NAME: SHEHRYAR KHAN

ROLL NO: 12394 LAB TASK: 15

SUBMITTED TO: SIR JAMAL

Introduction

 Define graphs and their key components (vertices, edges, directed/undirected)

Here's a detailed definition of graphs and their key components:

Graphs:

- A graph is a non-linear data structure that represents relationships between entities.
- It consists of a set of vertices (also called nodes or points) and a set of edges
 (also called links or lines) that connect pairs of vertices.
- Graphs are used to model various real-world scenarios, such as social networks, maps, transportation systems, computer networks, and many more.

Key Components:

- 1. Vertices (Nodes):
 - Represent entities or objects in the graph.
 - Can be labeled with numbers, letters, or any other meaningful identifiers.
 - Examples: people in a social network, cities on a map, web pages on the internet.
- 2. Edges (Links):
 - Represent relationships or connections between vertices.

- Can be either directed or undirected.
- May have weights associated with them to represent additional information (e.g., distance, cost, capacity).

Types of Graphs:

1. Directed Graphs:

- Edges have a direction, indicating a one-way relationship from one vertex to another.
- Used to model situations where relationships have a specific flow or hierarchy.
- Example: A flowchart, a citation network.

2. Undirected Graphs:

- Edges do not have a direction, representing bidirectional relationships between vertices.
- Used to model situations where connections are mutual or symmetric.
- Example: A friendship network, a road map.

Additional Concepts:

- Adjacency: Two vertices are adjacent if they are connected by an edge.
- Degree of a Vertex: The number of edges incident to a vertex (either incoming or outgoing in directed graphs).
- Path: A sequence of vertices connected by edges.
- Cycle: A path that starts and ends at the same vertex.
- Explain real-world applications of graphs (social networks, maps, web pages)

Here are some real-world applications of graphs:

1. Social Networks:

- Graphs are the underlying structure of social networks like Facebook, Twitter, and LinkedIn.
- Vertices represent people, and edges represent friendships or connections between them.
- Graph algorithms are used for:
 - Friend recommendations
 - Identifying influential users
 - Analyzing community structure
 - Detecting fake accounts or bots

2. Maps and Navigation:

- Maps can be modeled as graphs, with vertices representing locations (cities, intersections) and edges representing roads or paths.
- Graph algorithms are used for:
 - Finding shortest paths between locations
 - Route planning for vehicles or pedestrians
 - Traffic analysis and optimization
 - Location-based services (e.g., finding nearby restaurants or points of interest)

3. Web Pages and the Internet:

- The internet can be viewed as a massive graph, with web pages as vertices and hyperlinks as edges.
- Graph algorithms are used for:
 - Web search engines (e.g., Google's PageRank algorithm)
 - Recommending related content or products

Analyzing website structure and link popularity

•

4. Transportation Networks:

- Graphs are used to model transportation systems like airlines, railways, and roadways.
- Vertices represent stations or airports, and edges represent routes or connections.
- Graph algorithms are used for:
 - Scheduling flights or trains
 - Optimizing routes for delivery services
 - Planning infrastructure expansion

•

5. Biological Networks:

- Graphs are used to represent relationships between biological entities, such as protein-protein interactions, gene regulatory networks, and metabolic pathways.
- Graph algorithms are used for:
 - Identifying key genes or proteins involved in diseases
 - Drug discovery and development
 - Understanding biological processes

•

6. Recommendation Systems:

- Graphs are used to model user preferences and item relationships in recommendation systems.
- Vertices represent users and items, and edges represent interactions (e.g., ratings, purchases).

- Graph algorithms are used for:
 - Recommending movies, music, books, or products
 - Personalizing user experiences

•

- 7. Task Scheduling and Resource Allocation:
 - Graphs are used to model tasks and dependencies in project management and scheduling.
 - Vertices represent tasks, and edges represent dependencies between them.
 - Graph algorithms are used for:
 - Scheduling tasks efficiently
 - Allocating resources to tasks
 - Optimizing project timelines

•

Discuss graph representation methods (adjacency list, adjacency matrix)

Here's a detailed discussion of graph representation methods:

Graphs can be represented in computer memory using two primary methods:

- 1. Adjacency List:
 - Structure:
 - An array of lists, where each index in the array represents a vertex.
 - The list at each index stores the vertices that are directly connected to that vertex (its neighbors).

•

- Pros:
 - Efficient for sparse graphs (graphs with relatively few edges).
 - Space-efficient, as it only stores edges that actually exist.
 - Fast for adding and removing edges.

• Cons:

- Less efficient for dense graphs (graphs with many edges).
- Slower for checking if an edge exists between two vertices.
- Example:
- Python

```
graph = {
    0: [1, 2],
    1: [2, 3],
    2: [0, 3],
    3: [1]
}
```

2. Adjacency Matrix:

- Structure:
 - A 2D matrix where rows and columns represent vertices.

 The value at matrix[i][j] represents the presence or weight of an edge between vertices i and j.

•

- Pros:
 - Fast for checking if an edge exists between two vertices (constant time).
 - Can easily represent weighted graphs.

•

- Cons:
 - Space-inefficient for sparse graphs, as it stores all possible edges even if they don't exist.
 - Less efficient for adding and removing edges (requires updating multiple matrix elements).

•

• Example:

Python

```
graph = [

[0, 1, 1, 0],

[0, 0, 1, 1],

[1, 1, 0, 1],

[0, 1, 1, 0]
```

•

•

- Adjacency list is generally preferred for sparse graphs due to its space efficiency and faster edge operations.
- Adjacency matrix is preferred for dense graphs or when quick edge existence checks are crucial.
- The choice also depends on the specific algorithms you plan to use and the nature of the graph operations you'll be performing most frequently.

Lab 1: Creating Graphs in Python

• Use Python's built-in dict or defaultdict to create adjacency lists

**Here's how to create adjacency lists using Python's built-in dict and defaultdict:

1. Using dict:

Python

```
graph = {}
```

```
# Add vertices
```

```
graph[0] = [1, 2] # Vertex 0 is connected to vertices 1 and 2
graph[1] = [2, 3]
graph[2] = [0, 3]
graph[3] = [1]
```

2. Using defaultdict (more convenient for adding edges):

Python

```
graph = defaultdict(list)
```

```
# Add edges directly without checking for vertex existence
graph[0].append(1)
graph[0].append(2)
graph[1].append(2)
graph[1].append(3)
graph[2].append(0)
graph[2].append(3)
graph[3].append(1)
```

Explanation:

- dict:
 - Stores key-value pairs, where keys represent vertices and values represent lists of adjacent vertices.
 - You need to create the list for a vertex before adding edges to it.
- defaultdict:
 - A subclass of dict that automatically creates a default value for a key
 when it's accessed for the first time.

 Here, the default value is an empty list, so you can directly append edges without checking if the vertex exists in the dictionary.

Example Usage:

def

```
Python
# Print neighbors of vertex 2
print(graph[2]) # Output: [0, 3]

# Check if there's an edge between 1 and 3
if 3 in graph[1]:
    print("Edge exists between 1 and 3")
```

Implement a Graph class using adjacency lists

Here's a Python implementation of a Graph class using adjacency lists:

```
Python
class
Graph:

def
__init__(self):
    self.adjacency_list = {}
```

```
add vertex(self, vertex):
if vertex not
in self.adjacency_list:
           self.adjacency list[vertex] = []
def
add edge(self, vertex1, vertex2):
 self.adjacency list[vertex1].append(vertex2)
    # For undirected graphs, add the edge in both directions
 if not self.is directed():
           self.adjacency_list[vertex2].append(vertex1)
   def print graph(self):
      for vertex, neighbors in self.adjacency list.items():
           print(f"{vertex} -> {neighbors}")
   def is directed(self):
       return False # Override for directed graphs
```

Explanation:

• <u>__init___()</u>: Initializes an empty adjacency list to store the graph's vertices and edges.

- add vertex(): Adds a new vertex to the graph.
- add_edge(): Adds an edge between two vertices. For undirected graphs, it adds the edge in both directions.
- print_graph(): Prints the graph's adjacency list for visualization.
- is_directed(): A placeholder method to indicate whether the graph is directed or undirected. Override this method in subclasses for directed graphs.

Example Usage:

Python

```
graph = Graph()

graph.add_vertex(0)

graph.add_vertex(1)

graph.add_vertex(2)

graph.add_edge(0, 1)

graph.add_edge(0, 2)

graph.add_edge(1, 2)

graph.print_graph()
```

Output:

 $0 \rightarrow [1, 2]$

1 -> [0, 2]

2 -> [0, 1]

• Practice creating simple graphs with vertices and edges

Here are some examples to practice creating simple graphs with vertices and edges:

1. Simple Undirected Graph:

graph.print_graph()

```
Python
graph = Graph() # Create an undirected graph instance
# Add vertices
graph.add_vertex('A')
graph.add vertex('B')
graph.add_vertex('C')
graph.add vertex('D')
# Add edges
graph.add edge('A',
graph.add_edge('A', 'C')
graph.add edge('B', 'D')
graph.add edge('C', 'D')
```

Output:

```
A -> ['B', 'C']
B -> ['A', 'D']
C -> ['A', 'D']
D -> ['B', 'C']
2. Directed Graph:
```

```
Python
class DirectedGraph(Graph):
def is_directed(self):
   return True
# Create a directed graph instance
directed graph = DirectedGraph()
# Add vertices and edges (direction matters)
directed_graph.add_vertex('X')
directed_graph.add_vertex('Y')
directed_graph.add_vertex('Z')
directed graph.add edge('X', 'Y')
directed_graph.add_edge('Y', 'Z')
directed graph.add edge('Z', 'X')
```

```
directed_graph.print_graph()
```

Output:

```
X -> ['Y']

Y -> ['Z']

Z -> ['X']
```

3. Graph with Weighted Edges:

Python

```
class WeightedGraph(Graph):
    def add_edge(self, vertex1, vertex2, weight):
        self.adjacency_list[vertex1].append((vertex2, weight))
        if not self.is_directed():
            self.adjacency_list[vertex2].append((vertex1, weight))

# Create a weighted graph instance
weighted_graph = WeightedGraph()

# Add vertices and weighted edges
weighted_graph.add_vertex('1')
weighted_graph.add_vertex('1')
```

```
weighted_graph.add_vertex('3')
weighted_graph.add_edge('1', '2', 5)
weighted_graph.add_edge('1', '3', 2)
weighted_graph.add_edge('2', '3', 1)

# Print the graph with weights
for vertex, neighbors in weighted_graph.adjacency_list.items():
    print(f"{vertex} -> {[(neighbor, weight) for neighbor, weight in neighbors]}")
```

Output:

Lab 2: Graph Traversal Algorithms

Implement Depth-First Search (DFS) recursively and iteratively

Here's the Python implementation of Depth-First Search (DFS) both recursively and iteratively:

Recursive DFS:

Python

Explanation:

- 1. Base Case: If a vertex is already visited, don't explore it again.
- 2. Recursive Step:
 - Mark the current vertex as visited.
 - Print it (or perform any desired action).
 - Recursively explore each unvisited neighbor.

3.

Iterative DFS:

```
Python
def
dfs_iterative(graph, start):
    visited = set()
    stack = [start]
```

```
while stack:
    vertex = stack.pop()

    if vertex not

in visited:
        visited.add(vertex)

        print(vertex, end=" ")

        stack.extend(graph[vertex])  # Add neighbors to the stack
in reverse order
```

Explanation:

- 1. Initialization: Create a set to track visited vertices and a stack to manage the traversal.
- 2. Exploration:
 - Pop a vertex from the stack.
 - o If it's not visited, mark it as visited and print it.
 - Add its neighbors to the stack to explore them later.

Key Points:

- Both implementations explore vertices as deeply as possible before backtracking.
- Recursive DFS uses the call stack for exploration, while iterative DFS uses an explicit stack.
- Choose the implementation based on your preference and the problem's requirements.
- Implement Breadth-First Search (BFS) using a queue

Here's the Python implementation of Breadth-First Search (BFS) using a queue:

Python

```
def bfs(graph, start):
    visited = set()
    queue = [start]

while queue:
    vertex = queue.pop(0)  # Dequeue from the front
    if vertex not in visited:
        visited.add(vertex)
        print(vertex, end=" ")
        queue.extend(graph[vertex])  # Add neighbors to the queue
```

Explanation:

- 1. Initialization: Create a set to track visited vertices and a queue to manage the traversal.
- 2. Exploration:
 - Dequeue a vertex from the front of the queue.
 - If it's not visited, mark it as visited and print it.
 - Enqueue its neighbors to explore them later, ensuring level-by-level traversal.

3.

Visual Representation of BFS:

Key Points:

- BFS explores vertices level by level, starting from the source vertex.
- It uses a queue to maintain the order of vertices to explore.
- It's often used to find the shortest paths between vertices in unweighted graphs.
- Visualize graph traversals using diagrams or Python libraries

Here are visual examples of graph traversals and Python libraries for visualization:

1. Visual Representations of DFS and BFS:

DFS:

BFS:

- 2. Python Libraries for Graph Visualization:
 - NetworkX: A powerful library for creating, manipulating, and analyzing graphs.
 - matplotlib: A general-purpose plotting library that can be used with NetworkX to create graph visualizations.

Example using NetworkX and matplotlib:

Python

import networkx as nx

import matplotlib.pyplot as plt

Create a graph

```
G = nx.Graph()
G.add_edges_from([('A', 'B'), ('A', 'C'), ('B', 'D'), ('C', 'D'), ('B', 'E'), ('D', 'F')])

# Perform DFS or BFS traversal (e.g., using the implementations provided earlier)

# ...

# Visualize the graph with highlighted traversal paths

nx.draw(G, with_labels=True, node_color='lightblue', edge_color='gray')

# Highlight edges in the traversal path (replace with actual edges from your traversal)

nx.draw_networkx_edges(G, edgelist=[('A', 'B'), ('B', 'D'), ('D', 'F')], edge_color='red', width=2)

plt.show()
```

This code will produce a visualization of the graph with the traversal path highlighted in red, enabling you to visually trace the traversal algorithm's progress.

Lab 3: Graph Paths and Shortest Paths

• Implement algorithms to find paths between vertices (e.g., iterative DFS)

Here's a Python implementation of iterative DFS with modifications to find paths between vertices:

```
Python
```

```
def find path dfs iterative(graph, start, goal):
    stack = [(start, [start])] # Tuples of (vertex, path)
    visited = set()
   while stack:
        (vertex, path) = stack.pop()
        if vertex not in visited:
            visited.add(vertex)
            if vertex == goal:
                 return path
            stack.extend((neighbor, path + [neighbor]) for neighbor in
graph[vertex])
    return None
                  # No path found
Explanation:
   1. Initialization:
            Create a stack to manage the traversal, storing tuples of (vertex, path).
            Create a set to track visited vertices.
   2.
  3. Exploration:
```

Pop a vertex and its path from the stack.

- o If the vertex is not visited:
 - Mark it as visited.
 - If it's the goal vertex, return the path.
 - Push its neighbors and their extended paths onto the stack.

0

4.

Key Points:

- The path list in each tuple tracks the vertices visited during the traversal.
- When the goal vertex is found, the complete path from the start vertex is returned.
- If no path exists, the function returns None.

Example Usage:

```
Python
```

```
graph = {
    'A': ['B', 'C'],
    'B': ['D', 'E'],
    'C': ['F'],
    'D': [],
    'E': ['F'],

    'F': []
}

path = find path dfs iterative(graph, 'A', 'F')
```

```
print(path) # Output: ['A', 'B', 'D'] or ['A', 'C', 'F'] or ['A', 'B',
'E', 'F'] (depending on traversal order)
```

Introduce Dijkstra's algorithm for finding shortest paths in weighted graphs

Here's an introduction to Dijkstra's algorithm for finding shortest paths in weighted graphs:

Purpose:

- Finds the shortest paths from a source vertex to all other vertices in a weighted graph.
- Weights can represent distances, travel times, costs, or other measures of edge lengths.

Key Concepts:

- Priority Queue: Used to efficiently select the next vertex to explore based on its current tentative distance.
- Tentative Distance: The shortest known distance from the source vertex to a given vertex at a particular point in the algorithm's execution.
- Visited Set: Keeps track of vertices whose shortest distances have already been finalized.

Algorithm Steps:

1. Initialization:

- Mark all vertices as unvisited.
- Assign a tentative distance of zero to the source vertex and infinity to all other vertices.

- Create a priority queue and insert the source vertex with its tentative distance.
- 2.

3. Exploration:

- While the priority queue is not empty:
 - Remove the vertex with the smallest tentative distance from the queue.
 - Mark it as visited.
 - For each of its unvisited neighbors:
 - Calculate the tentative distance to the neighbor through the current vertex.
 - If this tentative distance is less than the neighbor's current tentative distance, update the neighbor's distance and priority in the queue.

0

-

4.

- 5. Finalization:
 - The final shortest distances from the source vertex to all other vertices are stored in their respective tentative distance values.

6.

Key Points:

- Dijkstra's algorithm only works for non-negative edge weights.
- It's a single-source shortest path algorithm, meaning it finds shortest paths from a single source to all other vertices.
- It has a time complexity of O(V^2) for dense graphs and O(E log V) for sparse graphs, where V is the number of vertices and E is the number of edges.

Apply shortest path algorithms to real-world scenarios (e.g., navigation)

Here are examples of how shortest path algorithms are applied in real-world scenarios:

1. Navigation Systems:

- GPS routing: Dijkstra's algorithm is often used to find the shortest or fastest route between two points on a road network, considering factors like distance, traffic conditions, and speed limits.
- In-car navigation systems: They use shortest path algorithms to guide drivers to their destinations, dynamically adjusting routes based on real-time traffic updates.
- Public transportation routing: Algorithms find the quickest or most efficient routes across multiple modes of transport, taking into account schedules, delays, and transfer times.

2. Logistics and Delivery:

- Vehicle routing: Algorithms optimize delivery routes for trucks, ensuring efficient delivery of goods to multiple locations while minimizing travel time and fuel costs.
- Package delivery: Companies use shortest path algorithms to plan efficient routes for couriers, considering factors like package weight, delivery deadlines, and traffic patterns.
- Supply chain optimization: Algorithms help optimize the flow of goods through complex supply chains, minimizing transportation costs and ensuring timely delivery.

3. Network Routing:

- Internet routing: Protocols like OSPF (Open Shortest Path First) use shortest path algorithms to determine the most efficient paths for data packets to travel through the internet.
- Telephone networks: Algorithms route calls through the most cost-effective paths, considering factors like call duration, time of day, and network congestion.

4. Social Networks:

- Friend recommendation: Algorithms suggest potential friends based on the shortest paths between users in the social network, considering factors like mutual friends and interests.
- Information diffusion: Algorithms analyze how information spreads through social networks by identifying the shortest paths between users who share content.

5. Gaming:

- Pathfinding in games: Algorithms guide characters through game environments, finding the shortest or safest routes to objectives while avoiding obstacles and enemies.
- Strategy games: Algorithms calculate optimal troop movements and resource allocation based on the shortest paths between locations and resource nodes.

Exercises:

Here are 10 lab exercises for practicing graph data structures in Python:

1. Graph Creation and Manipulation:

- Create graphs: Implement functions to create graphs using both adjacency list and adjacency matrix representations.
- Add and remove elements: Implement functions to add and remove vertices and edges from a graph.
- Visualize graphs: Use NetworkX or matplotlib to visualize graphs and explore their structure.

2. Graph Traversals:

- DFS and BFS implementations: Implement both recursive and iterative versions of Depth-First Search (DFS) and Breadth-First Search (BFS).
- Traversal applications:
 - Find connected components in a graph.
 - Identify cycles in a graph.
 - Determine if a graph is bipartite.

3. Pathfinding Algorithms:

- Iterative DFS: Implement iterative DFS to find paths between vertices in a general graph.
- Dijkstra's algorithm: Implement Dijkstra's algorithm to find the shortest paths from a source vertex to all other vertices in a weighted graph.
- Pathfinding applications:
 - Find the shortest route between cities on a map.
 - Determine the most efficient sequence of tasks in a project.

4. Graph Properties and Analysis:

- Calculate graph properties:
 - Degree of vertices.

- Density of a graph.
- Diameter of a graph.

•

 Analyze network characteristics: Use these properties to analyze the structure and patterns of different networks.

5. Topological Sorting:

- Implement topological sorting: Implement an algorithm to topologically sort a directed acyclic graph (DAG), ordering vertices based on their dependencies.
- Applications:
 - Schedule tasks in a project with dependencies.
 - Resolve dependency conflicts in software packages.

•

6. Minimum Spanning Trees:

- Prim's or Kruskal's algorithm: Implement Prim's or Kruskal's algorithm to find the minimum spanning tree of a weighted graph.
- Applications:
 - Design cost-efficient networks (e.g., telecommunications, transportation).
 - Identify clusters in data.

•

7. Graph Coloring:

- Implement graph coloring: Implement an algorithm to color the vertices of a graph so that no adjacent vertices share the same color.
- Applications:
 - Schedule tasks or exams to avoid conflicts.
 - Assign frequencies to radio stations to avoid interference.

8. A Search:*

- *Implement A search:** Implement A* search, a pathfinding algorithm that uses heuristics to guide its exploration.
- Applications:
 - Pathfinding in games with complex terrains.
 - Route planning in navigation systems.

9. Graph Isomorphism:

- Explore graph isomorphism: Investigate techniques for determining if two graphs are structurally identical.
- Applications:
 - Pattern recognition in molecules.
 - Identifying similar social networks.

10. Graph Optimization:

- Solve optimization problems:
 - Traveling Salesman Problem: Find the shortest possible route that visits every vertex exactly once and returns to the starting vertex.
 - Graph partitioning: Divide a graph into subgraphs with specific properties.
 - Graph clustering: Identify groups of vertices that are closely connected.

SHELLIRA RANGE OF THE SHELLIRA SHELLIRA