

W = emgr(f, g, s, t, w, pr, nf, ut, us, xs, um, xm);

emgr – Empirical Gramian Framework (Version 3.6)

Mandatory Arguments

f	System Vector Field	(Function Handle) $\mathbf{x} = \mathbf{f}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{f} = @(\mathbf{x}, \mathbf{u}, \mathbf{p}) \mathbf{A}*\mathbf{x} + \mathbf{B}*\mathbf{u} + \mathbf{F}*\mathbf{p};$
g	Output Functional	(Function Handle) $\mathbf{y} = \mathbf{g}(\mathbf{x}, \mathbf{u}, \mathbf{p})$	i.e.: $\mathbf{g} = @(\mathbf{x}, \mathbf{u}, \mathbf{p}) \mathbf{C}*\mathbf{x} + \mathbf{D}*\mathbf{u};$
		1	$\mathbf{y} = \mathbf{x}$
s	System Dimensions	(Vector)	$\mathbf{s} = [\mathbf{J}, \mathbf{N}, \mathbf{o}]$ (Inputs, States, Outputs)
t	Time	(Vector)	$\mathbf{t} = [\mathbf{s}, \mathbf{h}, \mathbf{T}]$ (Start, Step, Stop)
w	Gramian Type	(Character)	
		'c'	Empirical Controllability Gramian (returns WC)
		'o'	Empirical Observability Gramian (returns WO)
		'x'	Empirical Cross Gramian (returns WX)
		'y'	Empirical Linear Cross Gramian (returns WY)
		's'	Empirical Sensitivity Gramian (returns WS = { WC , WS })
		'i'	Empirical Identifiability Gramian (returns WI = { WO , WI })
		'j'	Empirical Joint Gramian (returns WJ = { WX , WI })

Optional Arguments

pr	Parameters	(Vector)	Column Vector of System Parameters (Default: pr = 0)
		(Matrix)	Set of Parameter Column Vectors ('s', 'i', 'j' require two)
nf	Options	(Vector)	Ten Components (Default: nf = 0), see Option Flags
ut	Input Function	(Scalar)	Uniformly Scaled Impulse Input (Default: ut = 1)
		(Vector)	Individual Scaled Impulse Input (J x 1)
		(Matrix)	Discrete Input Function (J x (T-S)/h)
		(Function Handle)	Function Handle (u = ut(t))
		∞	Chirp Function
us	Steady-State Input	(Scalar)	Uniform Steady-State Input (Default: us = 0)
		(Vector)	Individual Steady-State Input (J x 1)
xs	Steady State	(Scalar)	Uniform Steady State (Default: xs = 0)
		(Vector)	Individual Steady States (N x 1)
um	Input Scales	(Scalar)	Uniform Maximum Input Scales (Default: um = 1)
		(Vector)	Individual Maximum Input Scales (J x 1)
		(Matrix)	Custom Input Scales (J x *)
xm	Steady-State Scales	(Scalar)	Uniform Maximum Steady State Scales (Default: xm = 1)
		(Vector)	Individual Maximum Steady-State Scales (N x 1)
		(Matrix)	Custom Steady-State Scales (N x *)

Option Flags

nf (1)	Trajectory Centering
0	None (Default)
1	Initial State
2	Final Steady State
3	Arithmetic Average
4	Median
5	Midrange
6	Root-Mean-Squared
nf (2)	Input Scale Sequence
0	Linear (Default)
1	Logarithmic
2	Geometric
3	Single
4	Sparse
nf (3)	State Scale Sequence
0	Linear (Default)
1	Logarithmic
2	Geometric
3	Single
4	Sparse
nf (4)	Input Transformation
0	Unit (Default)
1	Inverse
2	Dyadic
3	Single
nf (5)	State Transformation
0	Unit (Default)
1	Inverse
2	Dyadic
3	Single

nf (6)	Preconditioning
0	None (Default)
1	Jacobi (Double Run)
2	Steady-State Scaled
nf (7)	Non-Symmetric Cross Gramian
0	Off (Default)
1	Non-Sym. Cross-Gramian (WX, WJ only)
nf (8)	Robust Parameters
0	Off (Default)
1	Treat Parameters as Inputs
nf (9)	Center Parameter Scales
0	Mean Centered Parameters
1	Logarithmic Centered Parameters
nf (10)	Exclusive Options
0	None (Default)
1	Mean-Centering (WS only)
1	Detailed Identifiability (WI only)
1	do not symmetrize WX (WX, WJ only)

Custom Solver

Set global variable **ODE** to solver function handle with signature: **y** = **solver(f,g,h,T,x,u,p);**
default solver: 2nd Order Ralston's Runge-Kutta

Minimal Usage: W = emgr(f,g,s,t,w);

About Info: V = emgr('version');

More Info, Examples and Download at:

<http://gramian.de>

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