1. The code of Main:

```
package edu.neu.coe.info6205.symbolTable;
import java.util.Random;
public class test {
   public static void main(String[] args) {
     Random random = new Random(); int value = 1;
     BSTSimple<Integer, Integer> bst;
     //i is the initial number of seeds
     //if operation = 0, choose "put";
     //if operation = 1,choose "delete";
     //if operation = 2,choose "get"
     //the number of operation times are 1000
     for(int j = 100; j \le 2000; j+=20) {
         bst = new BSTSimple<>();
     long averageput = 0;
     long averagedelete = 0;
     long averageget = 0;
     long count0 = 0;
     long count1 = 0;
     long count2 = 0;
     long totaltime0 = 0;
     long totaltime1 = 0;
     long totaltime2 = 0;
      for(int i = 0; i < j; i++) {
            bst.put(i, value);
      for(int ot = 0; ot < j*1000; ot++) {
         int operation = random.nextInt(3);
         int key = random.nextInt(j *2);
     if (operation == 0) {
     long stime0 = System.nanoTime();
     bst.put(key, value);
     long etime0 = System.nanoTime();
     totaltime0 += (etime0 - stime0);
      count0++;
      }
     else if(operation == 1) {
     long stime1 = System.nanoTime();
     bst.delete(key);
     long etime1 = System.nanoTime();
          totaltime1 += (etime1 - stime1);
```

```
count1++;
      }
      else {
      long stime2 = System.nanoTime();
      bst.get(key);
      long etime2 = System.nanoTime();
      totaltime2 += (etime2 - stime2);
      count2++;
      }
      }
      averageput = totaltime0/count0;
      averagedelete = totaltime1/count1;
      averageget = totaltime2/count2;
      System.out.println(j + " "+ averageput + " " +
averagedelete + " " + averageget);
      System.out.println(Math.log(j)+" "+Math.sqrt(j));
   }
}
```

2. The results of code running.

```
540 352 389 259
6.29156913955832 23.2379000772445
560 253 286 182
6.327936783729195 23.664319132398465
580 265 303 187
6.363028103540465 24.08318915758459
600 316 336 217
6.396929655216146 24.49489742783178
620 262 297 188
6.429719478039138 24.899799195977465
640 403 453 281
6.461468176353717 25.298221281347036
660 321 374 228
6.492239835020471 25.69046515733026
680 345 403 244
6.522092798170152 26.076809620810597
700 296 334 210
6.551080335043404 26.457513110645905
720 327 370 229
6.579251212010101 26.832815729997478
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import java.util.Random;
      public class test {
public static void main(String[] args) {
5 <del>-</del> 6 7
                  Random random = new Random(); int value = 1;

BSTSimple<Integer, Integer> bst;

//i is the initial number of seeds

//if operation = 0, choose "put";

//if operation = 1, choose "delete";

//if operation = 2, choose "get"

//the number of operation times are 1000

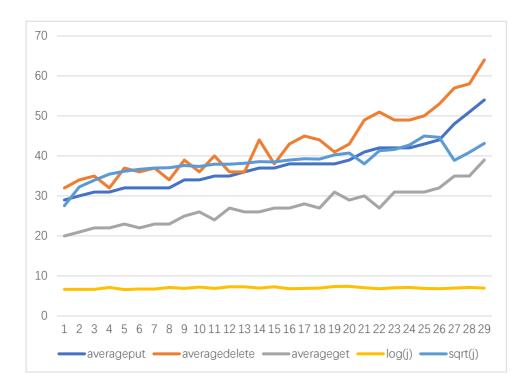
for(int i = 100 i = 2000 i = 2000)
  11
                    for(int i = 100: i <= 2000: i+=20) {
```

This test implements insertion function, delete function, and search function. The number of nodes I randomly generated was 100 and the number of operations was 1000, and then the number of randomly generated nodes was gradually increased. I made 96 tests in all. The number of nodes ranged from 1000 to 2000. The value is between log(n) and n.

Averageput	averagedelete	averageget	log(j)	sqrt(j)
29	32	20	6.63332	27.56811
30	34	21	6.68461	32.28427
31	35	22	6.65929	33.92848
31	32	22	7.138867	35.496478
32	37	23	6.60665	36.20294

32	36	22	6.70931	36.63564
32	37	23	6.75693	36.98275
32	34	23	7.17012	37.05551
34	39	25	6.90775	37.62278
34	36	26	7.24423	37.41657
35	40	24	6.92756	37.93743
35	36	27	7.27239	37.94733
36	36	26	7.28619	38.20994
37	44	26	6.96602	38.55764
37	38	27	7.29981	38.47077
38	43	27	6.80239	39
38	45	28	6.88755	39.30495
38	44	27	6.94698	39.24903
38	41	31	7.39018	40.24922
39	43	29	7.41457	40.7431
41	49	30	7.05618	38.05877
42	51	27	6.82437	41.33152
42	49	31	7.09008	41.64102
42				
	49	31	7.15462	42.77708
43	49 50	31 31	7.154626.86693	42.77708 44.98387
43 44				

51	58	35	7.10661	40.92851
54	64	39	7 00306	43 16625



The search operation is the least complex and the insertion operation is not as complex as the deletion operation. Their complexity are all between $O(N^1/2)$ and $O(\lg N)$, the put and delete operation are tend to $O(N^1/2)$ and the search operation tends to $O(\lg N)$.