

# Convolutional Encoding and Viterbi Decoding

```
EbNodB = 0:0.5:10; % SNR values in dB
gamma = 10.^(EbNodB / 10); % Convert SNR from dB to linear scale
ES = 1; % Signal energys
nsim = 5000;
inputsz = 50;
input = rand(1,inputsz) > 0.5;
```

**i) For  $k = 1$  ,  $n = 2$  ,  $K_c = 3$  and  $r = 1/2$**

```
k = 1;
n = 2;
r = k/n;
Kc = 3;
G = [[1 0 1]; [1 1 1]];

inputseq = input;
for i = 1 : Kc-1
    inputseq = [inputseq 0]; %padding zeros
end

%obtaining state diagram
s = statediag(G,Kc,n);

%obtaining encoded sequence
encodedseq = encoding(G,Kc,inputseq);

% BPSK modulation
modulatedsig = 1 - 2*encodedseq;

% for storing BER
harderrorrate1 = zeros(1,length(EbNodB));
softerrorrate1 = zeros(1,length(EbNodB));
theerrorrate1 = zeros(1,length(EbNodB));
hardnumerrors = zeros(size(EbNodB));
softnumerrors = zeros(size(EbNodB));

%Simulating errors for all values of EbNodB

for i = 1:length(EbNodB)
    %Generating noise
    noisepow=sqrt(1/(r*gamma(i)));
    BER_th = 0.5 * erfc(sqrt(1*gamma(i)));
```

```

        theerrorrate1(i) = BER_th;
    for j=1:nsim
        % SNR and noise simulation
        noise = (noisepow)*randn(size(modulatedsig)); % AWGN noise

        % Add noise to modulated signal
        recsignal = modulatedsig + noise;

        %For BPSK demodulation
        threshold = 0;

        %Calculating Demodulated signal
        demodulatedsig = zeros(size(recsignal));
        for k=1:length(recsignal)
            if(recsignal(k) < threshold)
                demodulatedsig(k) = 1;
            end
        end

        % Hard Decoding
        harddecseq = harddec(s,Kc,n,demodulatedsig,length(inputseq));

        %Soft Decoding
        softdecseq = softdec(s,Kc,n,recsignal,length(inputseq));

        %Computing the number of error bits in the decoded sequence
        for k=1:length(inputseq)
            if(harddecseq(k)~=inputseq(k))
                hardnumerrors(i) = hardnumerrors(i) + 1;
            end
            if(softdecseq(k)~=inputseq(k))
                softnumerrors(i) = softnumerrors(i) + 1;
            end
        end
    end

end

%Computing BER
harderrorrate1 = hardnumerrors / (nsim*length(inputseq));
softerrorrate1 = softnumerrors / (nsim*length(inputseq));

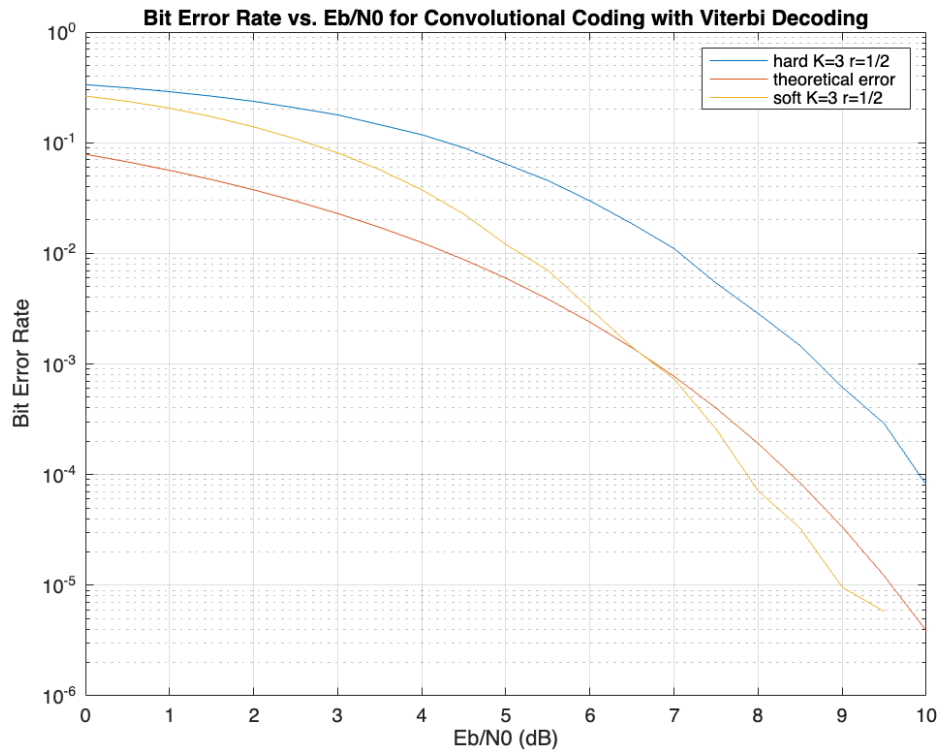
% Plot error rates vs. Eb/N0
semilogy(EbNodB, harderrorrate1);
hold on;
semilogy(EbNodB,theerrorrate1);
semilogy(EbNodB,softerrorrate1);
hold off;

```

```

xlabel('Eb/N0 (dB)');
ylabel('Bit Error Rate');
title('Bit Error Rate vs. Eb/N0 for Convolutional Coding with Viterbi Decoding');
legend('hard K=3 r=1/2', 'theoretical error', 'soft K=3 r=1/2');
grid on;

```



ii) For  $k = 1$  ,  $n = 3$  ,  $K_c = 4$  and  $r = 1/3$

```

k = 1;
n = 3;
r = k/n;
Kc = 4;
G = [[1 0 1 1];[1 1 0 1];[1 1 1 1]];

inputseq = input;
for i =1 : Kc-1
    inputseq = [inputseq 0]; %padding zeros
end

%obtaining state diagram
s = statediag(G,Kc,n);

%obtaining encoded sequence
encodedseq = encoding(G,Kc,inputseq);

```

```

% BPSK modulation
modulatedsig = 1 - 2*encodedseq;

% for storing BER
harderrorrate2 = zeros(1,length(EbNodB));
softerrorrate2 = zeros(1,length(EbNodB));
theerrorrate2 = zeros(1,length(EbNodB));
hardnumerrors = zeros(size(EbNodB));
softnumerrors = zeros(size(EbNodB));

%Simulating errors for all values of EbNodB

for i = 1:length(EbNodB)
    %Generating noise
    noisepow=sqrt(1/(r*gamma(i)));
    BER_th = 0.5 * erfc(sqrt(1*gamma(i)));
    theerrorrate2(i) = BER_th;
    for j=1:nsim
        % SNR and noise simulation
        noise = (noisepow)*randn(size(modulatedsig)); % AWGN noise

        % Add noise to modulated signal
        recsignal = modulatedsig + noise;

        %For BPSK demodulation
        threshold = 0;

        %Calculating Demodulated signal
        demodulatedsig = zeros(size(recsignal));
        for k=1:length(recsignal)
            if(recsignal(k) < threshold)
                demodulatedsig(k) = 1;
            end
        end

        % Hard Decoding
        harddecseq = harddec(s,Kc,n,demodulatedsig,length(inputseq));

        %Soft Decoding
        softdecseq = softdec(s,Kc,n,recsignal,length(inputseq));

        %Computing the number of error bits in the decoded sequence
        for k=1:length(inputseq)
            if(harddecseq(k)~=inputseq(k))
                hardnumerrors(i) = hardnumerrors(i) + 1;
            end
            if(softdecseq(k)~=inputseq(k))

```

```

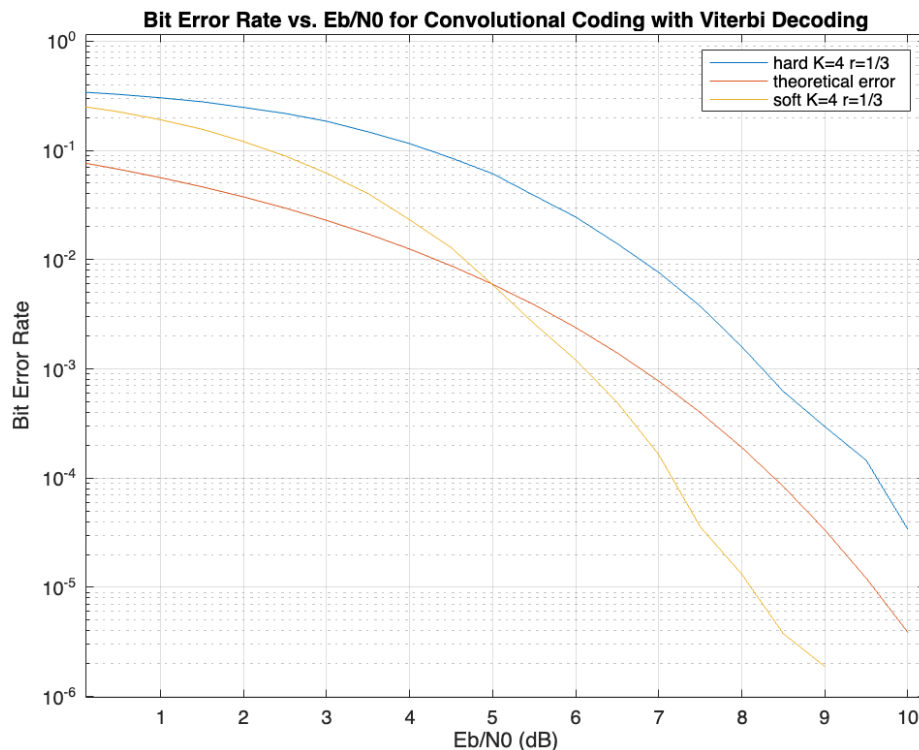
        softnumerrors(i) = softnumerrors(i) + 1;
    end
end

end

%Computing BER
harderrorrate2 = hardnumerrors / (nsim*length(inputseq));
softerrorrate2 = softnumerrors / (nsim*length(inputseq));

% Plot error rates vs. Eb/N0
semilogy(EbNodB, harderrorrate2);
hold on;
semilogy(EbNodB,theerrorrate2);
semilogy(EbNodB,softerrorrate2);
hold off;
xlabel('Eb/N0 (dB)');
ylabel('Bit Error Rate');
title('Bit Error Rate vs. Eb/N0 for Convolutional Coding with Viterbi Decoding');
legend('hard K=4 r=1/3', 'theoretical error', 'soft K=4 r=1/3');
grid on;

```



iii) For  $k = 1$  ,  $n = 3$  ,  $K_c = 6$  and  $r = 1/3$

```

k = 1;
n = 3;
r = k/n;
Kc = 6;
G = [ [1 0 0 1 1 1];[1,0,1,0,1,1];[1,1,1,1,0,1]];

inputseq = input;
for i =1 : Kc-1
    inputseq = [inputseq 0]; %padding zeros
end

%obtaining state diagram
s = statediag(G,Kc,n);

%obtaining encoded sequence
encodedseq = encoding(G,Kc,inputseq);

% BPSK modulation
modulatedsig = 1 - 2*encodedseq;

% for storing BER
harderrorrate3 = zeros(1,length(EbNodB));
softerrorrate3 = zeros(1,length(EbNodB));
theerrorrate3 = zeros(1,length(EbNodB));
hardnumerrors = zeros(size(EbNodB));
softnumerrors = zeros(size(EbNodB));

%Simulating errors for all values of EbNodB

for i = 1:length(EbNodB)
    %Generating noise
    noisepow=sqrt(1/(r*gamma(i)));
    BER_th = 0.5 * erfc(sqrt(1*gamma(i)));
    theerrorrate3(i) = BER_th;
    for j=1:nsim
        % SNR and noise simulation
        noise = (noisepow)*randn(size(modulatedsig)); % AWGN noise

        % Add noise to modulated signal
        recsignal = modulatedsig + noise;

        %For BPSK demodulation
        threshold = 0;

        %Calculating Demodulated signal
        demodulatedsig = zeros(size(recsignal));
        for k=1:length(recsignal)
            if(recsignal(k) < threshold)

```

```

        demodulatedsig(k) = 1;
    end
end

% Hard Decoding
harddecseq = harddec(s,Kc,n,demodulatedsig,length(inputseq));

%Soft Decoding
softdecseq = softdec(s,Kc,n,recsignal,length(inputseq));

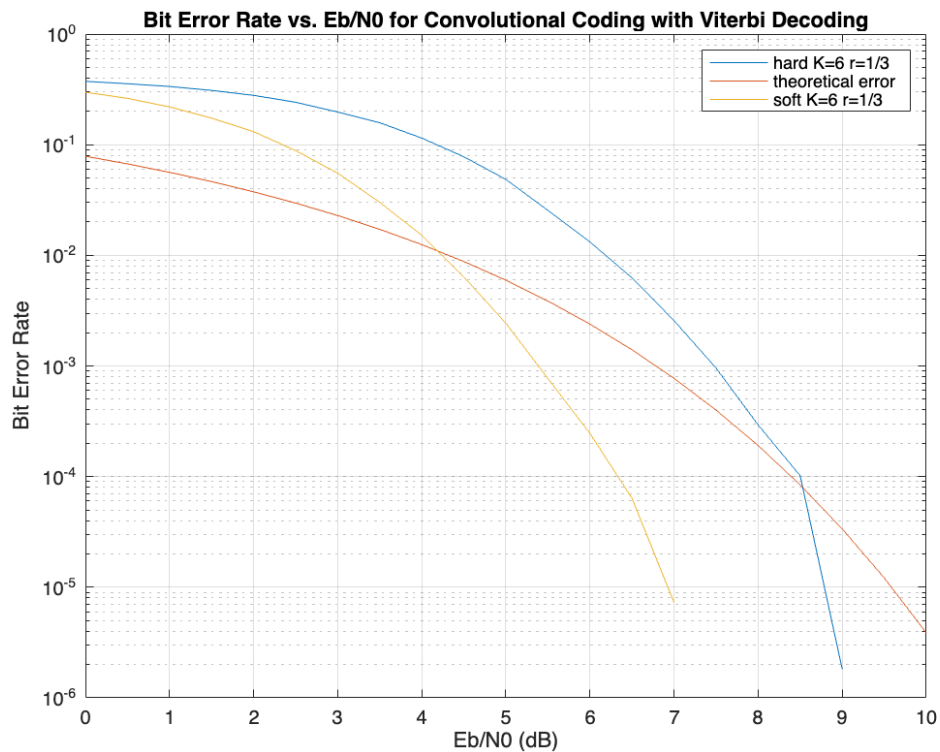
%Computing the number of error bits in the decoded sequence
for k=1:length(inputseq)
    if(harddecseq(k)~=inputseq(k))
        hardnumerrors(i) = hardnumerrors(i) + 1;
    end
    if(softdecseq(k)~=inputseq(k))
        softnumerrors(i) = softnumerrors(i) + 1;
    end
end
end

end

%Computing BER
harderrorrate3 = hardnumerrors / (nsim*length(inputseq));
softerrorrate3 = softnumerrors / (nsim*length(inputseq));

% Plot error rates vs. Eb/N0
semilogy(EbNodB, harderrorrate3);
hold on;
semilogy(EbNodB,theerrorrate3);
semilogy(EbNodB,softerrorrate3);
hold off;
xlabel('Eb/N0 (dB)');
ylabel('Bit Error Rate');
title('Bit Error Rate vs. Eb/N0 for Convolutional Coding with Viterbi Decoding');
legend('hard K=6 r=1/3', 'theoretical error', 'soft K=6 r=1/3');
grid on;

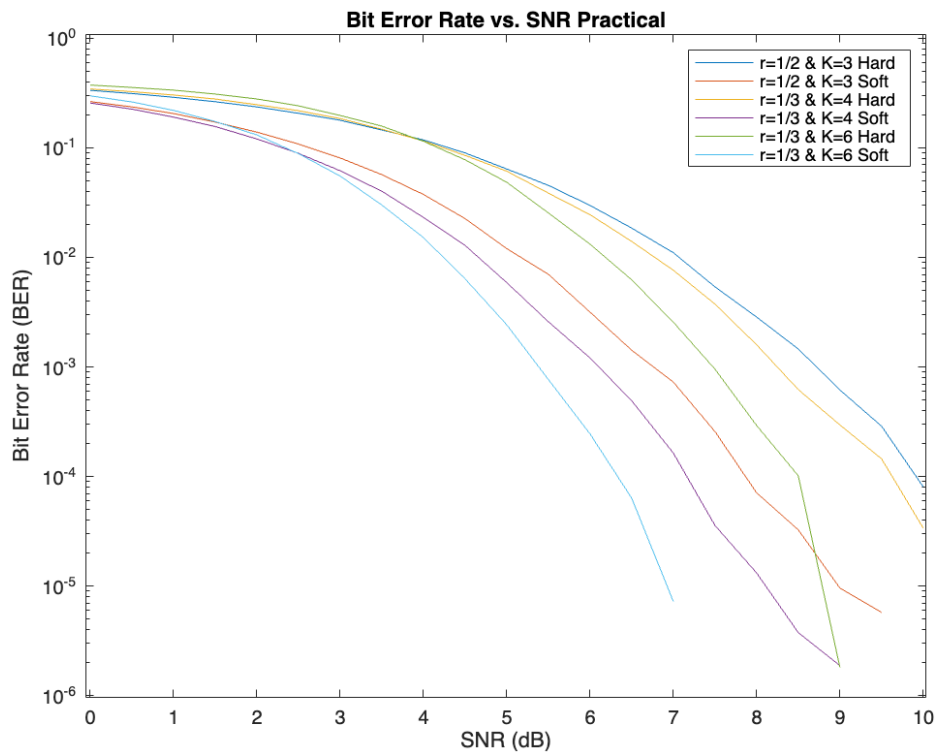
```



## Analysis Of Hard And Soft Decoding For All Rates

```
figure(1);
semilogy(EbNodB,harderrorrate1,EbNodB, softerrorrate1, EbNodB, harderrorrate2,
EbNodB, softerrorrate2, EbNodB, harderrorrate3, EbNodB, softerrorrate3);
xlabel('SNR (dB)');
ylabel('Bit Error Rate (BER)');
legend('r=1/2 & K=3 Hard','r=1/2 & K=3 Soft','r=1/3 & K=4 Hard','r=1/3 & K=4
Soft','r=1/3 & K=6 Hard','r=1/3 & K=6 Soft');
title('Bit Error Rate vs. SNR Practical');
```





## Function For State Diagram

```
function [outputArg] = statediag(G,Kc,n)

% Calculate the number of states based on the constraint length Kc
totnoofstate = 2^(Kc-1);

% Initialize an array to hold the binary representation of each state
arr = zeros(totnoofstate,Kc-1);
for i=0:totnoofstate-1
    % Convert the state index to binary representation
    x = int2bit(i,Kc-1);
    x1 = x';
    arr(i+1,:)=x1;
end

% Initialize the output array to hold the state diagram

outputArg = zeros(totnoofstate,4);

% In the first and the second columns, we are storing the output from the
corresponding state
% when the input bit is 0 and 1, respectively
% And in third and fourth columns, we are storing the next states,
% when the input bits are 0 and 1, respectively
```

```

for i=1:totnoofstate
    % Compute the output and next states for input 0
    arr0 = arr(i,:);
    arr0 = [0 arr0]; % Add input 0 to the state
    op0 = mod(G*arr0',2); % Compute the output
    outputArg(i,1)=bit2int(op0,n); % Store the output
    nextstate0 = [];
    for j=1:Kc-1
        nextstate0 = [nextstate0 arr0(j)]; % Compute the next state
    end
    x = bit2int(nextstate0',Kc-1); % Convert next state to integer
    outputArg(i,3)=x; % Store the next state for input 0

    % Compute the output and next states for input 1
    arr1 = arr(i,:);
    arr1 = [1 arr1]; % Add input 1 to the state
    op1 = mod(G*arr1',2); % Compute the output
    outputArg(i,2)=bit2int(op1,n); % Store the output
    nextstate1 = [];
    for j=1:Kc-1
        nextstate1 = [nextstate1 arr1(j)]; % Compute the next state
    end
    outputArg(i,4)=bit2int(nextstate1',Kc-1); % Store the next state for input 1
end
end

```

## Function For Encoding sequence

```

function [outputArg] = encoding(G,Kc,inputseq)

    encodmsg = [];

    % Initialize the shift register with the first element of the input
    % sequence
    arr = [inputseq(1)];

    % Pad the shift register array with Kc-1 zeros
    for i=1:Kc-1
        arr = [arr 0];
    end

    % Obtaining the encoded sequence for each input bit by multiplying shift
    % register array with G matrix
    for i=1:length(inputseq)
        arr1 = arr';
        arr2 = G*arr1;
    end

```

```

arr2 = mod(arr2,2);
encodmsg = [encodmsg arr2'];

% Shift the shift register to the right by one position
for j=Kc:-1:2
    arr(j) = arr(j-1);
end

% Update the first element of the shift register with the next input
if(i~=length(inputseq))
    arr(1)=inputseq(i+1);
end
end

outputArg = encodmsg;
end

```

## Function For Viterbi Hard Decoding

```

function [outputArg] = harddec(s,Kc,n,demod_seq,inplen)
% Calculating the number of rows and columns in the trellis
rows = 2^(Kc-1);
cols = inplen+1;

% Initialize 2-D arrays for storing the path metric, previous states and
% previous inputs
valarr = 1000*ones(rows,cols);
prevstate = -1*ones(rows,cols);
previnp= -1*ones(rows,cols);

% Setting the branch metric and previous state(path metric) for the initial
state as 0 and -1, respectively
valarr(1,1)=0;
prevstate(1,1)=-1;

% Iterate over each column of the trellis
for j=1:cols-1
    x=[];

    % Extracting n bits from the demodulated sequence corresponding to the
current column
    for i=n*j-(n-1):n*j
        x = [x demod_seq(i)];
    end

    % Iterate over each state of the trellis
    for i=1:rows

        % Check whether the state has a valid path metric

```

```

        if(valarr(i,j)~=1000)

            % Calculation for input bit 0
            op0 = s(i,1);
            ns0 = s(i,3)+1;
            op0_bin = int2bit(op0,n);
            op0_bin = op0_bin';

            % Calculating the hamming distance for transition 0
            hd0 = 0;
            for k=1:length(x)
                if(x(k)~=op0_bin(k))
                    hd0=hd0+1;
                end
            end

            % Update values in branch matrix if the transition improves the
metric
            if(hd0+valarr(i,j)<valarr(ns0,j+1))
                valarr(ns0,j+1) = hd0+valarr(i,j);
                prevstate(ns0,j+1) = i;
                prev_inp(ns0,j+1) = 0;
            end

            % Calculation for input bit 0
            op1 = s(i,2);
            ns1 = s(i,4)+1;
            op1_bin = int2bit(op1,n);
            op1_bin = op1_bin';

            % Calculating the hamming distance for transition 0
            hd1 = 0;
            for k=1:length(x)
                if(x(k)~=op1_bin(k))
                    hd1=hd1+1;
                end
            end

            % Update values if the transition improves the metric
            if(hd1+valarr(i,j)<valarr(ns1,j+1))
                valarr(ns1,j+1) = hd1+valarr(i,j);
                prevstate(ns1,j+1) = i;
                prev_inp(ns1,j+1) = 1;
            end
        end
    end
end
i = 1;
decodseq = [];

```

```

% Backtrack through the trellis to find the most likely sequence
for j=cols:-1:2
    decodseq = [decodseq prev_inp(i,j)];
    i = prevstate(i,j);
end

% Return the decoded sequence
outputArg = fliplr(decodseq);
end

```

## Function For Viterbi Soft Decoding

```

function [outputArg] = softdec(s,Kc,n,demod_seq,inplen)

% Soft decoding code almost same as Hard decoding, instead of
% demodulated signal, we pass the received signal and instead of
% hamming distance we use euclidean distance

% Calculating the number of rows and columns in the trellis
rows = 2^(Kc-1);
cols = inplen+1;

% Initialize 2-D arrays for storing the path metric, previous states and
% previous inputs
valarr = 1000*ones(rows,cols);
prevstate = -1*ones(rows,cols);
previnp= -1*ones(rows,cols);

% Setting the path metric and previous state for the initial state as 0 and -1,
respectively
valarr(1,1)=0;
prevstate(1,1)=-1;

% Iterate over each column of the trellis
for j=1:cols-1
    x=[];

    % Extracting n bits from the demodulated sequence corresponding to the
current column
    for i=n*j-(n-1):n*j
        x = [x demod_seq(i)];
    end

    % Iterate over each state of the trellis
    for i=1:rows

        % Check whether the state has a valid path metric
        if(valarr(i,j)~=1000)

```

```

    % Calculation for input bit 0
    op0 = s(i,1);
    ns0 = s(i,3)+1;
    op0_bin = int2bit(op0,n);
    op0_bin = op0_bin';
    op0_bin = 1 - 2*op0_bin;

    % Calculating the euclidean distance for transition 0
    path_metric0 = sum((x-op0_bin).^2);

    % Update values if the transition improves the metric
    if(path_metric0+valarr(i,j)<valarr(ns0,j+1))
        valarr(ns0,j+1) = path_metric0+valarr(i,j);
        prevstate(ns0,j+1) = i;
        prev_inp(ns0,j+1) = 0;
    end

    % Calculation for input bit 0
    op1 = s(i,2);
    ns1 = s(i,4)+1;
    op1_bin = int2bit(op1,n);
    op1_bin = op1_bin';
    op1_bin = 1 - 2*op1_bin;

    % Calculating the euclidean distance for transition 0
    path_metric1 = sum((x-op1_bin).^2);

    % Update values if the transition improves the metric
    if(path_metric1+valarr(i,j)<valarr(ns1,j+1))
        valarr(ns1,j+1) = path_metric1+valarr(i,j);
        prevstate(ns1,j+1) = i;
        prev_inp(ns1,j+1) = 1;
    end
end
end
end
i = 1;
decodseq = [];

% Backtrack through the trellis to find the most likely sequence
for j=cols:-1:2
    decodseq = [decodseq prev_inp(i,j)];
    i = prevstate(i,j);
end

% Return the decoded sequence
outputArg = fliplr(decodseq);
end

```

