

STA380 - Exercises

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STA-380 Exercises

Here is the github link: [STA-380 Exercises](#)

Green Buildings

The goal

An Austin real-estate developer is interested in the possible economic impact of “going green” in her latest project: a new 15-story mixed-use building on East Cesar Chavez, just across I-35 from downtown. Will investing in a green building be worth it, from an economic perspective? The baseline construction costs are \$100 million, with a 5% expected premium for green certification.

The developer has had someone on her staff, who’s been described to her as a “total Excel guru from his undergrad statistics course,” run some numbers on this data set and make a preliminary recommendation. Here’s how this person described his process.

I began by cleaning the data a little bit. In particular, I noticed that a handful of the buildings in the data set had very low occupancy rates (less than 10% of available space occupied). I decided to remove these buildings from consideration, on the theory that these buildings might have something weird going on with them, and could potentially distort the analysis. Once I scrubbed these low-occupancy buildings from the data set, I looked at the green buildings and non-green buildings separately. The median market rent in the non-green buildings was \$25 per square foot per year, while the median market rent in the green buildings was \$27.60 per square foot per year: about \$2.60 more per square foot. (I used the median rather than the mean, because there were still some outliers in the data, and the median is a lot more robust to outliers.) Because our building would be 250,000 square feet, this would translate into an additional $250000 \times 2.6 = \$650000$ of extra revenue per year if we build the green building.

Our expected baseline construction costs are \$100 million, with a 5% expected premium for green certification. Thus we should expect to spend an extra \$5 million on the green building. Based on the extra revenue we would make, we would recuperate these costs in $\$5000000 / \$650000 = 7.7$ years. Even if our occupancy rate were only 90%, we would still recuperate the costs in a little over 8 years. Thus from year 9 onwards, we would be making an extra \$650,000 per year in profit. Since the building will be earning rents for 30 years or more, it seems like a good financial move to build the green building.

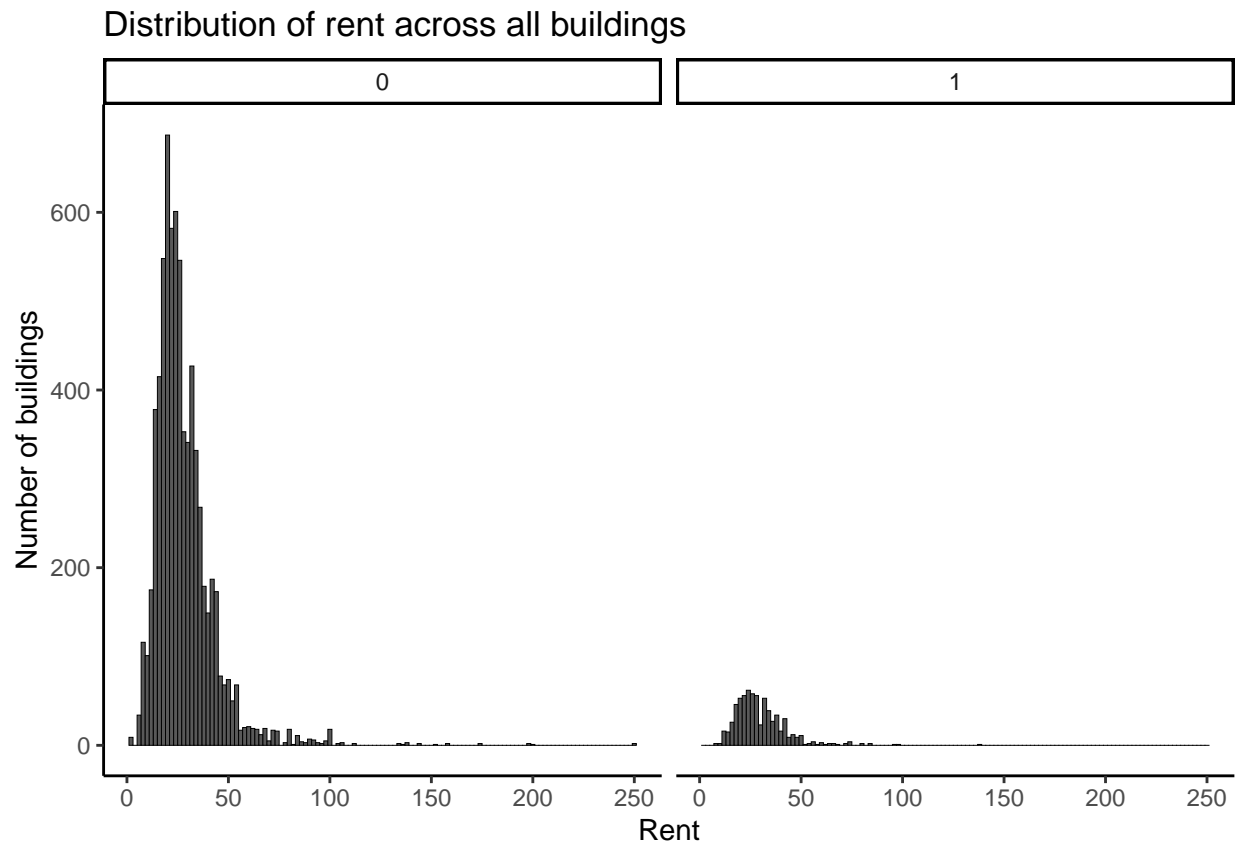
The developer listened to this recommendation, understood the analysis, and still felt unconvinced. She has therefore asked you to revisit the report, so that she can get a second opinion.

Do you agree with the conclusions of her on-staff stats guru? If so, point to evidence supporting his case. If not, explain specifically where and why the analysis goes wrong, and how it can be improved. Do you see the possibility of confounding variables for the relationship between rent and green status? If so, provide evidence for confounding, and see if you can also make a picture that visually shows how we might “adjust” for such a confounder.

Green Buildings Analysis

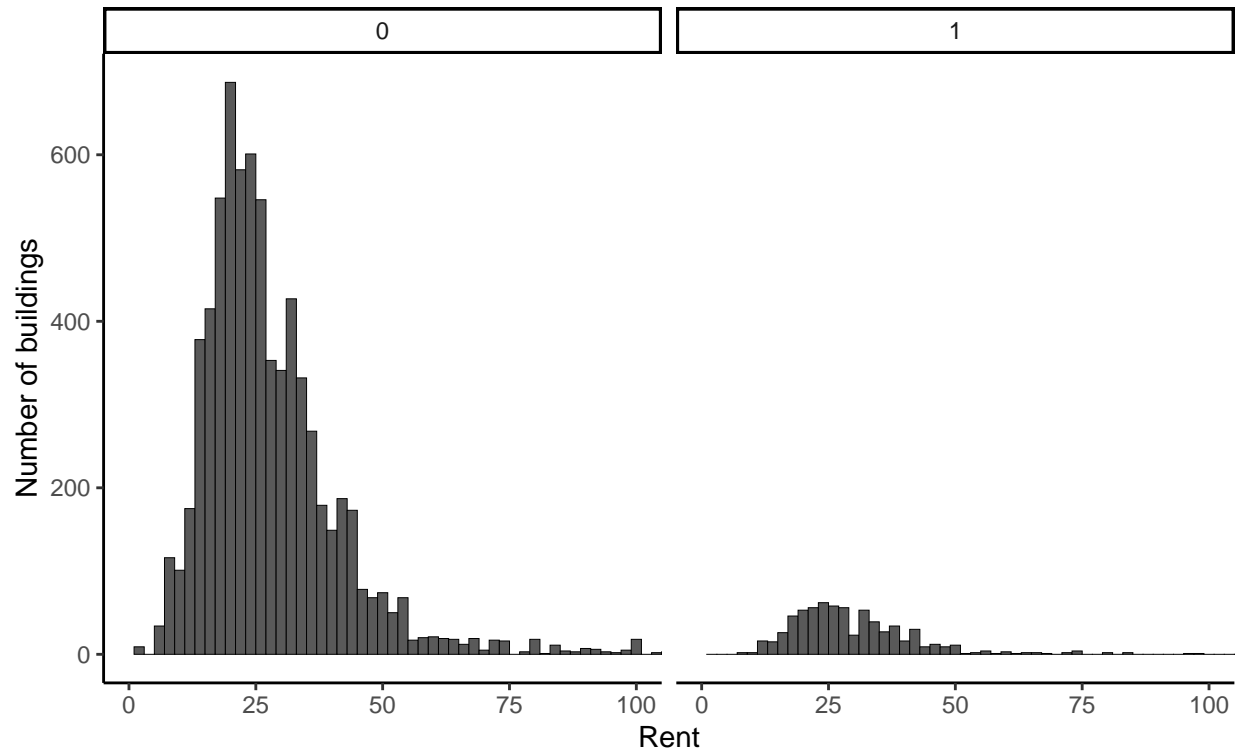
We found many flaws in the analysis done by the “excel guru”. We disagree with his figures as he only took the median of rent from both non-green and green building, then use the differences between the two to calculate extra revenue. He did not consider other factors that might be affecting the relationship between rent and green status which make his calculation inefficient. Furthermore, he only took into account the initial cost of 100 mil and the 5% premium, without considering other cost-benefits such as savings on electricity and gas usage in a green building. Next we will show some analysis we did to look for confounding variables.

Here, we are doing some data exploratory analysis on the dataset to discover trends and correlations.



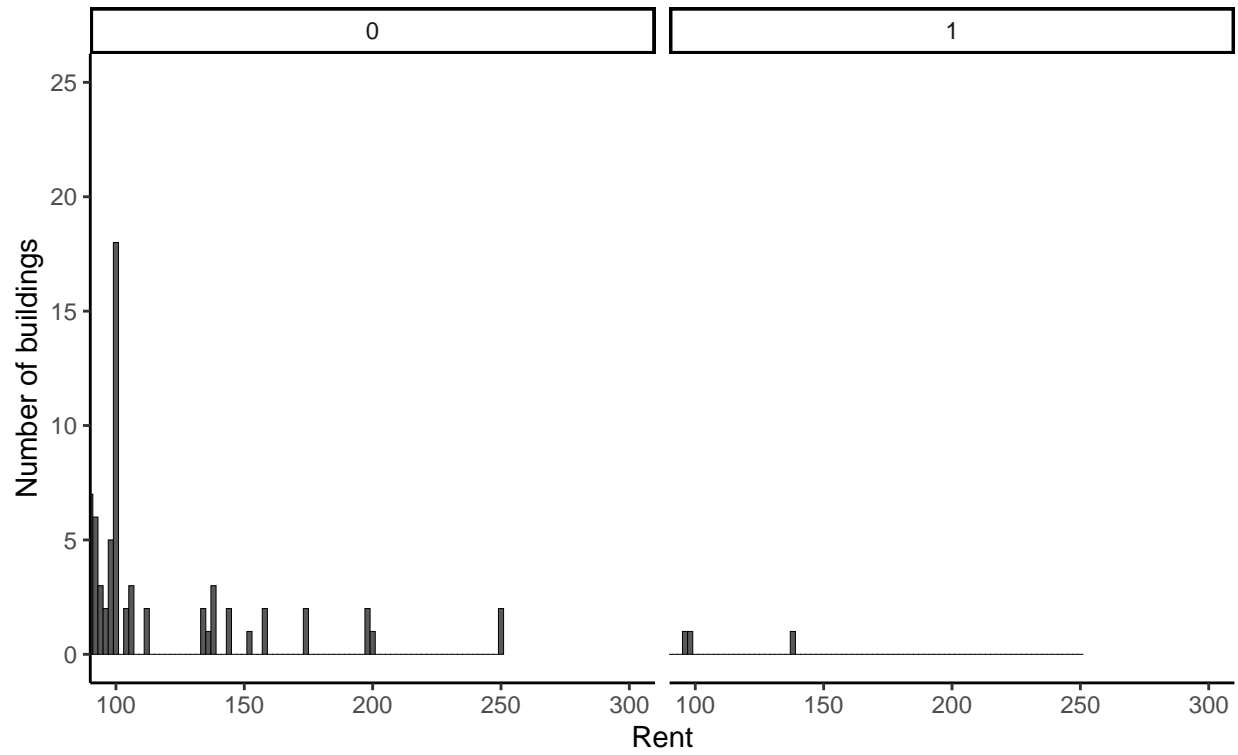
Distribution of rent across all buildings

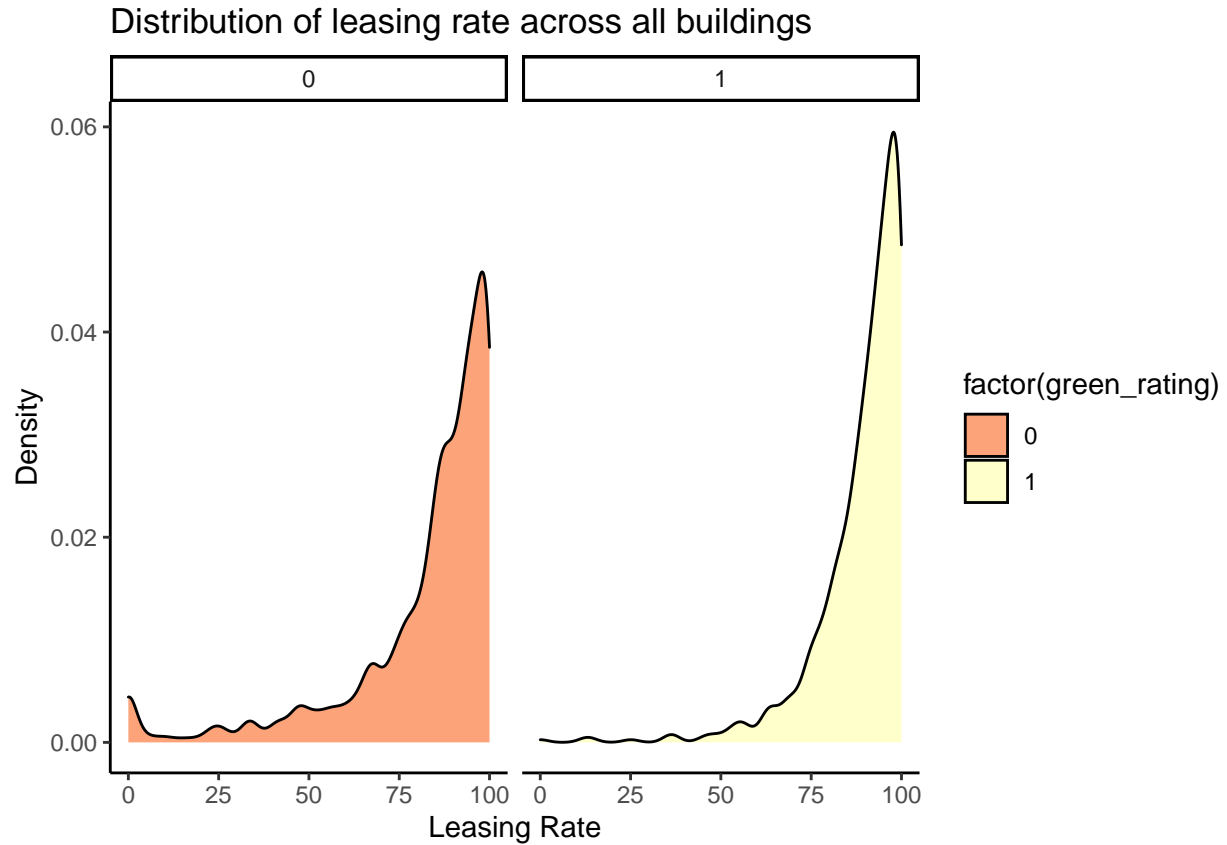
Rent below \$100



Distribution of rent across all buildings

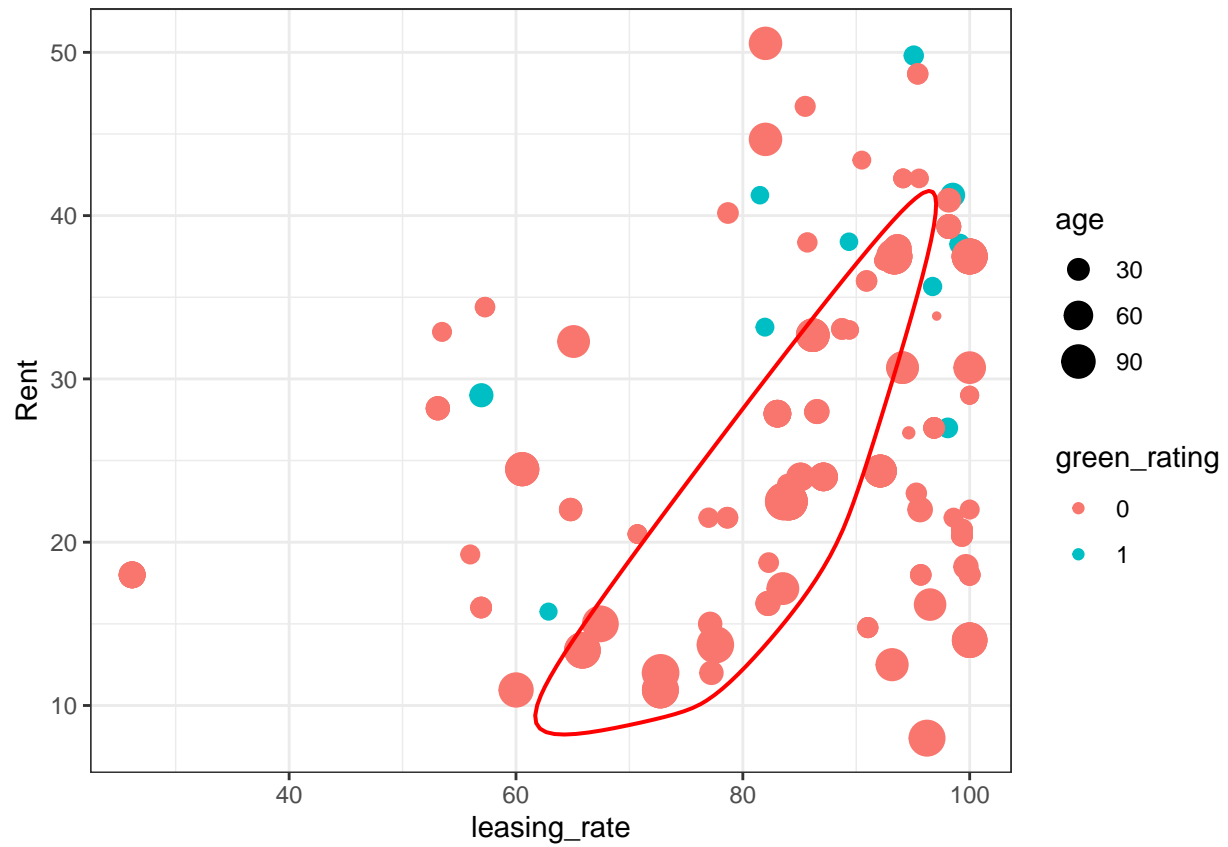
Rent above \$100



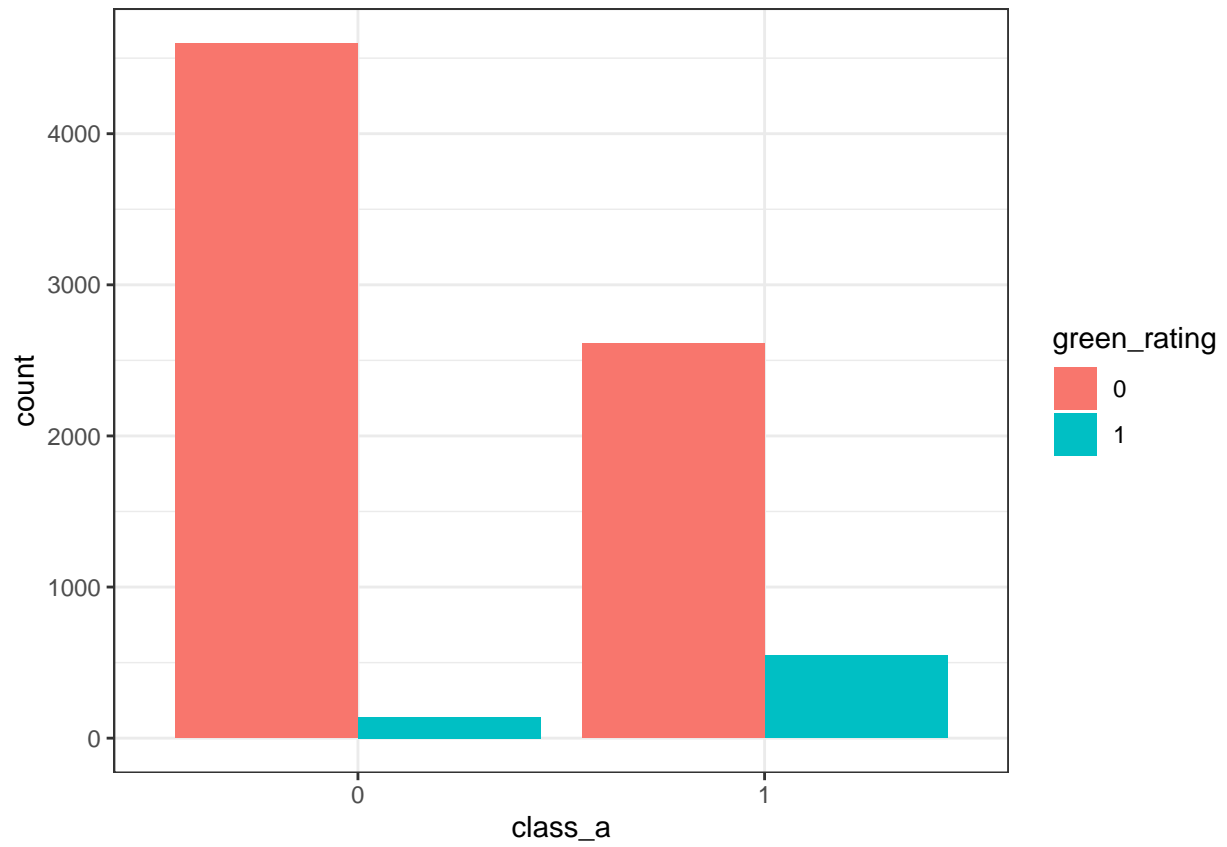


There are many factors that can have an effect on rent, like location, building quality, appliances and Other amenities, tenant/use mix, etc. Now we know that the target project is a new 15-story mixed-use building on East Cesar Chavez, just across I-35 from downtown. Since we have story information in the dataset, let's focus on the situation of 15-story buildings.

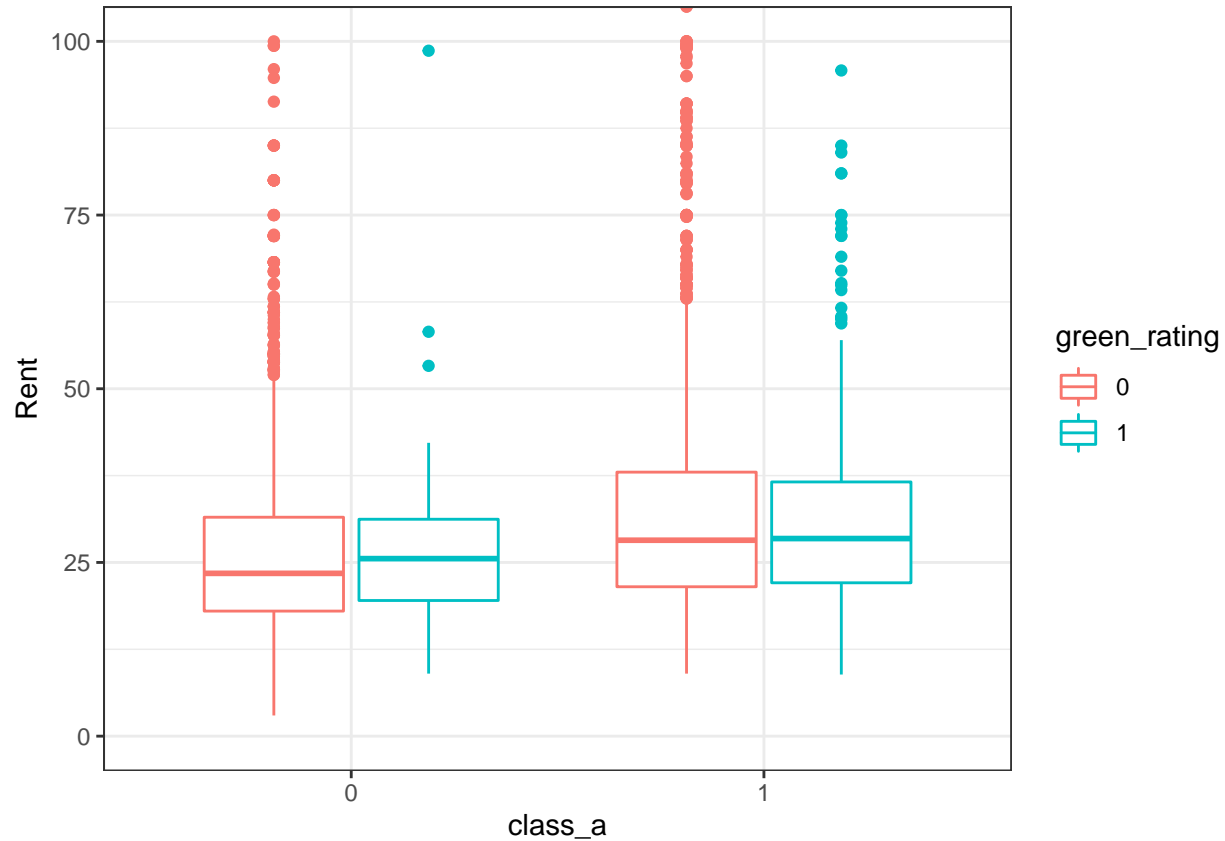
From the graphic, we can conclude that among 15-story building: 1.the average rent of green buildings is higher than that of non-green buildings; 2.the average occupancy rate of green buildings is higher than that of non-green buildings; 3.all green buildings have a class of a or b (however, does this bring extra cost)?



Here, we analyzed some variables that might be affecting the relationship between green status and rent.



Then we dived in on the relationship between class a and rent specifically and saw that class a building generally have a higher rent



Since most green buildings are of class a, class a can be a confounding variable that is also a part of the reason why rent increases in respect to green status. To adjust that, we can hold the class variable constant across buildings, and compute median rent from those buildings.

Profit calculations when class_a equals to 1.

```
## [1] "Report"

## [1] "Expected rent price for Green building: 28.44 Expected rent price for Non-Green building:28.2"

## [1] "Expected leasing rate for Green building: 0.9363 Expected rent price for Non-Green building:0.9"

## [1] "Expected yearly rent for Green building: 6657093 Expected yearly rent for Non-Green building:65"

## [1] "Expected electric Rate for the building: 0.032737397 Expected gas Rate for the building: 0.0102"

## [1] "Expected electric/gas usage for the Green building: 0.9 Expected electric/gas usage for the Non"

## [1] "Expected expenses for the Green building: 9682.55 Expected expenses for the Non-Green building:"

## [1] "Expected profit for Green Building: 6647410.45 Expected profit for Non-Green Building: 6519656."

## [1] "Expected profit difference between a green and non-green building: 127753.84"

## [1] "Expected payback period: 39.14"
```


Profit calculations when class_a equals to 0.

```
## [1] "Report"

## [1] "Expected rent price for Green building: 25.55 Expected rent price for Non-Green building:23.43"

## [1] "Expected leasing rate for Green building: 0.898 Expected rent price for Non-Green building:0.87"

## [1] "Expected yearly rent for Green building: 5735975 Expected yearly rent for Non-Green building:51"

## [1] "Expected electric Rate for the building: 0.032737397 Expected gas Rate for the building: 0.0102"

## [1] "Expected electric/gas usage for the Green building: 0.9 Expected electric/gas usage for the Non"

## [1] "Expected expenses for the Green building: 9682.55 Expected expenses for the Non-Green building:"

## [1] "Expected profit for Green Building: 5726292.45 Expected profit for Non-Green Building: 5094052.4"

## [1] "Expected profit difference between a green and non-green building: 632239.59"

## [1] "Expected payback period: 7.91"
```

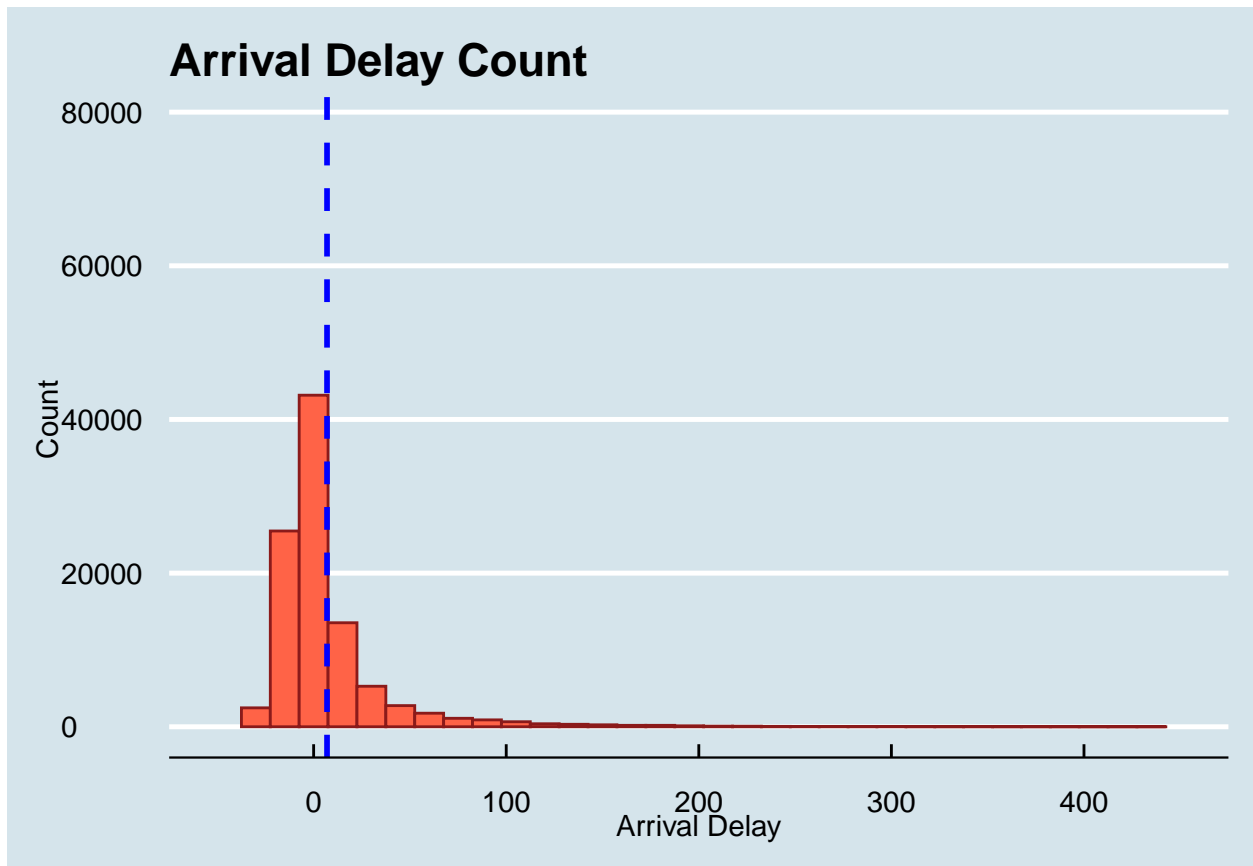
In conclusion, we suggest that the Austin real-estate developer should only compete in the non-class A market if they decided to make a green building. That is because a non-class A green building will generate more profit resulting in a shorter pay back period.

Flights at ABIA

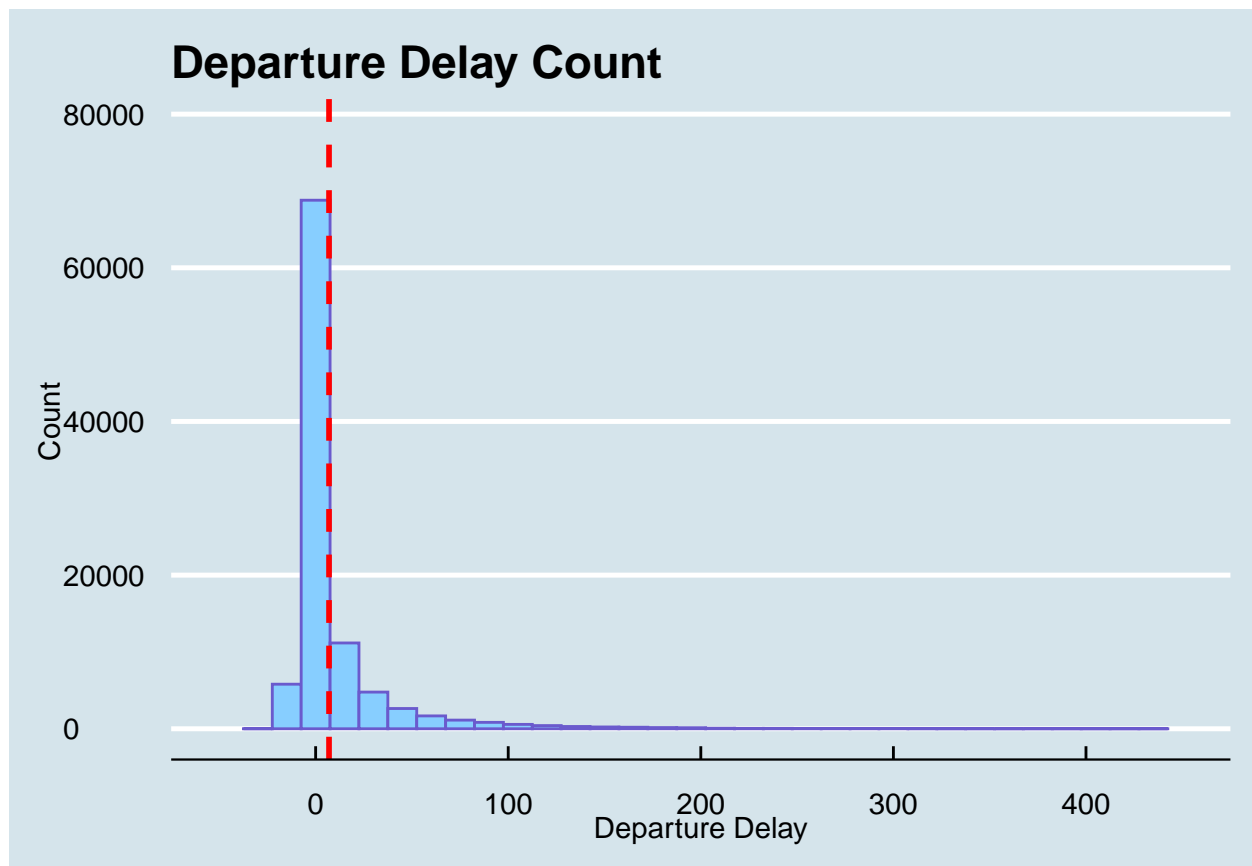
Your task is to create a figure, or set of related figures, that tell an interesting story about flights into and out of Austin. Provide a clear annotation/caption for each figure, but the figure should be more or less stand-alone, in that you shouldn't need many, many paragraphs to convey its meaning. Rather, the figure together with a concise caption should speak for itself as far as possible.

Airport Analysis

First, we want to create a histogram with the arriving and departing flights at Austin-Bergstrom. This includes looking at flights that were not delayed.



```
## [1] "The average arrival delay is 6.95 minutes."
```

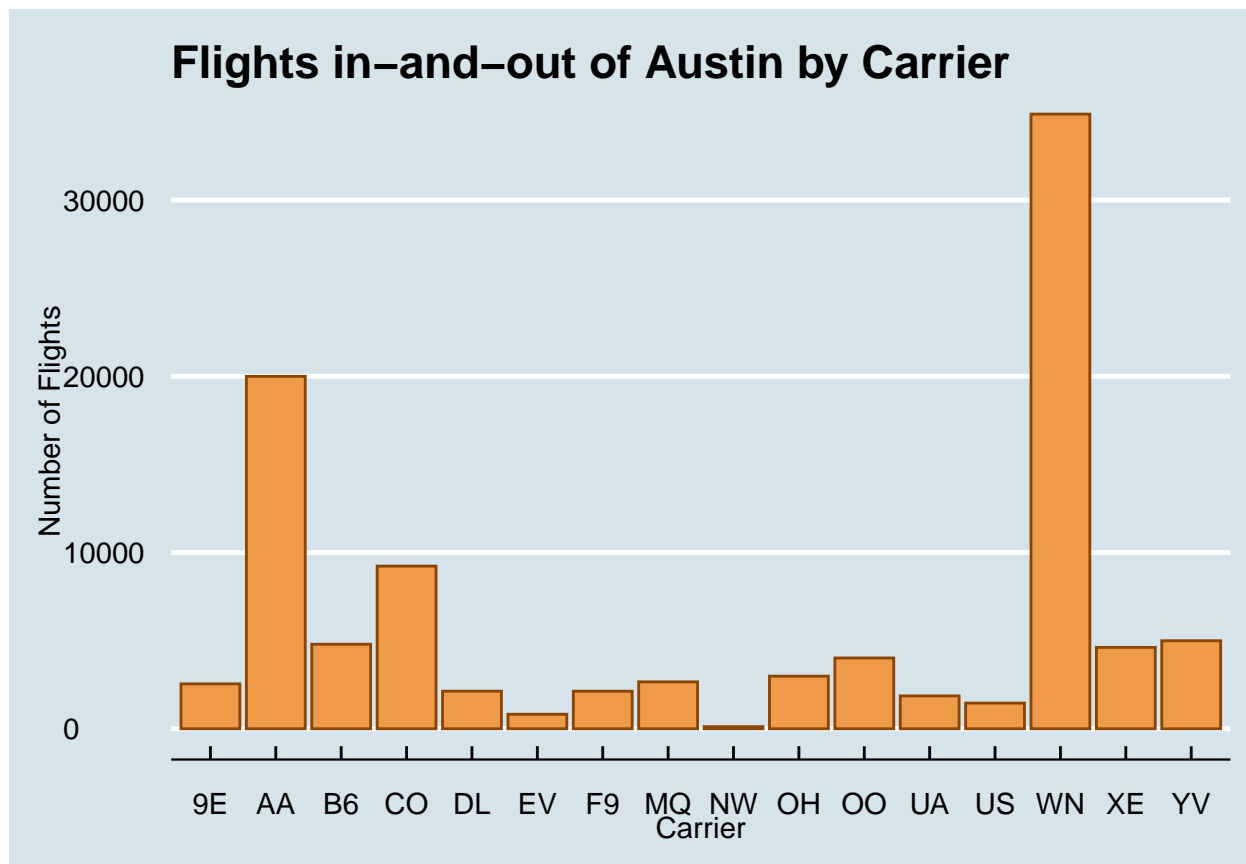


```
## [1] "The average departure delay is 9.04 minutes."
```

As we can see from the arrival histogram, most flights coming into Austin-Bergstrom are on time/early or delayed by less than 10 minutes. The flight departure histogram shows there are more delays in departures than arrivals. The departing flights have a delay that is around 2 minutes longer than that of an arriving flight.

Carrier Analysis

Next, we want to analyze the performance of the carriers at Austin-Bergstrom Airport.



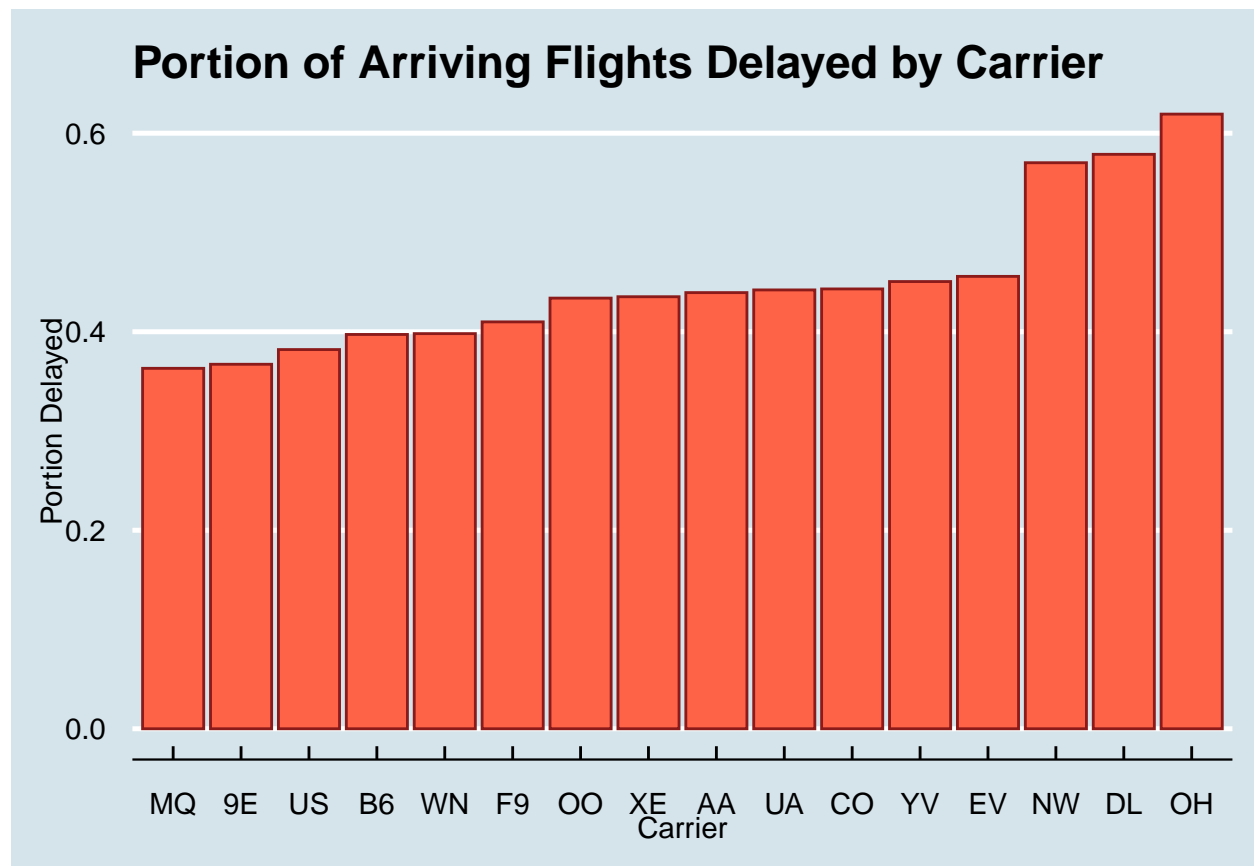
```
## [1] "Southwest had the highest flight count at AIBA with 34876."
```

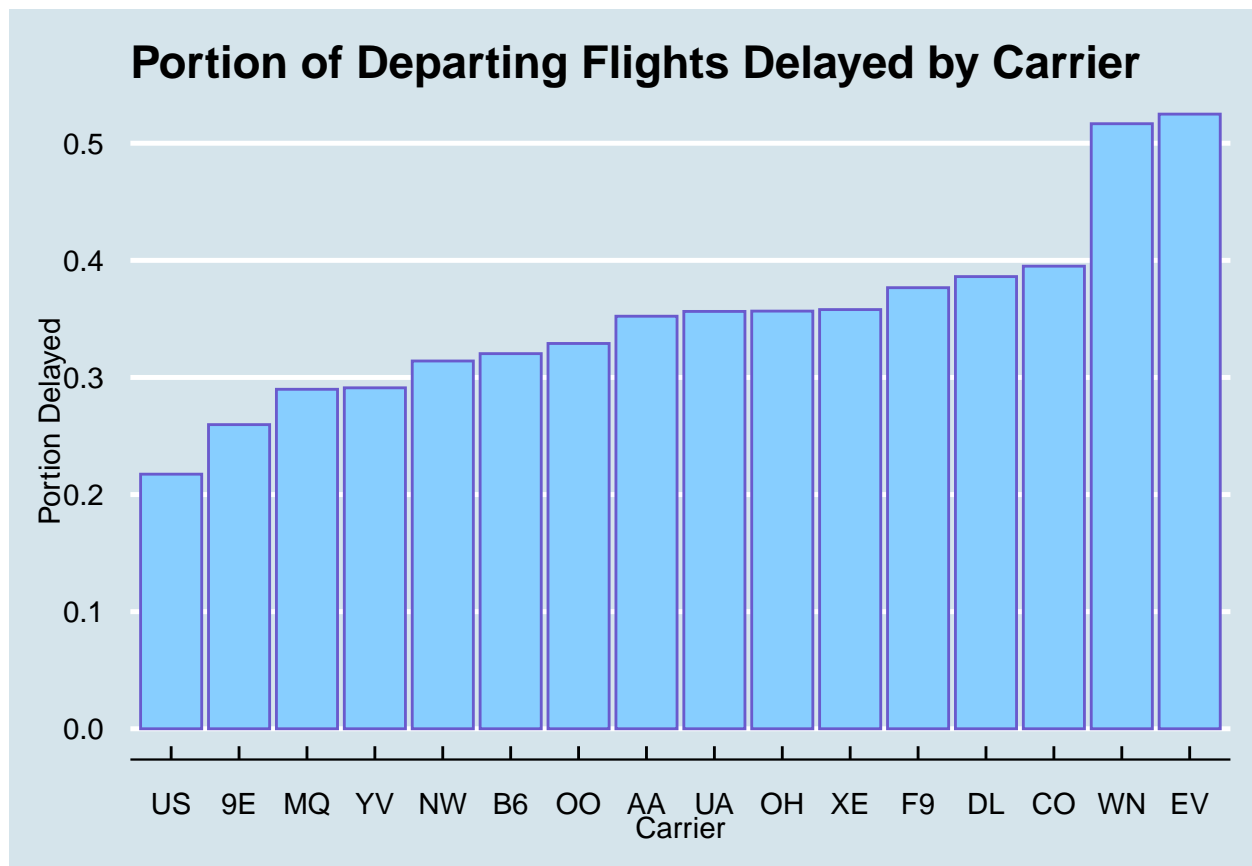
```
## [1] "Followed by American Airlines who had an AIBA flight count of 19995."
```

```
## [1] "The company with the least amount of flights at AIBA is Northwest Airlines with 121 flights."
```

If I am an Austin resident looking to open an airline credit card, I would look closely at what Southwest offers since they have the most flights at AIBA.

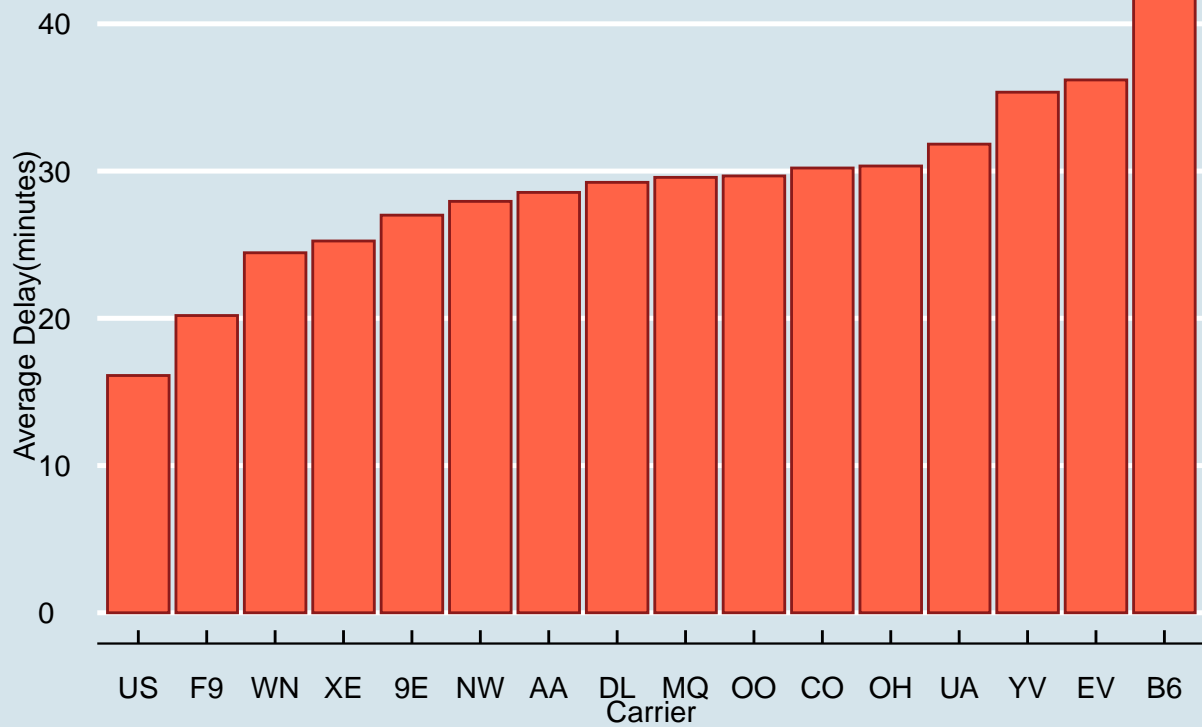
Let's take a look at the portion of flights delayed by each carrier.



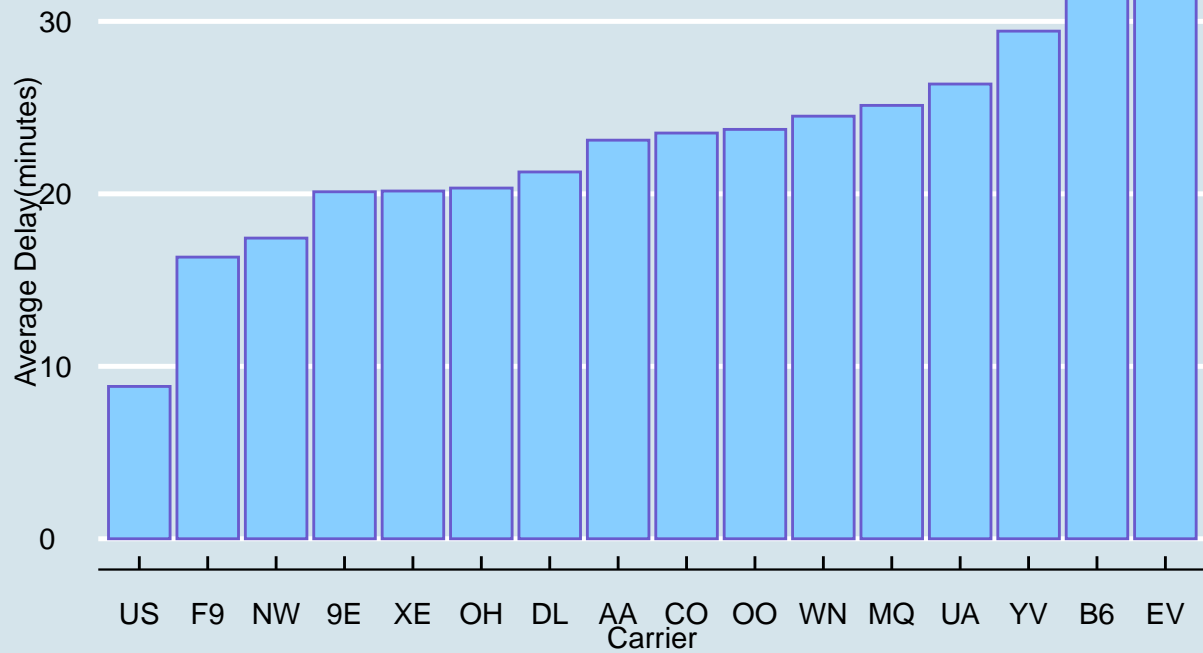


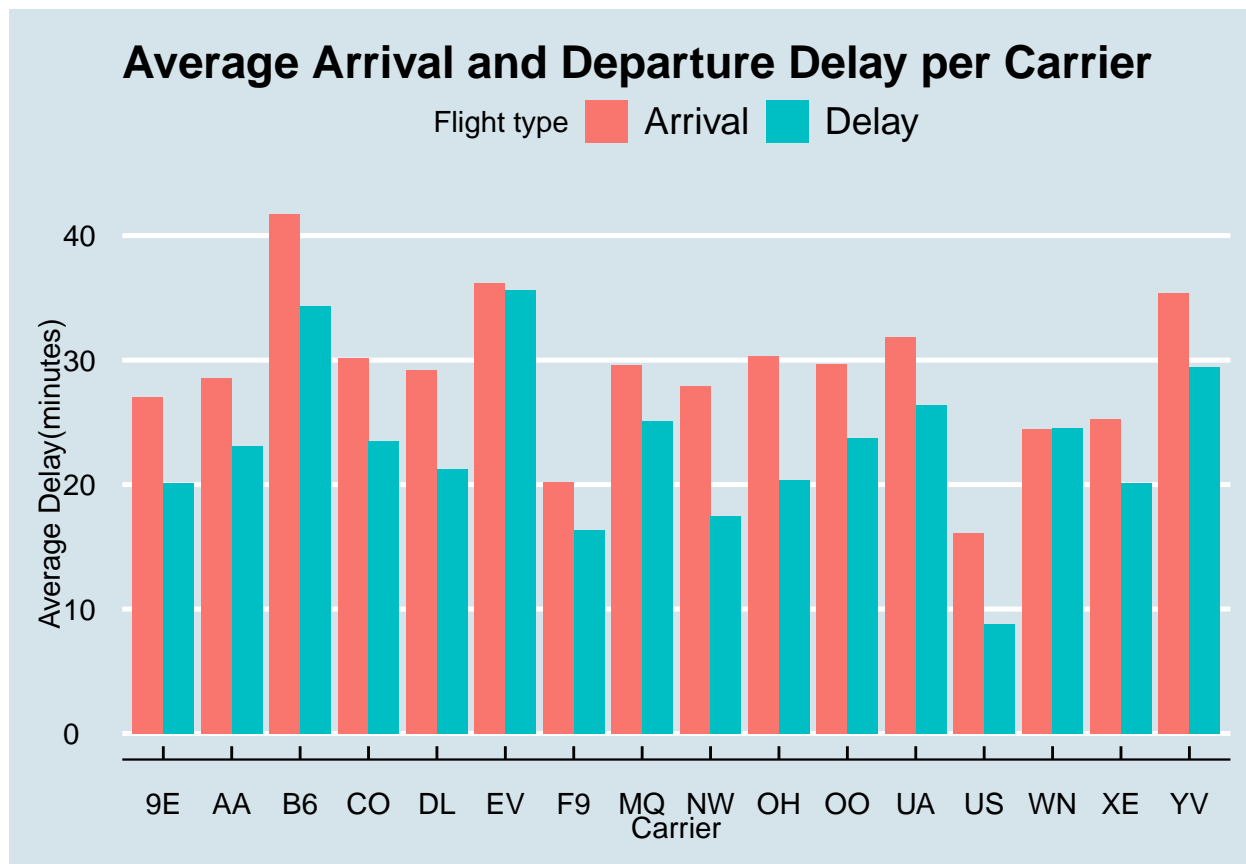
Not all delays are created equal. We must know the average time(minutes) that a carrier will delay a flight before we can make a judgement about which airline we want to avoid on future trips.

Average Arrival Delay by Carrier



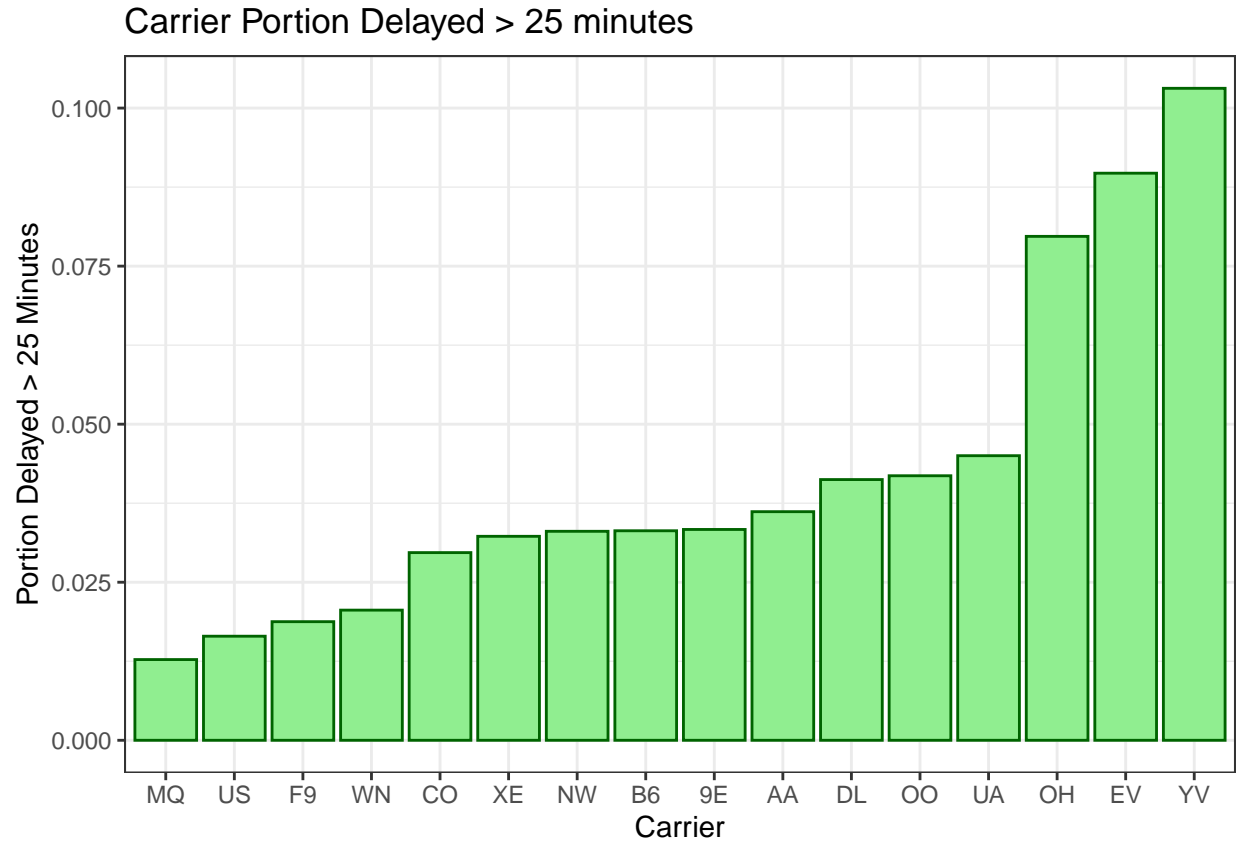
Average Departure Delay by Carrier





ExpressJet Airlines and Southwest Airlines have the highest portion of departing flights delayed, but ExpressJets' delays are around 10 minutes longer than Southwest delays. JetBlue is also intriguing because they are middle of the pack in terms of portion delayed, but their delays are averaging over 30 minutes. US Airways has the shortest delays of any of the carriers (arrival and departure), but they have a pretty low flight count at Austin-Bergstrom, so chances are that we won't get many destination and time options to work with an airline like US Airways.

A 10 minute delay can be a little annoying, but a 25 minute delay can ruin your plans. We want to look into which carrier is most likely to have a 25 minute delay.



The portion of flights delayed more than 25 minutes is extremely low, but the airline with the highest portion delayed more than 25 minutes is Mesa Airlines. We don't believe that the portion of delays greater than 25 minutes is an important factor when planning a trip so we don't need to worry about a long delay messing up our itinerary.

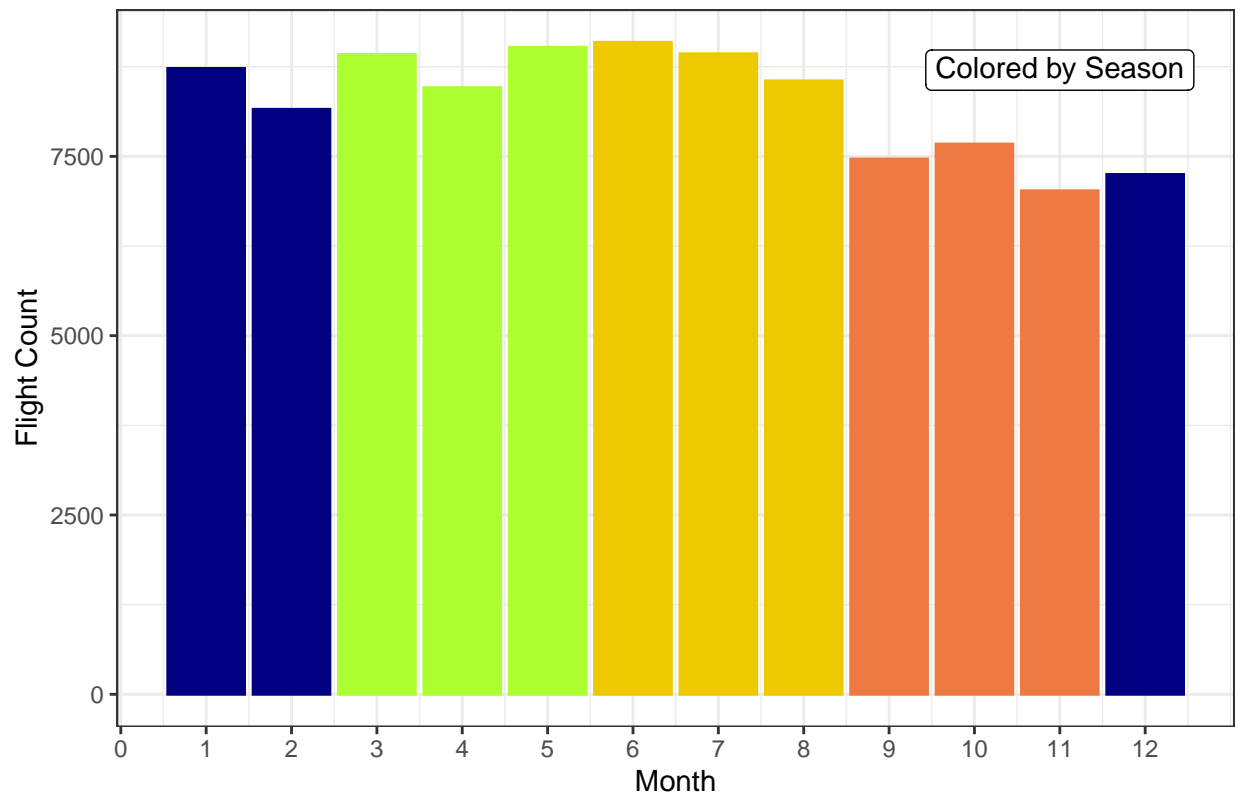
Carrier Conclusion

Southwest and American Airlines have the most flights in-and-out of Austin-Bergstrom, therefore they will have the most time/route options of any carrier. Southwest is on the high-end of departure delays, but on the low-end in terms of arrival delays. If we had to choose between Southwest and American Airlines based on the data, we would choose American Airlines since they have a lower portion of departures getting delayed and their departure delays are shorter than Southwest. Leaving on time is more important to us than arriving on time. JetBlue and ExpressJet are airlines that we would avoid, but it won't be hard since they do not have many flight options at ABIA.

Calendar Analysis

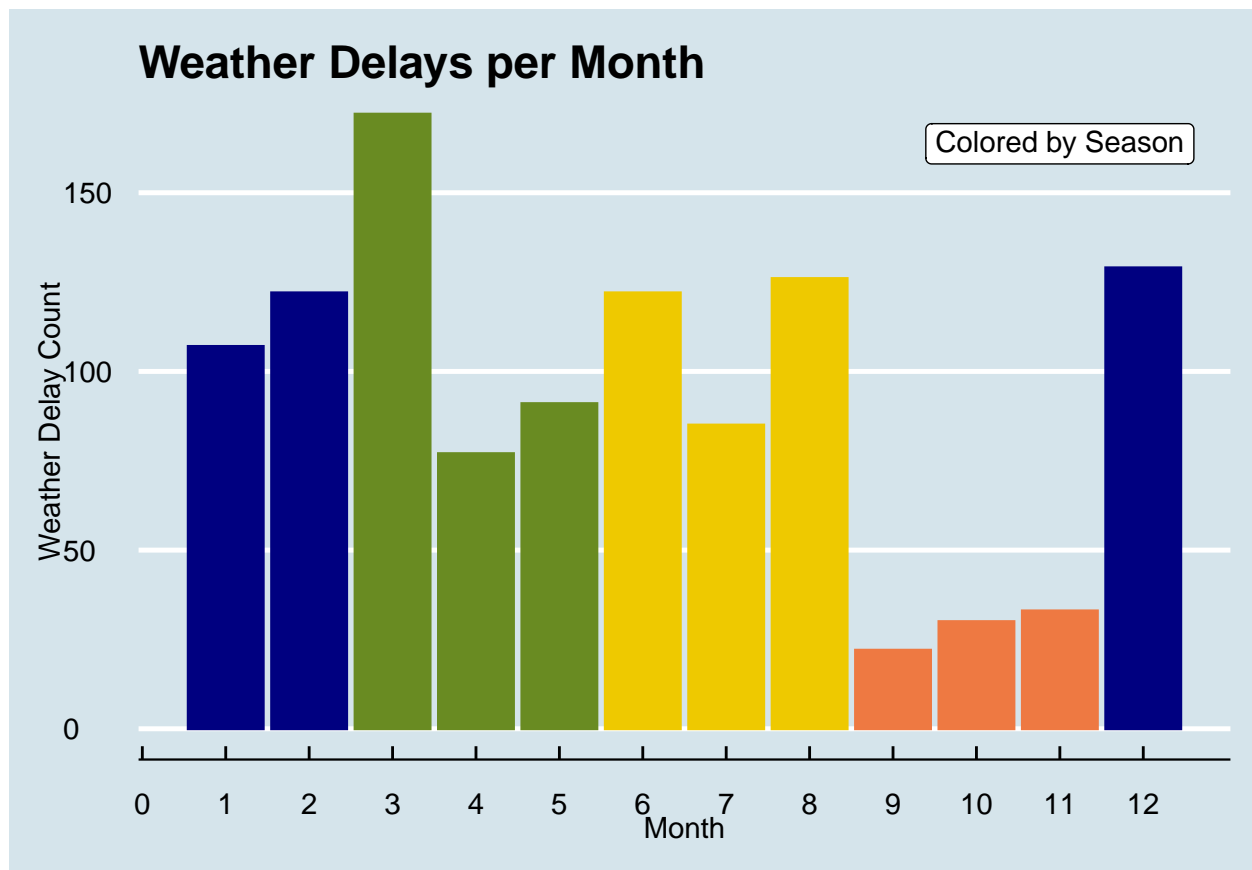
First, let's examine the number of flights per month at Austin-Bergstrom.

Total Flights per Month in-and-out of Austin



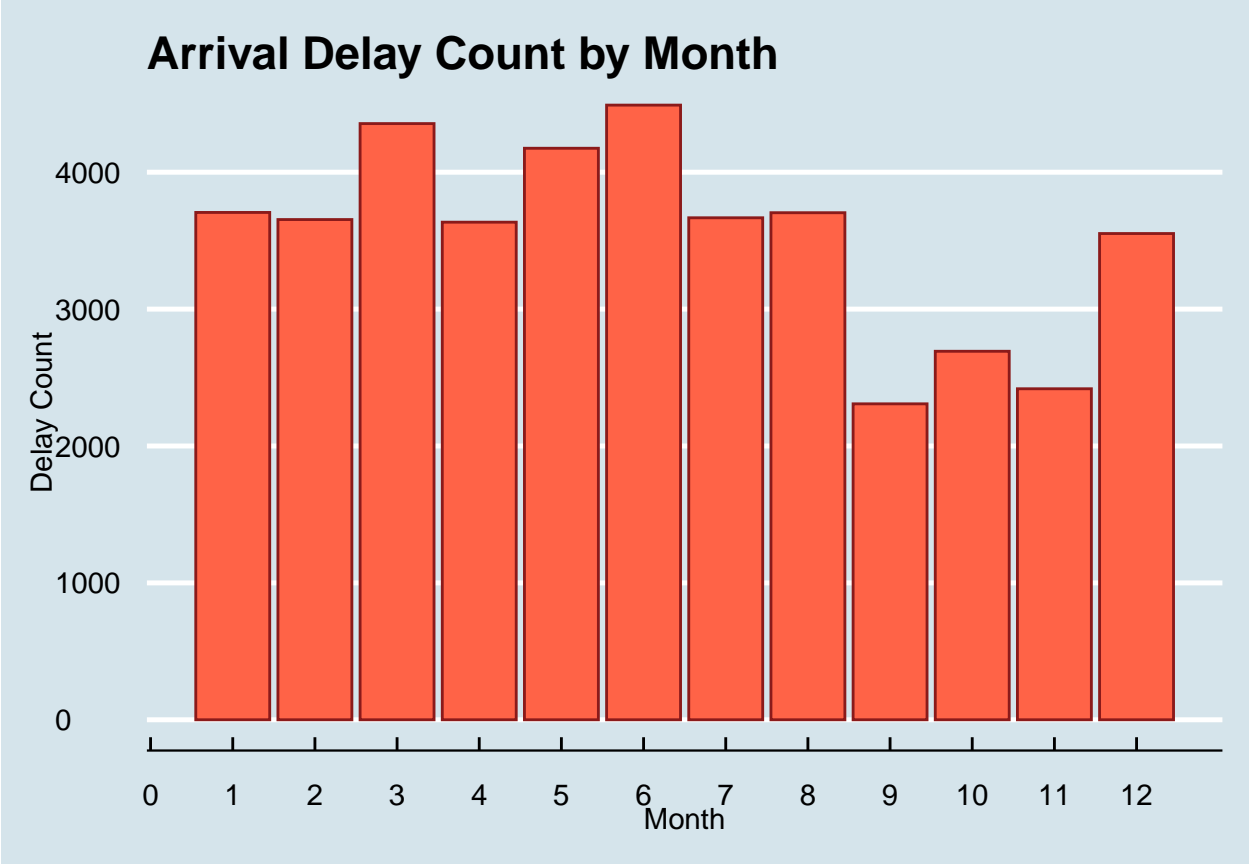
It is not surprising to see that the Spring and Summer have the highest flight count. We can not test this, but we believe Longhorn football is the reason for less flights in the Fall.

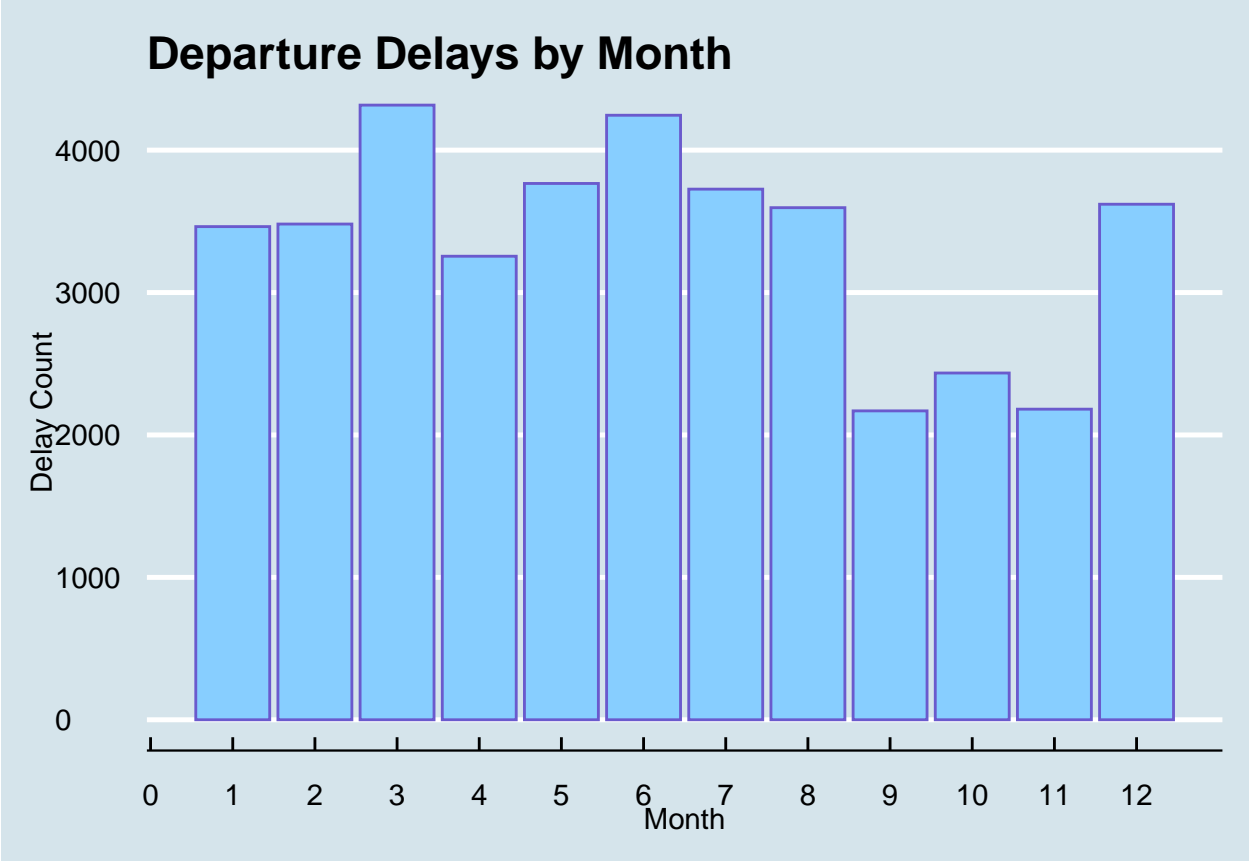
Texas weather can be hard to predict and changes so quickly, but we wanted to know which months have the most weather delays in Austin, Texas.

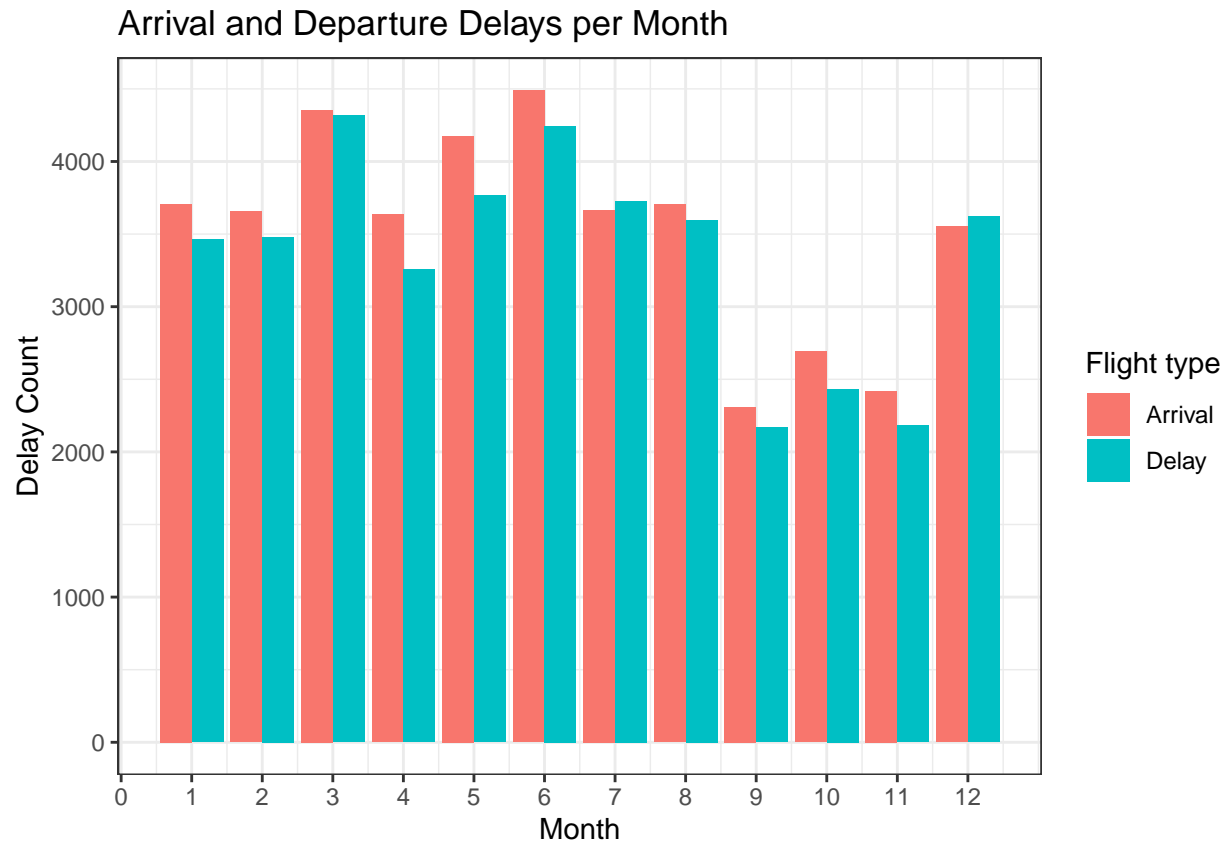


March has the most amount of weather delays, followed by December and August. When looking at seasonality the Winter months have the most of weather delays, while Autumn has the least amount.

Lastly, we want to investigate which months have the most delays and which months have the highest portion of delayed flights.

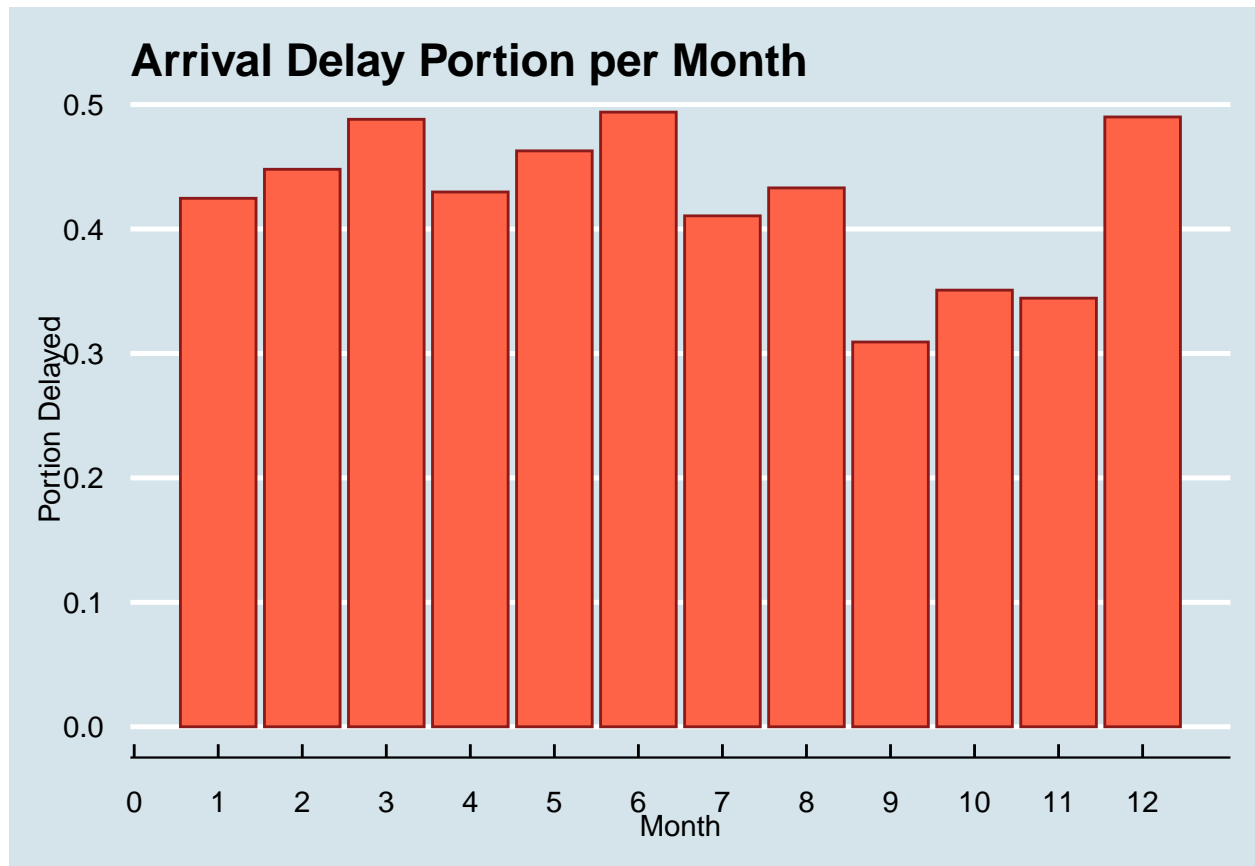


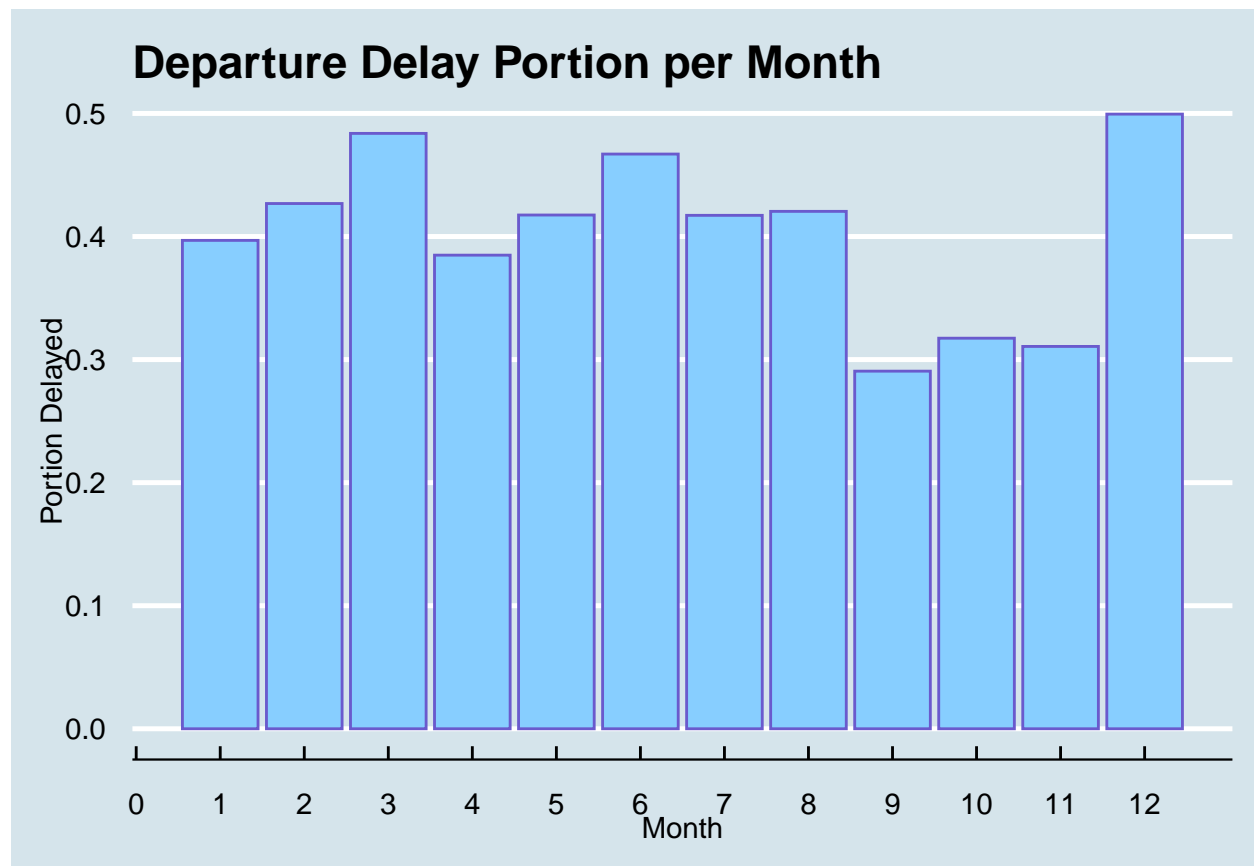


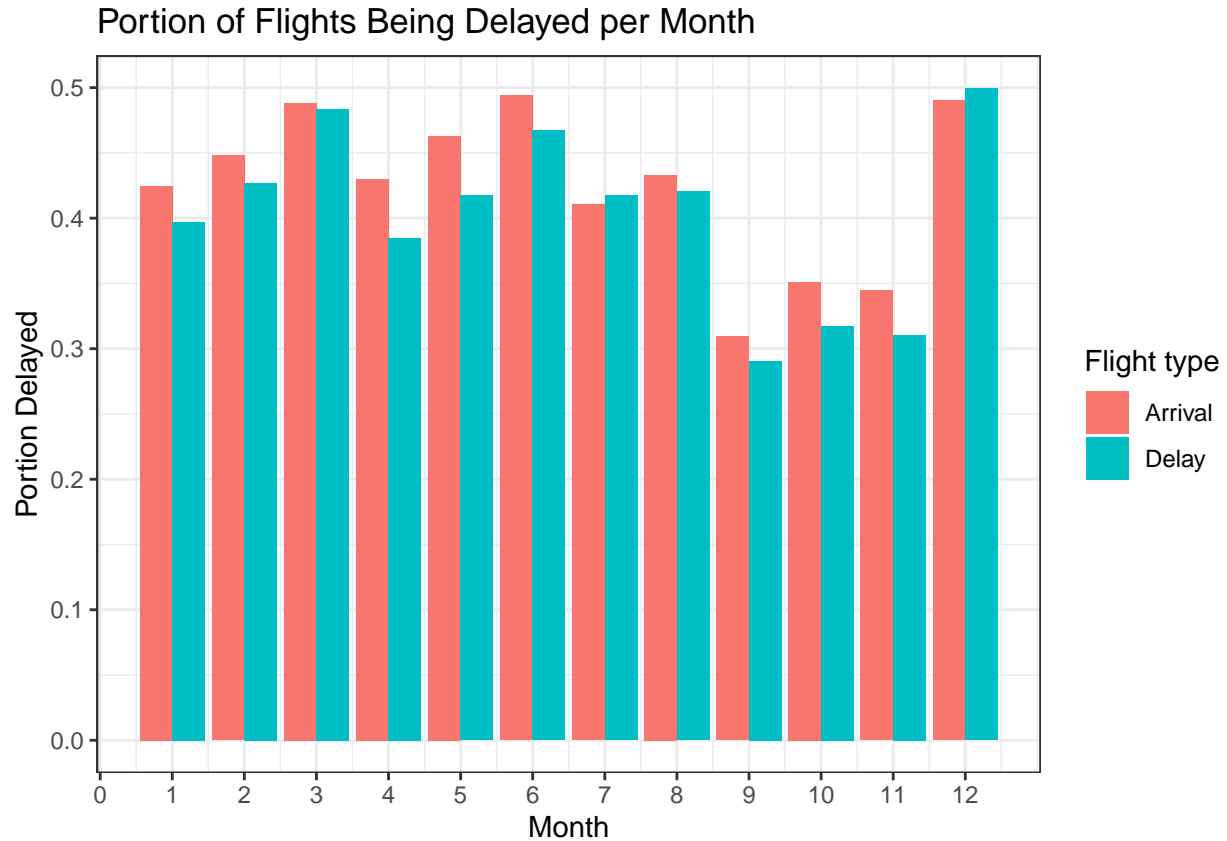


March and June have the most delays, and that is not shocking since Spring Break and early Summer are huge travel times at Austin-Bergstrom. We are surprised at the amount of delays in December since that is a month with the second lowest flight count in-and-out of Austin, Texas.

Do a higher portion of flights get delayed in December? We want to test that question next.







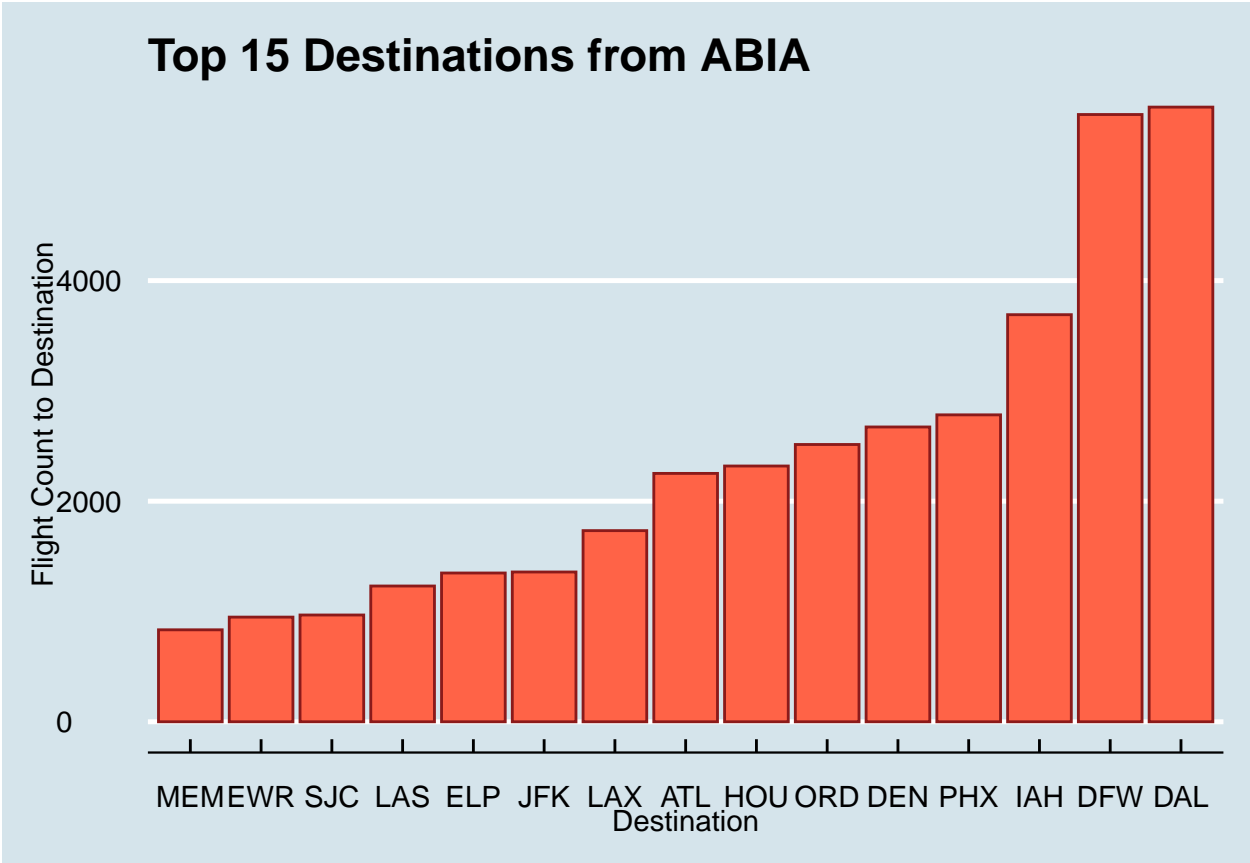
If you decide to fly out of Austin-Bergstrom in December, you have around a 50% chance of having your flight delayed. This graph adds validity to notion that airports around the holidays get crazy. They even made a movie about it called “Planes, Trains, and Automobiles”.

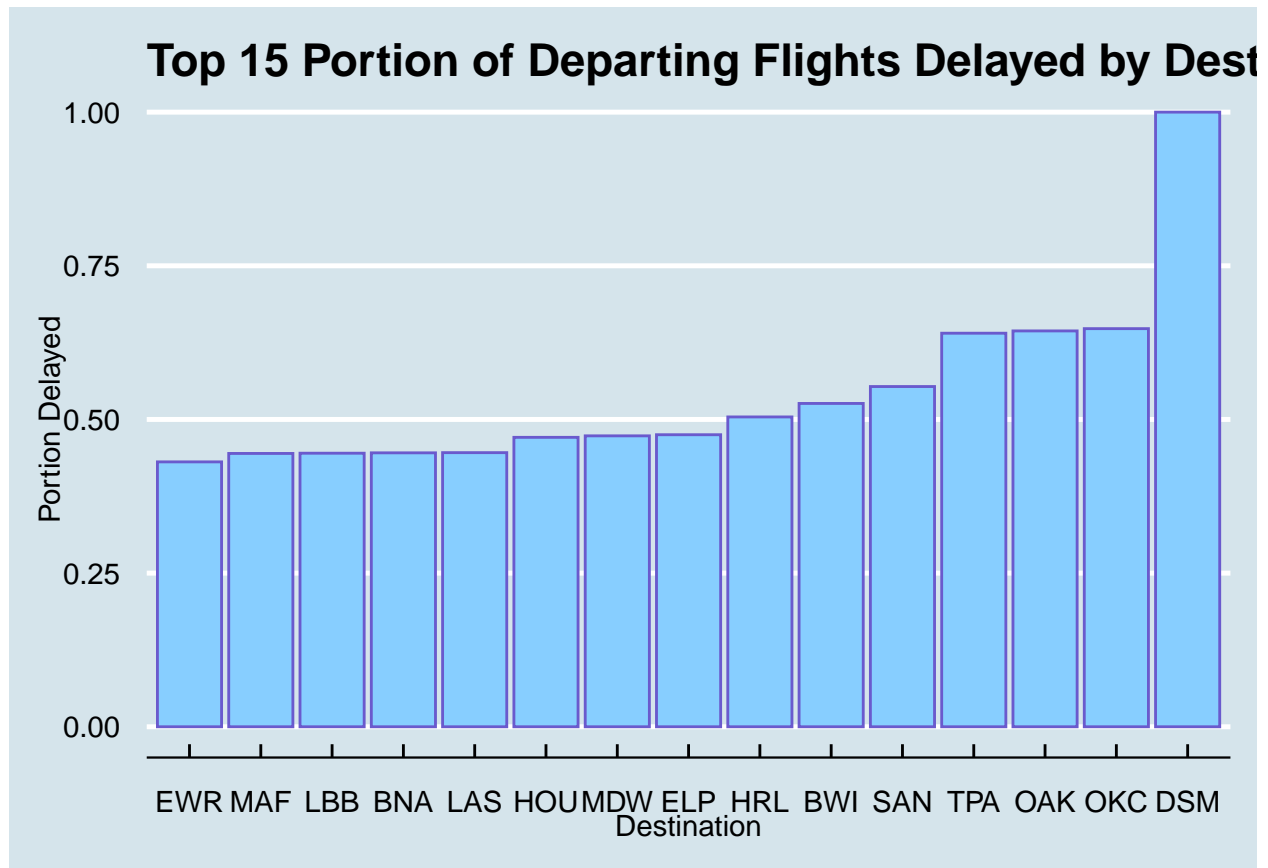
Calendar Conclusion

The Spring and Summer are the busiest seasons at ABIA. March(spring break) and June(school is finished) have the highest amount of delays, while December has the highest portion of delays. March is the month with the most amount of weather delays, but the Winter is the season with the most weather delays. In the future, we would like to revisit this dataset with more years so we can identify is March is typically a bad weather month in Austin or was March 2008 a bad weather month in Austin. The information we learned in the calendar section confirmed priors we had from our traveling experience, but it is nice to get confirmation.

Destination Analysis

We are interested to know where Austin residents are flying and how many of the popular destinations have a high portion of delayed flights.

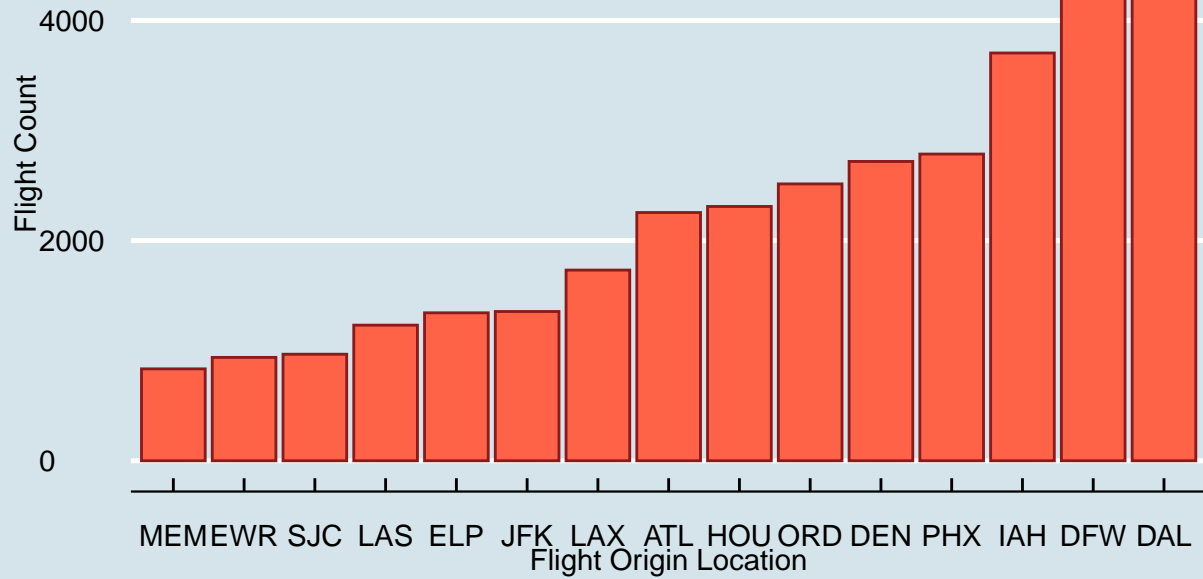


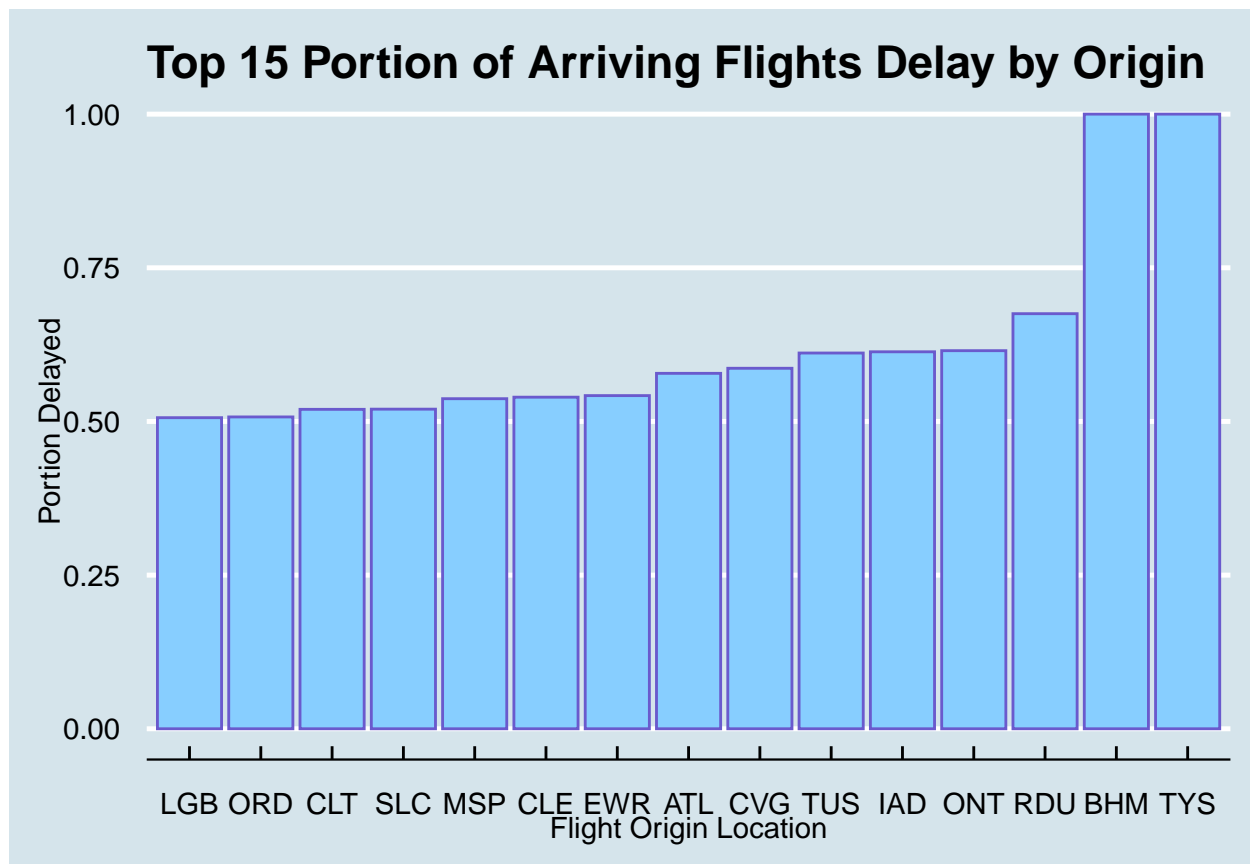


We have a large amount of flights that are in the state of Texas with 4 of the top 7 airport destinations being in Texas. When we look at the portion of flights delayed by destination, Houston(Hobby) and Newark are the only airports in the top 15 flight count and top 15 portion delayed. There is only 1 flight to Des Moines, Iowa and it was delayed, so that explains why it has a high portion of flights delayed.

Nobody likes getting home later than expected, let's look at the arrival delays by flight origin location.

Top 15 Airports flying into Austin





The arrival flight count looks pretty similar to the departure flight count. Newark is the only airport on both lists again! They need to get it together.

Destination Analysis

A large chunk of flights leaving Austin-Bergstrom end up staying in the state of Texas. Most of the popular flight routes are pretty efficient and do not have a large portion of flights being delayed(arrival and departure). You just might want to think twice before you book a flight to Newark, New Jersey.

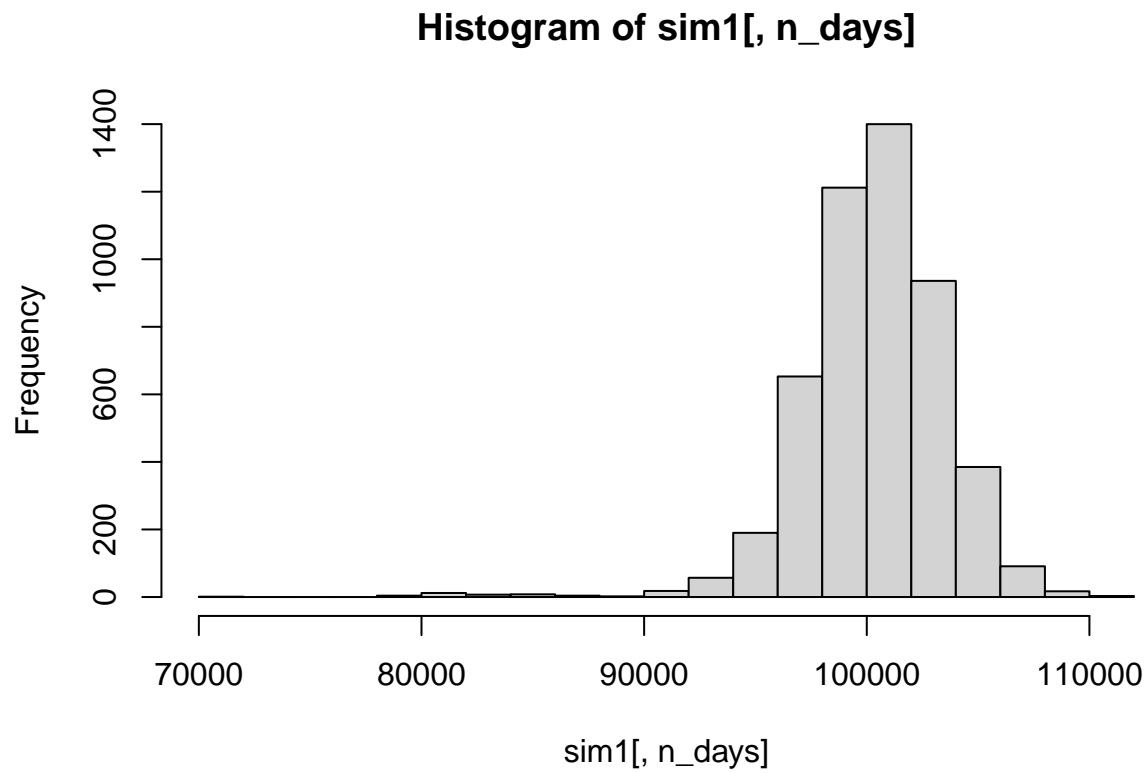
Portfolio Modeling

In this problem, you will construct three different portfolios of exchange-traded funds, or ETFs, and use bootstrap resampling to analyze the short-term tail risk of your portfolios. You should assume that your portfolios are rebalanced each day at zero transaction cost. For example, if you're allocating your wealth evenly among 5 ETFs, you always redistribute your wealth at the end of each day so that the equal five-way split is retained, regardless of that day's appreciation/depreciation

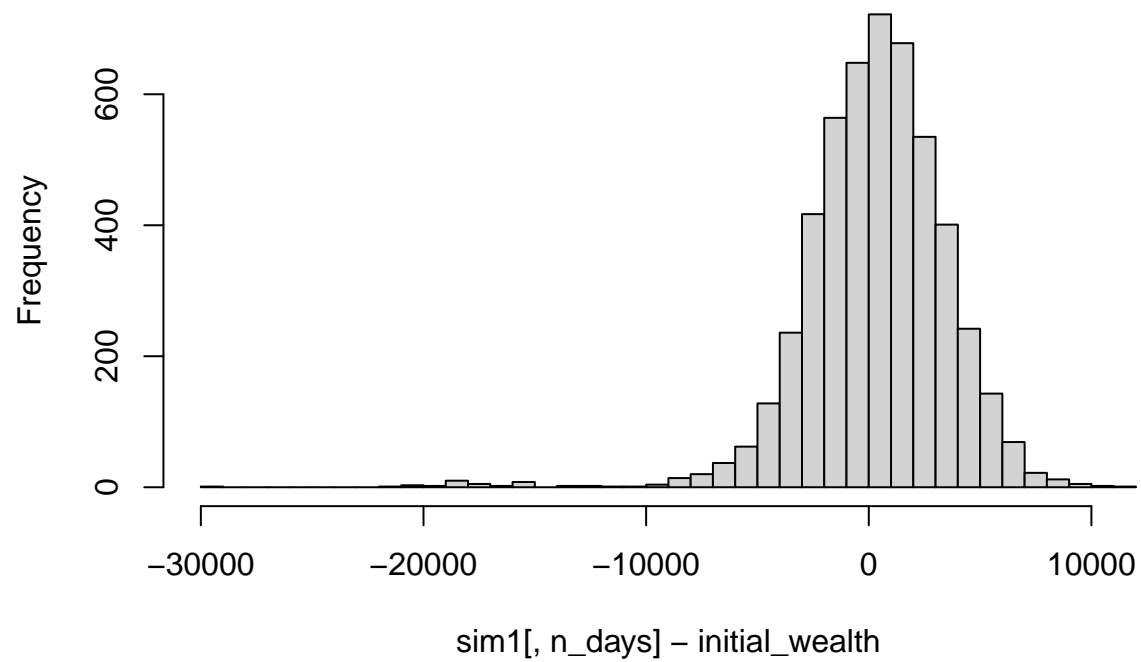
- Construct three different possibilities for an ETF-based portfolio, each involving an allocation of your \$100,000 in capital to somewhere between 3 and 10 different ETFs.
- Download the last five years of daily data on your chosen ETFs
- Use bootstrap resampling to estimate the 4-week (20 trading day) value at risk of each of your three portfolios at the 5% level.
- Write a report summarizing your portfolios and your VaR findings.

Portfolio (1) — Aggressive Portfolio

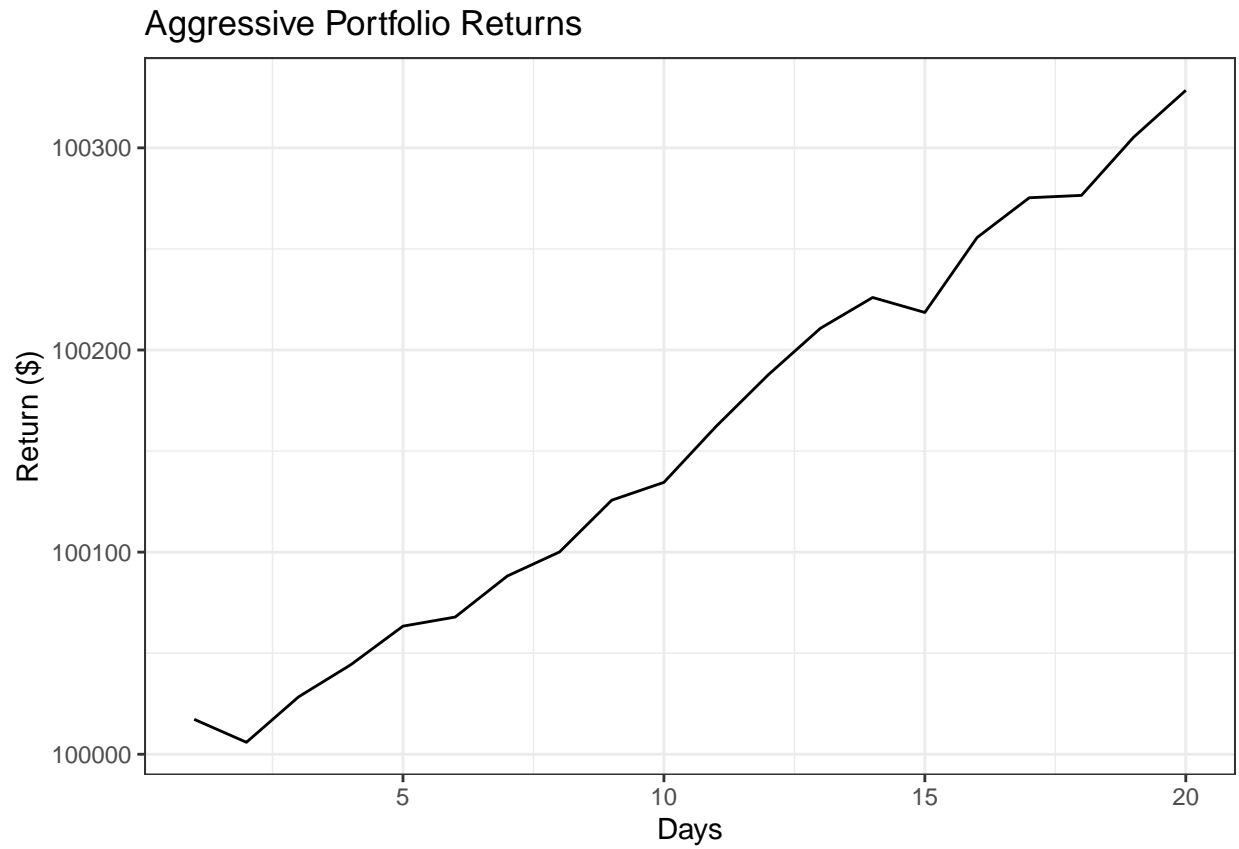
Currency ETFs (20%) + Corporate Bonds ETFs (30%) + Equities ETFs (50%)



Histogram of $\text{sim1[, n_days]} - \text{initial_wealth}$



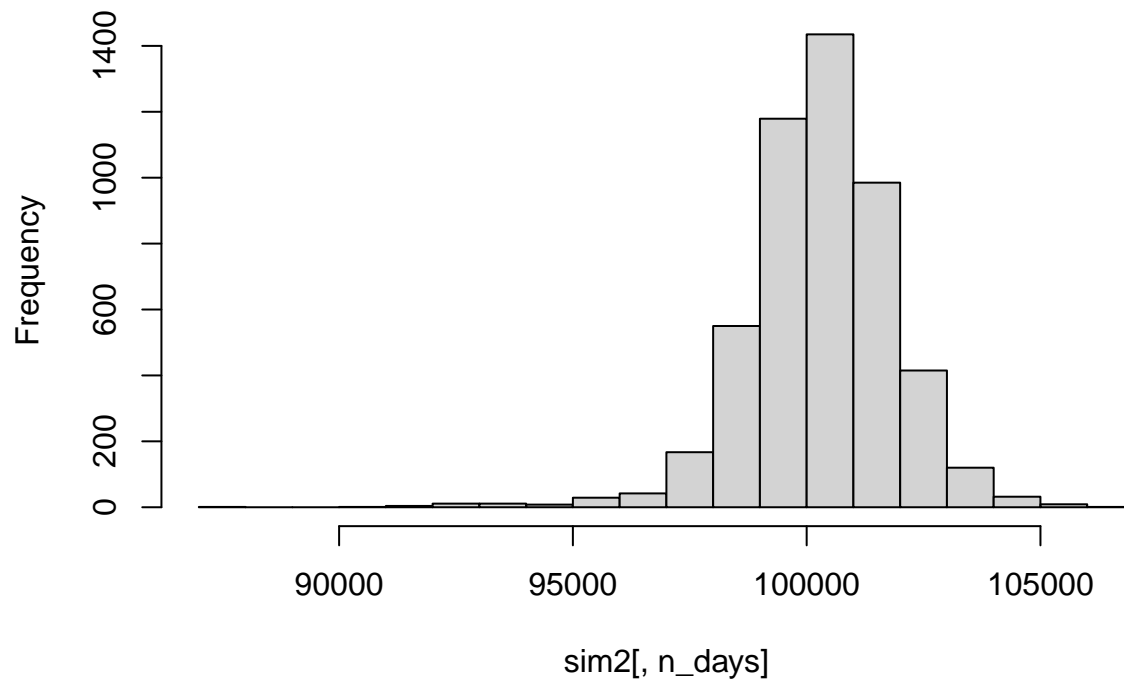
```
## [1] "5% value at risk is: -4377.32300281821"
```

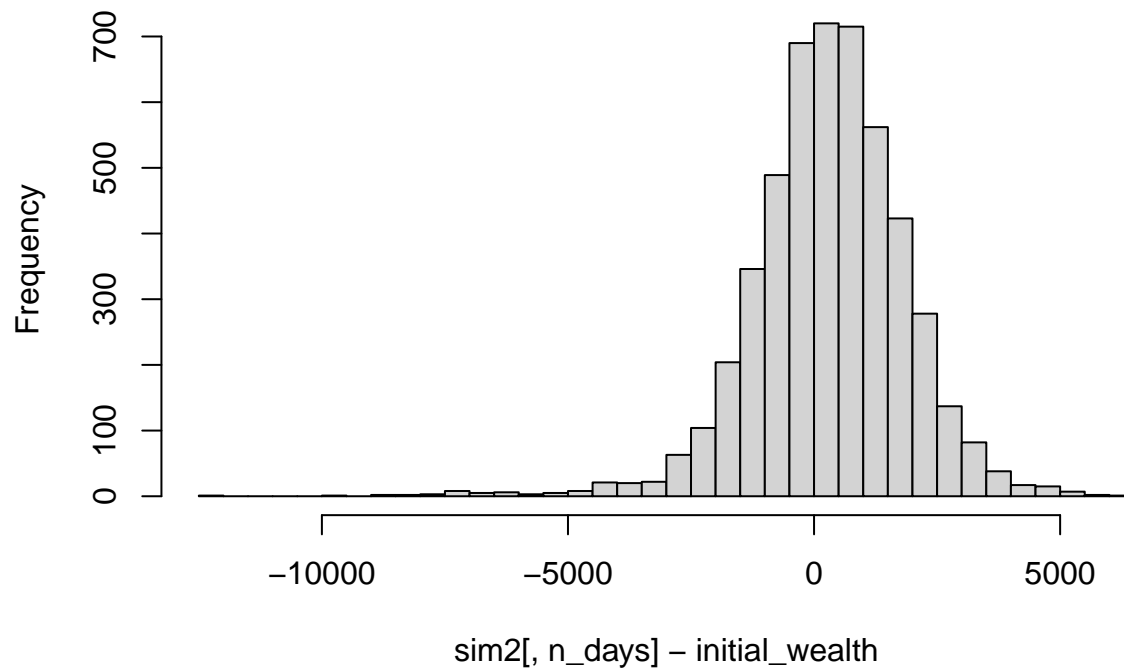
Portfolio (2) — Moderate Portfolio

Currency ETFs (30%) + Corporate Bonds ETFs (50%) + Equities ETFs (20%)

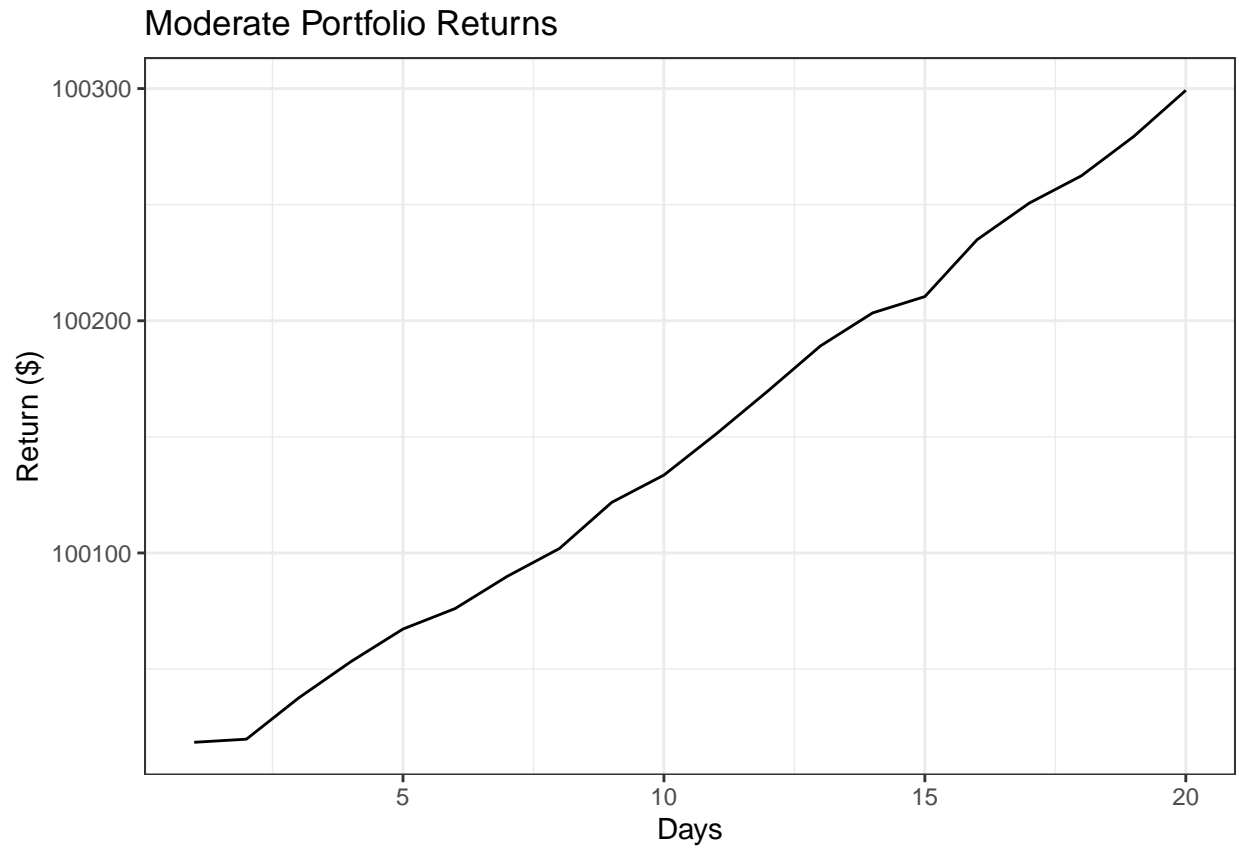
Histogram of sim2[, n_days]



Histogram of $\text{sim2[, n_days]} - \text{initial_wealth}$



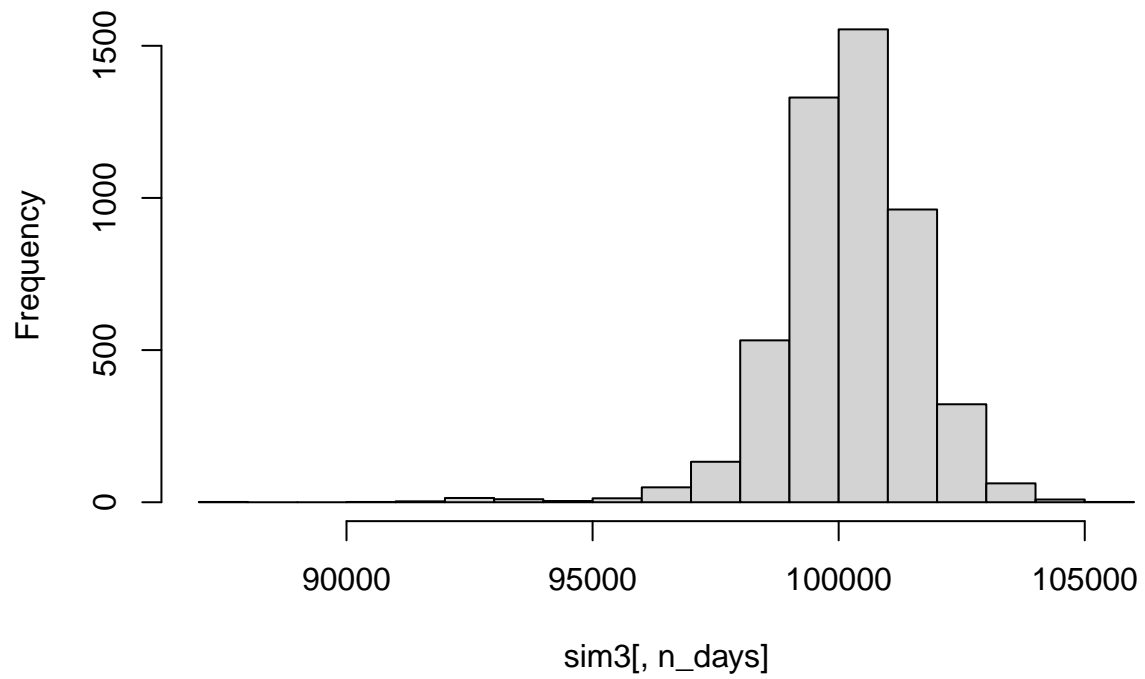
```
## [1] "5% value at risk is: -2093.34202874161"
```



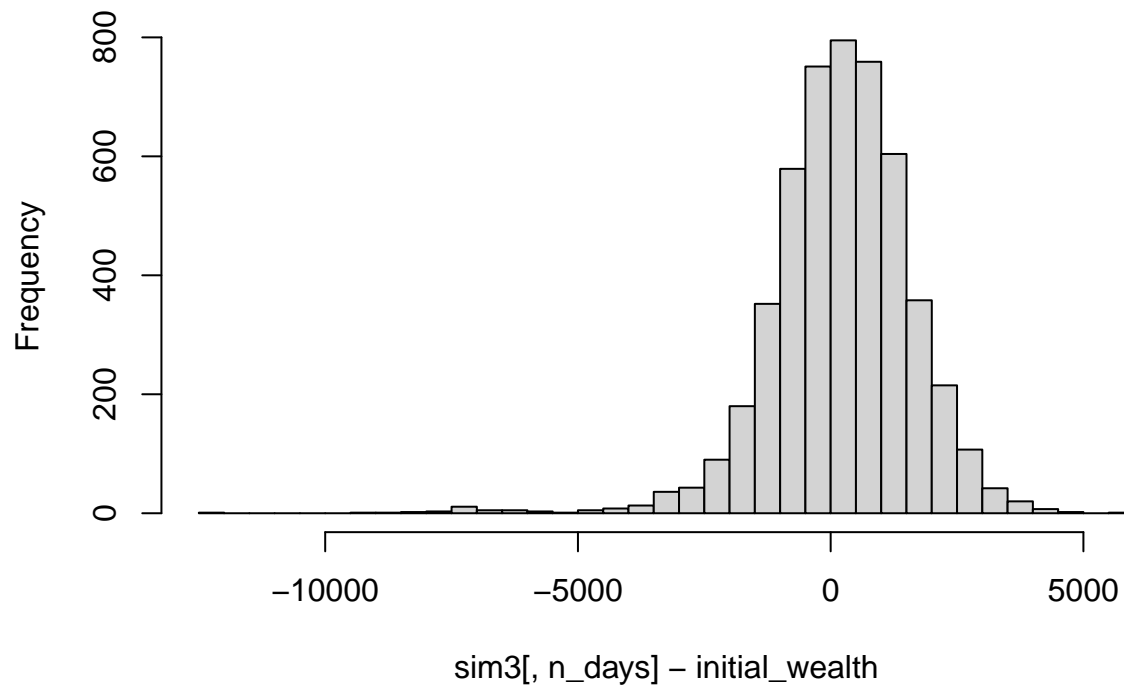
Portfolio (3) — Conservative Portfolio

Currency ETFs (50%) + Corporate Bonds ETFs (30%) + Equities ETFs (20%)

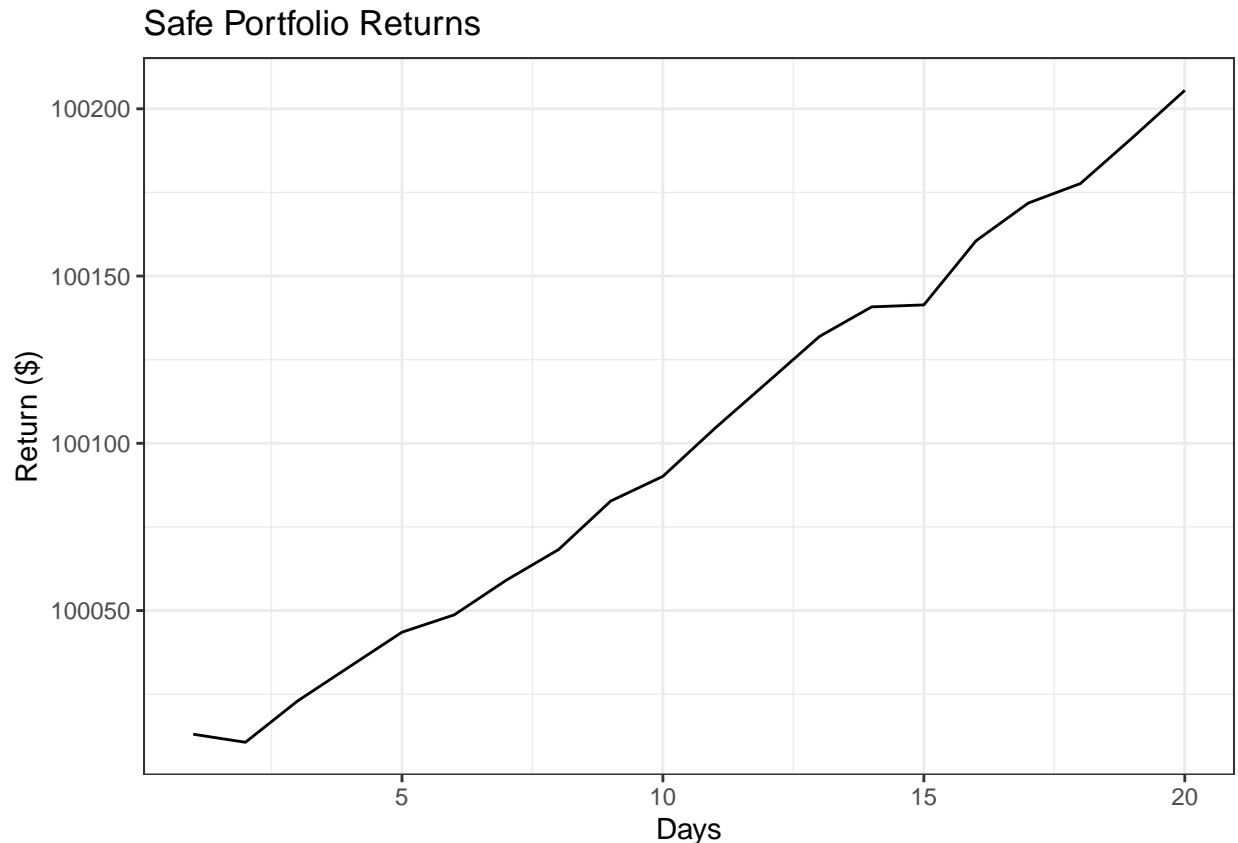
Histogram of sim3[, n_days]



Histogram of sim3[, n_days] – initial_wealth



```
## [1] "5% value at risk is: -1895.6922740784"
```



Portfolio Analysis

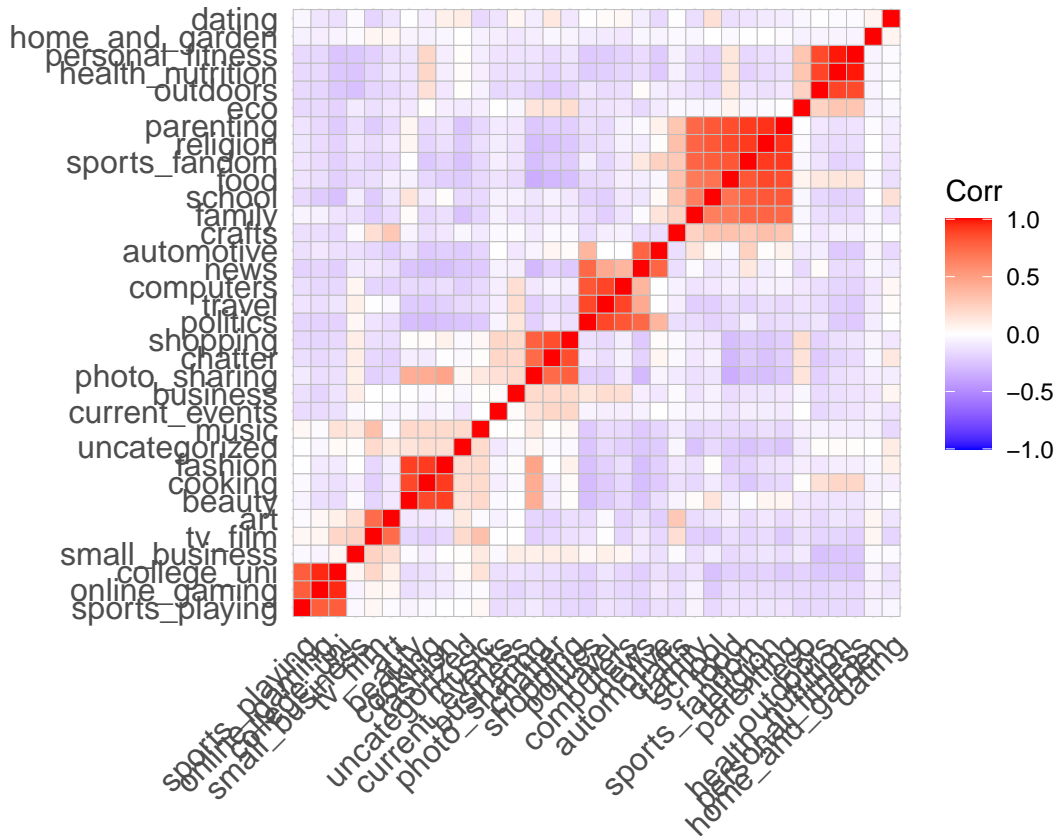
Across the three portfolios, we can see that the return on average increases over the 20 days period. However, the aggressive model return vs days line graph fluctuate a little bit more than the other two portfolios. This can be seen on the VaR as well, while the aggressive portfolio has the highest average return, it also has the highest VaR at 5%. Comparing the returns and VaR of all three models, the moderate portfolio is the best option for us because it has a relatively high return that not too far from that of the aggressive model (100296.8 vs 100325.4) and a 5% VaR that is far lower than that of the aggressive model (2060.641 vs 4354.693). The conservative model on the other hand has the lowest VaR (1870.43) but the return (100203.6) is also the lowest therefore we don't think it is the best option comparing to the moderate model.

Market Segmentation

This was data collected in the course of a market-research study using followers of the Twitter account of a large consumer brand that shall remain nameless—let's call it "NutrientH20" just to have a label. The goal here was for NutrientH20 to understand its social-media audience a little bit better, so that it could hone its messaging a little more sharply. Your task is to analyze this data as you see fit, and to prepare a concise report for NutrientH20 that identifies any interesting market segments that appear to stand out in their social-media audience. You have complete freedom in deciding how to pre-process the data and how to define "market segment." (Is it a group of correlated interests? A cluster? A latent factor? Etc.) Just use the data to come up with some interesting, well-supported insights about the audience, and be clear about what you did.

First, let's take a look at data correlation. Practically, if our data is not highly correlated, we might not need a PCA. As the graph shows, some of our variables are quite correlated. Thus, we can proceed to PCA

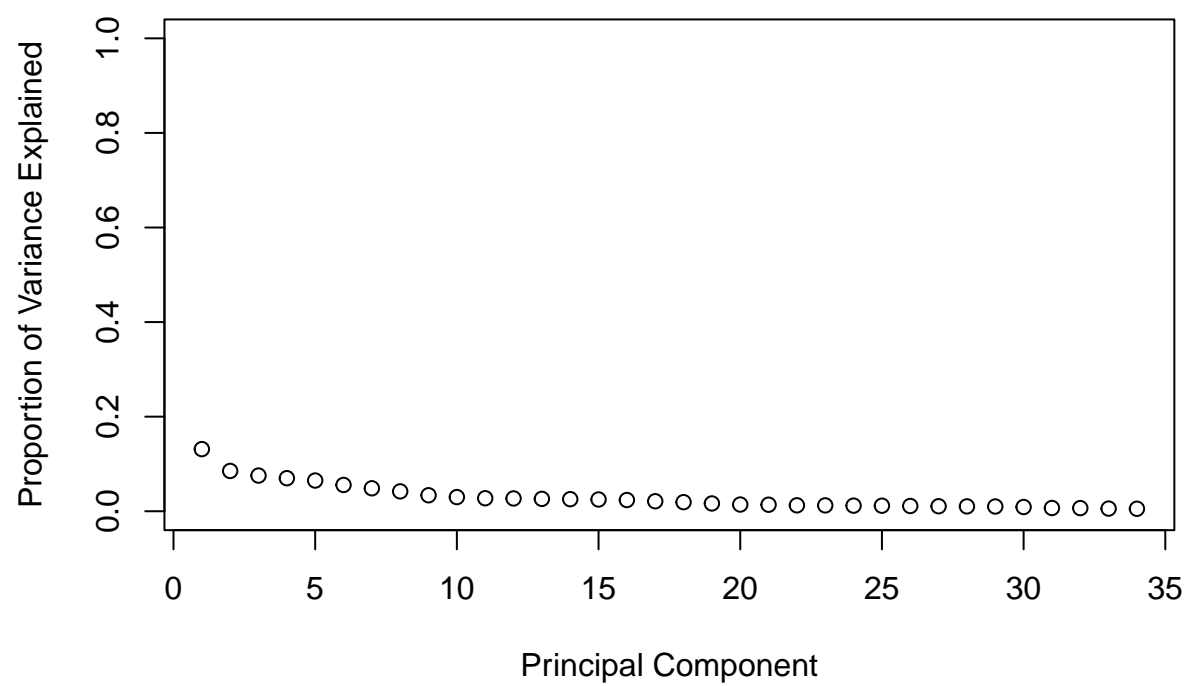
and create a smaller subset of variables.

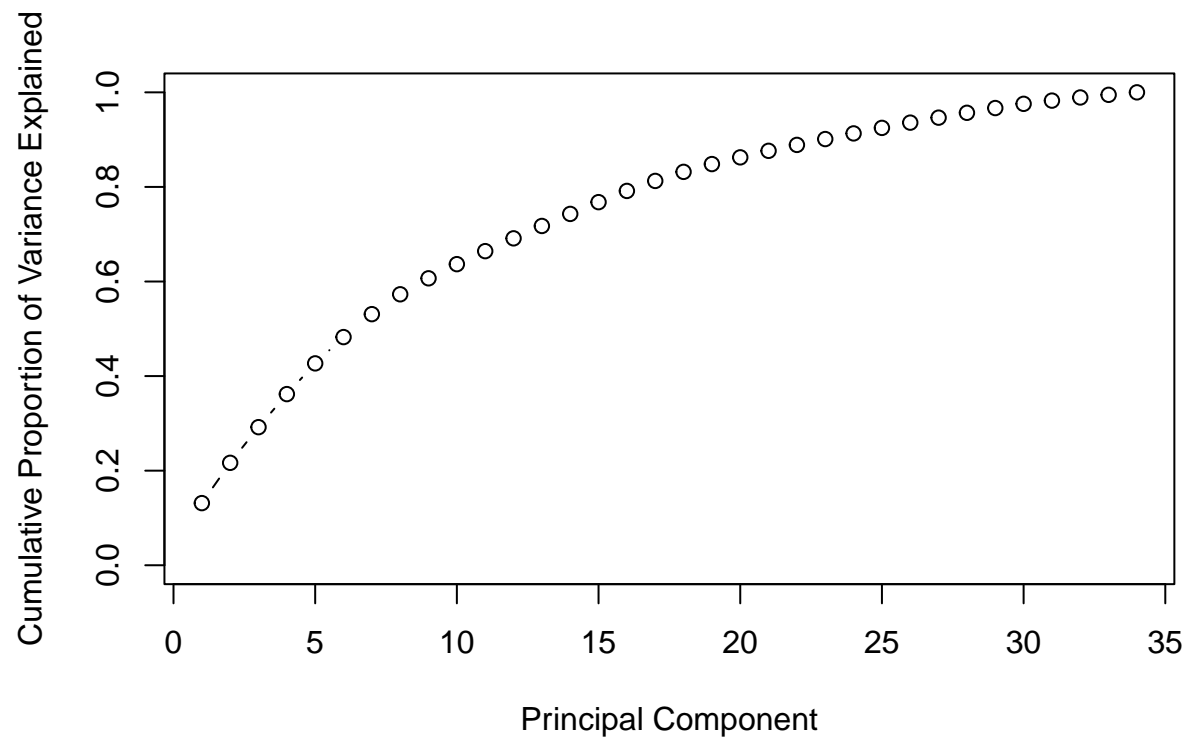


Principal Component Analysis

Importance of components:

	PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8
## Standard deviation	2.113	1.7020	1.6012	1.5416	1.486	1.3750	1.2845	1.195
## Proportion of Variance	0.131	0.0852	0.0754	0.0699	0.065	0.0556	0.0485	0.042
## Cumulative Proportion	0.131	0.2166	0.2920	0.3619	0.427	0.4824	0.5310	0.573
	PC9	PC10	PC11	PC12	PC13	PC14	PC15	PC16
## Standard deviation	1.0716	1.009	0.9670	0.9593	0.9433	0.9314	0.9193	0.8984
## Proportion of Variance	0.0338	0.030	0.0275	0.0271	0.0262	0.0255	0.0249	0.0237
## Cumulative Proportion	0.6067	0.637	0.6642	0.6913	0.7174	0.7429	0.7678	0.7915
	PC17	PC18	PC19	PC20	PC21	PC22	PC23	PC24
## Standard deviation	0.8479	0.8076	0.7481	0.6950	0.6851	0.6524	0.6490	0.6361
## Proportion of Variance	0.0211	0.0192	0.0165	0.0142	0.0138	0.0125	0.0124	0.0119
## Cumulative Proportion	0.8127	0.8319	0.8483	0.8625	0.8763	0.8889	0.9012	0.9132
	PC25	PC26	PC27	PC28	PC29	PC30	PC31	
## Standard deviation	0.6314	0.6145	0.5979	0.5905	0.584	0.55084	0.48213	
## Proportion of Variance	0.0117	0.0111	0.0105	0.0103	0.010	0.00892	0.00684	
## Cumulative Proportion	0.9249	0.9360	0.9465	0.9567	0.967	0.97570	0.98254	
	PC32	PC33	PC34					
## Standard deviation	0.47489	0.43661	0.42132					
## Proportion of Variance	0.00663	0.00561	0.00522					
## Cumulative Proportion	0.98917	0.99478	1.00000					





```
## $loadings
##
## Loadings:
##          PC1    PC2    PC3    PC4    PC5    PC6
## chatter                    -0.555
## current_events              -0.197
## travel                     0.486
## photo_sharing             -0.180
## uncategorized             -0.125
## tv_film                   -0.274
## sports_fandom             0.434
## politics                  0.559
## food                     0.380
## family                   0.325
## home_and_garden
## music                   -0.131
## news                    0.411
## online_gaming            -0.527
## shopping                 -0.535
## health_nutrition         0.579
## college_uni              -0.568
## sports_playing           -0.444
## cooking                 -0.553
## eco                     0.199
## computers                0.442
## business                0.115
```

```

## outdoors                0.495
## crafts                   0.152                -0.107
## automotive              0.205                -0.103
## art                     -0.212
## religion                0.446
## beauty                  -0.538
## parenting              0.430
## dating
## school                 0.361
## personal_fitness        0.563
## fashion                 -0.551
## small_business          -0.132 -0.135
##
##          PC1  PC2  PC3  PC4  PC5  PC6
## SS loadings  1.000 1.000 1.000 1.000 1.000 1.000
## Proportion Var 0.029 0.029 0.029 0.029 0.029 0.029
## Cumulative Var 0.029 0.059 0.088 0.118 0.147 0.176
##
## $rotmat
##      [,1] [,2] [,3] [,4] [,5] [,6]
## [1,] 0.71630 -0.3661 0.293277 0.2622 -0.27490 -0.3501
## [2,] 0.65715 0.5184 -0.006587 -0.2251 0.25277 0.4299
## [3,] -0.19764 0.2958 0.855499 -0.3238 -0.14407 -0.1264
## [4,] -0.11015 0.1578 0.322297 0.8153 0.40637 0.1711
## [5,] 0.05910 -0.2564 0.068959 -0.2909 0.81865 -0.4138
## [6,] -0.01935 -0.6474 0.270992 -0.1626 0.06684 0.6900

```

From the above PC summary, we can see that some PC have attributes that could fit in to the description of a specific segment such as PC1 which corresponds to an mid-aged population who have kids and are more traditional, and PC4 which corresponds to a population that is more health focused. With these information, we can compare and contrast with our clustering models later.

Welcome! Want to learn more? See two factoextra-related books at <https://goo.gl/ve3WBa>

```

##
## Call:
## PCA(X = tweets_scale, scale.unit = FALSE, ncp = 10, graph = F)
##
##
## Eigenvalues
##          Dim.1  Dim.2  Dim.3  Dim.4  Dim.5  Dim.6  Dim.7
## Variance      4.466  2.896  2.564  2.376  2.208  1.890  1.650
## % of var.     13.137  8.520  7.541  6.990  6.496  5.560  4.853
## Cumulative % of var. 13.137 21.657 29.198 36.188 42.684 48.244 53.097
##          Dim.8  Dim.9  Dim.10 Dim.11 Dim.12 Dim.13 Dim.14
## Variance      1.428  1.148  1.018  0.935  0.920  0.890  0.867
## % of var.      4.200  3.377  2.995  2.750  2.706  2.617  2.552
## Cumulative % of var. 57.297 60.674 63.669 66.419 69.126 71.743 74.295
##          Dim.15 Dim.16 Dim.17 Dim.18 Dim.19 Dim.20 Dim.21
## Variance      0.845  0.807  0.719  0.652  0.560  0.483  0.469
## % of var.      2.486  2.374  2.114  1.918  1.646  1.421  1.380
## Cumulative % of var. 76.781 79.155 81.269 83.187 84.834 86.254 87.634
##          Dim.22 Dim.23 Dim.24 Dim.25 Dim.26 Dim.27 Dim.28

```

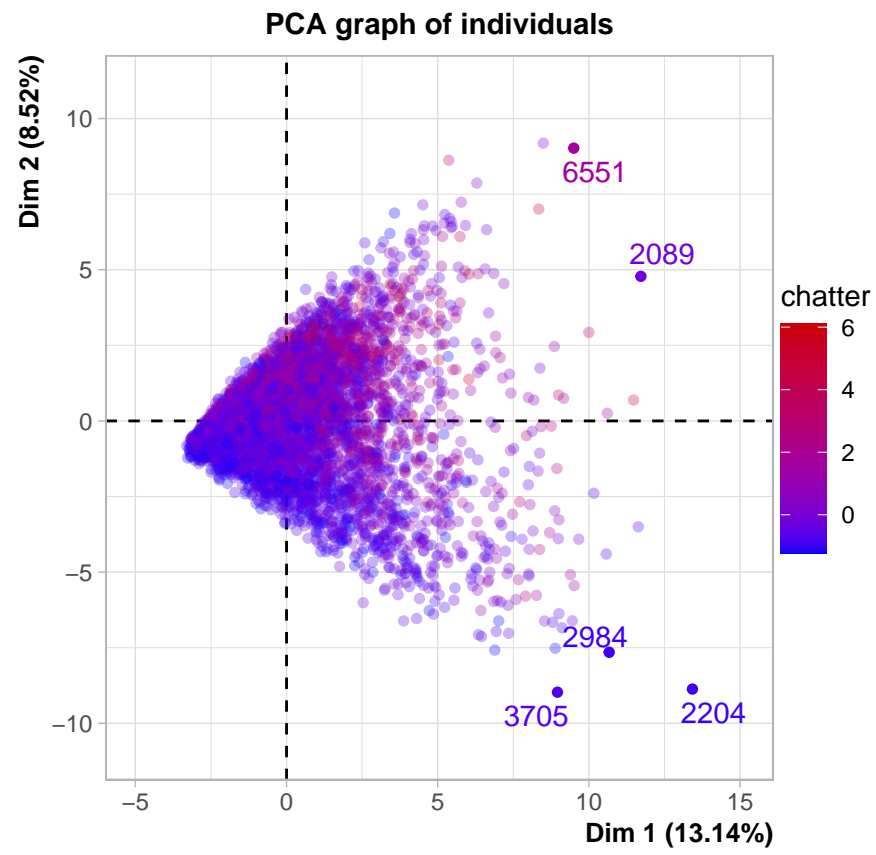
```

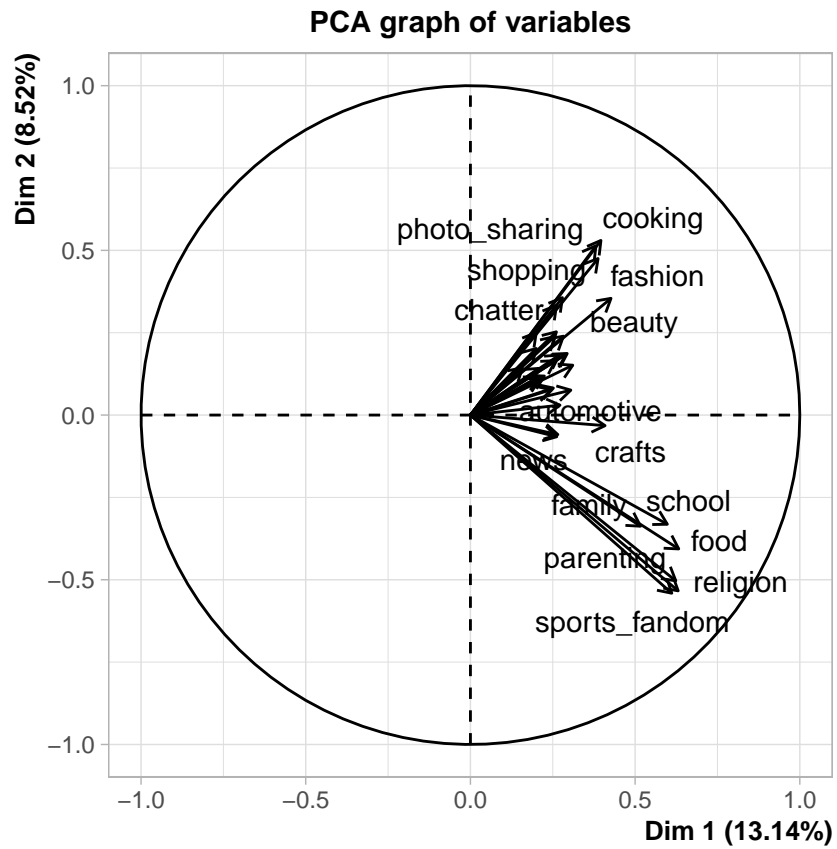
## Variance          0.426  0.421  0.405  0.399  0.378  0.357  0.349
## % of var.         1.252  1.239  1.190  1.173  1.111  1.051  1.026
## Cumulative % of var. 88.886 90.125 91.315 92.488 93.598 94.649 95.675
##                   Dim.29 Dim.30 Dim.31 Dim.32 Dim.33 Dim.34
## Variance          0.341  0.303  0.232  0.225  0.191  0.177
## % of var.         1.003  0.892  0.684  0.663  0.561  0.522
## Cumulative % of var. 96.678 97.570 98.254 98.917 99.478 100.000
##
## Individuals (the 10 first)
##                   Dist    Dim.1    ctr    cos2    Dim.2    ctr    cos2
## 1 | 6.659 | 1.197 0.004 0.032 | 0.811 0.003 0.015 |
## 2 | 4.762 | 0.406 0.001 0.007 | -1.994 0.019 0.175 |
## 3 | 6.177 | 0.193 0.000 0.001 | 1.207 0.007 0.038 |
## 4 | 5.300 | -1.393 0.006 0.069 | -0.314 0.000 0.004 |
## 5 | 3.515 | -1.603 0.008 0.208 | 0.762 0.003 0.047 |
## 6 | 4.343 | -0.701 0.002 0.026 | 0.623 0.002 0.021 |
## 7 | 6.033 | -0.713 0.002 0.014 | -0.046 0.000 0.000 |
## 8 | 5.549 | 0.526 0.001 0.009 | 2.865 0.039 0.267 |
## 9 | 8.205 | 2.127 0.014 0.067 | 2.905 0.040 0.125 |
## 10 | 9.407 | 5.779 0.102 0.377 | -4.345 0.089 0.213 |
##                   Dim.3    ctr    cos2
## 1 -2.413 0.031 0.131 |
## 2 -0.190 0.000 0.002 |
## 3 0.907 0.004 0.022 |
## 4 0.273 0.000 0.003 |
## 5 0.303 0.000 0.007 |
## 6 0.624 0.002 0.021 |
## 7 3.350 0.060 0.308 |
## 8 -0.947 0.005 0.029 |
## 9 -3.510 0.066 0.183 |
## 10 -0.616 0.002 0.004 |
##
## Variables (the 10 first)
##                   Dim.1    ctr    cos2    Dim.2    ctr    cos2    Dim.3    ctr
## chatter | 0.261 1.529 0.068 | 0.333 3.828 0.111 | 0.115 0.515
## current_events | 0.205 0.941 0.042 | 0.115 0.458 0.013 | 0.077 0.233
## travel | 0.252 1.421 0.063 | 0.082 0.233 0.007 | 0.683 18.213
## photo_sharing | 0.381 3.252 0.145 | 0.514 9.121 0.264 | -0.027 0.029
## uncategorized | 0.200 0.894 0.040 | 0.250 2.165 0.063 | -0.057 0.126
## tv_film | 0.208 0.973 0.043 | 0.142 0.694 0.020 | 0.130 0.662
## sports_fandom | 0.611 8.367 0.374 | -0.541 10.098 0.293 | -0.080 0.247
## politics | 0.272 1.656 0.074 | 0.030 0.031 0.001 | 0.792 24.445
## food | 0.632 8.957 0.400 | -0.406 5.703 0.165 | -0.168 1.095
## family | 0.516 5.971 0.267 | -0.337 3.930 0.114 | -0.077 0.234
##                   cos2
## chatter 0.013 |
## current_events 0.006 |
## travel 0.467 |
## photo_sharing 0.001 |
## uncategorized 0.003 |
## tv_film 0.017 |
## sports_fandom 0.006 |
## politics 0.627 |
## food 0.028 |

```

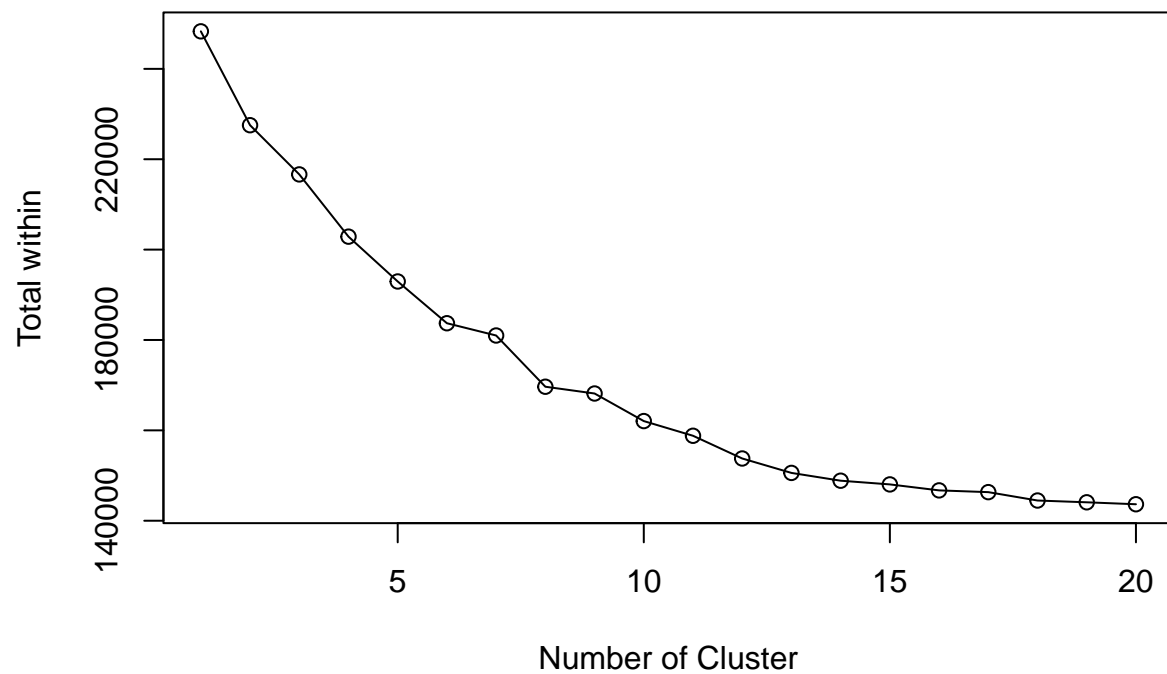
family

0.006 |



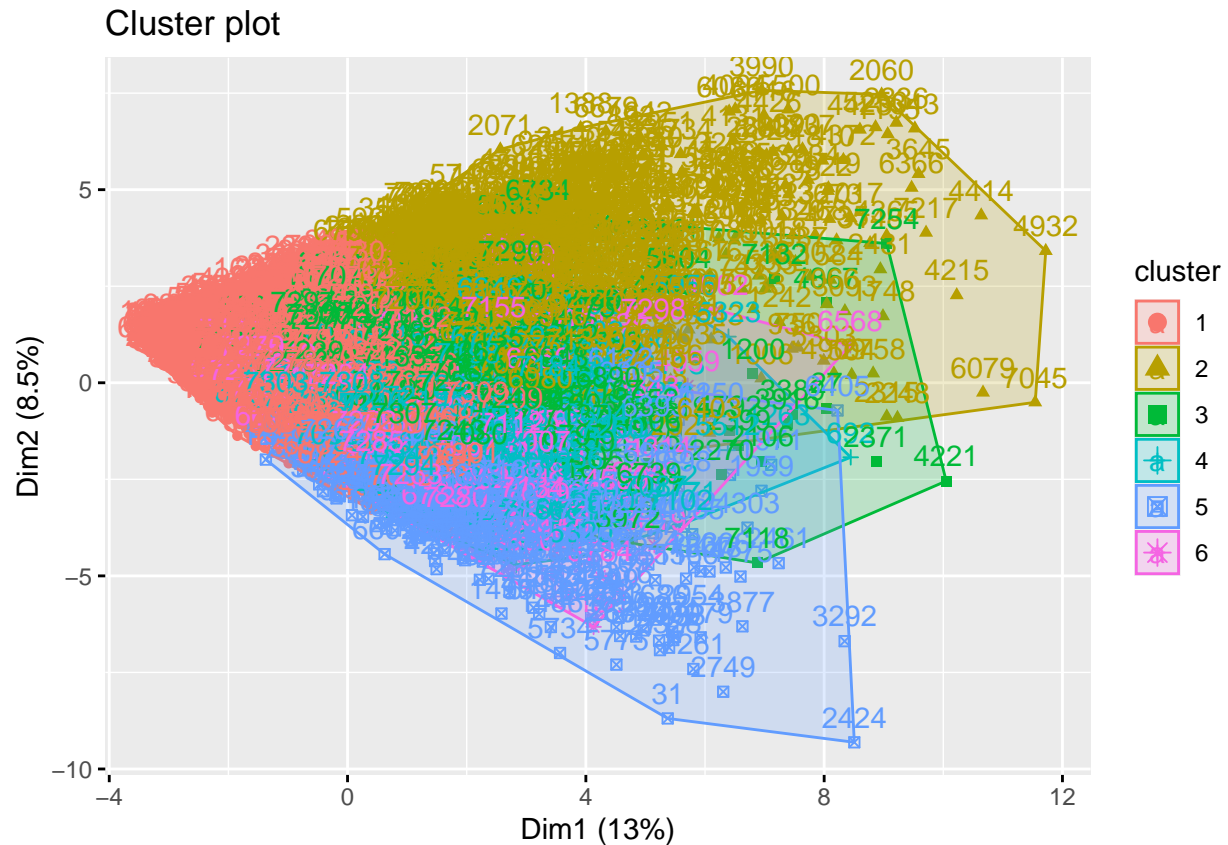


Identifying number of clusters we should generate.



From above figure, we can choose 6 or 10 clusters.

First, we will do a 6 cluster analysis.



```
## [1] "Cluster Breakdown"

##
##      1      2      3      4      5      6
## 0.57 0.10 0.09 0.11 0.07 0.05

## # A tibble: 6 x 2
##   cluster1 count
##     <int> <int>
## 1         1  4171
## 2         2   724
## 3         3   655
## 4         4   827
## 5         5   534
## 6         6   393
```

The biggest cluster is cluster #1, which account for around 57% out of 6 six clusters.

Clusters Profiling

Non-scaled clusters The characteristic summary of NutrientH20's Twitter followers in the same cluster are as follows (not scaled):

Cluster 1: Highest photo_sharing Cluster 2: Highest photo_sharing, sports_fandom, food, religion, parenting Cluster 3: Highest travel, politics, news, photo_sharing, computers Cluster 4: Highest

health_nutrition(10 points higher than 5), personal_fitness, cooking, outdoors, photo_sharing Cluster 5: Highest photo_sharing(highest among clusters), cooking (7 points higher than cluster 4),beauty, fashion,health_nutrition Cluster 6: Highest college_uni, online_gaming, photo_sharing,sports_playing

```
## [1] "The mean for all the values in the cluster is 1.62458623379831"
```

##	1	2	3	4	5	6
## chatter	4.3361	4.3052	4.5573	4.3615	4.8258	4.4020
## current_events	1.4407	1.6644	1.6504	1.5381	1.7697	1.4962
## travel	1.0741	1.2831	5.6076	1.2213	1.4700	1.5522
## photo_sharing	2.3143	2.6630	2.5313	2.7013	6.0393	2.8041
## uncategorized	0.7183	0.7652	0.7603	0.9420	1.2547	0.9186
## tv_film	1.0110	1.0967	1.2092	0.9915	1.1049	1.7379
## sports_fandom	0.9588	5.8191	2.0290	1.1536	1.1086	1.3104
## politics	1.0209	1.1119	8.9695	1.2539	1.3839	1.2799
## food	0.7475	4.4903	1.4595	2.1040	1.0206	1.2265
## family	0.5627	2.4406	0.9252	0.7497	0.8727	1.0534
## home_and_garden	0.4313	0.6506	0.6137	0.6191	0.6105	0.6183
## music	0.5730	0.7307	0.6473	0.7279	1.2959	0.9440
## news	0.6857	1.0138	5.3328	1.1137	1.0225	0.8015
## online_gaming	0.5766	1.0000	0.8260	0.8368	1.1049	9.7226
## shopping	1.2949	1.4959	1.3725	1.5042	2.0468	1.3333
## health_nutrition	1.1005	1.8605	1.6534	12.0169	2.2266	1.7455
## college_uni	0.9187	1.2251	1.3237	0.9407	1.5843	10.7277
## sports_playing	0.4263	0.7417	0.6427	0.5852	0.8202	2.6565
## cooking	0.8619	1.6229	1.2595	3.3071	10.7322	1.4758
## eco	0.3707	0.6436	0.5863	0.9214	0.5581	0.4962
## computers	0.3618	0.7058	2.4656	0.5659	0.7041	0.5598
## business	0.3390	0.4903	0.6748	0.4776	0.6142	0.4224
## outdoors	0.3862	0.6865	0.9053	2.7074	0.7753	0.6336
## crafts	0.3553	1.0608	0.6260	0.6034	0.6273	0.5903
## automotive	0.5649	1.0290	2.3603	0.6312	0.8558	0.8575
## art	0.6035	0.8605	0.7130	0.7545	0.9382	1.2239
## religion	0.5195	5.1464	1.0366	0.7328	0.8296	0.8244
## beauty	0.3452	1.0898	0.4656	0.4281	3.8652	0.4300
## parenting	0.4402	4.0000	0.9420	0.7424	0.7397	0.6641
## dating	0.5404	0.8481	1.0687	1.0242	0.9139	0.7430
## school	0.4625	2.6464	0.7313	0.5683	0.9850	0.4936
## personal_fitness	0.6521	1.1809	1.0107	6.4619	1.3315	0.9822
## fashion	0.5145	1.0428	0.6672	0.7799	5.5356	0.8855
## small_business	0.2647	0.3895	0.4824	0.2902	0.4925	0.4504

The above cluster is not scaled so we can find a lot of repetition of attributes between clusters, specifically photo_sharing which is present in all clusters most likely because photo_sharing is one of the most common attributes for tweets. Although still descriptive, some details might be left out. Next we will take a look at scaled clusters.

Scaled clusters The characteristic summary of NutrientH20's Twitter followers in the same cluster are as follows (scaled):

Cluster 1: Highest food, personal_fitness, out_doors, cooking, health_nutrition Cluster 2: Highest sports_fandom, food, school, religion, parenting Cluster 3: Highest travel, politics, news, automotive, computers Cluster 4: Highest health_nutrition(higher than 1), personal_fitness(higher than 1), outdoors(higher

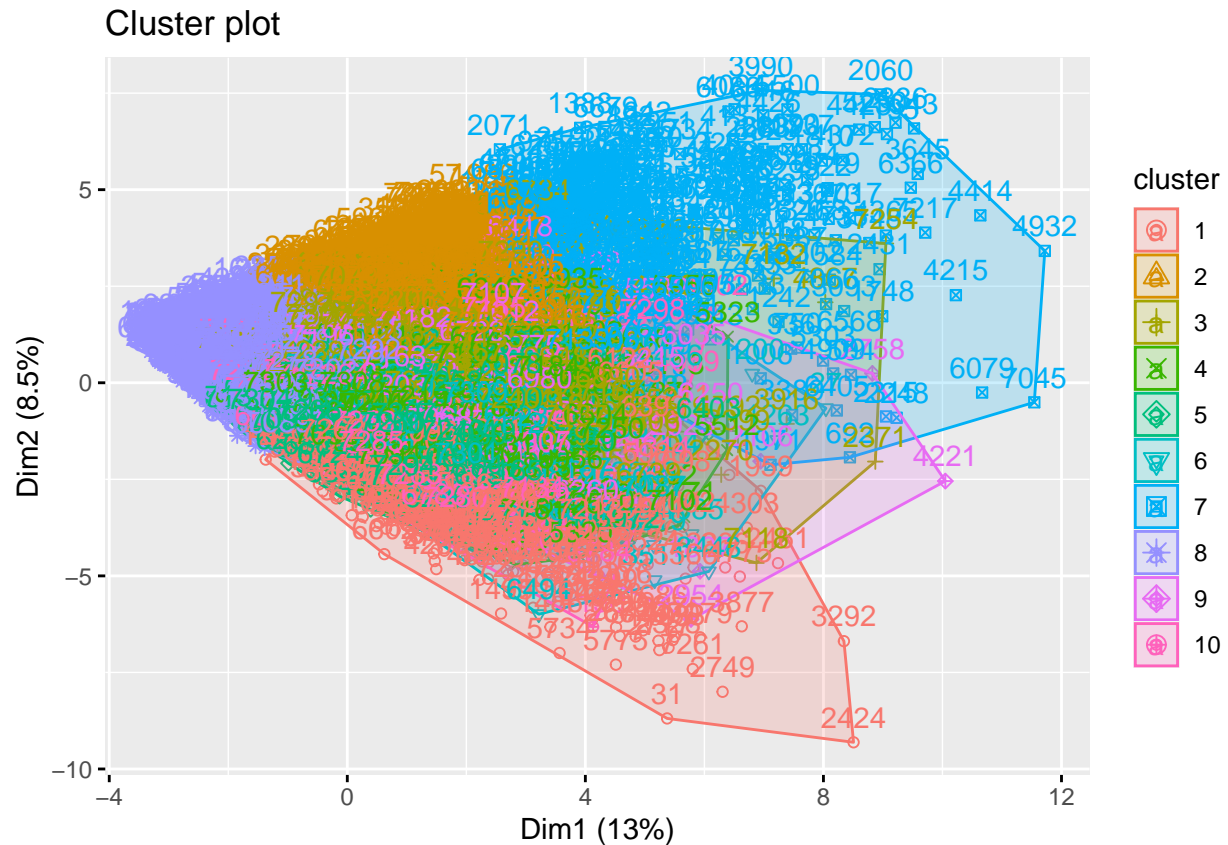
than 1), eco, food(higher than 1 lower than 2) Cluster 5: Highest photo_sharing, cooking (higher than cluster 1), beauty, fashion, music Cluster 6: Highest college_uni, online_gaming, art,sports_playing,tv_film

```
## [1] "The mean for all the values in the cluster is 0.28608804493521"
```

##	1	2	3	4	5	6
## chatter	-0.01666	-0.025385	0.0457914	-0.009484	0.121653	0.001952
## current_events	-0.06230	0.114003	0.1029825	0.014481	0.196992	-0.018546
## travel	-0.21664	-0.125803	1.7530823	-0.152683	-0.044604	-0.008923
## photo_sharing	-0.14508	-0.017510	-0.0656900	-0.003481	1.217785	0.034109
## uncategorized	-0.08980	-0.039501	-0.0447432	0.150069	0.485446	0.124992
## tv_film	-0.04186	0.009346	0.0765829	-0.053512	0.014238	0.392669
## sports_fandom	-0.29209	1.962482	0.2043666	-0.201729	-0.222582	-0.128963
## politics	-0.25875	-0.228892	2.3489996	-0.182288	-0.139650	-0.173769
## food	-0.36053	1.767278	0.0442489	0.410623	-0.205294	-0.088258
## family	-0.25859	1.422324	0.0658814	-0.091202	0.018861	0.180672
## home_and_garden	-0.11297	0.187178	0.1367814	0.144126	0.132327	0.143052
## music	-0.10846	0.043337	-0.0368978	0.040708	0.587527	0.248757
## news	-0.24925	-0.094523	1.9420929	-0.047439	-0.090440	-0.194626
## online_gaming	-0.23227	-0.074801	-0.1395308	-0.135512	-0.035798	3.169283
## shopping	-0.05913	0.051280	-0.0164822	0.055881	0.353979	-0.038011
## health_nutrition	-0.32802	-0.159339	-0.2052930	2.094727	-0.078090	-0.184850
## college_uni	-0.22030	-0.115747	-0.0821276	-0.212788	0.006798	3.126782
## sports_playing	-0.22184	0.099918	-0.0010290	-0.059681	0.180002	2.053039
## cooking	-0.33517	-0.111933	-0.2185262	0.382100	2.560121	-0.155083
## eco	-0.17050	0.189734	0.1140072	0.556256	0.076786	-0.004856
## computers	-0.24040	0.053325	1.5559028	-0.066124	0.051889	-0.071336
## business	-0.12366	0.095416	0.3624940	0.077028	0.274794	-0.002943
## outdoors	-0.31748	-0.067226	0.1152212	1.617305	0.006808	-0.111301
## crafts	-0.18996	0.675606	0.1421077	0.114418	0.143809	0.098400
## automotive	-0.18380	0.155345	1.1280980	-0.135325	0.028791	0.030034
## art	-0.06835	0.090984	-0.0004596	0.025301	0.139151	0.316258
## religion	-0.30080	2.148517	-0.0270607	-0.187921	-0.136668	-0.139400
## beauty	-0.26893	0.293701	-0.1779437	-0.206354	2.391017	-0.204864
## parenting	-0.30908	2.051873	0.0237228	-0.108618	-0.110437	-0.160562
## dating	-0.09538	0.076378	0.1995532	0.174700	0.113108	0.017724
## school	-0.24861	1.607968	-0.0200891	-0.158639	0.195602	-0.222126
## personal_fitness	-0.33473	-0.116148	-0.1865197	2.066681	-0.053932	-0.198299
## fashion	-0.26417	0.024683	-0.1806957	-0.119050	2.481053	-0.061331
## small_business	-0.10087	0.104060	0.2566533	-0.058970	0.273181	0.204014

With the above two clusters formed based on scaled and non-scaled data, we found that the scaled clusters gives less overlaps of attributes between clusters and generally more informative attributes than the non-scaled one.

Next, we will do a 10 cluster analysis.



```
## [1] "Cluster Breakdown"
```

```
##
##      1      2      3      4      5      6      7      8      9     10
## 0.06 0.09 0.08 0.10 0.12 0.05 0.04 0.39 0.03 0.04
```

```
## # A tibble: 10 x 2
##   cluster2 count
##   <int> <int>
## 1       1   448
## 2       2   648
## 3       3   548
## 4       4   705
## 5       5   867
## 6       6   392
## 7       7   311
## 8       8  2878
## 9       9   186
## 10      10   321
```

The biggest cluster is cluster #8, which account for around 40% out of 10 clusters.

Clusters Profiling

The characteristic summary of NutrientH20's Twitter followers in the same cluster are as follows (without chatter):

Cluster 1: Highest cooking, photo_sharing, fashion, beauty Cluster 2: Highest sports_fandom, religion, food, parenting Cluster 3: Highest politics, travel, news Cluster 4: Highest health_nutrition, personal_nutrition, cooking Cluster 5: Highest photo_sharing, shopping Cluster 6: Highest tv_film, art Cluster 7: Highest sports_fandom, religion, food, parenting Cluster 8: Highest health_nutrition, photo_sharing, current_events, travel Cluster 9: Highest dating, photo_sharing, school Cluster 10: Highest college_uni, online_gaming

##	1	2	3	4	5	6	7	8
## chatter	4.0714	3.4167	4.0967	3.7333	9.8847	3.9515	4.2412	3.1251
## current_events	1.7433	1.4614	1.5967	1.4809	2.0242	1.9490	1.8264	1.2571
## travel	1.4442	0.9306	6.0547	1.2199	1.0923	2.1964	1.5659	1.0274
## photo_sharing	5.8996	1.8256	2.2774	2.3362	6.0900	2.4337	3.0707	1.5757
## uncategorized	1.2366	0.6759	0.6788	0.9149	0.7993	1.4668	0.7492	0.6286
## tv_film	0.8460	0.7099	0.9945	0.8071	0.8420	5.6020	1.1125	0.7224
## sports_fandom	1.0781	3.8611	2.0493	1.1574	1.1338	1.2959	7.6592	0.7568
## politics	1.3862	1.0062	9.5036	1.2610	1.4556	1.6352	1.4051	0.9736
## food	0.9665	2.9691	1.4325	2.1617	0.7774	1.6173	5.8810	0.5924
## family	0.8393	1.7068	0.9033	0.7362	0.8281	0.7066	3.0675	0.4527
## home_and_garden	0.5871	0.5093	0.5602	0.5915	0.5502	0.7551	0.7717	0.3676
## music	1.2567	0.5355	0.6095	0.6667	0.8512	1.7066	0.9132	0.4451
## news	1.0513	0.8565	5.4635	1.1957	0.7451	1.3112	1.3087	0.6894
## online_gaming	1.1719	0.6682	0.8321	0.8837	0.7451	0.7066	1.4502	0.5844
## shopping	1.7388	0.9398	1.1807	1.2638	4.2330	1.4031	1.6302	0.6953
## health_nutrition	2.1920	1.2284	1.5383	12.6582	1.5998	1.8724	2.6141	1.1689
## college_uni	1.5424	0.7978	1.2682	0.9007	1.2491	2.5918	1.5949	0.8287
## sports_playing	0.8147	0.4846	0.6077	0.5872	0.5721	0.7577	0.9035	0.3902
## cooking	11.5179	0.9676	1.2500	3.4511	1.2203	1.4796	2.4920	0.8846
## eco	0.4955	0.4336	0.5639	0.9376	0.7463	0.5689	0.8199	0.2728
## computers	0.6987	0.4799	2.7026	0.5433	0.5917	0.4872	0.8746	0.3204
## business	0.5647	0.3519	0.6460	0.4454	0.6471	0.6709	0.6077	0.2397
## outdoors	0.7835	0.5216	0.8814	2.8851	0.4787	0.6939	0.8071	0.3860
## crafts	0.5558	0.6590	0.5602	0.5617	0.5294	1.1199	1.3344	0.2467
## automotive	0.8281	0.8580	2.2737	0.6199	1.0854	0.5383	1.3055	0.4868
## art	0.7210	0.4923	0.4197	0.5943	0.3795	4.8903	0.8232	0.3176
## religion	0.7679	3.2886	1.0255	0.7319	0.4983	1.1199	6.7428	0.3471
## beauty	4.1696	0.6682	0.4288	0.4213	0.3818	0.6888	1.5080	0.3138
## parenting	0.7366	2.4043	0.9635	0.7333	0.5352	0.6071	5.3859	0.3134
## dating	0.6094	0.3781	0.8741	0.7816	0.4383	0.4719	0.7395	0.3204
## school	0.8973	1.6235	0.6642	0.4922	0.6840	0.6658	3.4727	0.2915
## personal_fitness	1.3125	0.7145	0.9982	6.7106	1.0784	1.0842	1.6785	0.6550
## fashion	5.8772	0.6327	0.6022	0.7418	0.7209	0.8929	1.3730	0.4309
## small_business	0.4397	0.2701	0.4270	0.2397	0.4083	0.7959	0.4469	0.1970
## cluster1	5.0000	1.6960	2.9909	3.9957	1.5790	2.0842	2.0450	1.0330
##	9	10						
## chatter	7.9624	3.9688						
## current_events	1.5914	1.4081						
## travel	1.6452	1.5607						
## photo_sharing	2.6989	2.6573						
## uncategorized	1.5538	0.7788						
## tv_film	0.9462	1.2960						
## sports_fandom	1.2581	1.2243						
## politics	1.5484	1.2991						
## food	1.0914	1.1869						
## family	0.7366	1.0436						

## home_and_garden	0.9570	0.5826
## music	0.6505	0.6262
## news	1.0108	0.8318
## online_gaming	0.9839	10.8941
## shopping	1.1989	1.1433
## health_nutrition	2.2688	1.7695
## college_uni	1.4301	11.3458
## sports_playing	0.9301	2.8224
## cooking	1.4677	1.5701
## eco	0.6237	0.4735
## computers	0.7151	0.5607
## business	0.7204	0.3551
## outdoors	0.8602	0.5857
## crafts	0.8226	0.5327
## automotive	0.5806	0.8910
## art	0.7097	1.1651
## religion	1.0914	0.6916
## beauty	1.0161	0.3925
## parenting	1.0215	0.6760
## dating	9.2527	0.6511
## school	2.3172	0.4517
## personal_fitness	1.3495	1.0312
## fashion	2.5323	0.8660
## small_business	0.5860	0.3925
## cluster1	2.1720	6.0000

Here we repeat the same process as we did for 6 clusters using non-scaled data and we can see that each cluster became more specific and smaller. This made it more difficult to identify what segment of the market the clusters could be referring to thus we pick 6 clusters as our optimal cluster.

Market Segmentation Analysis

Based on the 6 clusters(scaled), we found that cluster one correspond to a more generalized segment of twitter followers with attributes that you would expect from someone who follows the company and you don't see any outstanding attributes, all of their numbers are close to the mean with nothing above 0.5. From cluster 2, we can see that parenting and religion is the top 2 attributes (above 2) listed along with other attributes that are also significant (above 1), this corresponds to the segment of twitter followers who are mid-aged, have kids, and have a more traditional life style. Cluster 3's top attributes are political, news, travel, automotives, and computers, where political and news takes the lead among these attributes. This segment of followers are likely those who are interested in political topics and what is going on in the world, also might be more interested in the cars and the IT realm. All of these attributes align with upper middle class males who has a more luxurious life style and invest in their hobbies. In cluster 4, we identify attributes such as health_nutrition, personal_fitness, outdoors which appears in cluster 1 but have a higher frequency than cluster 1. Eco was also a significant attribute in this cluster. From these attributes, we can see that this segment of followers are those who are more active in their daily life, more aware of the environment, and lead a healthy lifestyle. From cluster 5, some significant attributes are photo_sharing, cooking(higher than cluster 1), beauty, and fashion, which correlates to the segment of followers that are more active on social media, sharing food contents to audience on a daily basis. This could be a crowd of online influencers such as food bloggers that already have an established audience, which the company could reach out to for endorsement/promotions to gain consumers. Finally, cluster 6 have some interesting attributes such as college_uni, sports_playing, and online_gaming which are significant (above 2) comparing to the mean threshold we used (0.3) along with some attributes like art and tv_film that is only a little above the threshold. This cluster correspond to college students who are interested in sports and gaming, which leans more in

the male college student side but can still be inclusive of female college students as well. Furthermore, our clusters also share similar attributes as the loadings result in our PCA, which show that these segments are most likely true.

Author Attribution

Revisit the Reuters C50 corpus that we explored in class. Your task is to build the best model you can, using any combination of tools you see fit, for predicting the author of an article on the basis of that article's textual content. Describe clearly what models you are using, how you constructed features, and so forth. Yes, this is a supervised learning task, but it potentially draws on a lot of what you know about unsupervised learning, since constructing features for a document might involve dimensionality reduction.

In the C50train directory, you have 50 articles from each of 50 different authors (one author per directory). Use this training data (and this data alone) to build the model. Then apply your model to predict the authorship of the articles in the C50test directory, which is about the same size as the training set. Describe your data pre-processing and analysis pipeline in detail.

In this section, we are processing the training data to eliminate stop words, removing punctuation, make terms lowercase and more. The end result is a document term matrix with tf-idf weights with 801 terms.

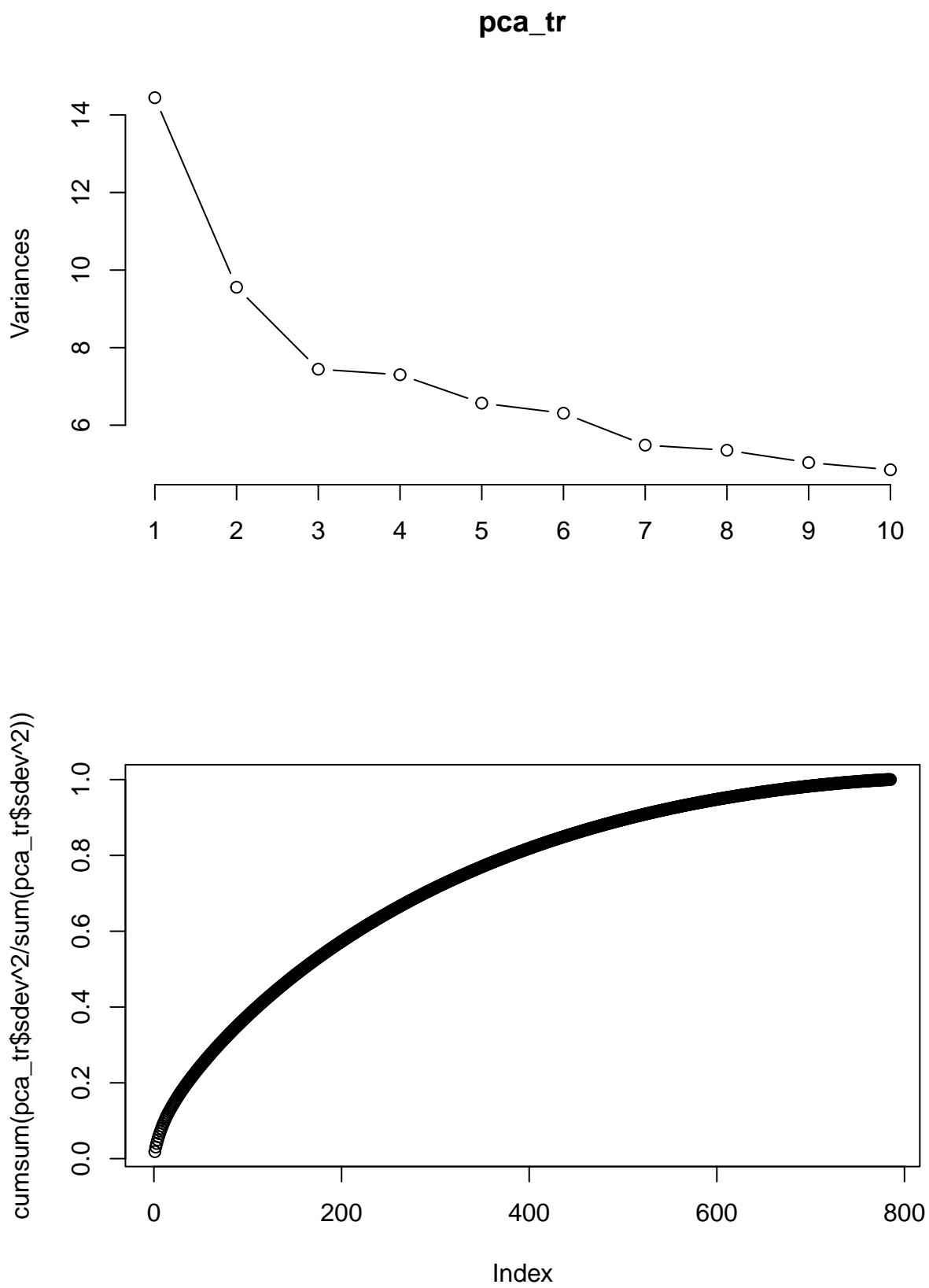
```
## <<DocumentTermMatrix (documents: 2500, terms: 801)>>
## Non-/sparse entries: 240686/1761814
## Sparsity           : 88%
## Maximal term length: 18
## Weighting          : term frequency - inverse document frequency (normalized) (tf-idf)
```

In this section, we do the same processing step we did for the training set to the testing set.

Here we are getting rid of all the words that are in the testing set but not in the training set to make the two matrix the same length.

```
## <<DocumentTermMatrix (documents: 2500, terms: 801)>>
## Non-/sparse entries: 241658/1760842
## Sparsity           : 88%
## Maximal term length: 18
## Weighting          : term frequency - inverse document frequency (normalized) (tf-idf)
```

Principal Component Analysis



##	Standard deviation	Proportion of Variance	Cumulative Proportion
##	1.21607	0.00188	0.50074

In this section, we are trying to reduce the dimensions using PCA. We found that at PC159, around 50% of the variance is explained, therefore we use that as a cutoff for the number of features(PC) we pass in to our model.

Naive-Bayes

```
## Accuracy
## 0.0192
```

Random Forest

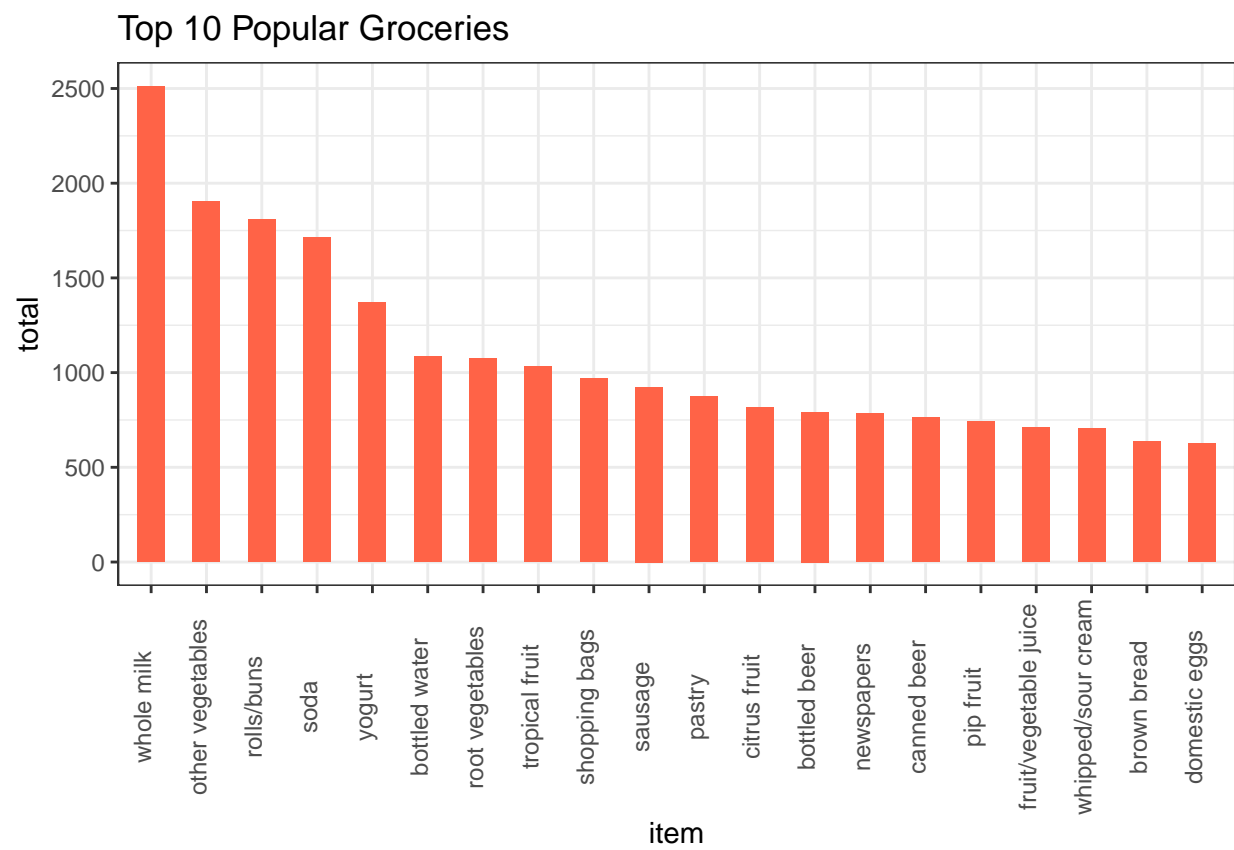
```
## Accuracy
## 0.7456
```

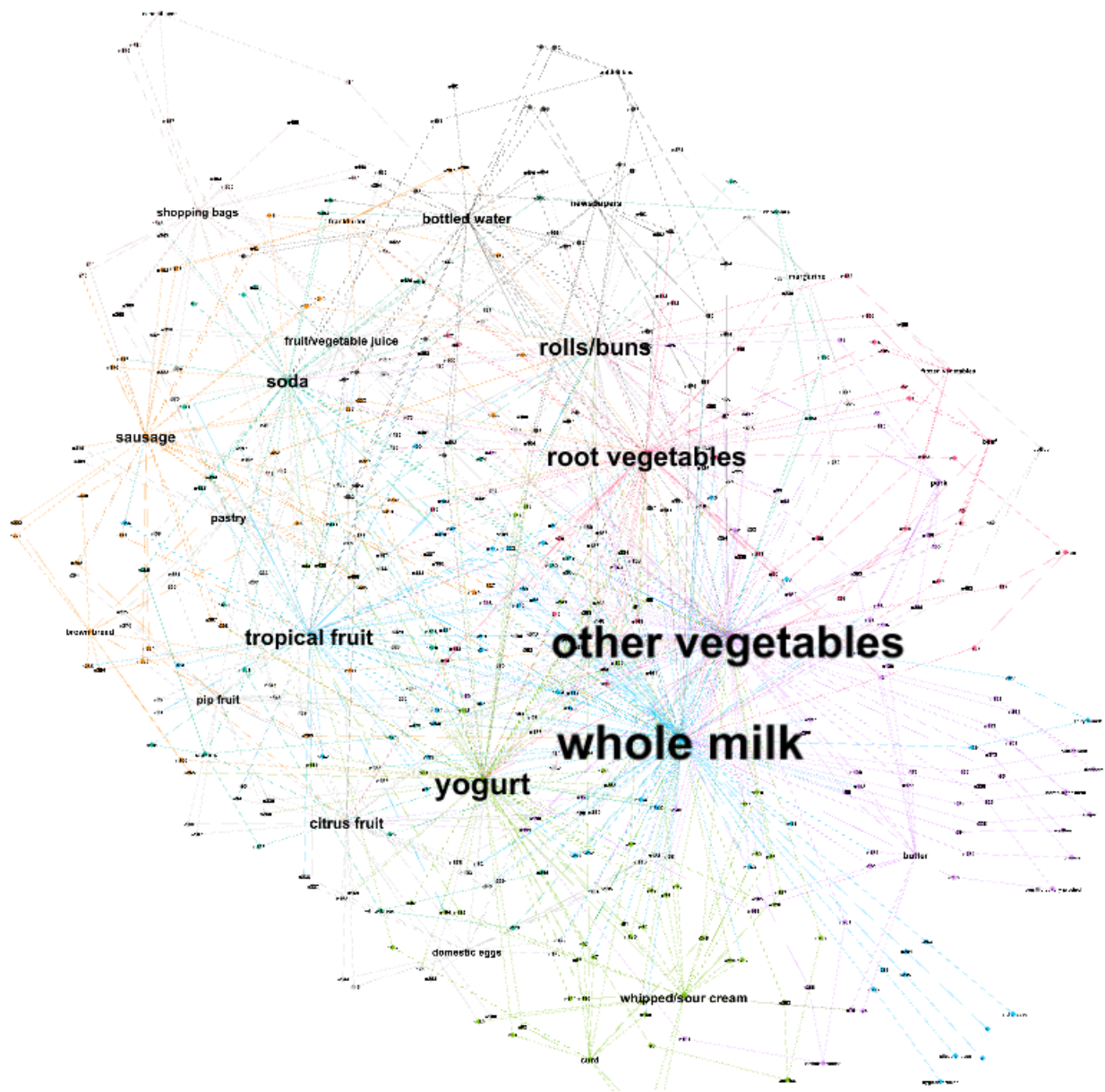
In this section, we tried different kinds of model for classifying the documents. The random forest model had the highest accuracy which is around 75%

Association Rule Mining

Use the data on grocery purchases and find some interesting association rules for these shopping baskets. Pick your own thresholds for lift and confidence; just be clear what these thresholds are and how you picked them. Do your discovered item sets make sense? Present your discoveries in an interesting and concise way.

Exploratory Analysis

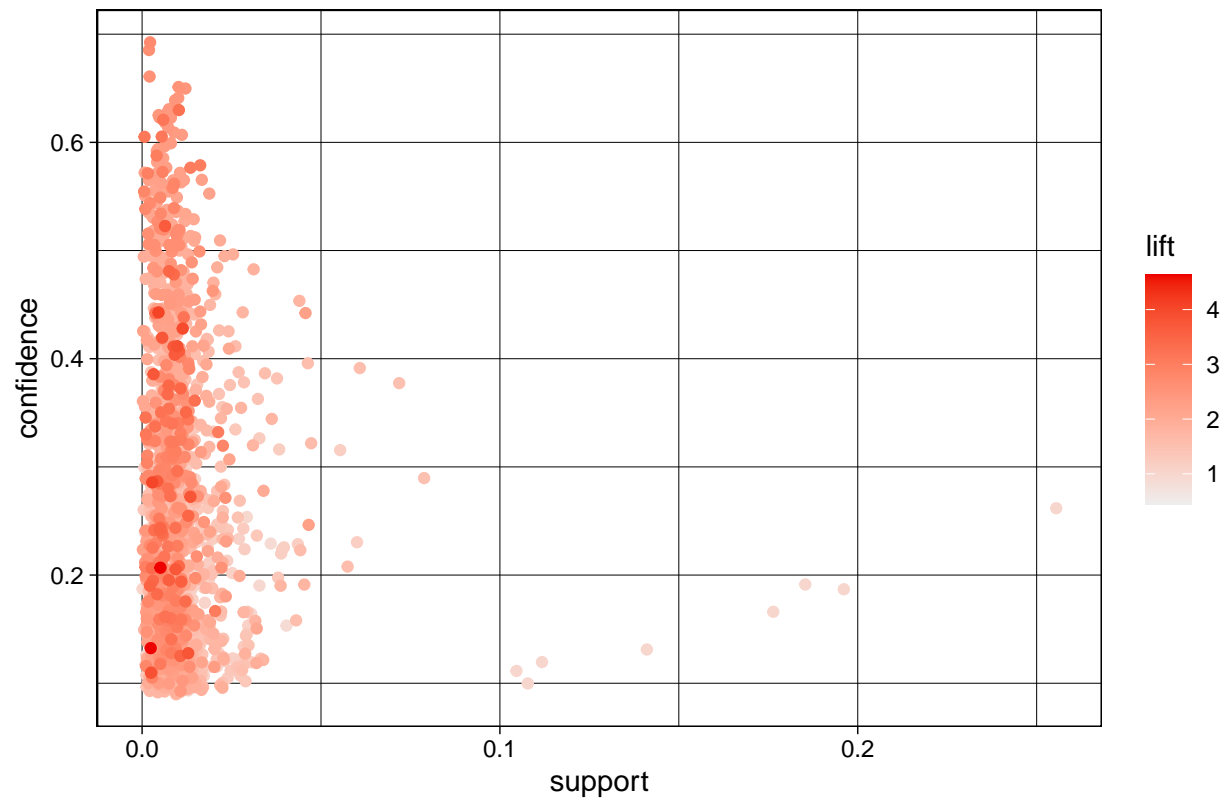




Whole Milk was by far the most popular grocery with a count near 2500.

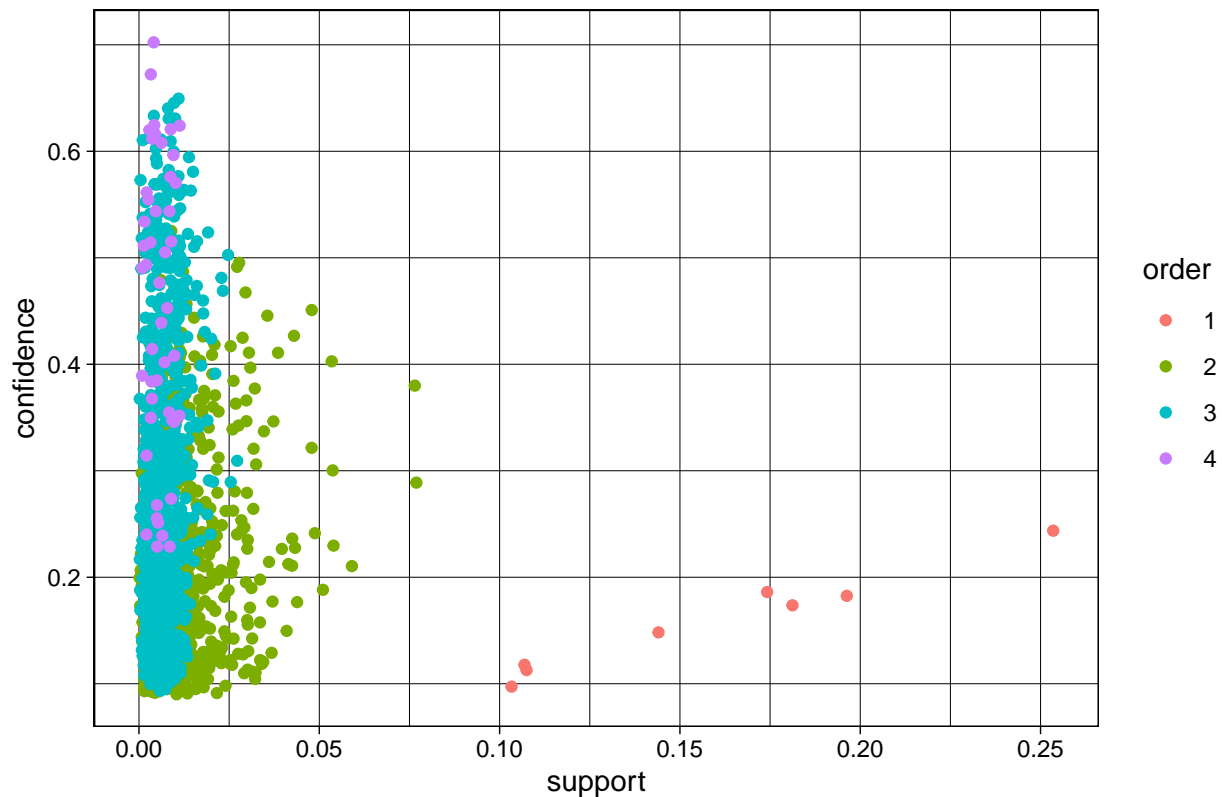
To reduce overplotting, jitter is added! Use jitter = 0 to prevent jitter.

Scatter plot for 1582 rules



To reduce overplotting, jitter is added! Use jitter = 0 to prevent jitter.

Scatter plot for 1582 rules

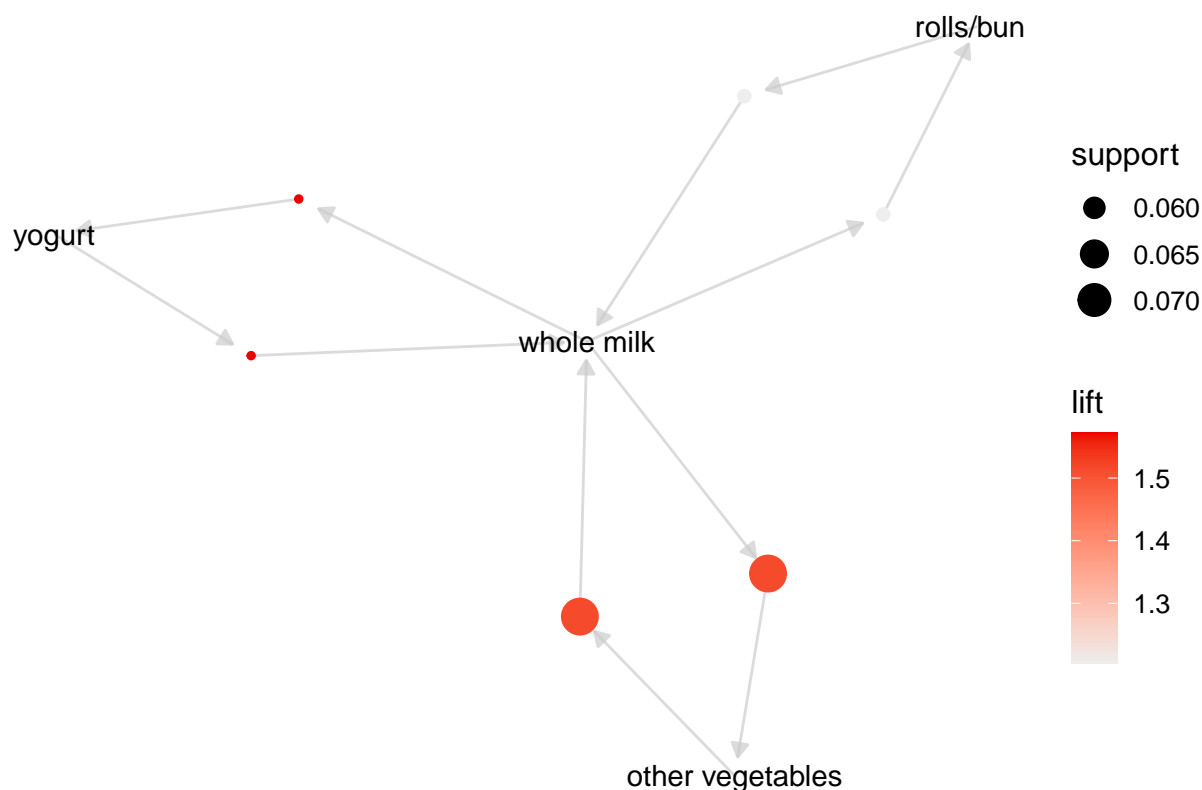


From this scatter plot, we can see that the large majority of rules have support values less than 0.025 but a varying confidence. There also is a slight correlation that the larger lifts have lower confidences. We can see that the size of the rules are clustered in a way that lower support valued rules have larger rule sizes.

Networks

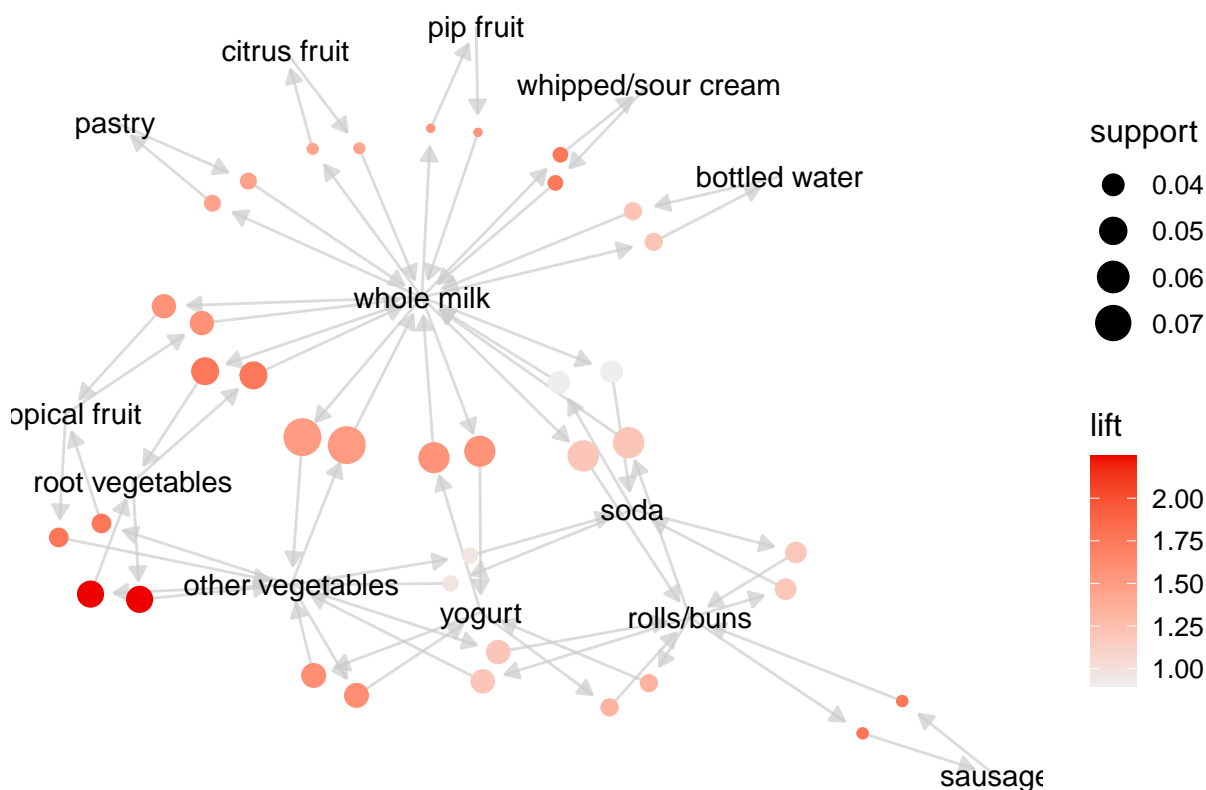
We only have 6 rules due to the using a support of .05 and confidence threshold of .1.

##	lhs	rhs	support	confidence	coverage	lift
## [1]	{yogurt}	=> {whole milk}	0.05602	0.4016	0.1395	1.572
## [2]	{whole milk}	=> {yogurt}	0.05602	0.2193	0.2555	1.572
## [3]	{rolls/buns}	=> {whole milk}	0.05663	0.3079	0.1839	1.205
## [4]	{whole milk}	=> {rolls/buns}	0.05663	0.2216	0.2555	1.205
## [5]	{other vegetables}	=> {whole milk}	0.07483	0.3868	0.1935	1.514
## [6]	{whole milk}	=> {other vegetables}	0.07483	0.2929	0.2555	1.514
##	count					
## [1]	551					
## [2]	551					
## [3]	557					
## [4]	557					
## [5]	736					
## [6]	736					



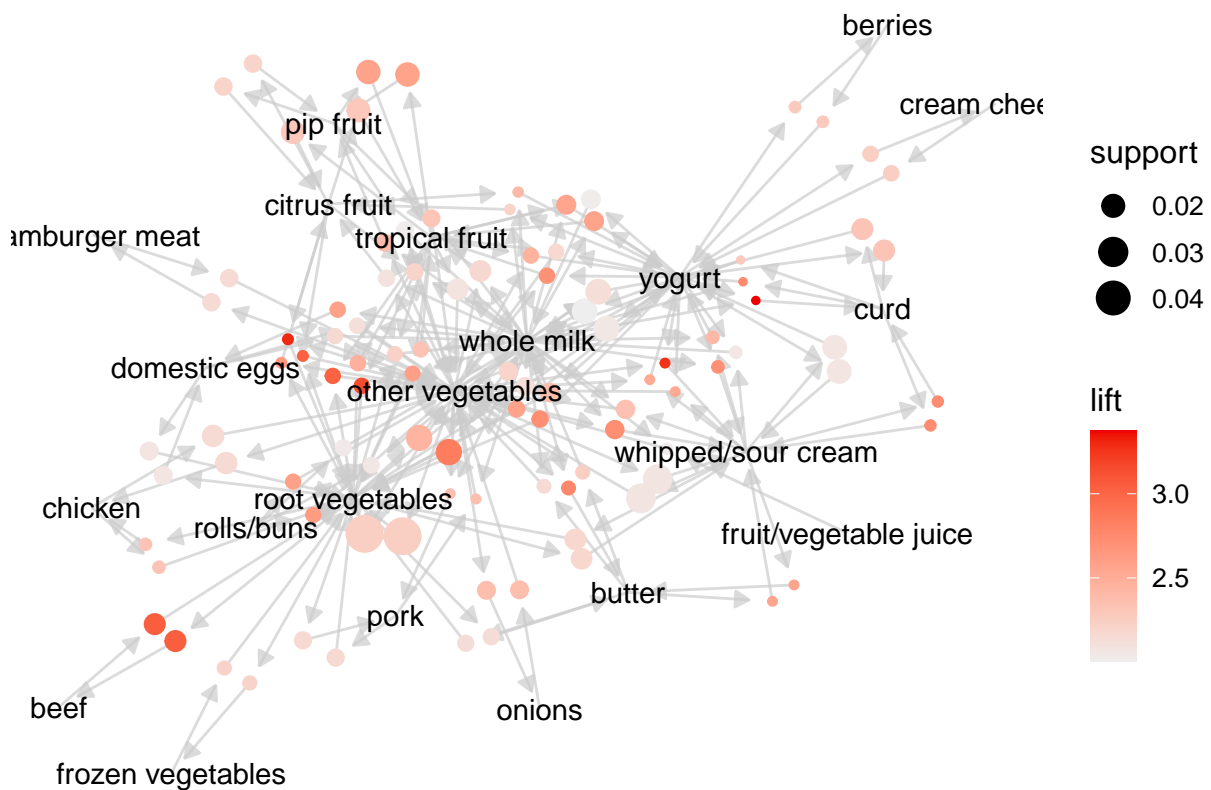
Now, we have 38 rules when using a support of .03 and confidence threshold of .05. Due to the size of the rules, we are only including the first 10 rules in our output.

##	lhs	rhs	support	confidence	coverage
## [1]	{whipped/sour cream}	=> {whole milk}	0.03223	0.4496	0.07168
## [2]	{whole milk}	=> {whipped/sour cream}	0.03223	0.1261	0.25552
## [3]	{pip fruit}	=> {whole milk}	0.03010	0.3978	0.07565
## [4]	{whole milk}	=> {pip fruit}	0.03010	0.1178	0.25552
## [5]	{pastry}	=> {whole milk}	0.03325	0.3737	0.08897
## [6]	{whole milk}	=> {pastry}	0.03325	0.1301	0.25552
## [7]	{citrus fruit}	=> {whole milk}	0.03050	0.3686	0.08277
## [8]	{whole milk}	=> {citrus fruit}	0.03050	0.1194	0.25552
## [9]	{sausage}	=> {rolls/buns}	0.03060	0.3258	0.09395
## [10]	{rolls/buns}	=> {sausage}	0.03060	0.1664	0.18393
##	lift	count			
## [1]	1.760	317			
## [2]	1.760	317			
## [3]	1.557	296			
## [4]	1.557	296			
## [5]	1.463	327			
## [6]	1.463	327			
## [7]	1.442	300			
## [8]	1.442	300			
## [9]	1.771	301			
## [10]	1.771	301			



Finally, we have 522 rules when we relaxed our thresholds to support being equal to .01 and our confidence threshold being equal to .01. Due to the size of the rules, we are only including the first 10 rules in our output.

##	lhs	rhs	support	confidence	coverage	lift
## [1]	{hard cheese}	=> {whole milk}	0.01007	0.41079	0.02450	1.608
## [2]	{whole milk}	=> {hard cheese}	0.01007	0.03940	0.25552	1.608
## [3]	{butter milk}	=> {other vegetables}	0.01037	0.37091	0.02796	1.917
## [4]	{other vegetables}	=> {butter milk}	0.01037	0.05360	0.19349	1.917
## [5]	{butter milk}	=> {whole milk}	0.01159	0.41455	0.02796	1.622
## [6]	{whole milk}	=> {butter milk}	0.01159	0.04536	0.25552	1.622
## [7]	{ham}	=> {whole milk}	0.01149	0.44141	0.02603	1.728
## [8]	{whole milk}	=> {ham}	0.01149	0.04497	0.25552	1.728
## [9]	{sliced cheese}	=> {whole milk}	0.01078	0.43983	0.02450	1.721
## [10]	{whole milk}	=> {sliced cheese}	0.01078	0.04218	0.25552	1.721
##	count					
## [1]	99					
## [2]	99					
## [3]	102					
## [4]	102					
## [5]	114					
## [6]	114					
## [7]	113					
## [8]	113					
## [9]	106					
## [10]	106					



Association Rule Mining Analysis

From these, we can see that whole milk is the most important item, and that makes sense as it is a staple in most diets. Next would be yogurt and other vegetables, which also makes sense as they are staple items. Some other things that we see, are that meat is correlated with vegetables, so putting some coupons or deals for meat in the veggie section could help increase meat sales. Perhaps, we can put some berries next in the yogurt aisle to encourage people to buy berries and make a nice parfait. Between dairy items such as milk(whole and butter) and cheese(hard and slices), there seems to be a high lift value. These dairy items are compliments of each other so putting them in close proximity of each other will increase sales of these items.