

1 Canonical ensemble of an incompressible AB diblock copolymer melt

1.1 Notation and microscopic degrees of freedom

We consider a melt of n identical AB diblock copolymers in a volume V at temperature T . Each chain is described by a space curve $\mathbf{R}_j(s)$ ($j = 1, \dots, n$) parametrized by the contour variable $s \in [0, N]$, where

- N is the total number of segments (monomers) per chain,
- f is the A-block fraction, so $s \in [0, fN]$ is type A and $s \in [fN, N]$ is type B,
- b is the statistical segment length,
- the mean total segment density is

$$\rho_0 = \frac{nN}{V} = \frac{1}{v_0}, \quad (1)$$

with v_0 the (reference) segment volume.

- \mathbf{R}^{nN} is the short notation of $[\mathbf{R}_1(s), \mathbf{R}_2(s), \dots, \mathbf{R}_n(s)]$

The canonical partition function (including the standard $n!$ and thermal wavelength prefactor) is written as

$$Z_c(n, V, T) = \frac{1}{n! (\lambda_T^3)^{nN}} \prod_{j=1}^n \int \mathcal{D}\mathbf{R}_j \exp[-\beta U_0[\mathbf{R}^{nN}] - \beta U_1[\mathbf{R}^{nN}]] \delta[\hat{\rho}_A + \hat{\rho}_B - \rho_0], \quad (2)$$

where $\beta = (k_B T)^{-1}$ and $\delta[\dots]$ is a functional delta enforcing incompressibility. Here $\hat{\rho}_A, \hat{\rho}_B$ are the microscopic (operator-valued) segment densities defined below.

1.2 Step 1: Chain model (continuous Gaussian chain)

For the continuous Gaussian chain model,

$$\beta U_0[\mathbf{R}^{nN}] = \frac{3}{2b^2} \sum_{j=1}^n \int_0^N \left| \frac{d\mathbf{R}_j(s)}{ds} \right|^2 ds. \quad (3)$$

1.3 Step 2: Flory–Huggins interaction and contact potential

Assume (as in your notes) that A segments interact only with B segments, through a pair potential $u(|\mathbf{r} - \mathbf{r}'|)$. Then

$$\beta U_1[\mathbf{R}^{nN}] = \sum_{j=1}^n \sum_{k=1}^n \int_0^{fN} ds \int_{fN}^N ds' u(|\mathbf{R}_j(s) - \mathbf{R}_k(s')|). \quad (4)$$

Choose the standard contact form

$$u(r) = v_0 \chi_{AB} \delta(r), \quad (5)$$

so the interaction becomes local in space. Introduce the microscopic densities

$$\hat{\rho}_A(\mathbf{r}) \equiv \sum_{j=1}^n \int_0^{fN} ds \delta(\mathbf{r} - \mathbf{R}_j(s)), \quad (6)$$

$$\hat{\rho}_B(\mathbf{r}) \equiv \sum_{j=1}^n \int_{fN}^N ds \delta(\mathbf{r} - \mathbf{R}_j(s)). \quad (7)$$

Using the contact form (5), Eq. (4) reduces to

$$\beta U_1[\mathbf{R}^{nN}] = v_0 \chi_{AB} \int d\mathbf{r} \hat{\rho}_A(\mathbf{r}) \hat{\rho}_B(\mathbf{r}). \quad (8)$$

1.4 Step 3: Insert identities to introduce collective density fields

We now insert functional identities (one for each species density):

$$1 = \int \mathcal{D}\rho_A \delta[\rho_A - \hat{\rho}_A], \quad 1 = \int \mathcal{D}\rho_B \delta[\rho_B - \hat{\rho}_B]. \quad (9)$$

Inserting (9) into (2) gives

$$\begin{aligned} Z_c(n, V, T) &= \frac{1}{n! (\lambda_T^3)^{nN}} \prod_{j=1}^n \int \mathcal{D}\mathbf{R}_j \int \mathcal{D}\rho_A \int \mathcal{D}\rho_B \exp[-\beta U_0 - \beta U_1] \\ &\quad \times \delta[\hat{\rho}_A + \hat{\rho}_B - \rho_0] \delta[\rho_A - \hat{\rho}_A] \delta[\rho_B - \hat{\rho}_B]. \end{aligned} \quad (10)$$

1.5 Step 4: Use the delta constraints

Because $\delta[\rho_A - \hat{\rho}_A]$ and $\delta[\rho_B - \hat{\rho}_B]$ enforce $\rho_\alpha = \hat{\rho}_\alpha$ inside the functional integral, we may replace

$$\delta[\hat{\rho}_A + \hat{\rho}_B - \rho_0] \rightarrow \delta[\rho_A + \rho_B - \rho_0], \quad v_0 \chi_{AB} \int d\mathbf{r} \hat{\rho}_A \hat{\rho}_B \rightarrow v_0 \chi_{AB} \int d\mathbf{r} \rho_A \rho_B. \quad (11)$$

Then (10) becomes

$$\begin{aligned} Z_c(n, V, T) &= \frac{1}{n! (\lambda_T^3)^{nN}} \prod_{j=1}^n \int \mathcal{D}\mathbf{R}_j \int \mathcal{D}\rho_A \int \mathcal{D}\rho_B \exp[-\beta U_0[\mathbf{R}^{nN}]] \exp\left[-v_0 \chi_{AB} \int d\mathbf{r} \rho_A \rho_B\right] \\ &\quad \times \delta[\rho_A + \rho_B - \rho_0] \delta[\rho_A - \hat{\rho}_A] \delta[\rho_B - \hat{\rho}_B]. \end{aligned} \quad (12)$$

1.6 Step 5: Fourier representations of the functional deltas (introduce new fields)

Use the (formal) Fourier representation of a functional delta:

$$\delta[F] = \int \mathcal{D}w \exp\left(i \int d\mathbf{r} w(\mathbf{r}) F(\mathbf{r})\right). \quad (13)$$

Apply (13) to each constraint:

$$\delta[\rho_A - \hat{\rho}_A] = \int \mathcal{D}w_A \exp\left(i \int d\mathbf{r} w_A(\mathbf{r}) [\rho_A(\mathbf{r}) - \hat{\rho}_A(\mathbf{r})]\right), \quad (14)$$

$$\delta[\rho_B - \hat{\rho}_B] = \int \mathcal{D}w_B \exp\left(i \int d\mathbf{r} w_B(\mathbf{r}) [\rho_B(\mathbf{r}) - \hat{\rho}_B(\mathbf{r})]\right), \quad (15)$$

$$\delta[\rho_A + \rho_B - \rho_0] = \int \mathcal{D}\Xi \exp\left(i \int d\mathbf{r} \Xi(\mathbf{r}) [\rho_A(\mathbf{r}) + \rho_B(\mathbf{r}) - \rho_0]\right). \quad (16)$$

Substitute into (12) and group terms into (i) polymer-coordinate dependent pieces (containing $\hat{\rho}_A, \hat{\rho}_B$) and (ii) purely collective-field pieces:

$$\begin{aligned} Z_c(n, V, T) &= \frac{1}{n! (\lambda_T^3)^{nN}} \prod_{j=1}^n \int \mathcal{D}\mathbf{R}_j \exp[-\beta U_0[\mathbf{R}^{nN}]] \exp\left(-i \int d\mathbf{r} w_A \hat{\rho}_A - i \int d\mathbf{r} w_B \hat{\rho}_B\right) \\ &\quad \times \int \mathcal{D}\rho_A \mathcal{D}\rho_B \mathcal{D}w_A \mathcal{D}w_B \mathcal{D}\Xi \exp\left[-v_0 \chi_{AB} \int d\mathbf{r} \rho_A \rho_B\right] \\ &\quad \times \exp\left[i \int d\mathbf{r} \left(w_A \rho_A + w_B \rho_B + \Xi(\rho_A + \rho_B - \rho_0)\right)\right]. \end{aligned} \quad (17)$$

1.7 Step 6: Reduce the polymer-coordinate integrals to a single-chain partition function

First rewrite the microscopic coupling to w_A, w_B explicitly in terms of chain coordinates:

$$\int d\mathbf{r} w_A(\mathbf{r}) \hat{\rho}_A(\mathbf{r}) = \sum_{j=1}^n \int_0^{fN} ds w_A(\mathbf{R}_j(s)), \quad (18)$$

$$\int d\mathbf{r} w_B(\mathbf{r}) \hat{\rho}_B(\mathbf{r}) = \sum_{j=1}^n \int_{fN}^N ds w_B(\mathbf{R}_j(s)). \quad (19)$$

Therefore the polymer-coordinate factor in (17) becomes

$$\prod_{j=1}^n \int d\mathbf{R}_j \exp \left[-\frac{3}{2b^2} \int_0^N \left| \frac{d\mathbf{R}_j}{ds} \right|^2 ds - i \int_0^{fN} ds w_A(\mathbf{R}_j(s)) - i \int_{fN}^N ds w_B(\mathbf{R}_j(s)) \right]. \quad (20)$$

Because the chains are independent given the fields, this product factorizes:

$$\prod_{j=1}^n Z_{\text{chain}}[iw_A, iw_B] = (Z_{\text{chain}}[iw_A, iw_B])^n, \quad (21)$$

where the *single-chain partition function in the external fields* is

$$Z_{\text{chain}}[iw_A, iw_B] \equiv \int d\mathbf{R} \exp \left[-\frac{3}{2b^2} \int_0^N \left| \frac{d\mathbf{R}(s)}{ds} \right|^2 ds - i \int_0^{fN} ds w_A(\mathbf{R}(s)) - i \int_{fN}^N ds w_B(\mathbf{R}(s)) \right]. \quad (22)$$

Also define the ideal-chain (no external fields) partition function

$$Z_0 \equiv \int d\mathbf{R} \exp \left[-\frac{3}{2b^2} \int_0^N \left| \frac{d\mathbf{R}(s)}{ds} \right|^2 ds \right]. \quad (23)$$

Following your notes, introduce the *normalized* single-chain partition function

$$Q[iw_A, iw_B] \equiv \frac{Z_{\text{chain}}[iw_A, iw_B]}{Z_0}. \quad (24)$$

Thus, the polymer-coordinate contribution equals $(Z_0 Q[iw_A, iw_B])^n$.

1.8 Step 7: Rewrite Z_c as a field theory and define the effective Hamiltonian

Insert $(Z_0 Q)^n$ into (17). Then

$$Z_c(n, V, T) = \frac{Z_0^n}{n! (\lambda_T^3)^{nN}} \int d\rho_A d\rho_B dw_A dw_B d\Xi \exp \left[-\beta H[iw_A, iw_B, \rho_A, \rho_B, \Xi] \right], \quad (25)$$

with the effective Hamiltonian functional

$$\begin{aligned} \beta H[iw_A, iw_B, \rho_A, \rho_B, \Xi] = & v_0 \chi_{AB} \int d\mathbf{r} \rho_A(\mathbf{r}) \rho_B(\mathbf{r}) \\ & - i \int d\mathbf{r} [w_A(\mathbf{r}) \rho_A(\mathbf{r}) + w_B(\mathbf{r}) \rho_B(\mathbf{r}) + \Xi(\mathbf{r}) (\rho_A(\mathbf{r}) + \rho_B(\mathbf{r}) - \rho_0)] \\ & - n \ln Q[w_A, w_B]. \end{aligned} \quad (26)$$

1.9 Step 8: Mean-field (SCFT) saddle point equations

In SCFT (mean-field), we evaluate (25) by the saddle point of H :

$$\left. \frac{\delta \beta H}{\delta X(\mathbf{r})} \right|_* = 0, \quad X \in \{w_A(\mathbf{r}), w_B(\mathbf{r}), \rho_A(\mathbf{r}), \rho_B(\mathbf{r}), \Xi(\mathbf{r})\}. \quad (27)$$

(a) Variations with respect to w_A, w_B : densities from $\ln Q$. From (26),

$$\frac{\delta \beta H}{\delta w_A(\mathbf{r})} = -i\rho_A(\mathbf{r}) - n \frac{\delta \ln Q}{\delta w_A(\mathbf{r})}, \quad \frac{\delta \beta H}{\delta w_B(\mathbf{r})} = -i\rho_B(\mathbf{r}) - n \frac{\delta \ln Q}{\delta w_B(\mathbf{r})}. \quad (28)$$

Setting these to zero yields

$$\rho_A^*(\mathbf{r}) = in \left. \frac{\delta \ln Q}{\delta w_A(\mathbf{r})} \right|_*, \quad \rho_B^*(\mathbf{r}) = in \left. \frac{\delta \ln Q}{\delta w_B(\mathbf{r})} \right|_*. \quad (29)$$

To make (29) explicit, introduce the standard chain propagators. Define the forward propagator $q(\mathbf{r}, s)$ as the statistical weight density of a chain segment at position \mathbf{r} at contour length s , in the external fields. It satisfies the modified diffusion equation

$$\frac{\partial q}{\partial s} = \frac{b^2}{6} \nabla^2 q - i w_\alpha(\mathbf{r}) q, \quad q(\mathbf{r}, 0) = 1, \quad (30)$$

where $\alpha = A$ for $0 \leq s \leq fN$ and $\alpha = B$ for $fN \leq s \leq N$. Similarly, define the backward propagator $q^\dagger(\mathbf{r}, s)$ (from the chain end) by

$$\frac{\partial q^\dagger}{\partial s} = \frac{b^2}{6} \nabla^2 q^\dagger - i w_\alpha(\mathbf{r}) q^\dagger, \quad q^\dagger(\mathbf{r}, 0) = 1, \quad (31)$$

with $\alpha = B$ for $0 \leq s \leq (1-f)N$ and $\alpha = A$ for $(1-f)N \leq s \leq N$ (i.e. reverse block order). With these, the normalized single-chain partition function can be written as

$$Q[iw_A, iw_B] = \frac{1}{V} \int d\mathbf{r} q(\mathbf{r}, N) = \frac{1}{V} \int d\mathbf{r} q^\dagger(\mathbf{r}, N). \quad (32)$$

Then the standard result for the segment densities at the saddle point is

$$\rho_A^*(\mathbf{r}) = \frac{n}{V Q[w_A^*, w_B^*]} \int_0^{fN} ds q(\mathbf{r}, s; [w_A^*, w_B^*]) q^\dagger(\mathbf{r}, N-s; [w_A^*, w_B^*]), \quad (33)$$

$$\rho_B^*(\mathbf{r}) = \frac{n}{V Q[w_A^*, w_B^*]} \int_{fN}^N ds q(\mathbf{r}, s; [w_A^*, w_B^*]) q^\dagger(\mathbf{r}, N-s; [w_A^*, w_B^*]). \quad (34)$$

(These match the $q q^+$ expressions in your notes.)

(b) Variation with respect to Ξ : incompressibility. From (26),

$$\frac{\delta \beta H}{\delta \Xi(\mathbf{r})} = -i(\rho_A(\mathbf{r}) + \rho_B(\mathbf{r}) - \rho_0). \quad (35)$$

Thus the saddle point condition gives the incompressibility constraint:

$$\rho_A^*(\mathbf{r}) + \rho_B^*(\mathbf{r}) = \rho_0. \quad (36)$$

(c) **Variations with respect to ρ_A, ρ_B : relations between fields and densities.** From (26),

$$\frac{\delta\beta H}{\delta\rho_A(\mathbf{r})} = v_0\chi_{AB}\rho_B(\mathbf{r}) - iw_A(\mathbf{r}) - i\Xi(\mathbf{r}), \quad (37)$$

$$\frac{\delta\beta H}{\delta\rho_B(\mathbf{r})} = v_0\chi_{AB}\rho_A(\mathbf{r}) - iw_B(\mathbf{r}) - i\Xi(\mathbf{r}). \quad (38)$$

Setting them to zero yields

$$iw_A^*(\mathbf{r}) = v_0\chi_{AB}\rho_B^*(\mathbf{r}) - i\Xi^*(\mathbf{r}), \quad iw_B^*(\mathbf{r}) = v_0\chi_{AB}\rho_A^*(\mathbf{r}) - i\Xi^*(\mathbf{r}). \quad (39)$$

1.10 Step 9: Real-field form (common SCFT notation)

At the saddle point in an incompressible melt, the combinations iw_A^* and iw_B^* are real fields (while w_A^*, w_B^* themselves are purely imaginary in the Fourier representation). It is convenient to define real, N -scaled fields

$$\mu_A(\mathbf{r}) \equiv iN w_A^*(\mathbf{r}), \quad \mu_B(\mathbf{r}) \equiv iN w_B^*(\mathbf{r}), \quad \xi(\mathbf{r}) \equiv iN \Xi^*(\mathbf{r}), \quad (40)$$

so that (39) becomes

$$\frac{\mu_A(\mathbf{r})}{N} = v_0\chi_{AB}\rho_B^*(\mathbf{r}) + \frac{\xi(\mathbf{r})}{N}, \quad \frac{\mu_B(\mathbf{r})}{N} = v_0\chi_{AB}\rho_A^*(\mathbf{r}) + \frac{\xi(\mathbf{r})}{N}. \quad (41)$$

Moreover, Q is typically written as a functional of the real fields:

$$Q[\mu_A, \mu_B] = \frac{1}{V} \int d\mathbf{r} q(\mathbf{r}, N; [\mu_A, \mu_B]), \quad (42)$$

where the modified diffusion equation takes the same form as (30) but with $-iw_\alpha(\mathbf{r})$ replaced by $-\mu_\alpha(\mathbf{r})/N$ (piecewise in s by block type).

1.11 Final SCFT equations

The SCFT (mean-field) solution is obtained by solving the coupled set:

$$(I) \quad \rho_A^*(\mathbf{r}) = \frac{n}{V Q[\mu_A, \mu_B]} \int_0^{fN} ds q(\mathbf{r}, s) q^\dagger(\mathbf{r}, N-s), \quad (43)$$

$$(II) \quad \rho_B^*(\mathbf{r}) = \frac{n}{V Q[\mu_A, \mu_B]} \int_{fN}^N ds q(\mathbf{r}, s) q^\dagger(\mathbf{r}, N-s), \quad (44)$$

$$(III) \quad \rho_A^*(\mathbf{r}) + \rho_B^*(\mathbf{r}) = \rho_0, \quad (45)$$

$$(IV) \quad \frac{\mu_A(\mathbf{r})}{N} = v_0\chi_{AB}\rho_B^*(\mathbf{r}) + \frac{\xi(\mathbf{r})}{N}, \quad (46)$$

$$(V) \quad \frac{\mu_B(\mathbf{r})}{N} = v_0\chi_{AB}\rho_A^*(\mathbf{r}) + \frac{\xi(\mathbf{r})}{N}, \quad (47)$$

together with the forward/backward diffusion equations for q, q^\dagger (blockwise in s), and

$$(VI) \quad Q[\mu_A, \mu_B] = \frac{1}{V} \int d\mathbf{r} q(\mathbf{r}, N) = \frac{1}{V} \int d\mathbf{r} q^\dagger(\mathbf{r}, N). \quad (48)$$

$$(VII) \quad \frac{\partial q(\mathbf{r}, s)}{\partial s} = \frac{b^2}{6} \nabla^2 q(\mathbf{r}, s) - \frac{\mu_\alpha(\mathbf{r})}{N} q(\mathbf{r}, s), \quad q(\mathbf{r}, 0) = 1, \quad (49)$$

$$(VIII) \quad \frac{\partial q^\dagger(\mathbf{r}, s)}{\partial s} = \frac{b^2}{6} \nabla^2 q^\dagger(\mathbf{r}, s) - \frac{\mu_\alpha(\mathbf{r})}{N} q^\dagger(\mathbf{r}, s), \quad q^\dagger(\mathbf{r}, 0) = 1, \quad (50)$$

Under the mean field condition, the effective Hamiltonian in (26) is the Hemholtz free energy, can also be shown to be:

$$\begin{aligned} \beta H &\approx \beta A \\ &= v_0 \chi_{AB} \int d\mathbf{r} \rho_A^*(\mathbf{r}) \rho_B^*(\mathbf{r}) \\ &\quad - \int d\mathbf{r} \left[\frac{\mu_A(\mathbf{r})}{N} \rho_A^*(\mathbf{r}) + \frac{\mu_B(\mathbf{r})}{N} \rho_B^*(\mathbf{r}) + \frac{\xi(\mathbf{r})}{N} (\rho_A^*(\mathbf{r}) + \rho_B^*(\mathbf{r}) - \rho_0) \right] \\ &\quad - n \ln Q[w_A, w_B]. \end{aligned} \quad (51)$$

1.12 Further simplification

Let's define volume fraction $\phi_A(\mathbf{r})$ and $\phi_B(\mathbf{r})$

$$\tilde{s} = \frac{s}{N}, \quad \phi_A(\mathbf{r}) = \rho_A^*(\mathbf{r}) v_0 = \frac{\rho_A^*(\mathbf{r})}{\rho_0}, \quad \phi_B(\mathbf{r}) = \rho_B^*(\mathbf{r}) v_0 = \frac{\rho_B^*(\mathbf{r})}{\rho_0} \quad (52)$$

We can further self-consistent field system into:

$$(I) \quad \phi_A(\mathbf{r}) = \frac{1}{Q[\mu_A, \mu_B]} \int_0^f d\tilde{s} q(\mathbf{r}, \tilde{s}) q^\dagger(\mathbf{r}, 1 - \tilde{s}), \quad (53)$$

$$(II) \quad \phi_B(\mathbf{r}) = \frac{1}{Q[\mu_A, \mu_B]} \int_f^1 d\tilde{s} q(\mathbf{r}, \tilde{s}) q^\dagger(\mathbf{r}, 1 - \tilde{s}), \quad (54)$$

$$(III) \quad \phi_A(\mathbf{r}) + \phi_B(\mathbf{r}) = 1, \quad (55)$$

$$(IV) \quad \mu_A(\mathbf{r}) = N \chi_{AB} \phi_B(\mathbf{r}) + \xi(\mathbf{r}), \quad (56)$$

$$(V) \quad \mu_B(\mathbf{r}) = N \chi_{AB} \phi_A(\mathbf{r}) + \xi(\mathbf{r}), \quad (57)$$

$$(VI) \quad Q[\mu_A, \mu_B] = \frac{1}{V} \int d\mathbf{r} q(\mathbf{r}, 1) = \frac{1}{V} \int d\mathbf{r} q^\dagger(\mathbf{r}, 1), \quad (58)$$

$$(VII) \quad \frac{\partial q(\mathbf{r}, \tilde{s})}{\partial \tilde{s}} = \frac{Nb^2}{6} \nabla^2 q(\mathbf{r}, \tilde{s}) - \mu_\alpha(\mathbf{r}) q(\mathbf{r}, \tilde{s}), \quad q(\mathbf{r}, 0) = 1, \quad (59)$$

$$(VIII) \quad \frac{\partial q^\dagger(\mathbf{r}, \tilde{s})}{\partial \tilde{s}} = \frac{Nb^2}{6} \nabla^2 q^\dagger(\mathbf{r}, \tilde{s}) - \mu_\alpha(\mathbf{r}) q^\dagger(\mathbf{r}, \tilde{s}), \quad q^\dagger(\mathbf{r}, 0) = 1. \quad (60)$$

and the intrinsic property of free energy per chain can be written as :

$$\begin{aligned} \frac{\beta H}{n} &\approx \frac{\beta A}{n} \\ &= \frac{1}{V} \int d\mathbf{r} N \chi_{AB} \phi_A(\mathbf{r}) \phi_B(\mathbf{r}) \\ &\quad - \frac{1}{V} \int d\mathbf{r} [\mu_A(\mathbf{r}) \phi_A(\mathbf{r}) + \mu_B(\mathbf{r}) \phi_B(\mathbf{r}) + \xi(\mathbf{r}) (\phi_A(\mathbf{r}) + \phi_B(\mathbf{r}) - 1)] \\ &\quad - \ln Q[w_A, w_B]. \end{aligned} \quad (61)$$

The functional in Eq. (61) represents the intensive free energy per chain (in units of $k_B T$) within the mean-field approximation. Its physical interpretation is decomposed as follows: Physically, this free energy functional per chain decomposes into three distinct contributions:

- **Interaction Enthalpy:** The first integral, $\frac{1}{V} \int d\mathbf{r} N \chi_{AB} \phi_A(\mathbf{r}) \phi_B(\mathbf{r})$, represents the standard mean-field Flory–Huggins interaction energy. This term provides the thermodynamic drive for microphase separation by penalizing A-B contacts.
- **Field Coupling and Incompressibility:** The second integral subtracts the potential energy coupled to the auxiliary fields. This arises from the Legendre transformation relating the density-based internal energy to the field-based free energy. Specifically, the term involving $\xi(\mathbf{r})$ enforces the local incompressibility constraint $\phi_A(\mathbf{r}) + \phi_B(\mathbf{r}) = 1$ at the saddle point.
- **Conformational Entropy:** The term $-\ln Q[\mu_A, \mu_B]$ represents the dimensionless free energy of a single ideal Gaussian chain subjected to the external fields μ_A and μ_B . It encapsulates the loss of conformational entropy (chain stretching) required to satisfy the spatially varying field configurations.