

Residual Denoising Diffusion Models

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Abstract

We propose residual denoising diffusion models (RDDM), a novel dual diffusion process that decouples the traditional single denoising diffusion process into residual diffusion and noise diffusion. This dual diffusion framework expands the denoising-based diffusion models, initially uninterpretable for image restoration, into a unified and interpretable model for both image generation and restoration by introducing residuals. Specifically, our residual diffusion represents directional diffusion from the target image to the degraded input image and explicitly guides the reverse generation process for image restoration, while noise diffusion represents random perturbations in the diffusion process. The residual prioritizes certainty, while the noise emphasizes diversity, enabling RDDM to effectively unify tasks with varying certainty or diversity requirements, such as image generation and restoration. We demonstrate that our sampling process is consistent with that of DDPM and DDIM through coefficient transformation, and propose a partially path-independent generation process to better understand the reverse process. Notably, our RDDM enables a generic UNet, trained with only an L1 loss and a batch size of 1, to compete with state-of-the-art image restoration methods. We provide code and pre-trained models to encourage further exploration, application, and development of our innovative framework (<https://github.com/nachifur/RDDM>)

1. Introduction

In real-life scenarios, diffusion often occurs in complex forms involving multiple, concurrent processes, such as the dispersion of multiple gases or the propagation of different types of waves or fields. This leads us to ponder whether the denoising-based diffusion models [51] have limitations in focusing solely on denoising. Current diffusion-

Figure 1. Denoising diffusion process - DDPM (a) and our residual denoising diffusion process (b). For image restoration, we introduce residual diffusion to represent the diffusion direction from the target image to the input image.

-based image restoration methods [39, 48, 49, 82] extend the diffusion model to image restoration tasks by using degraded images as a condition input to implicitly guide the reverse generation process, without modifying the original denoising diffusion process [7, 51]. However, the reverse process starting from noise seems to be unnecessary, as the degraded image is already known. The forward process is non-interpretability for image restoration, as the diffusion process does not contain any information about the degraded image, as shown in Fig. (a).

In this paper, we explore a novel dual diffusion process and propose Residual Denoising Diffusion Models (RDDM), which can tackle the non-interpretability of a single denoising process for image restoration. In RDDM, we decouple the previous diffusion process into residual diffusion and noise diffusion. Residual diffusion prioritizes certainty and represents a directional diffusion from the target image to the conditional input image, and noise diffusion emphasizes diversity and represents random perturbations in the diffusion process. Thus, our RDDM can unify different tasks that require different certainty or diversity, e.g., image generation and restoration. Compared to denoising-based diffusion models for image restoration, the residuals in RDDM clearly indicate the forward diffusion direction and explicitly guide the reverse generation process for image restoration, as shown in Fig. (b).

Specifically, we redefine a new forward process that al-

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Figure 2. Decoupled dual diffusion framework. The previous forward diffusion process is decoupled into residual diffusion and noise diffusion, while in the reverse process, the simultaneous sampling can be decoupled into first removing the residuals and then removing noise.

allows simultaneous diffusion of residuals and noise, wherein the target image progressively diffuses into a purely noisy image for image generation or a noise-carrying input image for image restoration. Unlike the previous denoising diffusion model [7, 51], which uses one coefficient schedule to control the mixing ratio of noise and images, our RDDM employs two independent coefficient schedules to control the diffusion speed of residuals and noise. We found that this independent diffusion property is also evident in the reverse generation process, e.g., readjusting the coefficient schedule within a certain range during testing does not affect the image generation results, and removing the residuals firstly, followed by denoising (see Fig. 2), can also produce semantically consistent images. Our RDDM is compatible with widely used denoising diffusion models, i.e., our sampling process is consistent with that of DDPM [7] and DDIM [51] by transforming coefficient schedules. In addition, our RDDM natively supports conditional inputs, enabling networks trained with only a \bar{a}_t loss and a batch size of 1 to compete with state-of-the-art image restoration methods. We envision that our models can facilitate a unified and interpretable image-to-image distribution transformation methodology, highlighting that residuals and noise are equally important for diffusion models, e.g., the residual prioritizes certainty while the noise emphasizes diversity. The contributions of this paper are summarized as follows:

- We propose a novel dual diffusion framework to tackle the non-interpretability of a single denoising process for image restoration by introducing residuals. Our residual diffusion represents a directional diffusion from the target image to the conditional input image.
- We introduce a partially path-independent generation process that decouples residuals and noise, highlighting their roles in controlling directional residual shift (certainty)

and random perturbation (diversity), respectively.

- We design an automatic objective selection algorithm to choose whether to predict residuals or noise for unknown new tasks.
- Extensive experiments demonstrate that our method can be adapted to different tasks, e.g., image generation, restoration, inpainting and translation, focusing certainty or diversity, and involving paired or unpaired data.

2. Related Work

Denoising diffusion models (e.g., DDPM [7], SGM [52, 53], and DDIM [51]) were initially developed for image generation. Subsequent image restoration methods [39, 48] based on DDPM and DDIM feed a degraded image as a conditional input to a denoising network, e.g., DvSR [49], SR3 [49], and WeatherDiffusion [42], which typically require large sampling steps and batch sizes. Additionally, the reverse process starting from noise in these methods seems unnecessary and inefficient for image restoration tasks. Thus, SDEdit [41], ColdDiffusion [2], InDI [11], and I2SB [29] propose generating a clear image directly from a degraded image or noise-carrying degraded image. InDI [11] and I2SB [29], which also present unified image generation and restoration frameworks, are the most closely related to our proposed RDDM. Specifically, the forward diffusion of InDI, I2SB, and our RDDM consistently employs a mixture of three terms (i.e., input images, target images I_0 , and noise), extending beyond the denoising-based diffusion model [7, 51] which incorporates a mixture of two terms (i.e., I_0 and ϵ). However, InDI [11] and I2SB [29] opt for estimating the target image or its linear transformation term to replace the noise estimation, akin to a special case of our RDDM (SM-Res). In contrast, we introduce residual estimation while also embracing noise for both generation and restoration tasks. Our RDDM can further extend DDPM [7], DDIM [51], InDI [11], and I2SB [29] to independent double diffusion processes, and pave the way for the multi-dimensional diffusion process. We highlight that residuals and noise are equally important, e.g., the residual prioritizes certainty while the noise emphasizes diversity. In addition, our work is related to coefficient schedule design [4, 48], variance strategy optimization [3, 4, 24, 44], superimposed image decomposition [12, 81], curve integration [47], stochastic differential equations [53], and residual learning [5] for image restoration [1, 32, 56, 70, 72, 75]. See Appendix A.5 for detailed comparison.

3. Background

Denoising diffusion models [7, 50] aim to learn a distribution $p(I_0) := \int p(I_{0:T}) dI_{1:T}^1$ to approximate a tar-

¹To understand diffusion from an image perspective, we use x instead of ϵ in DDPM [17].

Figure 3. The proposed residual denoising diffusion model (RDDM) is a unified framework for image generation and restoration (a shadow removal task is shown here). We introduce residuals $\{r_s\}$ in RDDM, redefining the forward diffusion process to involve simultaneous diffusion of residuals and noise. The residuals ($r_s = I_{in} - I_0$) diffusion represents the directional diffusion from the target image to the degraded input image, while the noise (ϵ) diffusion represents the random perturbations in the diffusion process. In RDDM, I_0 gradually diffuses into $I_T = I_{in} + \epsilon$, $\epsilon \sim N(0; I)$. In the third column, I_T is a purely noisy image for image generation since $r_s = 0$, and a noise-carrying degraded image for image restoration as the degraded image.

get data distribution $q(I_0)$, where I_0 are target images and $I_1; \dots; I_T$ ($T = 1000$) are latent images of the same dimension as I_0 . In the forward process, $q(I_0)$ is diffused into a Gaussian noise distribution using a fixed Markov chain,

$$q(I_{1:T}|I_0) := \prod_{t=1}^T q(I_t|I_{t-1}); \quad (1)$$

$$q(I_t|I_{t-1}) := N(I_t; \sqrt{\alpha_t}I_{t-1}; (1 - \alpha_t)I); \quad (2)$$

where $p_{1:T} = \prod_{t=1}^T p(I_t|I_{t-1})$. $q(I_t|I_{t-1})$ can also be written as $I_t = \sqrt{\alpha_t}I_{t-1} + \sqrt{1 - \alpha_t}\epsilon$. In fact, it is simpler to sample I_t from I_0 by reparameterization [25, 26],

$$I_t = \sqrt{\alpha_t}I_0 + \sqrt{1 - \alpha_t}\epsilon; \quad (3)$$

where $\epsilon \sim N(0; I)$; $\alpha_t := \prod_{s=1}^t \alpha_s$. The reverse process is also a Markov chain starting at $p(I_T) = N(I_T; 0; I)$,

$$p(I_{0:T}) := p(I_T) \prod_{t=1}^T p(I_{t-1}|I_t); \quad (4)$$

$$p(I_{t-1}|I_t) := N(I_{t-1}; (I_t; t); \epsilon_t I); \quad (5)$$

where $p(I_{t-1}|I_t)$ is a learnable transfer probability (the variance schedule ϵ_t is fixed). A simplified loss function [17] is derived from the maximum likelihood of I_0 , i.e., $L(\theta) := E_{I_0 \sim q(I_0); \epsilon \sim N(0; I)} \|\epsilon - \epsilon_\theta(I_t; t)\|^2$. The estimated noise ϵ_θ can be used to represent in $p(I_{t-1}|I_t)$, thus I_{t-1} can be sampled from $p(I_{t-1}|I_t)$ step by step.

4. Residual Denoising Diffusion Models

Our goal is to develop a dual diffusion process to unify and interpret image generation and restoration. We modify the representation of $I_T = \epsilon$ in traditional DDPM to $I_T = I_{in} + \epsilon$ in our RDDM, where I_{in} is a degraded image (e.g., a shadow, low-light, or blurred image) for image restoration and is set to 0 for image generation. This modification is compatible with the widely used denoising diffusion model, e.g., $I_T = 0 + \epsilon$ is the pure noise ϵ for generation. For image restoration, I_T is a noisy-carrying degraded image ($I_{in} + \epsilon$), as shown in the third column in Fig. 3.

The modified forward process from I_0 to $I_T = I_{in} + \epsilon$ involves progressively degrading I_0 to I_{in} , and injecting noise ϵ . This naturally results in a dual diffusion process, a residual diffusion to model the transition from I_0 to I_{in} and a noise diffusion. For example, the forward diffusion process from the shadow-free image to the noisy carrying shadow image I_T involves progressively adding shadows and noise, as shown in the second row in Fig. 3.

In the following subsections, we detail the underlying theory and the methodology behind our RDDM. Inspired by residual learning [5, 31, 32], we redefine each forward diffusion process step in Section 4.1. For the reverse process, we present a training objective to predict the residuals and noise injected in the forward process in Section 4.2. In Section 4.3, we propose three sampling methods, i.e., residual prediction (SM-Res), noise prediction (SM-N), and “residual and noise prediction” (SM-Res-N).

4.1. Directional Residual Diffusion Process with Perturbation

To model the gradual degradation of image quality and the increment of noise, we define the single forward process step in our RDDM as follows:

$$I_t = I_{t-1} + I_{res}^t; \quad I_{res}^t \sim N(\epsilon_t I_{res}; \epsilon_t^2 I); \quad (6)$$

where I_{res}^t represents a directional mean shift (residual diffusion) with random perturbation (noise diffusion) from state I_{t-1} to state I_t , the residual I_{res} in I_{res}^t is the difference between I_{in} and I_0 (i.e., $I_{res} = I_{in} - I_0$), and two independent coefficient schedules ϵ and ϵ_t control the residual and noise diffusion, respectively. In fact, it is simpler to sample I_t from I_0 (like Eq. 3),

$$\begin{aligned} I_t &= I_{t-1} + \epsilon_t I_{res} + \epsilon_t \epsilon; \\ &= I_{t-2} + (\epsilon_{t-1} + \epsilon_t) I_{res} + (\epsilon_{t-1}^2 + \epsilon_t^2) \epsilon \\ &= \dots \\ &= I_0 + \epsilon I_{res} + \epsilon \epsilon; \end{aligned} \quad (7)$$

where $\mathbf{t} = 1, \dots, T$, $\mathbf{t} = \frac{P}{i=1} \mathbf{t}$ and $\mathbf{t} = \frac{P}{i=1} \mathbf{t}$. If $\mathbf{t} = T$, $T = 1$ and $\mathbf{t} = \mathbf{I}_{in} + \mathbf{t}$. \mathbf{t} can control the intensity of noise perturbation for image restoration (e.g., $\frac{2}{T} = 0.01$ for shadow removal), while $\frac{2}{T} = 1$ for image generation. From Eq. 6, the joint probability distributions in the forward process can be defined as:

$$q(\mathbf{I}_{1:T} | \mathbf{I}_0; \mathbf{I}_{res}) := \prod_{t=1}^T q(\mathbf{I}_t | \mathbf{I}_{t-1}; \mathbf{I}_{res}); \quad (8)$$

$$q(\mathbf{I}_t | \mathbf{I}_{t-1}; \mathbf{I}_{res}) := N(\mathbf{I}_t; \mathbf{I}_{t-1} + \mathbf{t} \mathbf{I}_{res}; \frac{2}{t} \mathbf{I}); \quad (9)$$

Eq. 7 defines the marginal probability distribution $q(\mathbf{I}_t | \mathbf{I}_0; \mathbf{I}_{res}) = N(\mathbf{I}_t; \mathbf{I}_0 + \mathbf{t} \mathbf{I}_{res}; \frac{2}{t} \mathbf{I})$. In fact, the forward diffusion of our RDDM is a mixture of three terms (i.e., \mathbf{I}_0 , \mathbf{I}_{res} , and \mathbf{I}), extending beyond the widely used denoising diffusion model that is a mixture of two terms, i.e., \mathbf{I}_0 and \mathbf{I} . A similar mixture form of three terms can be seen in several concurrent works, e.g., InDM [28], I2SB [29], IR-SDE [40], and ResShift [67].

4.2. Generation Process and Training Objective

In the forward process (Eq. 7), residuals \mathbf{I}_{res} and noise \mathbf{I} are gradually added to \mathbf{I}_0 , and then synthesized into \mathbf{I}_t , while the reverse process from \mathbf{I}_t to \mathbf{I}_0 involves the estimation of the residuals and noise injected in the forward process. We can train a residual network $\mathbf{f}_{res}(\mathbf{I}_t; \mathbf{t}; \mathbf{I}_{in})$ to predict \mathbf{I}_{res} and a noise network $\mathbf{f}_I(\mathbf{I}_t; \mathbf{t}; \mathbf{I}_{in})$ to estimate \mathbf{I} . Using Eq. 7, we obtain the estimated target images $\mathbf{I}_0 = \mathbf{I}_t - \mathbf{t} \mathbf{I}_{res} - \mathbf{t} \mathbf{I}$. If \mathbf{I}_0 and \mathbf{I}_{res} are given, the generation process is defined as,

$$p(\mathbf{I}_{t-1} | \mathbf{I}_t) := q(\mathbf{I}_{t-1} | \mathbf{I}_t; \mathbf{I}_0; \mathbf{I}_{res}); \quad (10)$$

where the transfer probability $q(\mathbf{I}_{t-1} | \mathbf{I}_t; \mathbf{I}_0; \mathbf{I}_{res})^2$ from \mathbf{I}_t to \mathbf{I}_{t-1} is,

$$q(\mathbf{I}_{t-1} | \mathbf{I}_t; \mathbf{I}_0; \mathbf{I}_{res}) = N(\mathbf{I}_{t-1}; \mathbf{I}_0 + \mathbf{t} \mathbf{I}_{res} + \frac{q}{t-1} \frac{2}{t} \mathbf{I}_t - \frac{(I_0 + \mathbf{t} \mathbf{I}_{res})}{t}, \frac{2}{t} \mathbf{I}); \quad (11)$$

where $\frac{2}{t} = \frac{2}{t} \frac{2}{t-1} = \frac{2}{t}$ and q controls whether the generation process is random ($q = 1$) or deterministic ($q = 0$). Using Eq. 10 and Eq. 11, \mathbf{I}_{t-1} can be sampled from \mathbf{I}_t via:

$$\mathbf{I}_{t-1} = \mathbf{I}_t - \left(\frac{q}{t-1} \frac{2}{t} \mathbf{I}_t - \frac{(I_0 + \mathbf{t} \mathbf{I}_{res})}{t} \right) + \mathbf{t} \mathbf{I}; \quad (12)$$

where $\mathbf{t} \sim N(0; \mathbf{I})$. When $q = 1$, our RDDM has the sum-constrained variance, while DDPM has preserving variance (see Appendix A.4). When $q = 0$ (i.e., $\mathbf{t} = 0$), the sampling process is deterministic,

$$\mathbf{I}_{t-1} = \mathbf{I}_t - \left(\frac{q}{t-1} \frac{2}{t} \mathbf{I}_t - \frac{(I_0 + \mathbf{t} \mathbf{I}_{res})}{t} \right); \quad (13)$$

²Eq. 11 does not change $q(\mathbf{I}_t | \mathbf{I}_0; \mathbf{I}_{res})$ in Appendix A.2.

We derive the following simplified loss function for training (Appendix A.1):

$$L_{res}(\mathbf{I}) := E_h \left[\sum_{i=1}^h \mathbf{I}_{res}(\mathbf{I}_t; \mathbf{t}; \mathbf{I}_{in})^2 \right]; \quad (14)$$

$$L(\mathbf{I}) := E_h \left[\sum_{i=1}^h \mathbf{I}(\mathbf{I}_t; \mathbf{t}; \mathbf{I}_{in})^2 \right]; \quad (15)$$

where the hyperparameters \mathbf{I}_{res} , $2f(0; 1g)$, and the training input image \mathbf{I}_t is synthesized using \mathbf{I}_0 , \mathbf{I}_{res} , and \mathbf{I} by Eq. 7. \mathbf{I}_t can also be synthesized using \mathbf{I}_0 (replaced \mathbf{I}_0 in Eq. 7 by $\mathbf{I}_0 = \mathbf{I}_{in} - \mathbf{I}_{res}$),

$$\mathbf{I}_t = \mathbf{I}_{in} + (\mathbf{t} - 1) \mathbf{I}_{res} + \mathbf{t} \mathbf{I}; \quad (16)$$

4.3. Sampling Method Selection Strategies

For the generation process (from \mathbf{I}_t to \mathbf{I}_{t-1}), \mathbf{I}_t and \mathbf{I}_{in} are known, and thus \mathbf{I}_{res} and \mathbf{I} can represent each other by Eq. 16. From Eq. 14, 15, 16, we propose three sampling methods as follows.

SM-Res. When $\mathbf{I}_{res} = 1$ and $\mathbf{I} = 0$, the residuals \mathbf{I}_{res} are predicted by a network, while the noise is represented as a transformation of \mathbf{I}_{res} using Eq. 16.

SM-N. When $\mathbf{I}_{res} = 0$ and $\mathbf{I} = 1$, the noise is predicted by a network, while the residuals \mathbf{I}_{res} are represented as a transformation of \mathbf{I} using Eq. 16.

SM-Res-N. When $\mathbf{I}_{res} = 1$ and $\mathbf{I} = 1$, both the residuals and the noise are predicted by networks.

To determine the optimal sampling method for real-world applications, we give empirical strategies and automatic selection algorithms in the following.

Empirical Research. Table 1 presents that the SM-Res shows better results for image restoration but offers a poorer FID for generation. On the other hand, the SM-N yields better frechet inception distance (FID in [6]) and inception scores (IS), but is ineffective in image restoration (e.g., PSNR 11.34 for shadow and 16.30 for low-light). This may be due to the inadequacy of using \mathbf{I}_{res} to represent \mathbf{I} in Eq. 16 for restoration tasks. We attribute these inconsistent results to the fact that residual predictions prioritize certainty, whereas noise predictions emphasize diversity. In our experiments, we use SM-N for image generation, SM-Res for low-light (LOL [61]), and SM-Res-N for other image restoration tasks. For an unknown new task, we empirically recommend using SM-N for those requiring greater diversity and SM-Res for tasks that demand higher certainty.

Automatic Objective Selection Algorithm (AOSA). To automatically choose between SM-Res or SM-N for an unknown task, we develop an automatic sampling selection algorithm in Appendix B.2. This algorithm requires only a single network and learns the hyperparameter in Eq. 15, enabling a gradual transition from combined residual and noise training (akin to SM-Res-N) to individual prediction (SM-Res or SM-N). This plug-and-play training strategy requires less than 1000 additional training iterations and is

Sampling Method	Generation (CelebA)		Shadow removal (ISTD)			Low-light (LOL)		Deraining (RainDrop)	
	FID (#)	IS (")	MAE(#)	PSNR(')	SSIM(")	PSNR(')	SSIM(")	PSNR(')	SSIM(")
SM-Res	31.47	1.73	4.76	30.72	0.959	25.39	0.937	31.96	0.9509
SM-N	23.25	2.05	81.01	11.34	0.175	16.30	0.649	19.15	0.7179
SM-Res-N	28.90	1.78	4.67	30.91	0.962	23.90	0.931	32.51	0.9563

Table 1. Sampling method analysis. The sampling steps are 10 on the CelebA [64] dataset, 5 on the ISTD [57] dataset, 2 on the LOL [61] dataset, and 5 on the RainDrop [45] dataset.

fully compatible with the current denoising-based diffusion methods [7]. Our RDDM using AOSA has the potential to provide a unified and interpretable methodology for modeling, training, and inference pipelines for unknown target tasks.

Comparison with Other Prediction Methods. Our SM-N is similar to DDIM [51] (or DDPM [17]), which only estimates the noise, and is consistent with DDPM and DDIM by transforming the coefficient/variance schedules in Eq. 12 (the proof in Appendix A.3),

$$\begin{aligned} \alpha_t &= \frac{\alpha_{t_{\text{DDIM}}}}{\alpha_{t_{\text{DDIM}}}}; \quad \alpha_t = \frac{\alpha_{t_{\text{DDIM}}}}{\alpha_{t_{\text{DDIM}}}}; \\ \beta_t &= \beta_{t_{\text{DDIM}}} \end{aligned} \quad (17)$$

In fact, current research has delved into numerous diffusion forms that extend beyond noise estimation. For example, IDDPM [44] proposes that it is feasible to estimate noise (ϵ), clean target images (I_0), or the mean term (μ) to represent the transfer probabilities (i.e., $|I_t - I_0|$) in Eq. 5). The score-based generative model (SGM) [49] and Schrödinger Bridge (ISB [49]) estimate the score of noisy data (i.e., the sum of residuals and noise $\sum_{t=1}^T I_{\text{res}}^t$). Cold-Diffusion [2] and InDI [11] estimate the clean target images (I_0). Rectified Flow [35] predicts the residuals (ϵ_{res}) to align with the image linear interpolation process without noise diffusion (i.e., $I_T = I_{\text{in}}$). A detailed comparison can be found in Appendix A.5.

These previous/concurrent works choose to estimate the noise, the residual, the target image, or its linear transformation term. In contrast, we introduce residual estimation while also embracing noise for both generation and restoration. Residuals and noise have equal and independent status, which is reflected in the forward process (Eq. 4), the reverse process (Eq. 3), and the loss function (Eq. 5). This independence means that the noise diffusion can even be removed and only the residual diffusion retained to model the image interpolation process (when $\beta = 0$ in Eq. 7, RDDM degenerates to Rectified Flow [35]). In addition, this property derives a decoupled dual diffusion framework in Section 5.

5. Decoupled Dual Diffusion Framework

Upon examining DDPM from the perspective of RDDM, we discover that DDPM indeed involves the simultaneous

Schedules	FID#	IS (")
Linear (DDIM [51])	28.39 ³	2.05
Scaled linear [48]	28.15	2.00
Squared cosine [4]	47.21	2.64
α_t (mean), β_t^2 (mean)	38.35	2.22
α_t (linearly increasing), β_t^2 (linearly increasing)	40.03	2.45
α_t (linearly decreasing), β_t^2 (linearly decreasing)	27.82	2.26
α_t (linearly decreasing), β_t^2 (linearly increasing)	23.25	2.05

Table 2. Coefficient schedules analysis on CelebA (64) [36]. In our RDDM, the residual diffusion and noise diffusion are decoupled, so one may design a better schedule in the decoupled coefficient space, e.g., α_t (linearly decreasing), β_t^2 (linearly increasing). To be fair, all coefficient schedules were retrained using the same network structure, training, and evaluation. The sampling method is SM-N with 10 sampling steps using Eq. 4.

diffusion of residuals and noise, which is evident as Eq. 4 becomes equivalent to Eq. 4 in Appendix A.3. We find that it is possible to decouple these two types of diffusion. Section 5.1 presents a decoupled forward diffusion process. In Section 5.2, we propose a partially path-independent generation process and decouple the simultaneous sampling into first removing the residuals and then removing noise (see Fig. 6(d) and Fig. 17). This decoupled dual diffusion framework sheds light on the roles of deresidual and denoising in the DDPM generation process.

5.1. Decoupled Forward Diffusion Process

Our defined coefficients (α_t ; β_t^2) offer a distinct physical interpretation. In the forward diffusion process (Eq. 4), α_t controls the speed of residual diffusion and β_t^2 regulates the speed of noise diffusion. In the reverse generation process (Eq. 13), α_t and β_t^2 are associated with the speed of removing residual and noise, respectively. In fact, there are no constraints on α_t and β_t^2 in Eq. 7, meaning that the residual diffusion and noise diffusion are independent of each other. Utilizing this decoupled property and the difference between these two diffusion processes, we should be able to design a better coefficient schedule, e.g., (linearly decreasing) and β_t^2 (linearly increasing) in Table 2. This aligns with the intuition that, during the reverse generation pro-

³ $\alpha_{t_{\text{DDIM}}}$ here is α_t of DDIM [51].

⁴Our RDDM is implemented based on the popular diffusion repository github.com/lucidrains/denoising-diffusion-pytorch. Differences in network structure and training details may lead to poorer FID. We have verified sampling consistency with DDIM [51] in Table 3(a) and Appendix A.3.

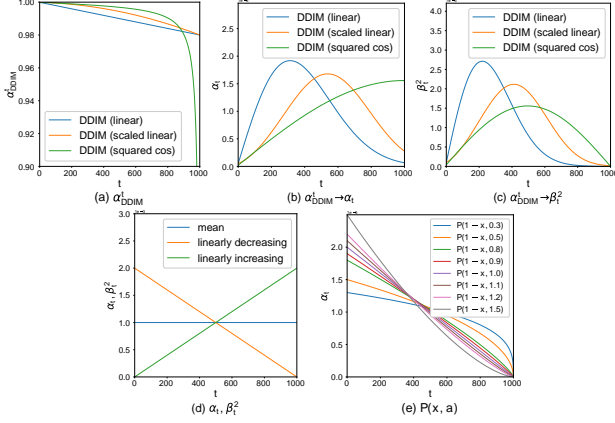


Figure 4. Coefficient transformation from DDIM [51] to RDDM using Eq.17. (a) We show several schedules for t_{DDIM} , e.g., linear [51], scaled linear [48], and squared cosine [41]. (b) We transform t_{DDIM} into t in our RDDM. (c) We transform t_{DDIM} into t^2 in our RDDM. (d) A few simple schedules. (e) $P(x; a)$ is a normalized power function (see Eq.6). "mean", "linearly increasing", and "linearly decreasing" in (d) can be denoted as $P(x; 0)$, $P(x; 1)$ and $P(1 - x; 1)$, respectively. See Algorithm 1 in Appendix A.3 for more details of (b) and (c).

Figure 5. Analysis of readjusting coefficient schedules. We find that changing the t schedule barely affects the denoising process in (f) and edited faces may have higher face scores when assessed using AI face scoring software. These images were generated using a pre-trained UNet on the CelebA-256 dataset [16] with 10 sampling steps.

cess (from T to 0), the estimated residuals become increasingly accurate while the estimated noise should also weaken progressively. Therefore, when t is close to 0, the deresidual pace should be faster and the denoising pace should be slower. Since our t and t^2 represent the speed of diffusion, we name the curve in Fig.4(b-d) the diffusion speed curve

5.2. Partially Path-independent Generation Process

In the original DDPM [17] or DDIM [51], when the t_{DDIM} schedule changes, it is necessary to retrain the denoising network because this alters the diffusion process [44, 48]. As shown in Fig.5(c)(d), directly changing the t_{DDIM} schedule causes denoising to fail. Here, we

propose a path-independent generation process, i.e., modifying the diffusion speed curve does not cause the image generation process to fail. We try to readjust the diffusion speed curve in the generation process. First, we convert the t_{DDIM} schedule of a pre-trained DDIM into the t and t^2 schedules of our RDDM using Eq.7 (from Fig. 5(a) to Fig. 5(b)). We then readjust the converted schedules using the normalized power function $P(x; a)$ in Fig. 5(f), without touching the t^2 schedule that controls noise diffusion, as shown in Fig. 5(f). $P(x; a)$ is defined as a is a parameter of the power function),

$$P(x; a) := x^a = \int_0^1 x^a dx; \text{ where } x = t/T; \quad (18)$$

These schedule modifications shown in Fig. 5 lead to the following key findings.

1. Fig. 5(f) shows that modifying the residual diffusion speed curve (t) leads to a drastic change in the generation results, probably due to t_{res} being represented as a transformation of t using Eq.16.
 2. As the time condition represents the current noise intensity in the denoising network ($(I_t; t; 0)$), modifying the noise diffusion speed curve (t) causes t to deviate from accurately indicating the current noise intensity, leading to denoising failure, as shown in Fig. 5(e).
- Nonetheless, we believe that, corresponding to the decoupled forward diffusion process, there should also be a path-independent reverse generation process. To develop a path-independent generation process, we improve the generation process based on the above two key findings:

1. Two networks are used to estimate t_{res} and t separately, i.e., SM-Res-N-2Net in Appendix B.2.
2. t and t^2 are used for the time conditions embedded in the network, i.e., $I_{res}(I_t; t; 0) \rightarrow I_{res}(I_t; t^2; 0)$, $(I_t; t; 0) \rightarrow (I_t; t^2; 0)$.

These improvements lead to a partially path-independent generation process, as evidenced by the results shown in Fig. 6(c).

Analysis of Partially Path-independence via Green's Theorem. "Path-independence" reminds us of Green's theorem in curve integration [47]. From Eq. 13, we have:

$$I_t - I_{t-1} = (t - t-1)I_{res} + (t - t-1); \quad (19)$$

$$dI(t) = I_{res}(I(t); (t - T); 0)dt + (I(t); (t - T); 0)dt; \quad (20)$$

where $I(t) = I(0) + (t)I_{res} + (t)$. Given inputs $I(t)$ and (t) , the denoising network learns to approximate the noise in $I(t)$ by estimating I_{res} . If this network is trained well and robust enough, it should be able to avoid the interference of

⁵<https://ux.xiaoice.com/beautyv3>

(a) CelebA (FID)		5 steps	10 steps	15 steps	20 steps	100 steps
DDIM		69.60	40.45	32.67	30.61	23.66
DDIM! RDDM		69.60	40.41	32.71	30.77	24.92

(b) Shadow Removal	MAE(#)			SSIM(")			PSNR(")		
	S	NS	ALL	S	NS	ALL	S	NS	ALL
DSC [19]	9.48	6.14	6.67	0.967	-	-	33.45	-	-
FusionNet [3]	7.77	5.56	5.92	0.975	0.880	0.945	34.71	28.61	27.19
BMNet [79]	7.60	4.59	5.02	0.988	0.976	0.959	35.61	32.80	30.28
DMTN [31]	7.00	4.28	4.72	0.990	0.979	0.965	35.83	33.01	30.42
Ours (RDDM)	6.67	4.27	4.67	0.988	0.979	0.962	36.74	33.18	30.91

(c) Low-light	PSNR(")	SSIM(")	LPIPS(#)	(d) Deraining	PSNR(")	SSIM(")
KinD++ [76]	17.752	0.760	0.198	AttnGAN [45]	31.59	0.9170
KinD++-SKF [68]	20.363	0.805	0.201	DuRN [34]	31.24	0.9259
DCC-Net [77]	22.72	0.81	-	RainAttn [46]	31.44	0.9263
SNR-Aware [66]	24.608	0.840	0.151	IDT [64]	31.87	0.9313
LLFlow [59]	25.19	0.93	0.11	RainDiff64 [82]	32.29	0.9422
LLFormer [58]	23.649	0.816	0.169	RainDiff128 [82]	32.43	0.9334
Ours (RDDM)	25.392	0.937	0.116	Ours (RDDM)	32.51	0.9563

Table 3. Quantitative comparison results of image generation on the CelebA 256 256 dataset [16], shadow removal on the ISTD dataset [57], low-light enhancement on the LOLE dataset, and deraining on the RainDrop dataset. "S, NS, ALL" in (b) denote shadow area (S), non-shadow area (NS) and whole image (ALL). The sampling steps are 5 for shadow removal and deraining, 2 for low-light.

Figure 6. Partially path-independent generation process. (a1) We trained a denoising network using the DDIM linear schedule [51]. (a2-a3) We modified the t_1 and t_2 schedules during testing. (b) We trained two networks to remove noise and residuals. In contrast to the sharply varying images in (a2-a3) and the noisy images in (b2-b3), (c) shows that we constructed a path independent generation process where modifications to the diffusion speed curve can generate a noise-free image with little variation in image semantics. (d) The simultaneous sampling in (d1) or (c) can be decomposed into first removing residuals and then noise (d2), or removing noise and then residuals (d3). In (d3), diversity is significantly reduced because noise is removed first.

the residual terms $(t)I_{\text{res}}$ in $I(t)$. This also applies to a robust residual estimation network. Thus, we have

$$\frac{\partial I_{\text{res}}(I(t); (t) T)}{\partial (t)} = 0; \frac{\partial (I(t); (t) T)}{\partial (t)} = 0 \quad (21)$$

If the equation in Formula 21 holds true, it serves as a necessary and sufficient condition for path independence in curve integration, which provides an explanation for why Fig. 6(c) achieves a partially path-independent generation process. The path-independent property is related to the network's resilience to disturbances and applies to disturbances that vary within a certain range. However, excessive disturbances can lead to visual inconsistencies, e.g., readjusting t_1 and t_2 to $P(x; 5)$. Thus, we refer to this generative property as partially path-independent. We also investigated two reverse paths to gain insight into the implications of the proposed partial path independence. In the first case, the residuals are removed first, followed by

the noise: $I(T) \xrightarrow{!_{\text{res}}} I(0) + \tau \xrightarrow{!^T} I(0)$. The second case involves removing the noise first and then the residuals: $I(T) \xrightarrow{!^T} I_{\text{in}} \xrightarrow{!_{\text{res}}} I(0)$. The first case (Fig 6(d2)) shows

6. Experiments

Image Generation. We can convert a pre-trained DDIM [51] to RDDM by coefficient transformation using Eq. 17, and generate images by Eq. 12. Table 3(a) verifies that the quality of the generated images before and after the conversion is nearly the same. We show the generated face images with 10 sampling steps in Fig 7(a).

Image Restoration. We extensively evaluate our method on several image restoration tasks, including shadow removal, low-light enhancement, deraining, and deblurring on 5 datasets. Notably, our RDDM uses an identical UNet and is trained with a batch size of 1 for all these tasks. In contrast, SOAT methods often involve elaborate network architectures, such as multi-stage [59, 80], multi-branch [10], Transformer [58], and GAN [27], or sophisticated loss functions like the chromaticity [80], texture similarity [74], and edge loss [70]. Table 3 and Fig. 7(b-c) show that our RDDM is competitive with the SOTA restoration

⁶<https://huggingface.co/google/ddpm-celebahq-256>

⁷The subtle differences in larger sampling steps may stem from errors introduced by numerical representation limitations during coefficient transformation, which may accumulate and amplify in larger sampling steps.

Figure 7. Application of our RDDM. (a) Image generation on the CelebA dataset [51]. (b) Shadow removal on the ISTD dataset [57]. (c) Low-light enhancement on the LOL dataset [61]. (d) Image inpainting (center and irregular mask). (e) The image translation process can be regarded as first translating the semantics and then generating the details. These images in (b) are magnified using Multiviewer [68].

tion methods. See Appendix B for more training details and comparison results. validates our RDDM.

We extend DDPM [17]/DDIM [51], initially uninterpretable for image restoration, into a unified and interpretable diffusion model for both image generation and restoration by introducing residuals. However, the residual diffusion process represents the directional diffusion from target images to conditional input images, which does not involve a priori information about the image restoration task, and therefore is not limited to it. Beyond image generation and restoration, we show examples of image inpainting and image translation to verify that our RDDM has the potential to be a unified and interpretable methodology for image-to-image distribution transformation. We do not intend to achieve optimal performance on all tasks by tuning all hyperparameters. The current experimental results show that RDDM 1) achieves consistent image generation performance with DDIM after coefficient transformation, 2) competes with state-of-the-art image restoration methods using a generic UNet with only an ℓ_1 loss, a batch size of 1, and fewer than 5 sampling steps, and 3) has satisfactory visual results of image inpainting and image translation (see Fig. 7(d-e), Fig. 14, or Fig. 15 in Appendix B.3), which

7. Conclusions

We present a unified dual diffusion model called Residual Denoising Diffusion Models (RDDM) for image restoration and image generation. This is a three-term mixture framework beyond the previous denoising diffusion framework with two-term mixture. We demonstrate that our sampling process is consistent with that of DDPM and DDIM through coefficient schedule transformation, and propose a partially path-independent generation process. Our experimental results on four different image restoration tasks show that RDDM achieves SOTA performance in no more than five sampling steps. We believe that our model and framework hold the potential to provide a unified methodology for image-to-image distribution transformation and pave the way for the multi-dimensional diffusion process.

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