CONVOLUTIONAL NEURAL NETWORKS



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- CNN Building Blocks
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RECAP: WHAT IS WRONG WITH FULLY CONNECTED DEEP NEURAL NETWORKS?

- Consider an image classification problem (indoor/outdoor scene).
- Image size = $64 \times 64 \times 3 = 12288$ (input layer)
- Suppose two hidden layers h1 = 1000 neurons, h2 = 500 neurons
- Outputs = 2 neurons (one for each class)
- How many parameters would we need to train??

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- Outputs = 2 neurons (one for each class)
- How many parameters would we need to train??
- $12288 \times 1000 + 1000 \times 500 + 500 \times 2 = 12789000$ (12.7 million) very small image and very small network
- What if the image size = $256 \times 256 \times 3$, and network has 4 layers with 1000 neurons and 1000 outputs?

RECAP: WHAT IS WRONG WITH FULLY CONNECTED DEEP NEURAL NETWORKS?

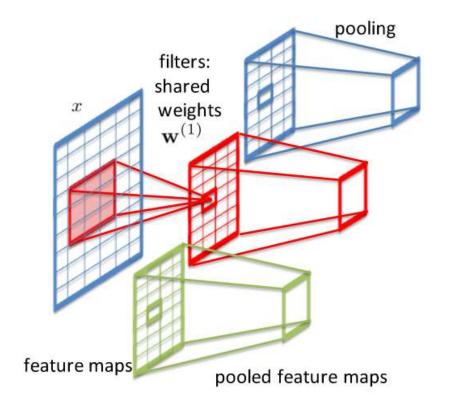
Too many parameters: MLP[1000-1000-1000] - 2 000 000 parameters require too much training data

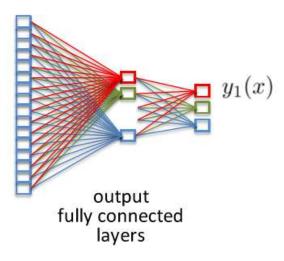
> Wasteful and do not generalize: no spatial invariance for images



RECAP: THE SOLUTION?

Convolutional neural networks (CNN)





BRIEF HISTORY: CNN



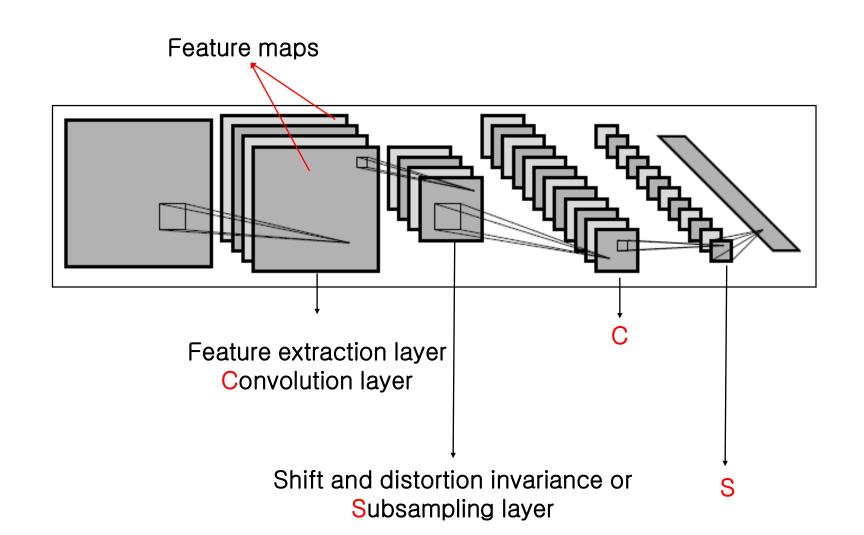
Yann LeCun, Professor of Computer Science The Courant Institute of Mathematical Sciences New York University Room 1220, 715 Broadway, New York, NY 10003, USA. (212)998-3283 yann@cs.nyu.edu

■ In 1995, Yann LeCun and Yoshua Bengio introduced the concept of convolutional neural networks.

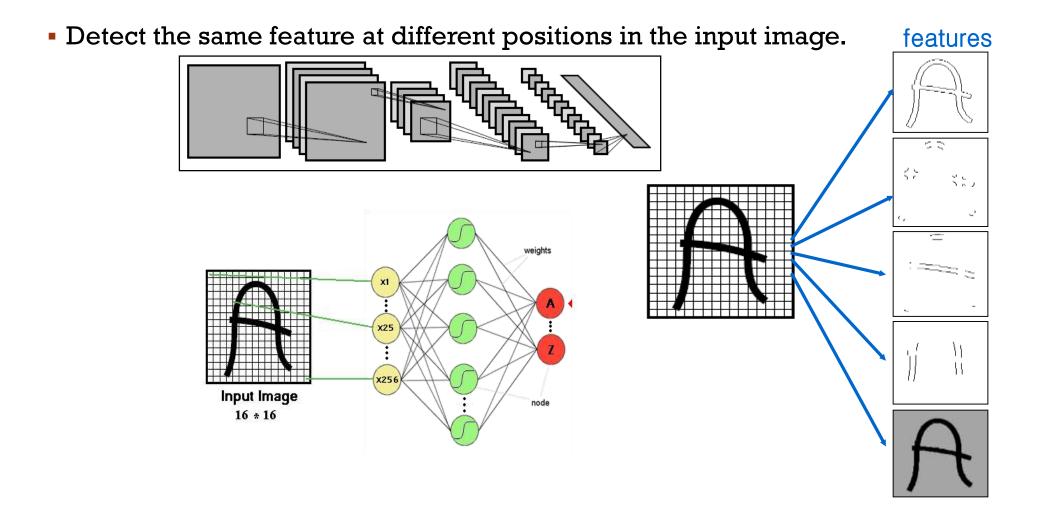
CONVOLUTIONAL NEURAL NETWORK

- CNN's Were neuro-biologically motivated by the findings of locally sensitive and orientation-selective nerve cells in the visual cortex.
- They designed a network structure that implicitly extracts relevant features.
- Convolutional Neural Networks are a special kind of multi-layer neural networks.
- CNN is a feed-forward network that can extract topological properties from an image.
- Like almost every other neural networks they are trained with a version of the back-propagation algorithm.
- Convolutional Neural Networks are designed to recognize visual patterns directly from pixel images with minimal preprocessing.
- They can recognize patterns with extreme variability (such as handwritten characters).

CNN BUILDING BLOCKS

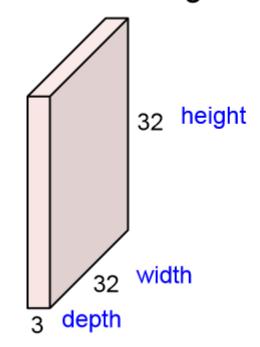


CONVOLUTION LAYER



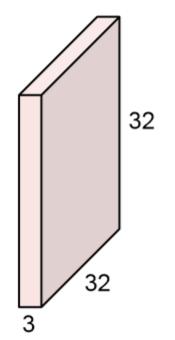
CONVOLUTION LAYER

32x32x3 image

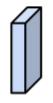


CONVOLUTION LAYER

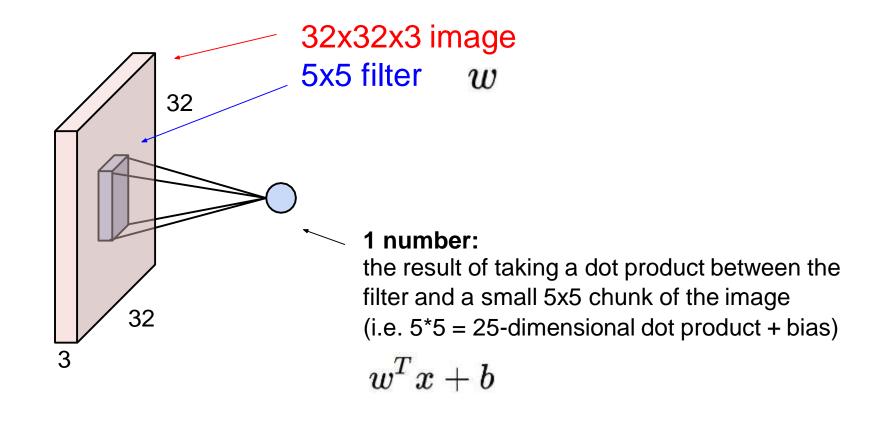
32x32x3 image

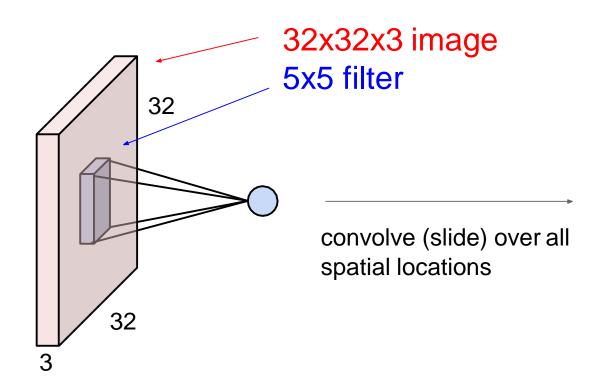


5x5x filter

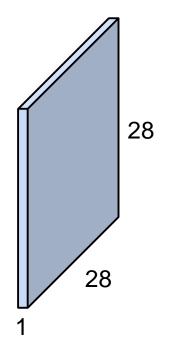


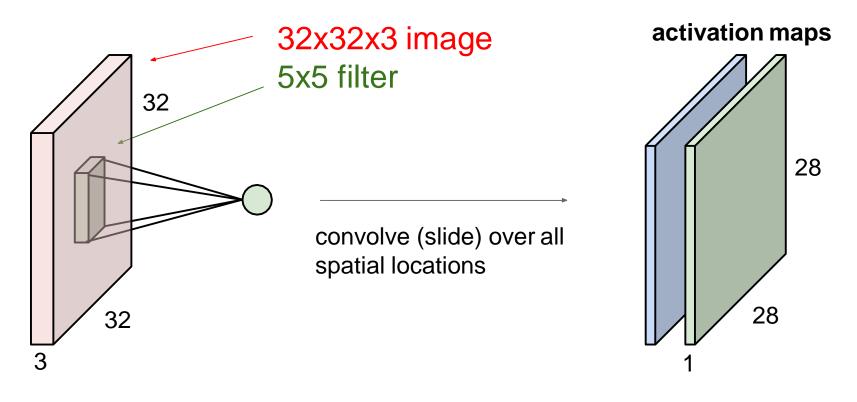
Convolve the filter with the image i.e. "slide over the image spatially, computing dot products"





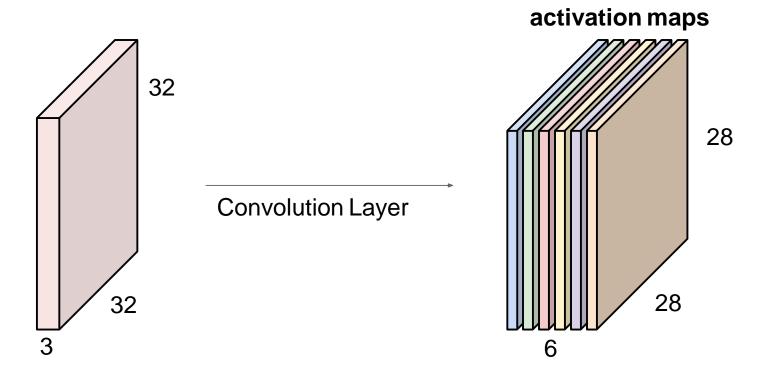
activation map





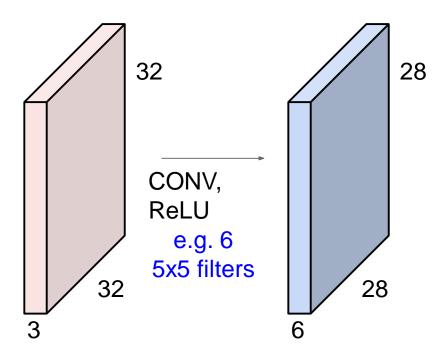
consider a second, green filter

• For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

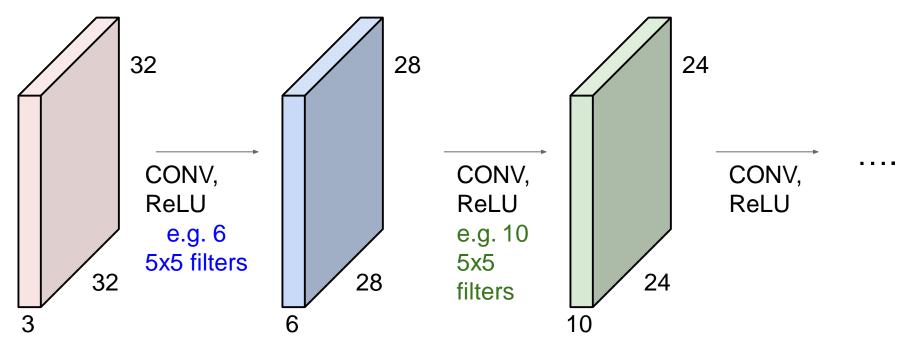


We stack these up to get a "new image" of size 28x28x6!

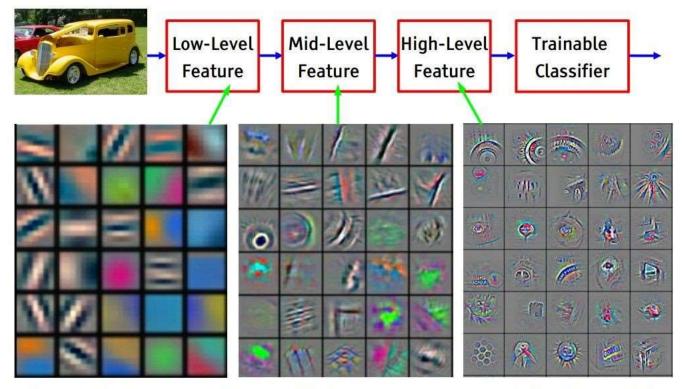
• **Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



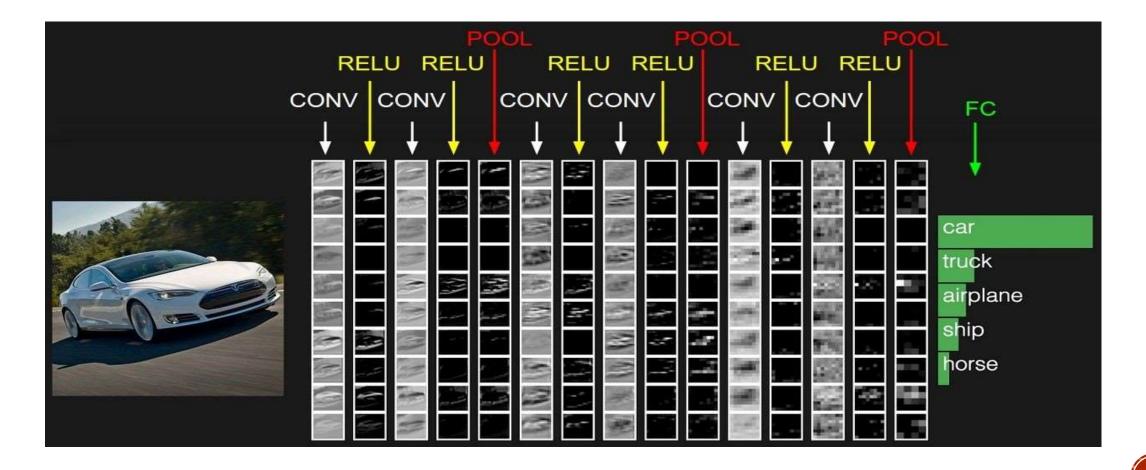
• **Preview:** ConvNet is a sequence of Convolutional Layers, interspersed with activation functions

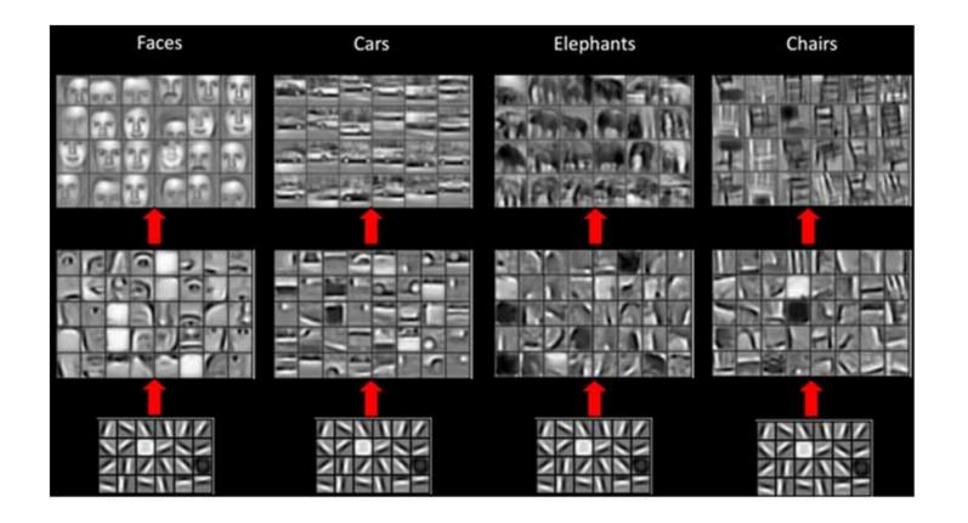


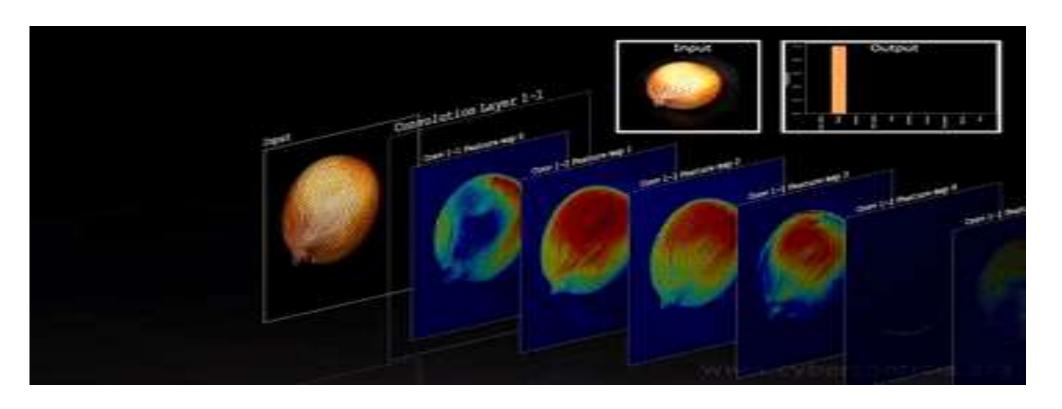
Preview

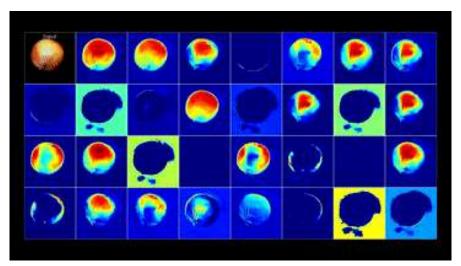


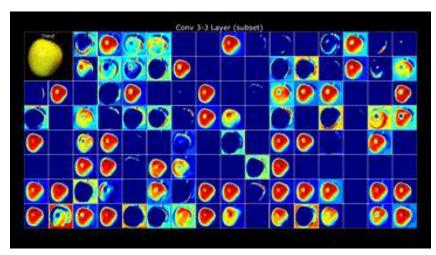
Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

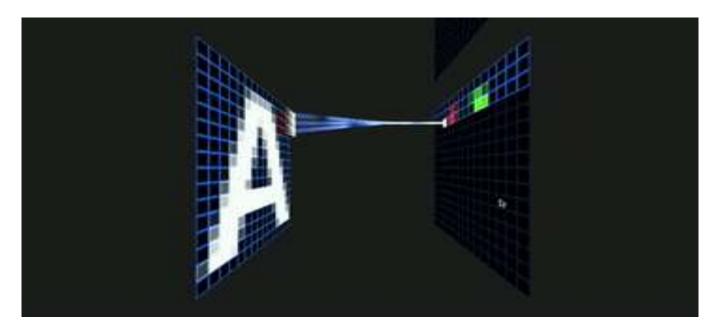




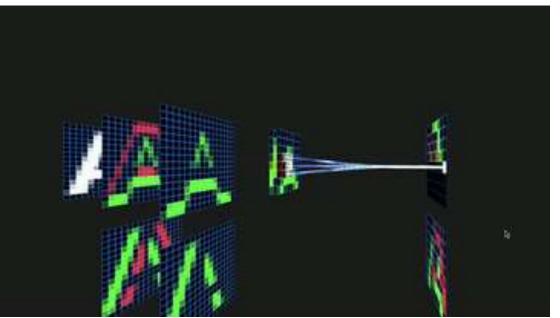




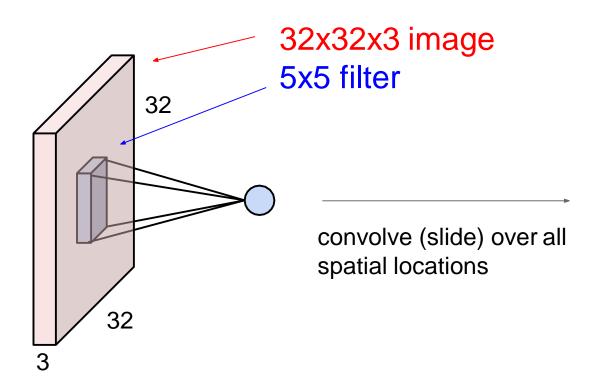




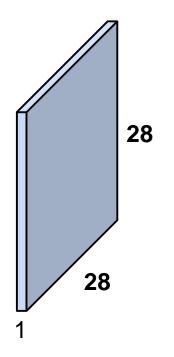




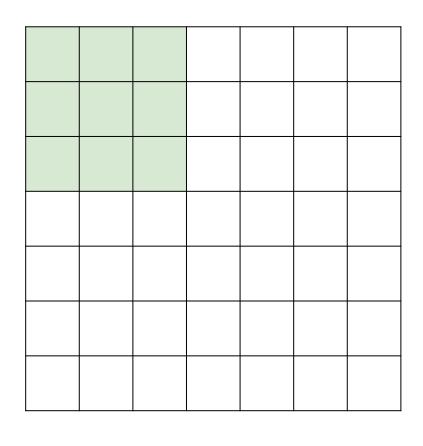
A closer look at spatial dimensions:



activation map



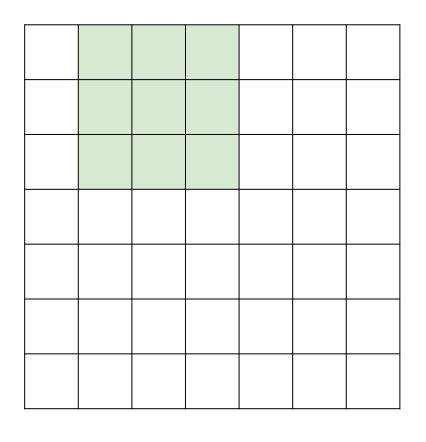
7



7x7 input (spatially) assume 3x3 filter



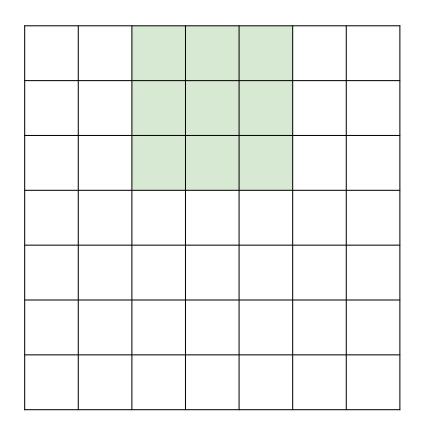
7



7x7 input (spatially) assume 3x3 filter



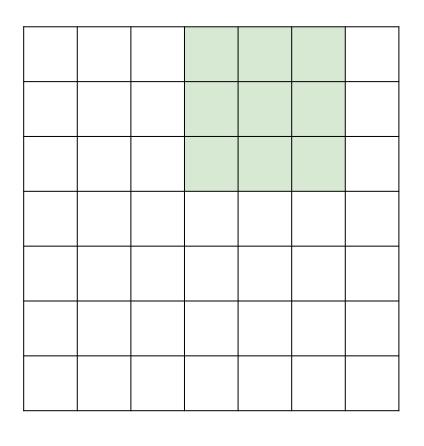
7



7x7 input (spatially) assume 3x3 filter



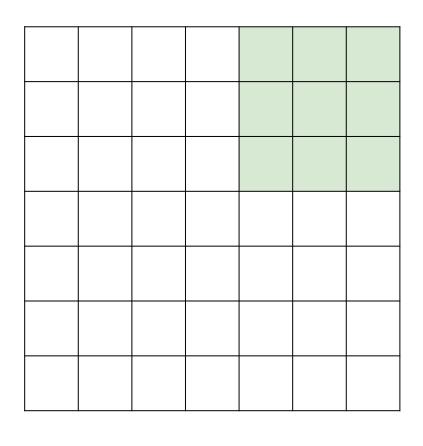
7



7x7 input (spatially) assume 3x3 filter



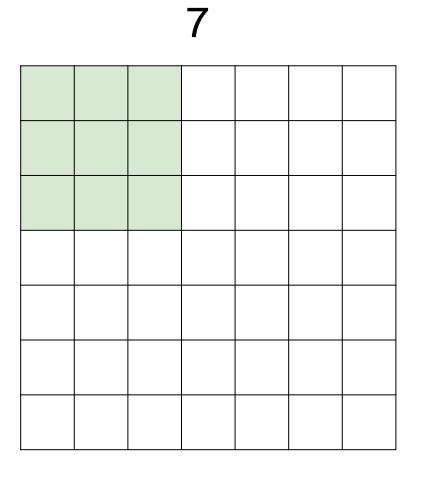
7



7x7 input (spatially) assume 3x3 filter

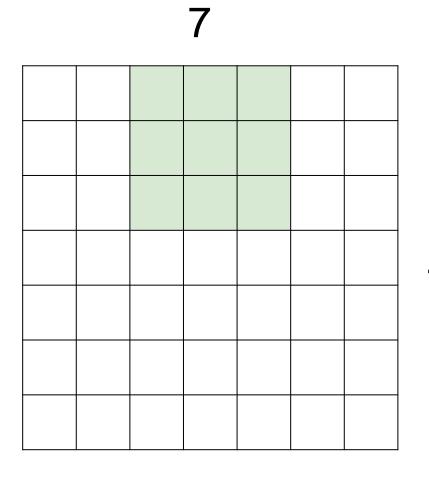
=> 5x5 output





7x7 input (spatially) assume 3x3 filter applied with stride 2



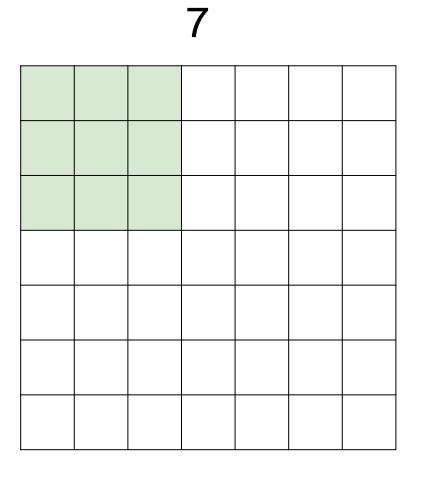


7x7 input (spatially) assume 3x3 filter applied with stride 2



7x7 input (spatially)
assume 3x3 filter
applied with stride 2
=> 3x3 output!





7x7 input (spatially) assume 3x3 filter applied with stride 3?



7x7 input (spatially) assume 3x3 filter applied with stride 3?

doesn't fit! cannot apply 3x3 filter on 7x7 input with stride 3.



	L		
F			

Output size: (N - F) / stride + 1

e.g. N = 7, F = 3:
stride 1 =>
$$(7 - 3)/1 + 1 = 5$$

stride 2 => $(7 - 3)/2 + 1 = 3$
stride 3 => $(7 - 3)/3 + 1 = 2.33$:\



IN PRACTICE: COMMON TO ZERO PAD THE BORDER

0	0	0	0	0	0		
0							
0							
0							
0							

e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?



IN PRACTICE: COMMON TO ZERO PAD THE BORDER

0	0	0	0	0	0		
0							
0							
0							
0							

e.g. input 7x7
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7x7 output!



IN PRACTICE: COMMON TO ZERO PAD THE BORDER

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0							
0							
0							
0							

e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

7x7 output!

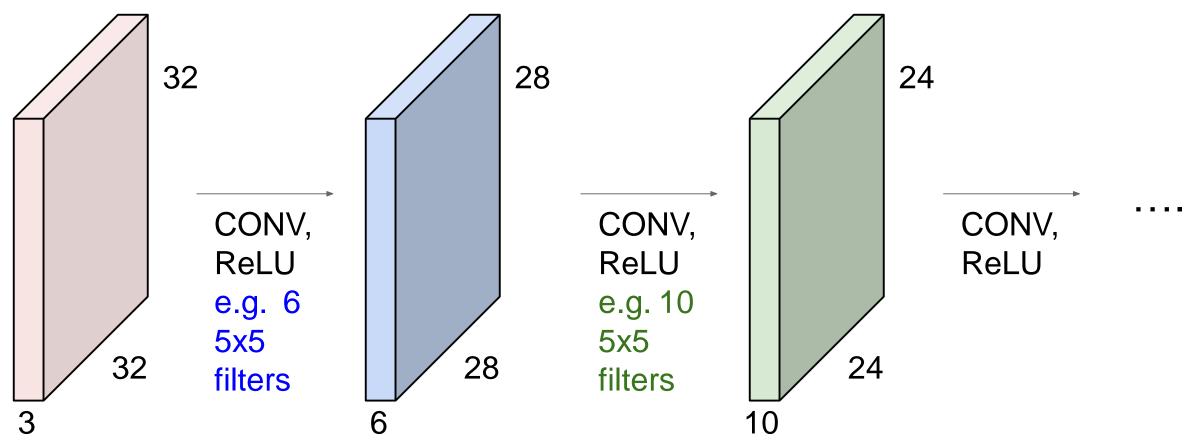
in general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with (F-1)/2. (will preserve size spatially)

```
e.g. F = 3 => zero pad with 1
F = 5 => zero pad with 2
F = 7 => zero pad with 3
```



REMEMBER BACK TO...

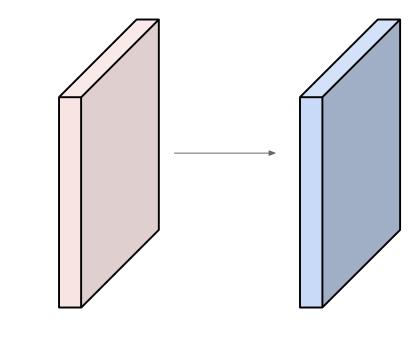
E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.





Examples time:

Input volume: **32x32x3**10 5x5 filters with stride 1, pad 2



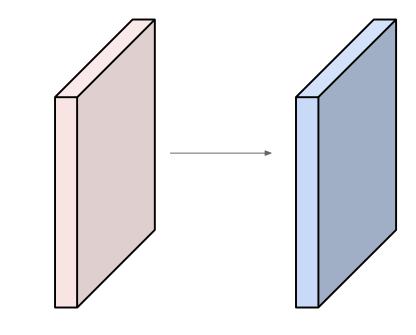
Output volume size: ?



Examples time:

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2



Output volume size:

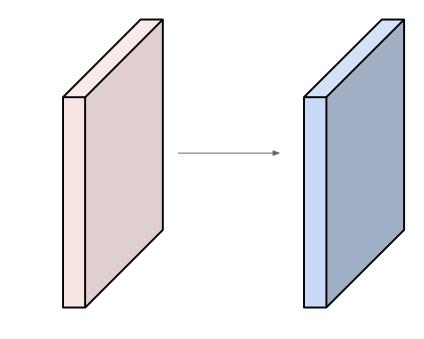
$$(32+2*2-5)/1+1 = 32$$
 spatially, so

32x32x10



Examples time:

Input volume: **32x32x3**10 5x5 filters with stride 1, pad 2



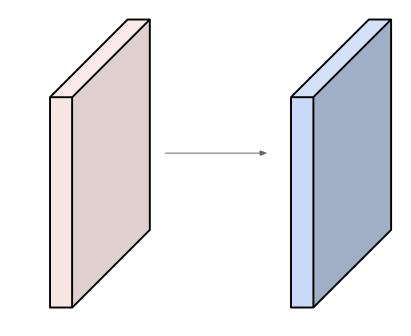
Number of parameters in this layer?



EXAMPLES TIME:

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2



Number of parameters in this layer? each filter has 5*5 + 1 = 26 params

$$=> 26*10 = 260$$

(+1 for bias)



Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_1 imes H_1 imes D_1$
- · Requires four hyperparameters:
 - Number of filters K,
 - their spatial extent F,
 - the stride S,
 - the amount of zero padding P.
- Produces a volume of size $W_2 imes H_2 imes D_2$ where:
 - $W_2 = (W_1 F + 2P)/S + 1$
 - \circ $H_2=(H_1-F+2P)/S+1$ (i.e. width and height are computed equally by symmetry)
 - D₂ = K
- With parameter sharing, it introduces F · F · D₁ weights per filter, for a total of (F · F · D₁) · K weights and K biases.
- In the output volume, the d-th depth slice (of size $W_2 imes H_2$) is the result of performing a valid convolution of the d-th filter over the input volume with a stride of S, and then offset by d-th bias.



Common settings:

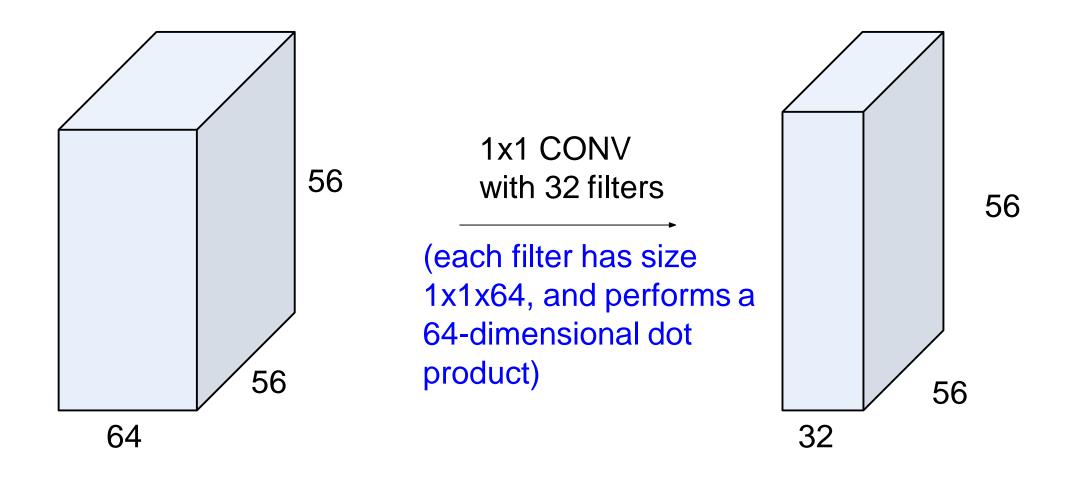
Summary. To summarize, the Conv Layer:

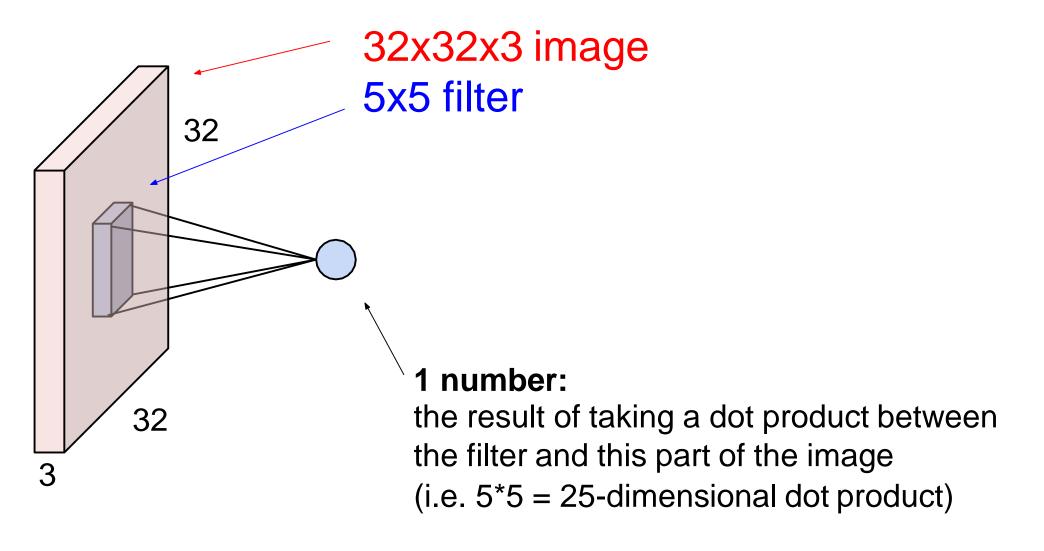
- Accepts a volume of size $W_1 imes H_1 imes D_1$
- Requires four hyperparameters:
 - Number of filters K,
 - their spatial extent F,
 - the stride S,
 - the amount of zero padding P.

- K = (powers of 2, e.g. 32, 64, 128, 512)
 - F = 3, S = 1, P = 1
 - F = 5, S = 1, P = 2
 - F = 5, S = 2, P = ? (whatever fits)
 - F = 1, S = 1, P = 0
- Produces a volume of size $W_2 imes H_2 imes D_2$ where:
 - $W_2 = (W_1 F + 2P)/S + 1$
 - \circ $H_2=(H_1-F+2P)/S+1$ (i.e. width and height are computed equally by symmetry)
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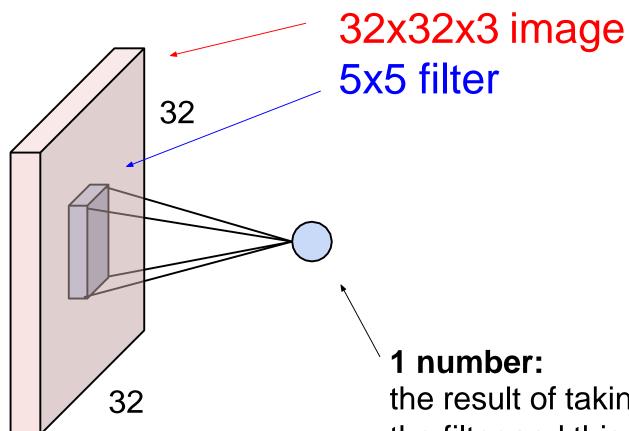


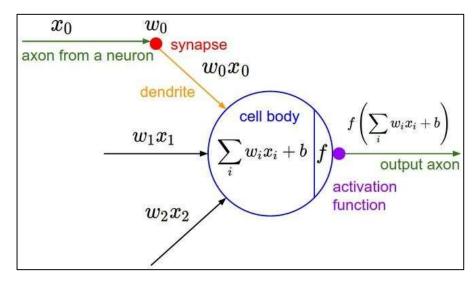
(BTW, 1X1 CONVOLUTION LAYERS MAKE PERFECT SENSE)







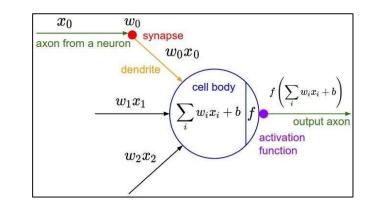


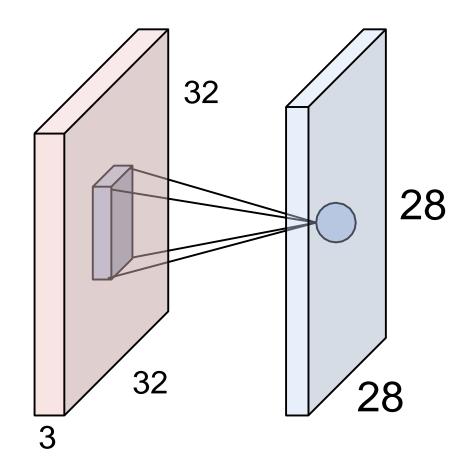


It's just a neuron with local connectivity...

the result of taking a dot product between the filter and this part of the image (i.e. 5*5 = 25-dimensional dot product)







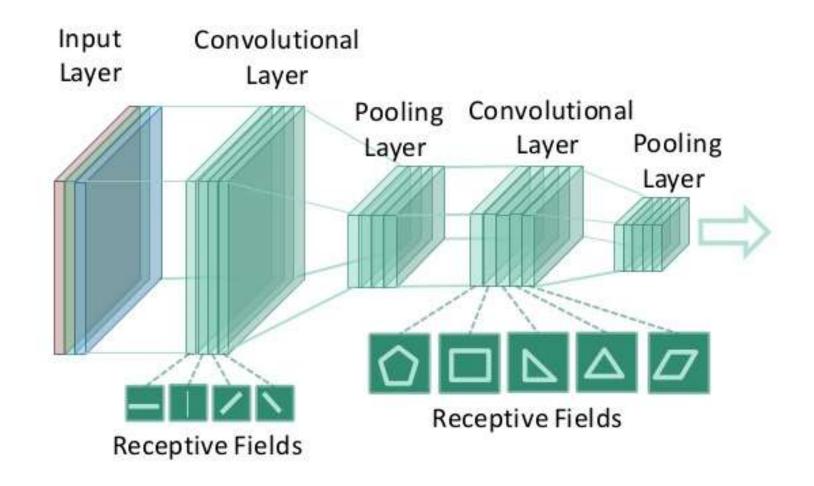
An activation map is a 28x28 sheet of neuron outputs:

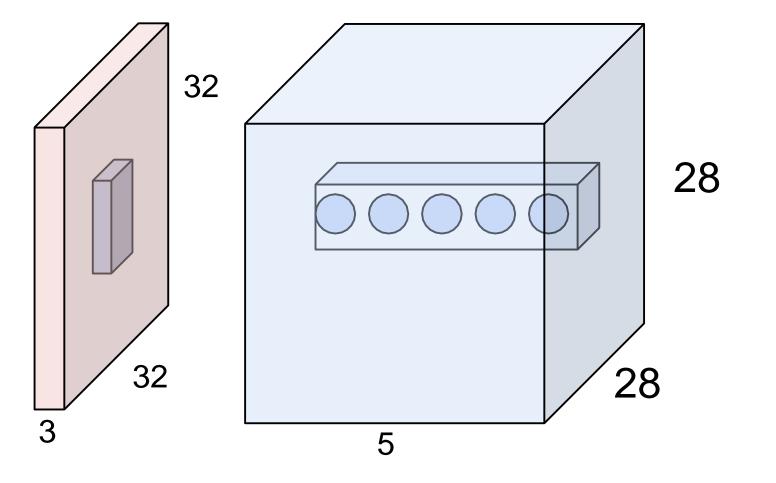
- 1. Each is connected to a small region in the input
- 2. All of them share parameters

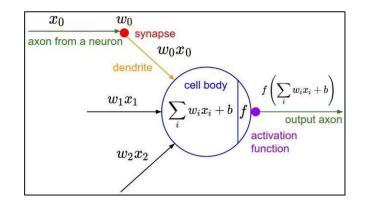
"5x5 filter" -> "5x5 receptive field for each neuron"



VISUAL PERCEPTION OF COMPUTER





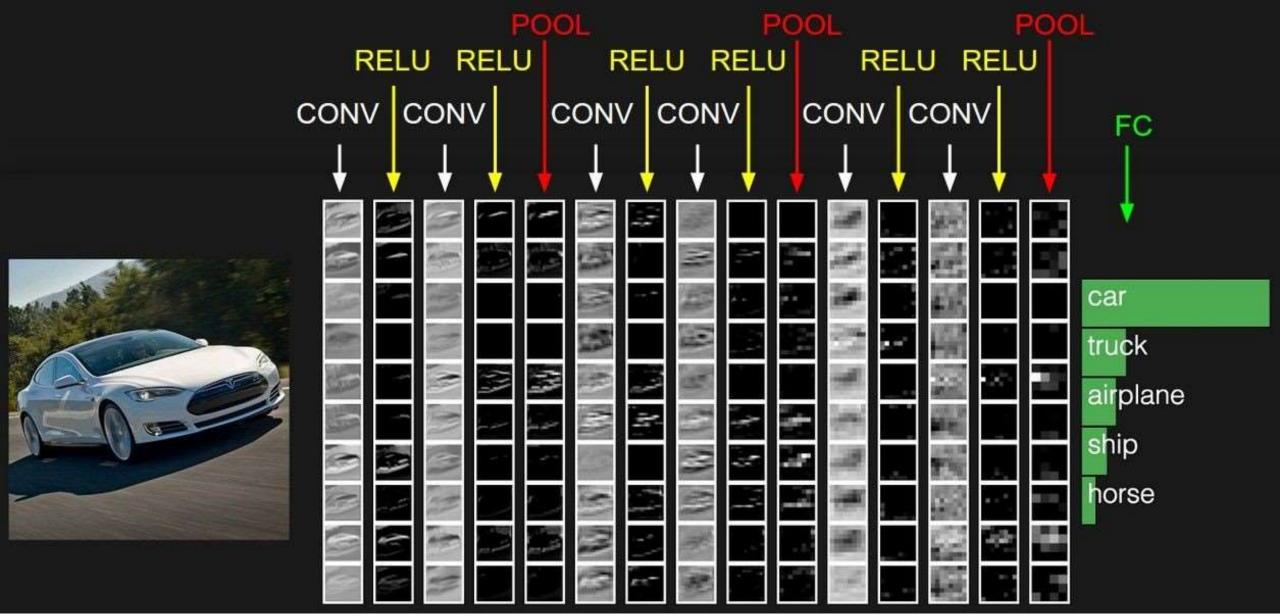


E.g. with 5 filters, CONV layer consists of neurons arranged in a 3D grid (28x28x5)

There will be 5 different neurons all looking at the same region in the input volume



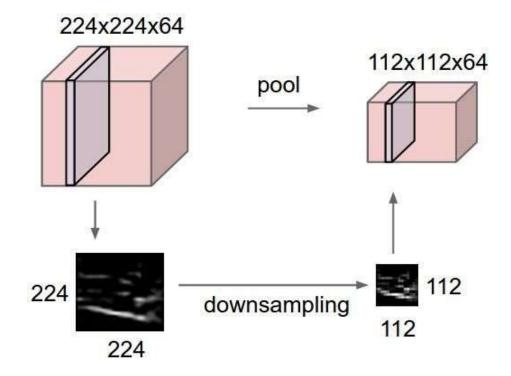
two more layers to go: POOL/FC





POOLING LAYER

- makes the representations smaller and more manageable
- operates over each activation map independently:





MAX POOLING

Single depth slice

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

max pool with 2x2 filters and stride 2

6	8
3	4



- Accepts a volume of size $W_1 imes H_1 imes D_1$
- Requires three hyperparameters:
 - their spatial extent F,
 - the stride S,
- Produces a volume of size $W_2 imes H_2 imes D_2$ where:
 - $W_2 = (W_1 F)/S + 1$
 - $H_2 = (H_1 F)/S + 1$
 - $D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

Common settings:

- Accepts a volume of size $W_1 imes H_1 imes D_1$
- Requires three hyperparameters:
 - their spatial extent F,
 - the stride S,
- ullet Produces a volume of size $W_2 imes H_2 imes D_2$ where:

$$W_2 = (W_1 - F)/S + 1$$

$$H_2 = (H_1 - F)/S + 1$$

•
$$D_2 = D_1$$

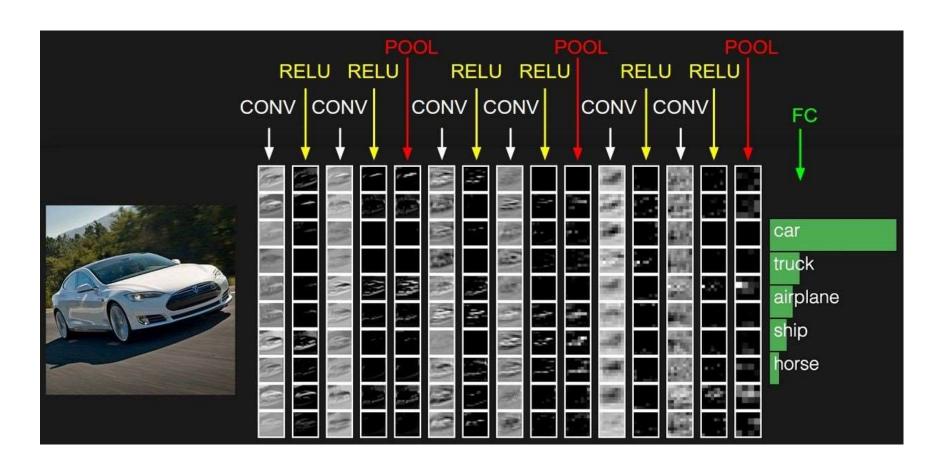
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

$$F = 2$$
, $S = 2$
 $F = 3$, $S = 2$



FULLY CONNECTED LAYER (FC LAYER)

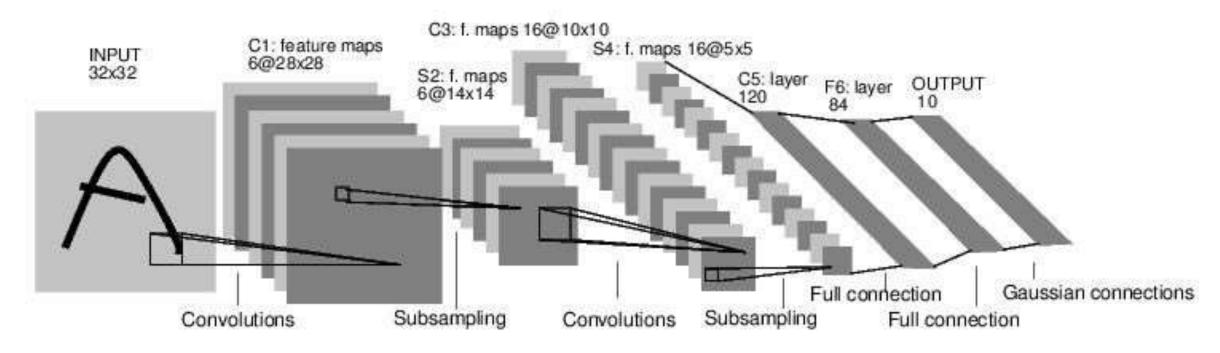
- CONTAINS NEURONS THAT CONNECT TO THE ENTIRE INPUT VOLUME, AS IN ORDINARY NEURAL NETWORKS





CASE STUDY: LENET-5

[LeCun et al., 1998]



Conv filters were 5x5, applied at stride 1 Subsampling (Pooling) layers were 2x2 applied at stride 2 i.e. architecture is [CONV-POOL-CONV-POOL-CONV-FC]



CASE STUDY: ALEXNET

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] CONV1: 96 11x11 filters at stride 4, pad 0

[27x27x96] MAX POOL1: 3x3 filters at stride 2

[27x27x96] NORM1: Normalization layer

[27x27x256] CONV2: 256 5x5 filters at stride 1, pad 2

[13x13x256] MAX POOL2: 3x3 filters at stride 2

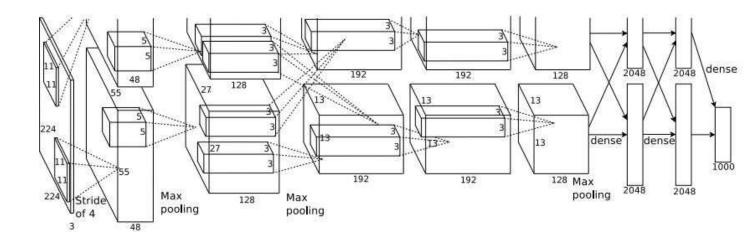
[13x13x256] NORM2: Normalization layer

[13x13x384] CONV3: 384 3x3 filters at stride 1, pad 1 [13x13x384] CONV4: 384 3x3 filters at stride 1, pad 1 [13x13x256] CONV5: 256 3x3 filters at stride 1, pad 1

[6x6x256] MAX POOL3: 3x3 filters at stride 2

[4096] FC6: 4096 neurons [4096] FC7: 4096 neurons

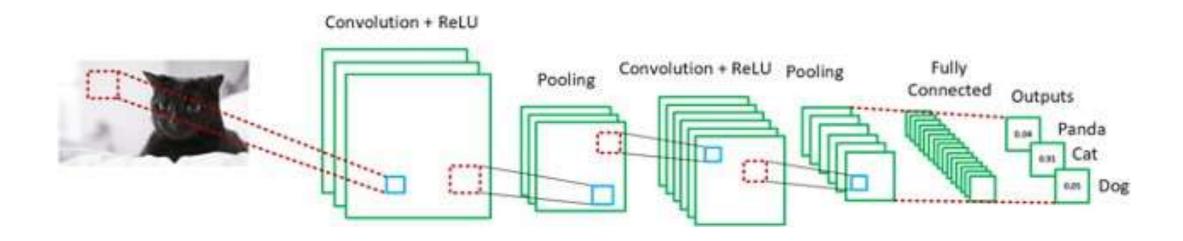
[1000] FC8: 1000 neurons (class scores)



TRANSFER LEARNING - 2 MAJOR TYPES

Feature Extractor Fine Tuning





TRANSFER LEARNING

- Transfer learning or inductive transfer is a research problem in machine learning that focuses on storing knowledge gained while solving one problem and applying it to a different but related problem.
- For example, knowledge gained while learning to recognize cars could apply when trying to recognize trucks. This area of research bears some relation to the long history of psychological literature on transfer of learning, although formal ties between the two fields are limited.

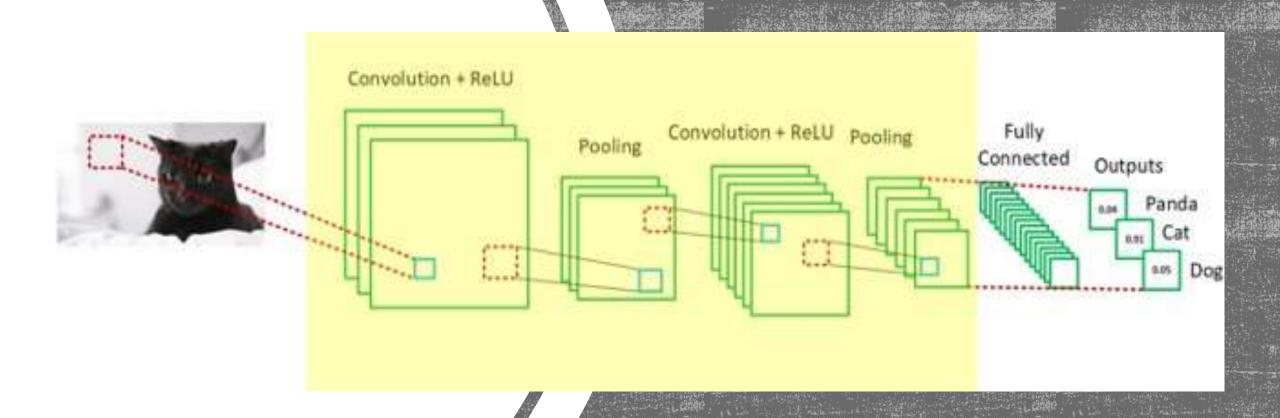
TRANSFER LEARNING

• The three major Transfer Learning scenarios look as follows:

1. ConvNet as fixed feature extractor.

• Take a ConvNet pretrained on ImageNet, remove the last fully-connected layer (this layer's outputs are the 1000 class scores for a different task like ImageNet), then treat the rest of the ConvNet as a fixed feature extractor for the new dataset.

1. CONVNET AS FIXED FEATURE EXTRACTOR.



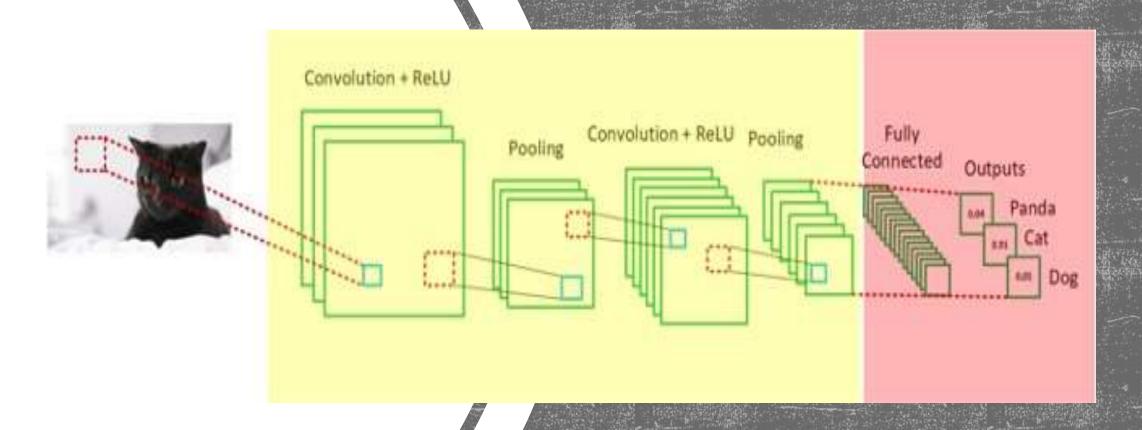
TRANSFER LEARNING

• The three major Transfer Learning scenarios look as follows:

2. Fine-tuning the ConvNet.

• The second strategy is to not only replace and retrain the classifier on top of the ConvNet on the new dataset, but to also fine-tune the weights of the pretrained network by continuing the backpropagation. It is possible to fine-tune all the layers of the ConvNet, or it's possible to keep some of the earlier layers fixed (due to overfitting concerns) and only fine-tune some higher-level portion of the network.

2. FINE-TUNING THE CONVNET



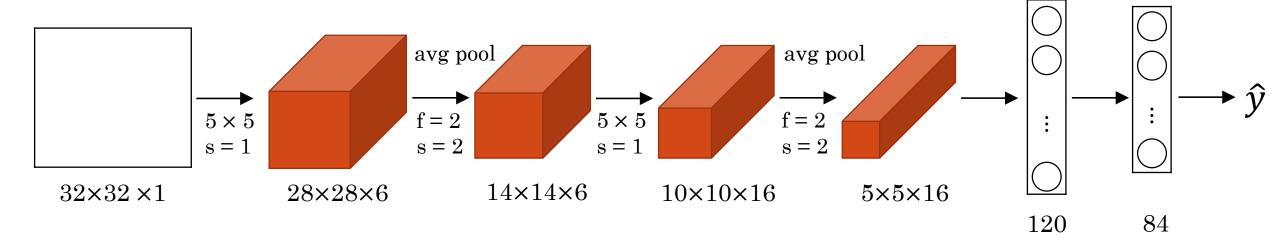
TRANSFER LEARNING - WHEN DO WE USE?



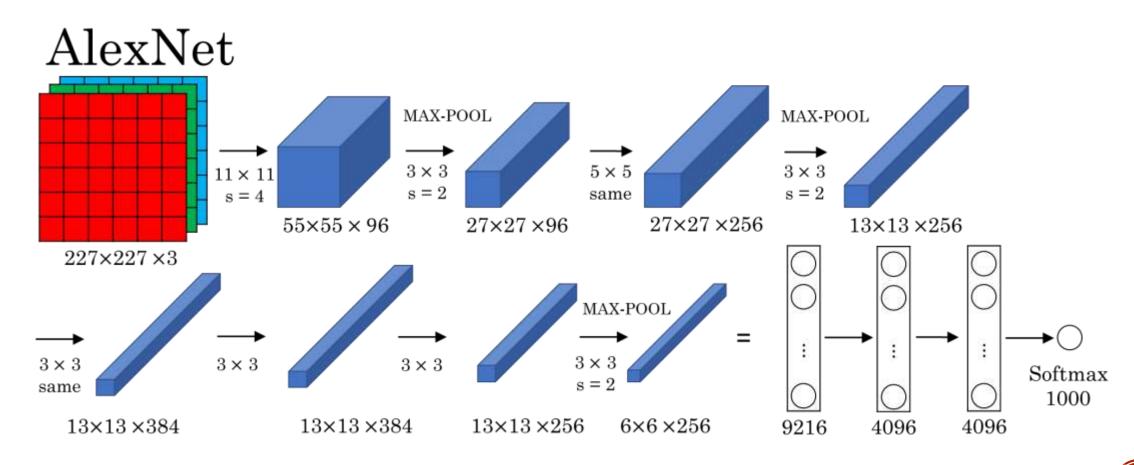
- Ideal scenario New dataset is large and similar to the pre-trained original dataset. Models should not overfit.
- Not ideal but still recommended New data is large but different.
- If data is small (even if similar) Transfer Learning and Fine Tuning can often overfit on the training data. A useful idea at times is to train a linear classier on the CNN outputs.

PLAIN NETWORKS

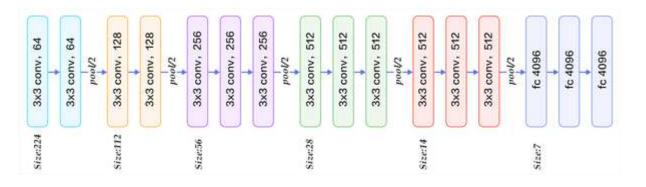
- Simple CNN architectures where connections among the layers follow simple straight-forward paths
- E.g. LeNet-5



PLAIN NETWORKS



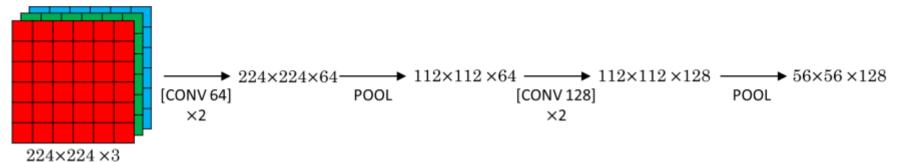
PLAIN NETWORKS



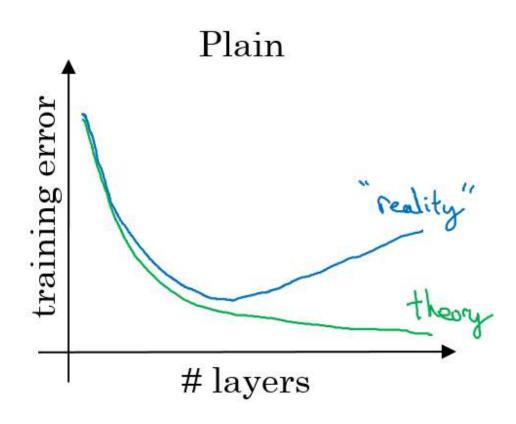
VGG - 16

 $CONV = 3 \times 3$ filter, s = 1, same

 $MAX-POOL = 2 \times 2$, s = 2



PROBLEMS WITH PLAIN NETWORKS



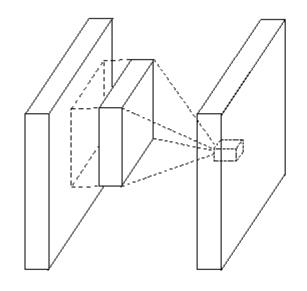
- Increasing number of layers increases computational complexity
- More layers does not always guarantee better performance

CNN MICROARCHITECTURES

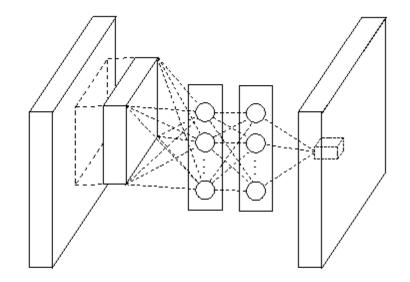
- Modern CNNs are made up of various types of building blocks where each building block has a particular structure and function. E.g.
 - MLPConv (Network-in-Network)
 - Inception Module (GoogleNet)
 - Fire Module (SqueezeNet)
 - Residual Block (ResNet) etc.

MLPCONV (NETWORK IN NETWORK)

Introduced series of lxl convolutions as a small network (MLP) inside the CNN



(a) Linear convolution layer



(b) Mlpconv layer

MLPCONV (NETWORK IN NETWORK)

 Introduced series of lxl convolutions as a small network (MLP) inside the CNN

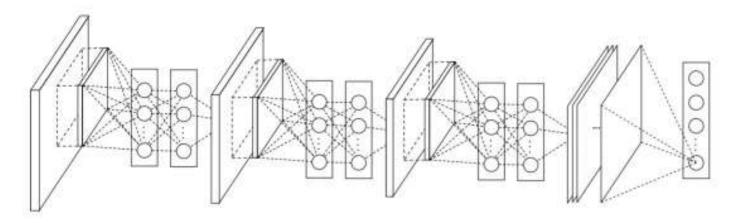
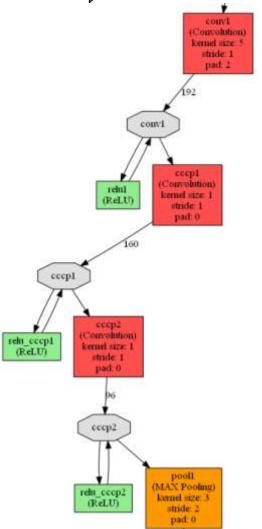
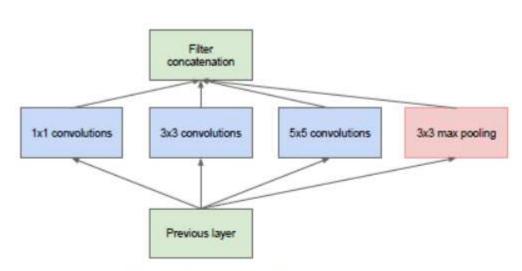


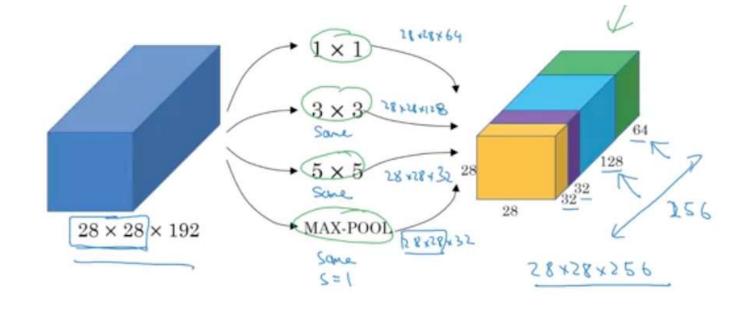
Figure 2: The overall structure of Network In Network. In this paper the NINs include the stacking of three mlpconv layers and one global average pooling layer.



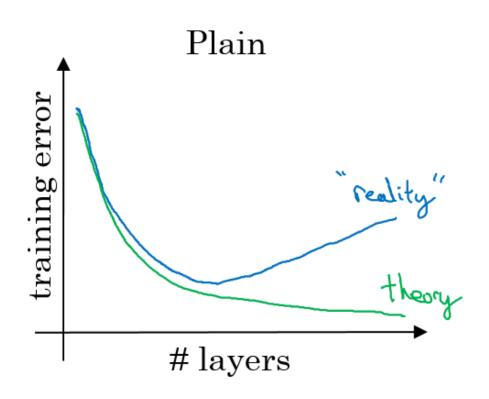
INCEPTION MODULE (GOOGLENET)

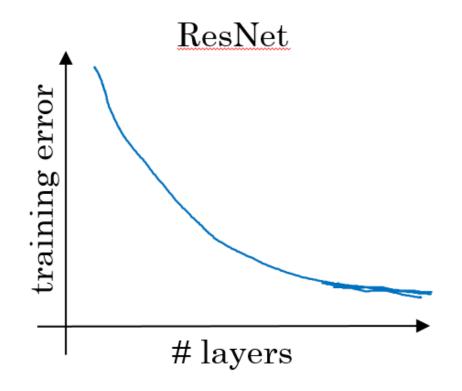


(a) Inception module, naïve version

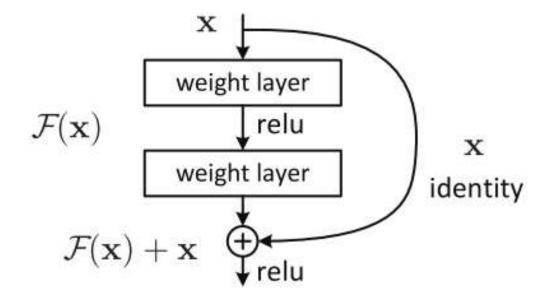


PROBLEMS WITH VERY DEEP NETWORKS

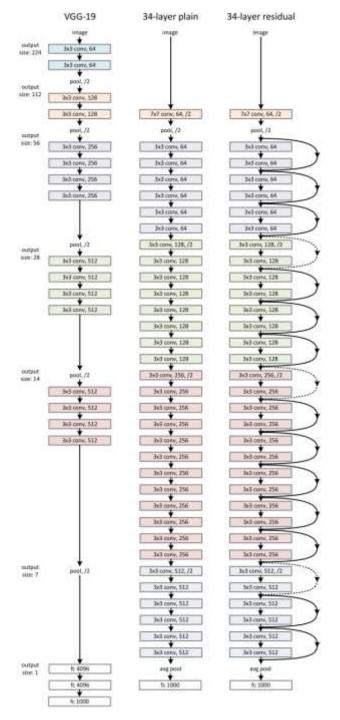


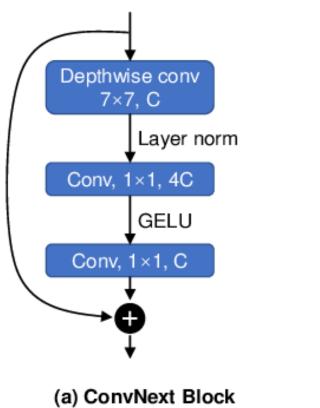


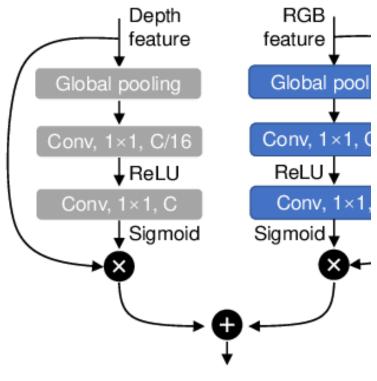
RESIDUAL BLOCK (RESNET)



Residual Block



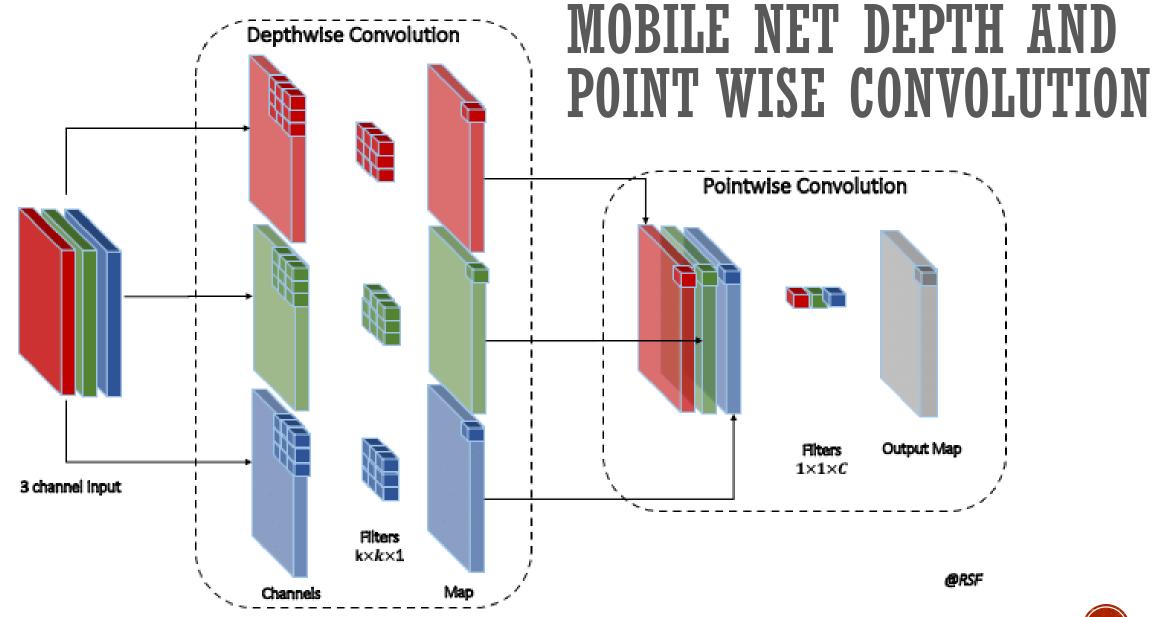




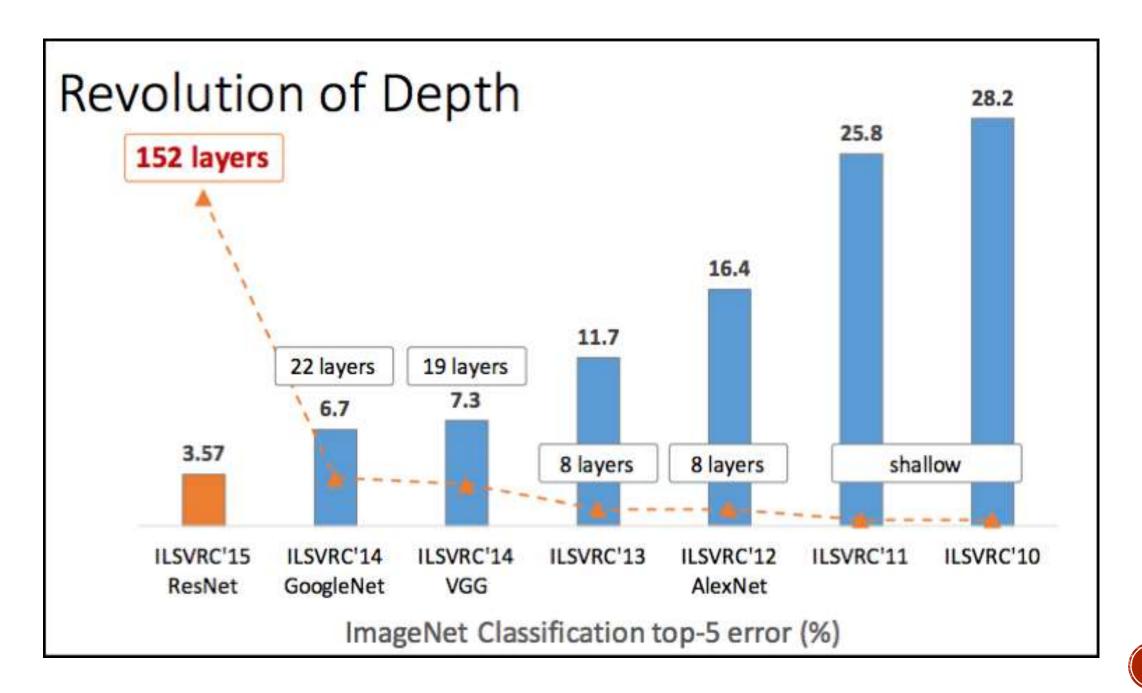
(b) Fusion Module

CONVNEXT MULTI-MODULE)







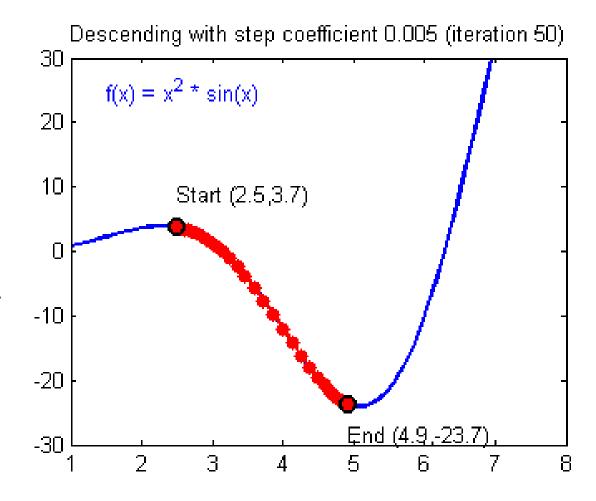


GRADIENT DESCENT OPTIMIZATION

• gradient descent, computes the gradient of the cost function w.r.t. to the parameters θ for the entire training dataset:

$$\theta = \theta - \eta \cdot \nabla_{\theta} J(\theta)$$
.

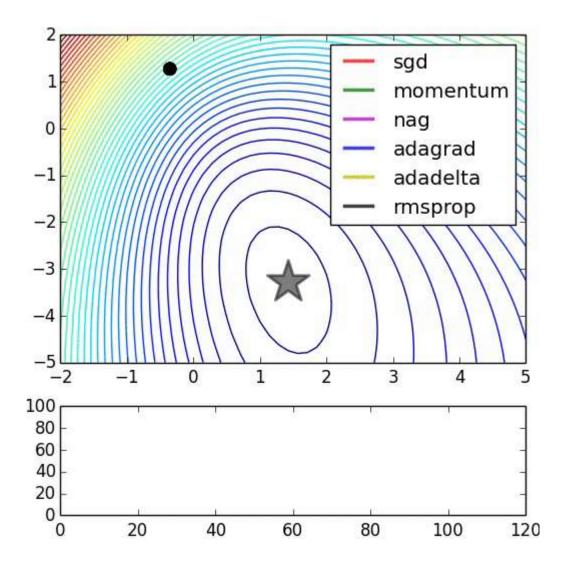
 Calculate the gradients for the whole dataset to perform just one update, batch gradient descent can be very slow



STOCHASTIC GRADIENT DESCENT

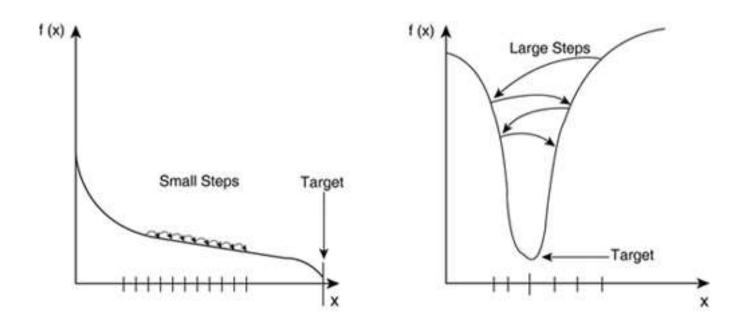
 Stochastic gradient descent (SGD) in contrast performs a parameter update for each training example x⁽ⁱ⁾ and label y⁽ⁱ⁾:

$$\theta = \theta - \eta \cdot \nabla_{\theta} J(\theta; x^{(i)}; y^{(i)}).$$



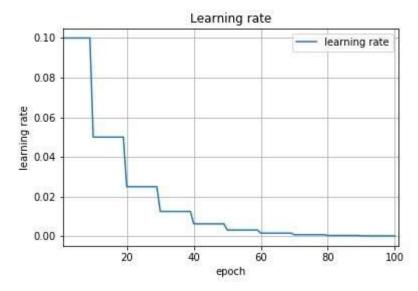
OPTIMIZATION CHALLENGES

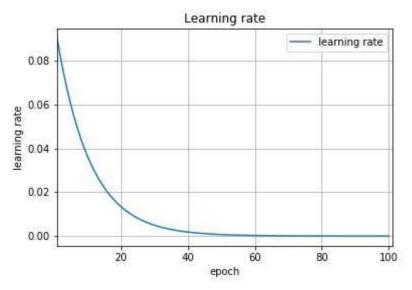
 Choosing a proper learning rate can be difficult. A learning rate that is too small leads to painfully slow convergence, while a learning rate that is too large can hinder convergence and cause the loss function to fluctuate around the minimum or even to diverge.



OPTIMIZATION CHALLENGES

• Learning rate schedules try to adjust the learning rate during training by e.g. annealing, i.e. reducing the learning rate according to a pre-defined schedule or when the change in objective between epochs falls below a threshold. These schedules and thresholds, however, have to be defined in advance and are thus unable to adapt to a dataset's characteristics



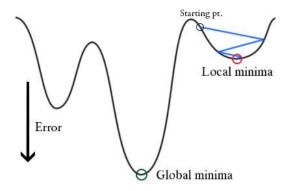


Step Decay Schedule

Exponential Decay Schedule

OPTIMIZATION CHALLENGES

- Additionally, the same learning rate applies to all parameter updates. If our data is sparse and our features have very different frequencies, we might not want to update all of them to the same extent, but perform a larger update for rarely occurring features.
- Another key challenge of minimizing highly non-convex error functions common for neural networks is avoiding getting trapped in their numerous suboptimal local minima.



GRADIENT DESCENT OPTIMIZATION ALGORITHMS (SOLVERS)

- SGD with Momentum
- SGD has trouble navigating ravines, i.e. areas where the surface curves much more steeply in one dimension than in another, which are common around local optima.



Image 2: SGD without momentum

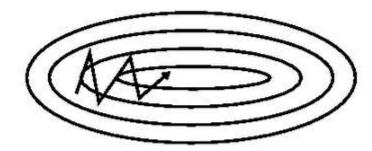


Image 3: SGD with momentum

• Momentum is a method that helps accelerate SGD in the relevant direction and dampens oscillations as can be seen in Image 3. It does this by adding a fraction γ of the update vector of the past time step to the current update vector:

$$v_t = \gamma v_{t-1} + \eta \nabla_{\theta} J(\theta) \ heta = \theta - v_t$$

The momentum term γ is usually set to 0.9 or a similar value.

GRADIENT DESCENT OPTIMIZATION ALGORITHMS (SOLVERS)

- SGD with Momentum
- Essentially, when using momentum, we push a ball down a hill. The ball accumulates momentum as it rolls downhill, becoming faster and faster on the way (until it reaches its terminal velocity if there is air resistance, i.e. γ <1).



Image 2: SGD without momentum

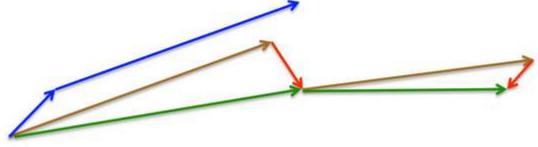


Image 3: SGD with momentum

NESTEROV ACCELERATED GRADIENT

- A ball that rolls down a hill, blindly following the slope, is highly unsatisfactory. We'd like to have a smarter ball, a ball that has a notion of where it is going so that it knows to slow down before the hill slopes up again.
- Nesterov accelerated gradient (NAG) is a way to give our momentum term this kind of prescience.
- We can effectively look ahead by calculating the gradient not w.r.t. to our current parameters θ but w.r.t. the approximate future position of our parameters:

$$egin{aligned} v_t &= \gamma v_{t-1} + \eta
abla_{ heta} J(heta - \gamma v_{t-1}) \ heta &= heta - v_t \end{aligned}$$



ADAGRAD

- It adapts the learning rate to the parameters, performing larger updates for infrequent and smaller updates for frequent parameters. For this reason, it is well-suited for dealing with sparse data.
- Adagrad uses a different learning rate for every parameter θ_i at every time step t

 $heta_{t+1} = heta_t - rac{\eta}{\sqrt{G_t + \epsilon}} \odot g_t.$

- $g_{t,i}$ to be the gradient of the objective function w.r.t. to the parameter θ_i at time step t
- $G_t \in \mathbb{R}^{d \times d}$ here is a diagonal matrix where each diagonal element i,i is the sum of the squares of the gradients w.r.t. θ_i up to time step t
- ϵ is a smoothing term that avoids division by zero
- One of Adagrad's main benefits is that it eliminates the need to manually tune the learning rate. Most implementations use a default value of 0.01 and leave it at that.

ADAGRAD

Adagrad's main weakness is its accumulation of the squared gradients in the denominator:

 $heta_{t+1} = heta_t - rac{\eta}{\sqrt{G_t + \epsilon}} \odot g_t.$

- Since every added term is positive, the accumulated sum keeps growing during training.
- This in turn causes the learning rate to shrink and eventually become infinitesimally small, at which point the algorithm is no longer able to acquire additional knowledge.
- This flaw has been resolved in AdaDelta.

OTHER VARIANTS

Adadelta

- It is an extension of Adagrad that seeks to reduce its aggressive, monotonically decreasing learning rate.
- Instead of accumulating all past squared gradients, Adadelta restricts the window of accumulated past gradients to some fixed size w.
- With Adadelta, we do not even need to set a default learning rate

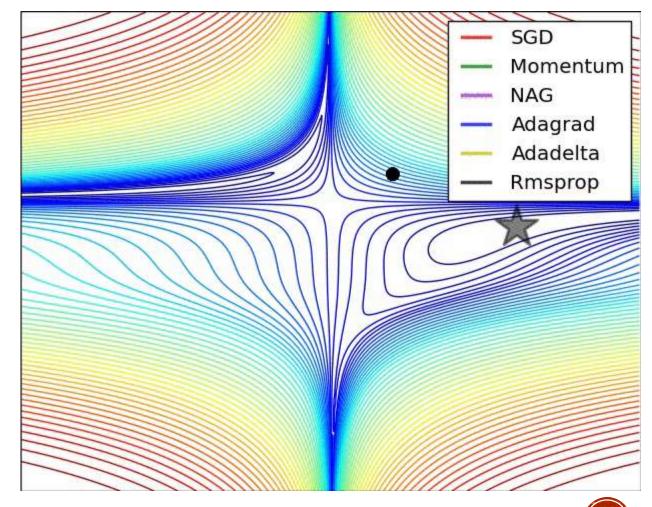
RMSprop

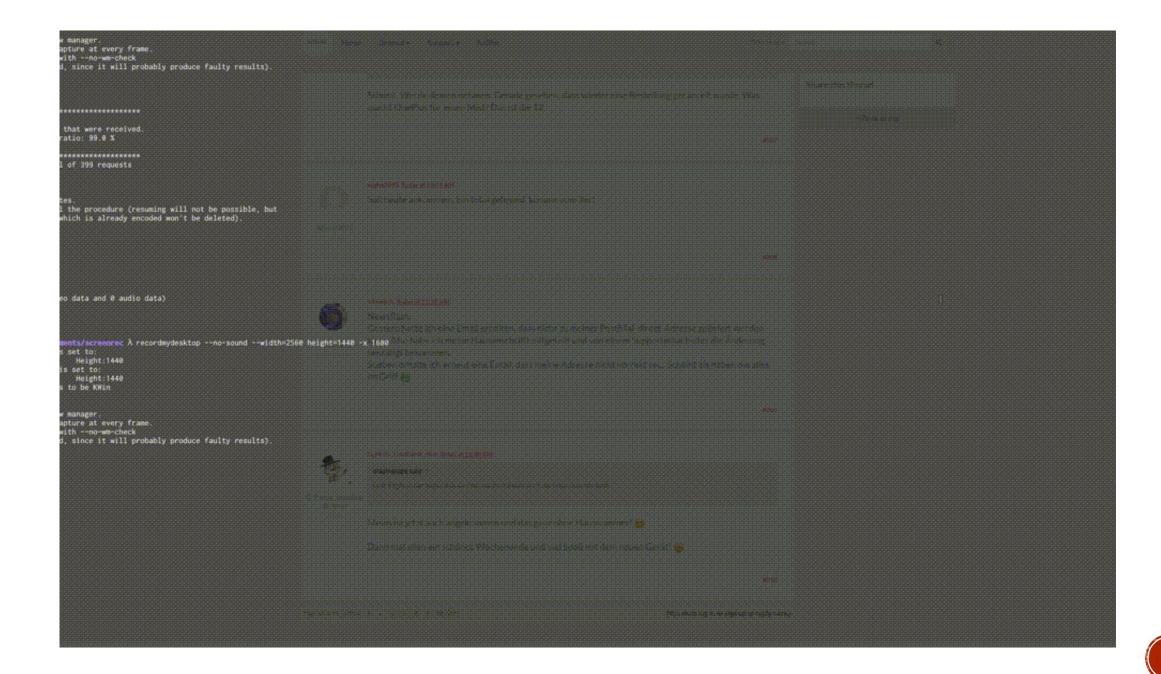
- It is an unpublished, adaptive learning rate method proposed by Geoff Hinton
- RMSprop divides the learning rate by an exponentially decaying average of squared gradients. Hinton suggests γ to be set to 0.9, while a good default value for the learning rate η is 0.001.

OTHER VARIANTS

Adam

- Adaptive Moment Estimation (Adam) is another method that computes adaptive learning rates for each parameter.
- momentum can be seen as a ball running down a slope, Adam behaves like a heavy ball with friction, which thus prefers flat minima in the error surface





ASSIGNMENT-1

- 1. Collect and label your own dataset for image classification
- 2. Construct a CNN model for your data (use existing nets as reference)
- 3. Report classification accuracy on the validation set

REFERENCES



Krizhevsky, Alex, Ilya Sutskever, and Geoffrey E. Hinton. "Imagenet classification with deep convolutional neural networks." In *Advances in neural information processing systems*, pp. 1097-1105, 2012.



Jia, Yangqing, Evan Shelhamer, Jeff Donahue, Sergey Karayev, Jonathan Long, Ross Girshick, Sergio Guadarrama, and Trevor Darrell. "Caffe: Convolutional architecture for fast feature embedding." In *Proceedings of the 22nd ACM international conference on Multimedia*, pp. 675-678. ACM, 2014.



http://ruder.io/optimizing-gradient-descent/