

$$\Omega = \iiint_V \frac{1}{r} d\tau \quad \rightarrow \quad U = G \rho \Omega$$

$$U = G \sum_{\ell=1}^m f_{\ell} \Omega_{\ell}$$

$$\Omega_{\ell} = ||| f_{ijk} |||$$

$$= (1 + \dots + 1) f_{\ell}$$

$$= f_{zzz} f_{\ell} + \dots - f_{111} f_{\ell}$$

$$\partial_{\alpha} U = G \rho \partial_{\alpha} \Omega, \quad \alpha = x, y, z$$

$$V = -c_m h \nabla \Omega^T \hat{h}$$

$$h \hat{h} = \begin{bmatrix} h_x \\ h_y \\ h_z \end{bmatrix}$$

$$\hat{h} = \begin{bmatrix} \cos I \cos \psi \\ \cos I \sin \psi \\ \sin I \end{bmatrix}$$

$$= - \underbrace{c_m}_{G\rho} \sum_{\ell=1}^m \left( \underbrace{h_x^{\ell}}_{g_x} \underbrace{\partial_x \Omega_{\ell}}_{g_x} + \underbrace{h_y^{\ell}}_{g_x} \underbrace{\partial_y \Omega_{\ell}}_{g_x} + \underbrace{h_z^{\ell}}_{g_z} \underbrace{\partial_z \Omega_{\ell}}_{g_z} \right)$$

$$= \left( -c_m \sum_{\ell=1}^m h_x^{\ell} \partial_x \Omega_{\ell} \right) + \dots + \left( -c_m \sum_{\ell=1}^m h_z^{\ell} \partial_z \Omega_{\ell} \right)$$

$$B_{\alpha} = -\partial_{\alpha} V$$

$$B_{\alpha} = \left( c_m \sum_{\ell=1}^m h_x^{\ell} \partial_{\alpha x} \Omega_{\ell} \right) + \dots + \left( c_m \sum_{\ell=1}^m h_z^{\ell} \partial_{\alpha z} \Omega_{\ell} \right)$$