

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages

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Implementing Variables and Environments

Dealing with variables

- Interpreters so far have been for languages without variables
 - No let-expressions, functions-with-arguments, etc.
 - Language in homework has all these things
- This segment describes in English what to do
 - Up to you to translate this to code
- Fortunately, what you have to implement is what we have been stressing since the very, very beginning of the course

Dealing with variables

- An environment is a mapping from variables (Racket strings) to values (as defined by the language)
 - Only ever put pairs of strings and values in the environment
- Evaluation takes place in an environment
 - Environment passed as argument to interpreter helper function
 - A variable expression looks up the variable in the environment
 - Most subexpressions use same environment as outer expression
 - A let-expression evaluates its body in a larger environment

The Set-up

So now a recursive helper function has all the interesting stuff:

```
(define (eval-under-env e env)
  (cond ... ; case for each kind of
    ))      ; expression
```

- Recursive calls must “pass down” correct environment

Then **eval-exp** just calls **eval-under-env** with same expression and the *empty environment*

On homework, environments themselves are just Racket lists containing Racket pairs of a string (the MUPL variable name, e.g., "**x**") and a MUPL value (e.g., (**int** 17))

A grading detail

- Stylistically `eval-under-env` would be a helper function one could define locally inside `eval-exp`
- **But do not do this on your homework**
 - We have grading tests that call `eval-under-env` directly, so we need it at top-level