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Program Structures & Algorithms

Fall 2021

Assignment No. 5

◎ Task (List down the tasks performed in the Assignment)

1. A cutoff (defaults to, say, 1000) which you will update according to the first argument in the command line when running. It's your job to experiment and come up with a good value for this cutoff. If there are fewer elements to sort than the cutoff, then you should use the system sort instead.
2. Recursion depth or the number of available threads. Using this determination, you might decide on an ideal number (t) of separate threads (stick to powers of 2) and arrange for that number of partitions to be parallelized (by preventing recursion after the depth of $\lg t$ is reached).
3. An appropriate combination of these.

◎ Relationship Conclusion:

1. It is better to sort in parallel than system sort
2. A good cutoff number is around 41% of the array size
3. An ideal number of separate threads is 8

◎ Evidence to support the conclusion:

1. Output

```
public static void main(String[] args) {  
    processArgs(args);  
    System.out.println("-----test cutoff-----");  
    System.out.println("Degree of parallelism: " + ForkJoinPool.getCommonPoolParallelism());  
    Random random = new Random();  
    // manually set the array size from 2000000 to 5000000  
    int[] array = new int[5000000]; // 2000000, 3000000, 4000000, 5000000  
}
```

Firstly, I tested the relationship between run time and cutoff number. As `ForkJoinPool.getCommonPoolParallelism()` was 7 which told me my cpu is 8, I chose thread number as 8 at

first to test different cutoff results. The output was long, so I just screenshot the part of the result.

the array size from 2000000 to 5000000, the cutoff from 25.5% to 50% of array size

Degree of parallelism: 7			Degree of parallelism: 7		
the number of threads is: 8			the number of threads is: 8		
cutoff: 510000	10times	Time:975ms	cutoff: 765000	10times	Time:1634ms
cutoff: 520000	10times	Time:816ms	cutoff: 780000	10times	Time:1293ms
cutoff: 530000	10times	Time:809ms	cutoff: 795000	10times	Time:1280ms
cutoff: 540000	10times	Time:863ms	cutoff: 810000	10times	Time:1279ms
cutoff: 550000	10times	Time:865ms	cutoff: 825000	10times	Time:1275ms
cutoff: 560000	10times	Time:906ms	cutoff: 840000	10times	Time:1276ms
cutoff: 570000	10times	Time:899ms	cutoff: 855000	10times	Time:1284ms
cutoff: 580000	10times	Time:846ms	cutoff: 870000	10times	Time:1319ms
cutoff: 590000	10times	Time:862ms	cutoff: 885000	10times	Time:1327ms
cutoff: 600000	10times	Time:847ms	cutoff: 900000	10times	Time:1307ms
cutoff: 610000	10times	Time:813ms	cutoff: 915000	10times	Time:1457ms
cutoff: 620000	10times	Time:825ms	cutoff: 930000	10times	Time:1433ms
cutoff: 630000	10times	Time:872ms	cutoff: 945000	10times	Time:1410ms
cutoff: 640000	10times	Time:838ms	cutoff: 960000	10times	Time:1602ms
cutoff: 650000	10times	Time:834ms	cutoff: 975000	10times	Time:1367ms
cutoff: 660000	10times	Time:850ms	cutoff: 990000	10times	Time:1407ms
cutoff: 670000	10times	Time:849ms	cutoff: 1005000	10times	Time:1385ms
cutoff: 680000	10times	Time:838ms	cutoff: 1020000	10times	Time:1379ms
cutoff: 690000	10times	Time:844ms	cutoff: 1035000	10times	Time:1403ms
cutoff: 700000	10times	Time:873ms	cutoff: 1050000	10times	Time:1392ms
cutoff: 710000	10times	Time:841ms	cutoff: 1065000	10times	Time:1358ms
cutoff: 720000	10times	Time:932ms	cutoff: 1080000	10times	Time:1400ms
cutoff: 730000	10times	Time:842ms	cutoff: 1095000	10times	Time:1462ms
cutoff: 740000	10times	Time:874ms	cutoff: 1110000	10times	Time:1359ms
cutoff: 750000	10times	Time:840ms	cutoff: 1125000	10times	Time:1321ms
cutoff: 760000	10times	Time:836ms	cutoff: 1140000	10times	Time:1321ms
cutoff: 770000	10times	Time:929ms	cutoff: 1155000	10times	Time:1329ms
cutoff: 780000	10times	Time:873ms	cutoff: 1170000	10times	Time:1316ms
cutoff: 790000	10times	Time:863ms	cutoff: 1185000	10times	Time:1317ms
cutoff: 800000	10times	Time:931ms	cutoff: 1200000	10times	Time:1310ms
cutoff: 810000	10times	Time:855ms	cutoff: 1215000	10times	Time:1290ms
cutoff: 820000	10times	Time:844ms	cutoff: 1230000	10times	Time:1281ms
cutoff: 830000	10times	Time:871ms	cutoff: 1245000	10times	Time:1274ms
cutoff: 840000	10times	Time:904ms	cutoff: 1260000	10times	Time:1275ms
cutoff: 850000	10times	Time:877ms	cutoff: 1275000	10times	Time:1280ms
cutoff: 860000	10times	Time:858ms	cutoff: 1290000	10times	Time:1281ms
cutoff: 870000	10times	Time:872ms	cutoff: 1305000	10times	Time:1276ms
cutoff: 880000	10times	Time:860ms	cutoff: 1320000	10times	Time:1276ms

Degree of parallelism: 7
the number of threads is: 8

cutoff: 1020000	10times	Time:2077ms
cutoff: 1040000	10times	Time:1738ms
cutoff: 1060000	10times	Time:1770ms
cutoff: 1080000	10times	Time:1719ms
cutoff: 1100000	10times	Time:1749ms
cutoff: 1120000	10times	Time:1747ms
cutoff: 1140000	10times	Time:1796ms
cutoff: 1160000	10times	Time:1955ms
cutoff: 1180000	10times	Time:1902ms
cutoff: 1200000	10times	Time:1832ms
cutoff: 1220000	10times	Time:1818ms
cutoff: 1240000	10times	Time:1800ms
cutoff: 1260000	10times	Time:1776ms
cutoff: 1280000	10times	Time:1811ms
cutoff: 1300000	10times	Time:1892ms
cutoff: 1320000	10times	Time:1858ms
cutoff: 1340000	10times	Time:1872ms
cutoff: 1360000	10times	Time:1741ms
cutoff: 1380000	10times	Time:1732ms
cutoff: 1400000	10times	Time:1725ms
cutoff: 1420000	10times	Time:1727ms
cutoff: 1440000	10times	Time:1750ms
cutoff: 1460000	10times	Time:1728ms
cutoff: 1480000	10times	Time:1738ms
cutoff: 1500000	10times	Time:1735ms
cutoff: 1520000	10times	Time:1729ms
cutoff: 1540000	10times	Time:1742ms
cutoff: 1560000	10times	Time:1730ms
cutoff: 1580000	10times	Time:1728ms
cutoff: 1600000	10times	Time:1730ms
cutoff: 1620000	10times	Time:1726ms
cutoff: 1640000	10times	Time:1728ms
cutoff: 1660000	10times	Time:1800ms
cutoff: 1680000	10times	Time:2002ms
cutoff: 1700000	10times	Time:1802ms
cutoff: 1720000	10times	Time:1743ms
cutoff: 1740000	10times	Time:1785ms
cutoff: 1760000	10times	Time:1904ms

Degree of parallelism: 7
the number of threads is: 8

cutoff: 1275000	10times	Time:2381ms
cutoff: 1300000	10times	Time:2166ms
cutoff: 1325000	10times	Time:2157ms
cutoff: 1350000	10times	Time:2163ms
cutoff: 1375000	10times	Time:2152ms
cutoff: 1400000	10times	Time:2139ms
cutoff: 1425000	10times	Time:2238ms
cutoff: 1450000	10times	Time:2263ms
cutoff: 1475000	10times	Time:2193ms
cutoff: 1500000	10times	Time:2213ms
cutoff: 1525000	10times	Time:2234ms
cutoff: 1550000	10times	Time:2230ms
cutoff: 1575000	10times	Time:2430ms
cutoff: 1600000	10times	Time:2287ms
cutoff: 1625000	10times	Time:2288ms
cutoff: 1650000	10times	Time:2282ms
cutoff: 1675000	10times	Time:2284ms
cutoff: 1700000	10times	Time:2507ms
cutoff: 1725000	10times	Time:2423ms
cutoff: 1750000	10times	Time:2189ms
cutoff: 1775000	10times	Time:2183ms
cutoff: 1800000	10times	Time:2178ms
cutoff: 1825000	10times	Time:2225ms
cutoff: 1850000	10times	Time:2220ms
cutoff: 1875000	10times	Time:2214ms
cutoff: 1900000	10times	Time:2290ms
cutoff: 1925000	10times	Time:2292ms
cutoff: 1950000	10times	Time:2116ms
cutoff: 1975000	10times	Time:2138ms
cutoff: 2000000	10times	Time:2106ms
cutoff: 2025000	10times	Time:2134ms
cutoff: 2050000	10times	Time:2104ms
cutoff: 2075000	10times	Time:2130ms
cutoff: 2100000	10times	Time:2130ms
cutoff: 2125000	10times	Time:2142ms
cutoff: 2150000	10times	Time:2101ms
cutoff: 2175000	10times	Time:2221ms
cutoff: 2200000	10times	Time:2155ms

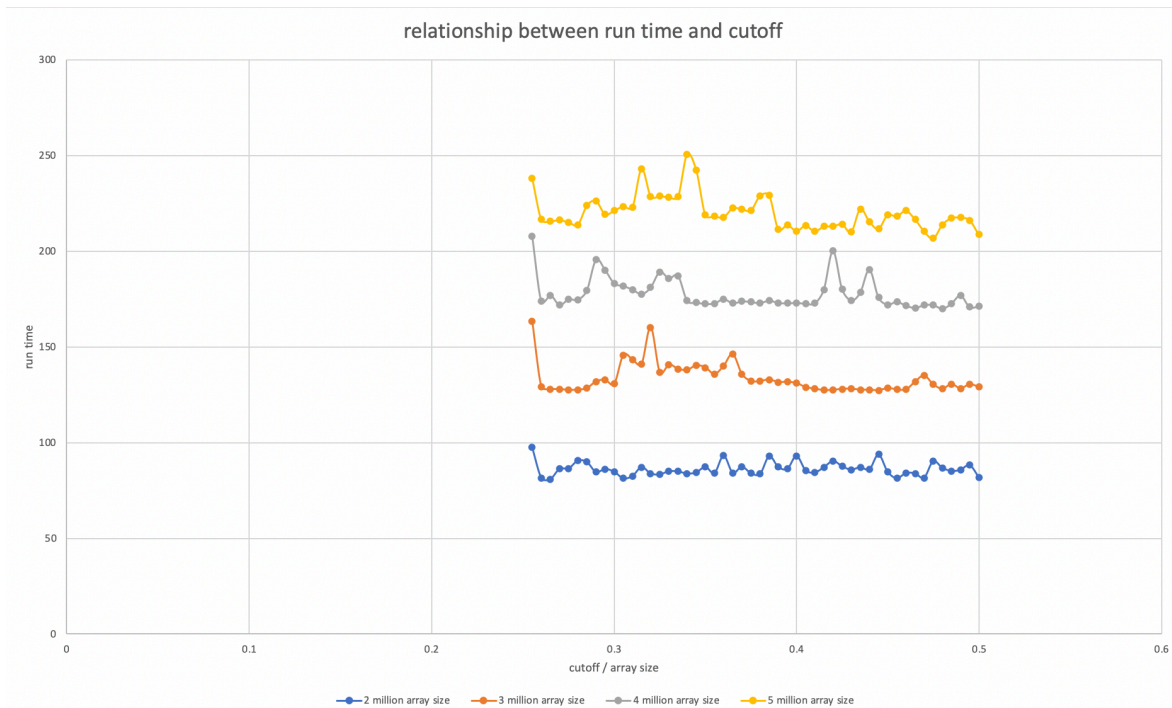
Secondly, I made an experiment on different thread numbers with a good cutoff which is 41% of the array size.

the array size from 2000000 to 5000000, the thread number from 2 to 256

-----test threads-----			-----test threads-----		
the number of threads: 2	10times	Time:1725ms	the number of threads: 2	10times	Time:2939ms
the number of threads: 4	10times	Time:1206ms	the number of threads: 4	10times	Time:1876ms
the number of threads: 8	10times	Time:797ms	the number of threads: 8	10times	Time:1224ms
the number of threads: 16	10times	Time:799ms	the number of threads: 16	10times	Time:1233ms
the number of threads: 32	10times	Time:816ms	the number of threads: 32	10times	Time:1215ms
the number of threads: 64	10times	Time:798ms	the number of threads: 64	10times	Time:1202ms
the number of threads: 128	10times	Time:814ms	the number of threads: 128	10times	Time:1217ms
the number of threads: 256	10times	Time:803ms	the number of threads: 256	10times	Time:1198ms

-----test threads-----			-----test threads-----		
the number of threads: 2	10times	Time:4094ms	the number of threads: 2	10times	Time:5247ms
the number of threads: 4	10times	Time:2829ms	the number of threads: 4	10times	Time:3484ms
the number of threads: 8	10times	Time:1759ms	the number of threads: 8	10times	Time:2308ms
the number of threads: 16	10times	Time:1712ms	the number of threads: 16	10times	Time:2271ms
the number of threads: 32	10times	Time:1714ms	the number of threads: 32	10times	Time:2226ms
the number of threads: 64	10times	Time:1722ms	the number of threads: 64	10times	Time:2274ms
the number of threads: 128	10times	Time:1727ms	the number of threads: 128	10times	Time:2234ms
the number of threads: 256	10times	Time:1746ms	the number of threads: 256	10times	Time:2288ms

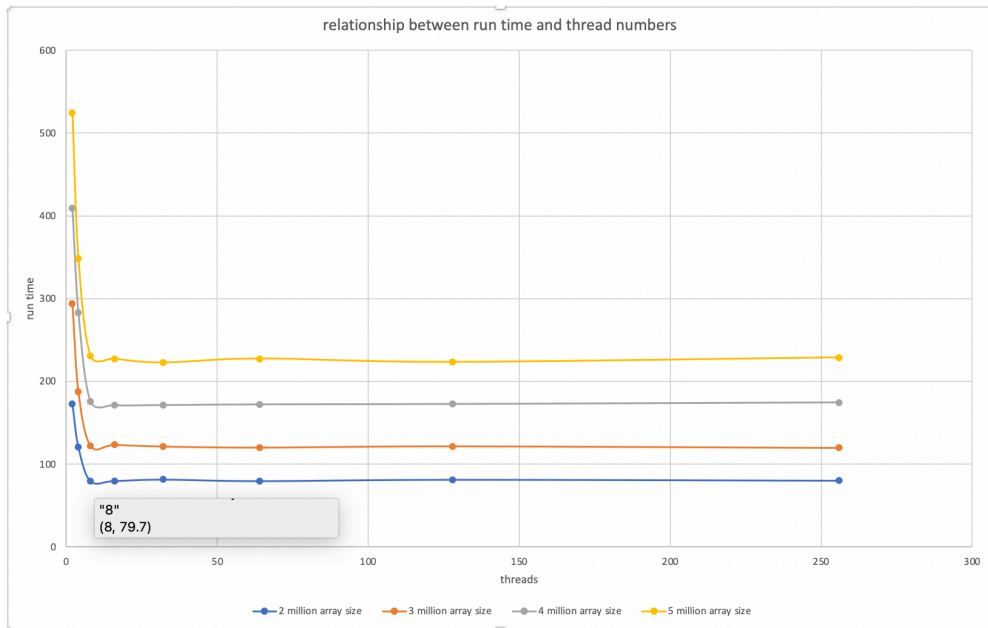
2. Graphical Representation



cutoff / array size	2 million array size	3 million array size	4 million array size	5 million array size
0.255	97.5	163.4	207.7	238.1
0.26	81.6	129.3	173.8	216.6
0.265	80.9	128	177	215.7
0.27	86.3	127.9	171.9	216.3
0.275	86.5	127.5	174.9	215.2
0.28	90.6	127.6	174.7	213.9
0.285	89.9	128.4	179.6	223.8
0.29	84.6	131.9	195.5	226.3
0.295	86.2	132.7	190.2	219.3
0.3	84.7	130.7	183.2	221.3
0.305	81.3	145.7	181.8	223.4
0.31	82.5	143.3	180	223
0.315	87.2	141	177.6	243
0.32	83.8	160.2	181.1	228.7
0.325	83.4	136.7	189.2	228.8
0.33	85	140.7	185.8	228.2
0.335	84.9	138.5	187.2	228.4
0.34	83.8	137.9	174.1	250.7
0.345	84.4	140.3	173.2	242.3
0.35	87.3	139.2	172.5	218.9
0.355	84.1	135.8	172.7	218.3
0.36	93.2	140	175	217.8
0.365	84.2	146.2	172.8	222.5
0.37	87.4	135.9	173.8	222
0.375	84	132.1	173.5	221.4
0.38	83.6	132.1	172.9	229
0.385	92.9	132.9	174.2	229.2
0.39	87.3	131.6	173	211.6
0.395	86.3	131.7	172.8	213.8
0.4	93.1	131	173	210.6
0.405	85.5	129	172.6	213.4
0.41	84.4	128.1	172.8	210.4
0.415	87.1	127.4	180	213
0.42	90.4	127.5	200.2	213
0.425	87.7	128	180.2	214.2
0.43	85.8	128.1	174.3	210.1
0.435	87.2	127.6	178.5	222.1
0.44	86	127.6	190.4	215.5
0.445	93.8	127.3	175.8	211.8
0.45	84.8	128.4	172.1	219
0.455	81.3	127.8	173.6	218.2
0.46	84	127.7	171.6	221.2
0.465	83.9	131.7	170.4	216.7
0.47	81.6	135	171.8	210.5
0.475	90.3	130.4	171.9	206.7
0.48	86.8	128.1	170	213.9
0.485	85.2	130.5	172.6	217.3
0.49	85.8	128.3	176.9	217.6
0.495	88.2	130.4	170.8	216.2
0.5	81.9	129.1	171.2	208.7

I chose cutoff / array size = 0.41 as a relatively good value.

threads	2 million array size	3 million array size	4 million array size	5 million array size
2	172.5	293.9	409.4	524.7
4	120.6	187.6	282.9	348.4
8	79.7	122.4	175.9	230.8
16	79.9	123.3	171.2	227.1
32	81.6	121.5	171.4	222.6
64	79.8	120.2	172.2	227.4
128	81.4	121.7	172.7	223.4
256	80.3	119.8	174.6	228.8



when the thread number is larger than 8, the run time is smaller and starts to flatten.