

NOTRE DAME UNIVERSITY BANGLADESH



Data Structure

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Subject: Data Structure

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① INSERT (LA, N, K, ITEM)

Here LA is a linear array with N elements and K is a positive integer such that $K \leq N$. This algorithm inserts an element ITEM into the Kth position in LA.

(1) [Initialize counter.] set $J := N$.

(2) Repeat Steps 3 and 4 while $J \geq K$.

(3) Set $LA[J+1] := LA[J]$.

(4) ~~Decrease~~ Set $J := J - 1$ [End of Step 2 loop].

(5) [Insert element.] set $LA[K] := ITEM$.

(6) [Reset N.] set $N := N + 1$ (7) Exit.

② Binary search

1	2	3	4	5	6	7	8	9	10	11	12	13
5	8	9	12	15	19	25	30	35	46	51	65	80

① $B = 1, E = 13$

$$\therefore M = \left\lfloor \frac{B+E}{2} \right\rfloor = \left\lfloor \frac{1+13}{2} \right\rfloor = 7$$

Mid [7] = 25 \neq item

$B > \text{item} (19)$

set $E = 7 - 1 = 6$

② $B = 1, E = 6$

$$M = \left\lfloor \frac{1+6}{2} \right\rfloor = 3.5 \approx 3$$

Mid [3] = 9 \neq item

$9 < \text{item} (19)$

set $E = 3 + 1 = 4$

③ $B = 4, E = 6$

$$\therefore M = \left\lfloor \frac{4+6}{2} \right\rfloor = 5$$

\therefore Mid [5] = 15 \neq item

$15 < \text{item}$

$B = 5 + 1 = 6$

④ $B = 6, E = 6$

$$\therefore M = \left\lfloor \frac{6+6}{2} \right\rfloor = 6$$

\therefore Mid [6] = 19 = item

\therefore 19 is found in index no. 6

2.6 Bubble Sort

11, 45, 8, 35, 2, 7

K=1

- (a) 11, 45, 8, 35, 2, 7
(b) 11, 45, 8, 35, 2, 7
 \Rightarrow 11, 8, 45, 35, 2, 7
(c) 11, 8, 45, 35, 2, 7
 \Rightarrow 11, 8, 35, 45, 2, 7
(d) 11, 8, 35, 45, 2, 7
 \Rightarrow 11, 8, 35, 2, 45, 7
(e) 11, 8, 35, 2, 45, 7
 \Rightarrow 11, 8, 35, 2, 7, 45

K=2

- (a) 11, 8, 35, 2, 7, 45
 \Rightarrow 8, 11, 35, 2, 7, 45
(b) 8, 11, 35, 2, 7, 45
(c) 8, 11, 35, 2, 7, 45
 \Rightarrow 8, 11, 2, 35, 7, 45
(d) 8, 11, 2, 35, 7, 45
 \Rightarrow 8, 11, 2, 7, 35, 45

K=3

- (a) 8, 11, 2, 7, 35, 45
(b) 8, 11, 2, 7, 35, 45
~~(c)~~ \Rightarrow 8, 2, 11, 7, 35, 45
(c) 8, 2, 11, 7, 35, 45
 \Rightarrow 8, 2, 7, 11, 35, 45

K=4

- (a) 8, 2, 7, 11, 35, 45
 \Rightarrow 2, 8, 7, 11, 35, 45
(b) 2, 8, 7, 11, 35, 45
 \Rightarrow 2, 7, 8, 11, 35, 45

K=5

- (a) 2, 7, 8, 11, 35, 45
 \Rightarrow 2, 7, 8, 11, 35, 45

③ What is Stack? Give an example. Do the following operation using stack where MAX Items in the stack can be 6.

PUSH: A, B, C, D, E

POP

POP

PUSH: F, G, H, I

POP

Ans: A stack is a list of elements in which an element may be inserted or deleted only at one end. But it must be done on the top of the stack.

→ Push: To insert an element into a stack.

→ Pop: To delete an element from a stack.

a) PUSH: A

$$T = 0 + 1 = 1$$

[A]

b) PUSH: B

$$T = 1 + 1 = 2$$

[B]
[A]

c) PUSH: C

$$T = 2 + 1 = 3$$

[C]
[B]
[A]

d) PUSH: D

$$T = 3 + 1 = 4$$

[D]
[C]
[B]
[A]

e) PUSH: E

$$T = 4 + 1 = 5$$

[E]
[D]
[C]
[B]
[A]

f) POP: ITEM

$$T = 5 - 1 = 4$$

[D]
[C]
[B]
[A]

g) POP: ITEM

$$T = 4 - 1 = 3$$

[C]
[B]
[A]

h) PUSH: F

$$T = 3 + 1 = 4$$

[F]
[C]
[B]
[A]

i) PUSH: G

$$T = 4 + 1 = 5$$

[G]
[F]
[C]
[B]
[A]

j) PUSH: H

$$T = 5 + 1 = 6$$

[H]
[G]
[F]
[C]
[B]
[A]

k) PUSH: ~~ITEM~~ T

$$T = 6 + 1 = 7$$

∴ MAX VALUE = 6

∴ STACK Overflow.

l) POP: ITEM

$$T = 6 - 1 = 5$$

[G]
[F]
[C]
[B]
[A]

④ Consider the following infix expression.

$(25 + (5 - 1) - 3 / (2 * 7))$ Use stack to translate the given expression into its equivalent postfix expression P.

Ans:

Symbol Scanned	Stack	Expression P
((
25		25
+	(+	25
((+ (25
5	(+ (25, 5
-	(+ (-	25, 5
1	(+ (-	25, 5, 1
)	(+	25, 5, 1 -
-	(-	25, 5, 1 - +
3	(-	25, 5, 1 - + 3
/	(- /	25, 5, 1 - + 3
((- / (25, 5, 1 - + 3
* 2	(- / (25, 5, 1 - + 3, 2
*	(- / (*	25, 5, 1 - + 3, 2
7	(- / (* 7	25, 5, 1 - + 3, 2, 7
)	(- /	25, 5, 1, - + 3, 2, 7 *
)		25, 5, 1, - + 3, 2, 7 * / -

① DELETE (LA, N, K, ITEM)

Here LA is a linear array with N elements and K is a positive integer such that $K \leq N$. This algorithm deletes the Kth element from LA.

(1) Set ITEM := LA[K].

(2) Repeat for $j = K$ to $N-1$:

Set LA[j] := LA[j+1]. [End of loop]

(3) Set N := N-1. (4) Exit.

② (Binary Search)

index →

1	2	3	4	5	6	7	8	9	10	11	12	13
1	7	11	17	23	29	31	44	51	56	61	71	99

① B=1, E=13

$$\therefore M = \left\lceil \frac{B+E}{2} \right\rceil = \left\lceil \frac{1+13}{2} \right\rceil = 7$$

Mid[7] = 31 \neq item

$31 > \text{item (24)}$

Set $E = 7-1 = 6$

② B=1, E=6

$$M = \left\lceil \frac{1+6}{2} \right\rceil = 3.5 \approx 3$$

Mid[3] = 11 \neq item

$11 < \text{item (24)}$

$B = 3+1 = 4$

③ B=4, E=6

$$\therefore M = \left\lceil \frac{4+6}{2} \right\rceil = 5$$

$\therefore \text{Mid}[5] = 23 \neq \text{item}$

$23 < \text{item}$

$B = 5+1 = 6$

④ B=6, E=6

$$\therefore M = \left\lceil \frac{6+6}{2} \right\rceil = 6$$

$\therefore \text{Mid}[6] = 29 = \text{item}$

$\therefore 29$ is found in index no. 6.

2.6 Bubble Sort 17, 51, 9, 32, 1, 6

K=1

- a) 17, 51, 9, 32, 1, 6
 b) 17, 51, 9, 32, 1, 6
 \Rightarrow 17, 9, 51, 32, 1, 6
 c) 17, 9, 51, 32, 1, 6
 \Rightarrow 17, 9, 32, 51, 1, 6
 d) 17, 9, 32, 51, 1, 6
 \Rightarrow 17, 9, 32, 1, 51, 6
 e) 17, 9, 32, 1, 51, 6
 \Rightarrow 17, 9, 32, 1, 6, 51

K=2

- a) 17, 9, 32, 1, 6, 51
 \Rightarrow 9, 17, 32, 1, 6, 51
 b) 9, 17, 32, 1, 6, 51
~~c) 9, 17, 32, 1, 6, 51~~
 \Rightarrow 9, 17, 1, 32, 6, 51
 d) 9, 17, 1, 32, 6, 51
 \Rightarrow 9, 17, 1, 6, 32, 51

K=3

- a) 9, 17, 1, 6, 32, 51
 b) 9, 17, 1, 6, 32, 51
 \Rightarrow 9, 1, 17, 6, 32, 51
 c) 9, 1, 17, 6, 32, 51
 \Rightarrow 9, 1, 6, 17, 32, 51

K=4

- a) 9, 1, 6, 17, 32, 51
 \Rightarrow 1, 9, 6, 17, 32, 51
 b) 1, 9, 6, 17, 32, 51
 \Rightarrow 1, 6, 9, 17, 32, 51

K=5

- a) 1, 6, 9, 17, 32, 51
 \Rightarrow 1, 6, 9, 17, 32, 51

③ PUSH: A, B, C, D, E
 POP
 PUSH: F, G, H, I
 POP

Stack: A stack is a list of elements in which an element may be inserted or deleted only at one end. But it must be done on the top of the stack.

→ Push: To insert an element into a stack.

→ POP: To delete an element from a stack.

a) PUSH: A
 $T = 0 + 1 = 1$

A

b) PUSH: B
 $T = 1 + 1 = 2$

B
A

c) PUSH: C
 $T = 2 + 1 = 3$

C
B
A

d) PUSH: D
 $T = 3 + 1 = 4$

D
C
B
A

e) PUSH: E
 $T = 4 + 1 = 5$

E
D
C
B
A

f) POP: ITEM
 $T = 5 - 1 = 4$

D
C
B
A

g) PUSH: F
 $T = 4 + 1 = 5$

F
D
C
B
A

h) PUSH: G
 $T = 5 + 1 = 6$

G
F
D
C
B
A

i) PUSH: H

$$T = 6 + 1 = 7$$

MAX STACK = 6

∴ STACK Overflow.

j) PUSH: I

STACK is already MAX.

k) POP: ITEM

$$T = 6 - 1 = 5$$

F
D
C
B
A

$$(4) (12/(7-3)+2*(1+5))$$

Symbol scanned	stack	Expression P
((
12	(12
/	(/	12
(((12
7	((12, 7
-	((-	12, 7
3	((-	12, 7, 3
)	(/	12, 7, 3, -
+	(/+	12, 7, 3, -, /
2	(/+	12, 7, 3, -, /, 2
*	(/+*	12, 7, 3, -, /, 2
((/+*(12, 7, 3, -, /, 2
1	(/+*(12, 7, 3, -, /, 2
+	(/+*(+	12, 7, 3, -, /, 2
5	(/+*(+	12, 7, 3, -, /, 2
)	(/+*	12, 7, 3, -, /, 2, +
)		12, 7, 3, -, /, 2, +, *, +