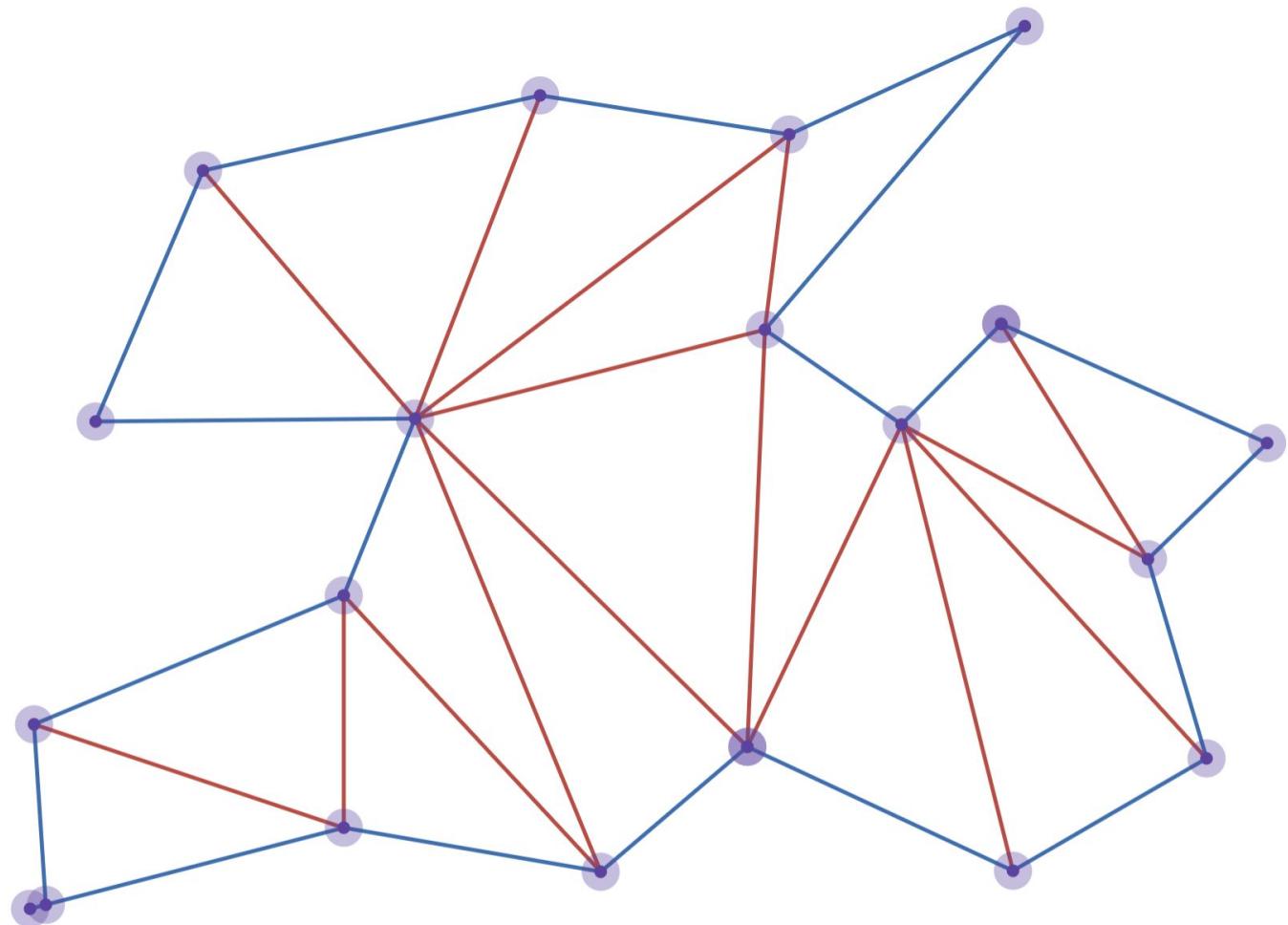




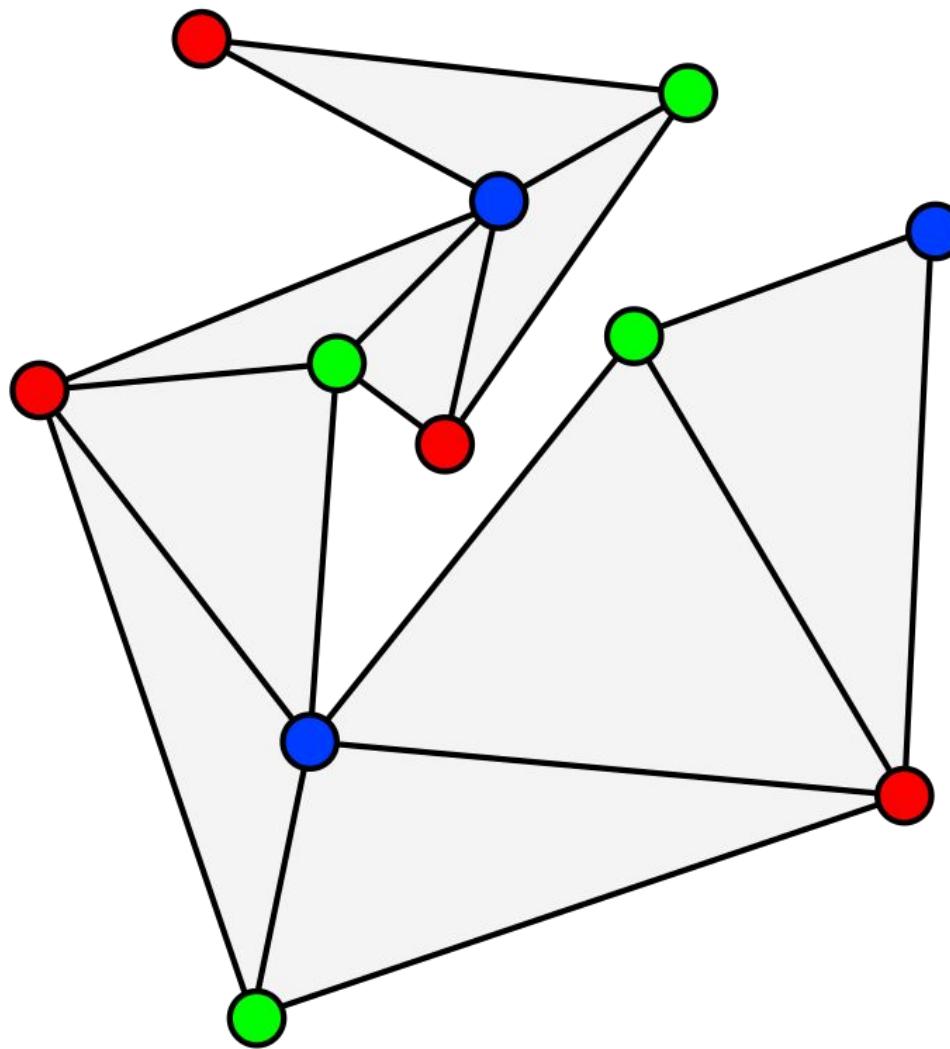








Placement of Guards?



Are As Many Guards Needed?

Can We Do Any Better?



Well yes, but actually no

Part II : Minimal # Guards

The Set Cover Problem

Optimization Online

(supported by the Mathematical Optimization Society)

A Practical Iterative Algorithm for the Art Gallery Problem using Integer Linear Programming

Davi C. Tozoni • Pedro J. de Rezende • Cid C. de Souza

Resources

- [A Combinatorial Problem in Geometry](#) by V.Chvatal
- [Solving the Art Gallery Problem](#) by CC ACADEMY
- [A Practical Iterative Algorithm for the Art Gallery Problem using Integer Linear Programming](#) by Tozoni
- [Could a 50-year-old math problem have saved the Louvre from robbery?](#)
- [A Constant-Factor Approximation Algorithm for Point Guarding an Art Gallery](#)