

W = emgr(f, g, s, t, w, pr, nf, ut, us, xs, um, xm);

emgr – Empirical Gramian Framework (Version 3.9)

Mandatory Arguments

f	System Vector Field	(Function Handle)	$\mathbf{x} = \mathbf{f}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{f} = @(x,u,p) \mathbf{A}*\mathbf{x} + \mathbf{B}*\mathbf{u} + \mathbf{F}*\mathbf{p};$
g	Output Functional	(Function Handle)	$\mathbf{y} = \mathbf{g}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{g} = @(x,u,p) \mathbf{C}*\mathbf{x} + \mathbf{D}*\mathbf{u};$
		1	$\mathbf{y} = \mathbf{x}$	
s	System Dimensions	(Vector)	$\mathbf{s} = [\mathbf{J}, \mathbf{N}, \mathbf{o}]$	(Inputs, States, Outputs)
t	Time	(Vector)	$\mathbf{t} = [\mathbf{h}, \mathbf{T}]$	(Step, Stop)
w	Gramian Type	(Character)		
		'c'	Empirical Controllability Gramian (returns WC)	
		'o'	Empirical Observability Gramian (returns WO)	
		'x'	Empirical Cross Gramian (returns WX)	
		'y'	Empirical Linear Cross Gramian (returns WY)	
		's'	Empirical Sensitivity Gramian (returns WS = { WC , WS })	
		'i'	Empirical Identifiability Gramian (returns WI = { WO , WI })	
		'j'	Empirical Joint Gramian (returns WJ = { WX , WI })	

Optional Arguments

pr	Parameters	(Vector)	Column Vector of System Parameters (Default: pr = 0)	
		(Matrix)	Set of Parameter Column Vectors ('s','i','j' requires two)	
nf	Options	(Vector)	Ten Components (Default: nf = 0), see Option Flags	
ut	Input Function	(Scalar)	Uniformly Scaled Impulse Input (Default: ut = 1)	
		(Vector)	Individual Scaled Impulse Input (J x 1)	
		(Matrix)	Discrete Input Function (J x (T-S)/h)	
		(Function Handle)	Function Handle (u = ut(t))	
		∞	Chirp Function	
us	Steady-State Input	(Scalar)	Uniform Steady-State Input (Default: us = 0)	
		(Vector)	Individual Steady-State Input (J x 1)	
xs	Steady State	(Scalar)	Uniform Steady State (Default: xs = 0)	
		(Vector)	Individual Steady States (N x 1)	
um	Input Scales	(Scalar)	Uniform Maximum Input Scales (Default: um = 1)	
		(Vector)	Individual Maximum Input Scales (J x 1)	
		(Matrix)	Custom Input Scales (J x *)	
xm	Steady-State Scales	(Scalar)	Uniform Maximum Steady State Scales (Default: xm = 1)	
		(Vector)	Individual Maximum Steady-State Scales (N x 1)	
		(Matrix)	Custom Steady-State Scales (N x *)	

Option Flags

nf (1)	Trajectory Centering			
	0	None (Default)		
	1	Initial State		
	2	Final Steady State		
	3	Arithmetic Average		
	4	Median		
	5	Midrange		
	6	Root-Mean-Squared		
nf (2)	Input Scale Sequence			
	0	Linear (Default)		
	1	Logarithmic		
	2	Geometric		
	3	Single		
	4	Sparse		
nf (3)	State Scale Sequence			
	0	Linear (Default)		
	1	Logarithmic		
	2	Geometric		
	3	Single		
	4	Sparse		
nf (4)	Input Transformation			
	0	Unit (Default)		
	1	Inverse		
	2	Dyadic		
	3	Single		
nf (5)	State Transformation			
	0	Unit (Default)		
	1	Inverse		
	2	Dyadic		
	3	Single		
nf (6)	Preconditioning			
	0	None (Default)		
	1	Jacobi (Double Run)		
	2	Steady-State Scaled		
nf (7)	Non-Symmetric Cross Gramian			
	0	Off (Default)		
	1	Non-Sym. Cross-Gramian (WX , WJ only)		
nf (8)	Robust Parameters			
	0	Off (Default)		
	1	Treat Parameters as Inputs		
nf (9)	Parameter Action			
	0	Active Parameters		
	1	Passive Parameters		
nf (10)	Center Parameter Scales			
	0	No Centering		
	1	Mean Centered Parameters		
	2	Logarithmic Centered Parameters		
nf (11)	Exclusive Options			
	0	None (Default)		
	1	Root-Mean-Square-Centering (WS only)		
	1	Schur Complement (WI only)		
	1	Detailed Schur Complement (WJ only)		
nf (12)	Gramian Symmetry			
	0	Assume Symmetry		
	1	Enforce Symmetry		

Custom Solver

Set global variable **ODE** to solver function handle with signature: **y = solver(f,g,t,x,u,p);**
default solver: 2nd Order Ralston's Runge-Kutta

Minimal Usage: W = emgr(f,g,s,t,w);

About Info: V = emgr('version');

More info at: <http://gramian.de>