

W = emgr(f, g, s, t, w, pr, nf, ut, us, xs, um, xm);

emgr – Empirical Gramian Framework (Version 4.0)

Mandatory Arguments

f	System Vector Field	(Function Handle)	$\mathbf{x} = \mathbf{f}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{f} = @(\mathbf{x}, \mathbf{u}, \mathbf{p}) \mathbf{A}*\mathbf{x} + \mathbf{B}*\mathbf{u} + \mathbf{F}*\mathbf{p};$
g	Output Functional	(Function Handle)	$\mathbf{y} = \mathbf{g}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{g} = @(\mathbf{x}, \mathbf{u}, \mathbf{p}) \mathbf{C}*\mathbf{x} + \mathbf{D}*\mathbf{u};$
			1	$\mathbf{y} = \mathbf{x}$
s	System Dimensions	(Vector)	$\mathbf{s} = [\mathbf{J}, \mathbf{N}, \mathbf{o}]$	(Inputs, States, Outputs)
t	Time	(Vector)	$\mathbf{t} = [\mathbf{h}, \mathbf{T}]$	(Step, Stop)
w	Gramian Type	(Character)		
			'c'	Empirical Controllability Gramian (returns WC)
			'o'	Empirical Observability Gramian (returns WO)
			'x'	Empirical Cross Gramian (returns WX)
			'y'	Empirical Linear Cross Gramian (returns WY)
			's'	Empirical Sensitivity Gramian (returns {WC,WS})
			'i'	Empirical Identifiability Gramian (returns {WO,WI})
			'j'	Empirical Joint Gramian (returns {WX,WI})

Optional Arguments

pr	Parameters	(Vector)	Column Vector of System Parameters (Default: pr = 0)
		(Matrix)	Set of Parameter Column Vectors ('s','i','j' requires two)
nf	Options	(Vector)	Ten Components (Default: nf = 0), see Option Flags
ut	Input Function	(Scalar)	Uniformly Scaled Impulse Input (Default: ut = 1)
		(Vector)	Individual Scaled Impulse Input (J x 1)
		(Matrix)	Discrete Input Function (J x (T-S)/h)
		(Function Handle)	Function Handle (u = ut(t))
		∞	Chirp Function
us	Steady-State Input	(Scalar)	Uniform Steady-State Input (Default: us = 0)
		(Vector)	Individual Steady-State Input (J x 1)
xs	Steady State	(Scalar)	Uniform Steady State (Default: xs = 0)
		(Vector)	Individual Steady States (N x 1)
um	Input Scales	(Scalar)	Uniform Maximum Input Scales (Default: um = 1)
		(Vector)	Individual Maximum Input Scales (J x 1)
		(Matrix)	Custom Input Scales (J x *)
xm	Steady-State Scales	(Scalar)	Uniform Maximum Steady State Scales (Default: xm = 1)
		(Vector)	Individual Maximum Steady-State Scales (N x 1)
		(Matrix)	Custom Steady-State Scales (N x *)

Option Flags

nf (1)	Trajectory Centering		
	0	None (Default)	
	1	Initial State	
	2	Final Steady State	
	3	Arithmetic Average	
	4	Root-Mean-Squared	
nf (2)	Input Scale Sequence		
	0	Single (Default)	
	1	Linear	
	2	Geometric	
	3	Logarithmic	
	4	Sparse	
nf (3)	State Scale Sequence		
	0	Single (Default)	
	1	Linear	
	2	Geometric	
	3	Logarithmic	
	4	Sparse	
nf (4)	Input Transformation		
	0	Unit (Default)	
	1	Inverse	
nf (5)	State Transformation		
	0	Unit (Default)	
	1	Inverse	
nf (6)	Preconditioning		
	0	None (Default)	
	1	Jacobi (Double Run)	
	2	Steady-State Scaled	
nf (7)	Non-Symmetric Cross Gramian (WX,WY,WJ only)		
	0	Off (Default)	
	1	Non-Sym. Cross-Gramian	
nf (8)	Parameter Action (WS,WI,WJ only)		
	0	Active Parameters (Default)	
	1	Passive Parameters	
nf (9)	Center Param. Scales (WS,WI,WJ only)		
	0	No Centering (Default)	
	1	Arithmetic Mean Centering	
	2	Geometric Mean Centering	
nf (10)	Schur complement Options (WI,WJ only)		
	0	Approx. Schur-Complement (Default)	
	1	Detailed Schur-Complement	

Custom Solver

Set global variable **ODE** to solver function handle with signature: **y = solver(f,g,t,x,u,p);**
default solver: 2nd Order Heun's Runge-Kutta

Custom Inner Product

Set global variable **DOT** to kernel handle with signature: **w = kernel(x,y);**
default kernel: Identity

Minimal Usage: W = emgr(f,g,s,t,w);

About Info: V = emgr('version');
