

int  $g(\overbrace{arr1}^{\text{ordered}}, \overbrace{arr2}^{\text{ordered}}, k)$

int  $f(\overbrace{arr1}^{\text{ordered}}, \overbrace{arr2}^{\text{same length}})$  getUpperMedian  
two arrs

$f(arr1, L_1, R_1, arr2, L_2, R_2)$

$arr1[L_1, \dots, R_1]$  make sure ordered  
 $arr2[L_2, \dots, R_2]$

$arr1[1, 2, 3, 4, \dots]$  length even

$arr2[1, 2, 3, 4, \dots]$

$arr1[1, 2, 3, 4]$

$arr2[1, 2, 3, 4]$  To return upper median, both smallest

if  $2 \leq 2$  return either value

$(1, 2)$   $(2, 3)$   $(\dots)$

if  $2 > 2$

$arr1[2] < arr2[1]$  can't be the best value

become  $[3, 2, 3] > [2, 1]$

$> [1]$

$[2, 3] > [2, 1]$   $> [1]$  ?  $[1, 2]$

$[1, 2]$   $[3, 2]$  one possible

if  $3 \leq 4$

$1, 2, 3, 4$

$1, 2, 3, 4$

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odd  $arr1[1, 2, 3, 4, 5]$   
 $arr2[1, 2, 3, 4, 5]$  10 numbers

$arr1[1, 2, 3, 4, 5]$  if  $3 \leq 3$  return

$arr2[1, 2, 3, 4, 5]$  if  $3 > 3$

Can't directly call f function because require same length

$2 \leq 3$  verify whether  $[3]$  is fifth small or not

if  $[3] \leq 2$  return  $[2]$  directly

else  $[1, 2][4, 5]$  in f function

same same length  
second largest is fifth largest interval

g function

$g(arr1, arr2)$  both sorted  
return kth smallest after combine

$arr1$  10 num  
 $arr2$  17 num

kth smallest  
Condition 1  $1 \leq k \leq 10$  within below smallest length

obtain first 7th from  $arr1$   
getUpperMedian

Condition 2  $len(s) < k \leq len(L)$   $k=15$

$arr1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$   
 $arr2: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$

$arr1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$  consider all arr  
 $arr2: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$

but this time still can't call getUpperMedian  
f( ) equal length

$arr1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$  consider all arr  
 $arr2: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$

check whether  $[5]$  is 15th smallest  
if yes: return  
if not: remove

$1, 2, 3, 4, 5, 6, 7, 8, 9, 10$   
 $6, 7, 8, 9, 10, 11, 12, 13, 14, 15$

f(10, 10)

Condition 2  $17 < k \leq 27$   
 $len(L) < k \leq len(s) + len(L)$  if  $k=23$

$arr1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$   
 $arr2: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$

can't merge  $[6, 7, 8, 9, 10]$  to f function

become  $[6, 7, 8, 9, 10]$  22 smallest

temporarily merge 2 num  
[6]  
[7]

$arr1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$   
 $arr2: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$

$[6]$   $19 + 4 = 23$

f( ) equal length

$O(\log(\log(\text{small})))$

```
def findKthNum(arr1, arr2, kth):
    longs = arr1 if len(arr1) >= len(arr2) else arr2
    shorts = arr1 if len(arr1) < len(arr2) else arr2
    l, s = len(longs), len(shorts)
    if kth <= s:
        return getUpMedian(shorts, 0, kth - 1, longs, 0, kth - 1)
    if kth > l: but smaller than sum
        if shorts[kth - l - 1] >= longs[l - 1]: exclude by hand
            return shorts[kth - l - 1]
        if longs[kth - s - 1] >= shorts[s - 1]: exclude by hand
            return longs[kth - s - 1]
        return getUpMedian(shorts, kth - l, s - 1, longs, kth - s, l - 1)
    if longs[kth - s - 1] >= shorts[s - 1]:
        return longs[kth - s - 1]
    return getUpMedian(shorts, 0, s - 1, longs, kth - s, kth - 1)
```