

### Problem statement

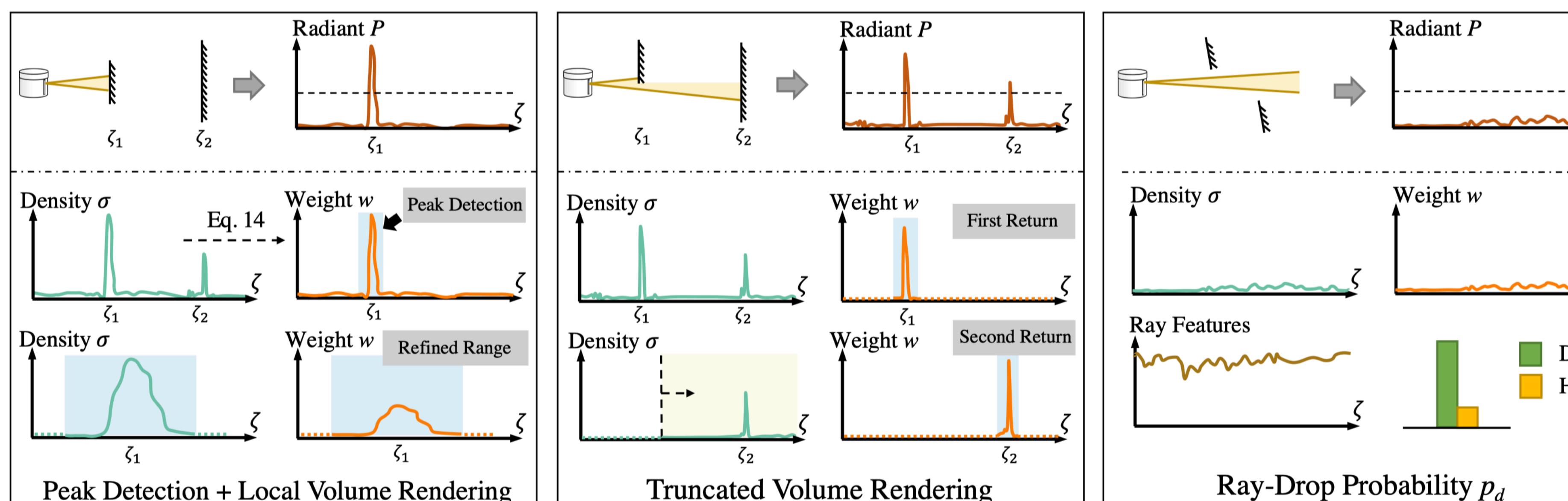
- Input:** LiDAR scans  $\mathbf{X} = \{\mathbf{X}_v\}_{v=1}^{n_v}$ , where each scan  $\mathbf{X}_v$  is associated with a sensor pose  $\mathbf{T}_v \in \text{SE}(3)$  and consists of  $n_r$  rays. Every ray  $\mathbf{r}(\mathbf{o}, \mathbf{d})$  records measurements  $(\zeta_1, e_1, p_d, p_s, \zeta_2, e_2)$  as:
  - $\zeta_*$ : range of the first/second return
  - $e_*$ : intensity of the first /second return
  - $p_d \in \{0,1\}$ : ray drop mask
  - $p_s \in \{0,1\}$ : two return mask
- Goal:** Render virtual LiDAR scans  $\mathbf{X}_{tgt}$  from novel sensor poses  $\mathbf{T}_{tgt}$ .

### Volume rendering for active sensor

- Range-dependent radiant power  $P(\zeta)$  at range  $\zeta$ : 
$$P(\zeta) = \int_0^{2\zeta/c} P_e(t)H(\zeta - \frac{ct}{2}) dt, \quad H(\zeta) = H_T(\zeta)H_C(\zeta)$$
- Probabilistic radiant power  $P_\zeta$  at range  $\zeta$ : 
$$P_\zeta = C \frac{T_\zeta^2 \cdot \sigma_\zeta \rho_\zeta}{\zeta^2} \cos(\theta) \delta(\zeta - \zeta_0), \quad H_C(\zeta) = T_\zeta^2 \frac{A_e}{\zeta^2}.$$
- Volume rendering of the probabilistic radiant: 
$$P = \sum_{j=1}^N \int_{\zeta_j}^{\zeta_{j+1}} C \frac{T_\zeta^2 \cdot \sigma_\zeta \rho_\zeta}{\zeta^2} \cos(\theta_j) d\zeta = \sum_{j=1}^N w_j \rho'_j.$$
- Active sensing versus passive sensing:
 
$$w_j = 2\alpha_{\zeta_j} \cdot \prod_{k=1}^{j-1} (1 - 2\alpha_{\zeta_k}), \quad w_j = \alpha_{\zeta_j} \cdot \prod_{k=1}^{j-1} (1 - \alpha_{\zeta_k}).$$

### Neural Field for LiDAR NVS

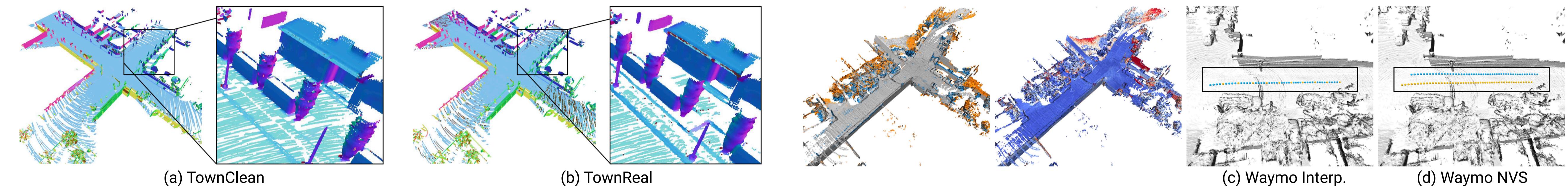
- Neural LiDAR field:  $F : (\mathbf{x}, \mathbf{d}) \mapsto (\sigma, \rho, p_d)$ .
- LiDAR beam rendering:



$$\text{Loss terms: } L = L_{\text{range}} + \lambda_e L_e + \lambda_d L_d + \lambda_s L_s.$$

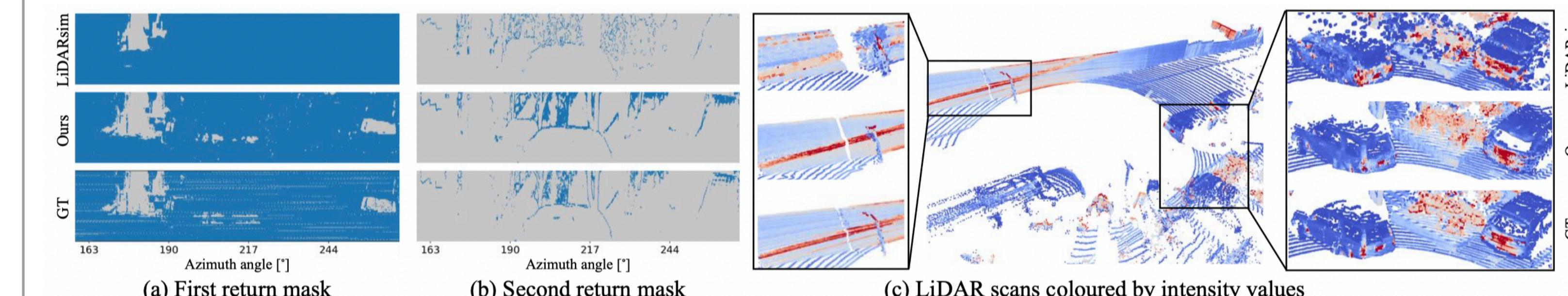
### Datasets and evaluation protocol

- TownClean and TownReal datasets that are simulated using *idealised* and *diverging beam profile*, respectively;
- Waymo Interp: four static scenes from Waymo Open datasets, 40/10 scans for training/testing;
- Waymo NVS: same scenes, train on entire 50 scans → test from different sensor trajectory → re-train on the novel views → test on the original 50 scans.



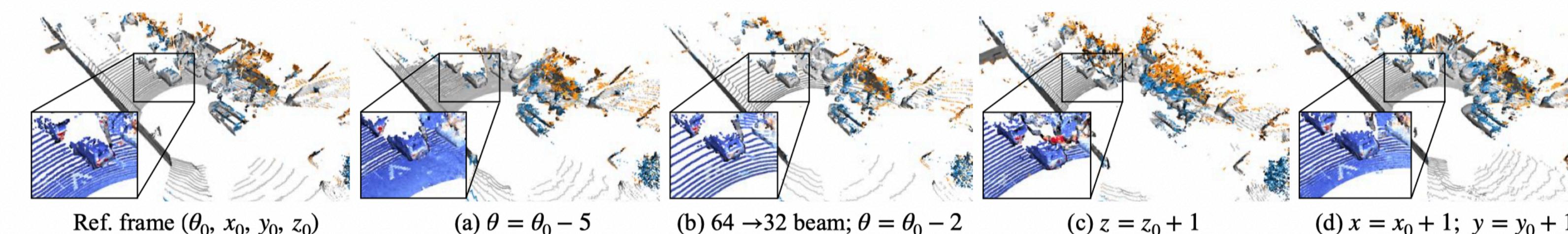
### Experimental results

- Comprehensive ray measurement evaluation of LiDAR NVS on Waymo Interp. dataset.

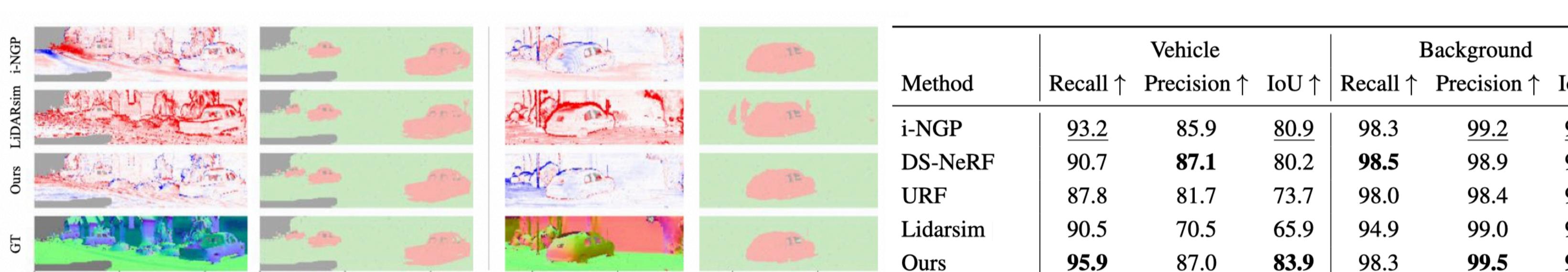


Method	First range			Second range			Intensity		Ray drop				
	Recall@50↑	MAE ↓	MedAE ↓	Seg. recall ↑	Seg. precision ↑	Recall@50↑	MAE ↓	MedAE ↓	MSE <sup>1st</sup> ↓	MSE <sup>2nd</sup> ↓	Recall ↑	Precision ↑	IoU ↑
LiDARsim	74.1	105.4	18.5	3.5	11.5	1.0	2258.0	1898.2	0.013	0.018	32.5	<b>85.5</b>	30.5
Central ray	92.8	32.8	5.6	79.8	62.9	61.1	589.1	21.8	0.004	0.009	64.3	81.7	<b>57.1</b>
Ours	92.3	36.1	5.7	82.1	55.6	67.4	505.1	13.4	<b>0.004</b>	<b>0.008</b>	<b>65.1</b>	78.0	56.1
GT mask	<b>93.2</b>	<b>29.7</b>	<b>5.6</b>	<b>100.0</b>	<b>79.8</b>	<b>116.0</b>	<b>8.1</b>	<b>0.004</b>	<b>0.011</b>	<b>65.1</b>	<b>78.0</b>	<b>56.1</b>	

- LiDAR novel view synthesis by changing the sensor elevation angle  $\theta$ , pose  $(x, y, z)$ , and number of beams.

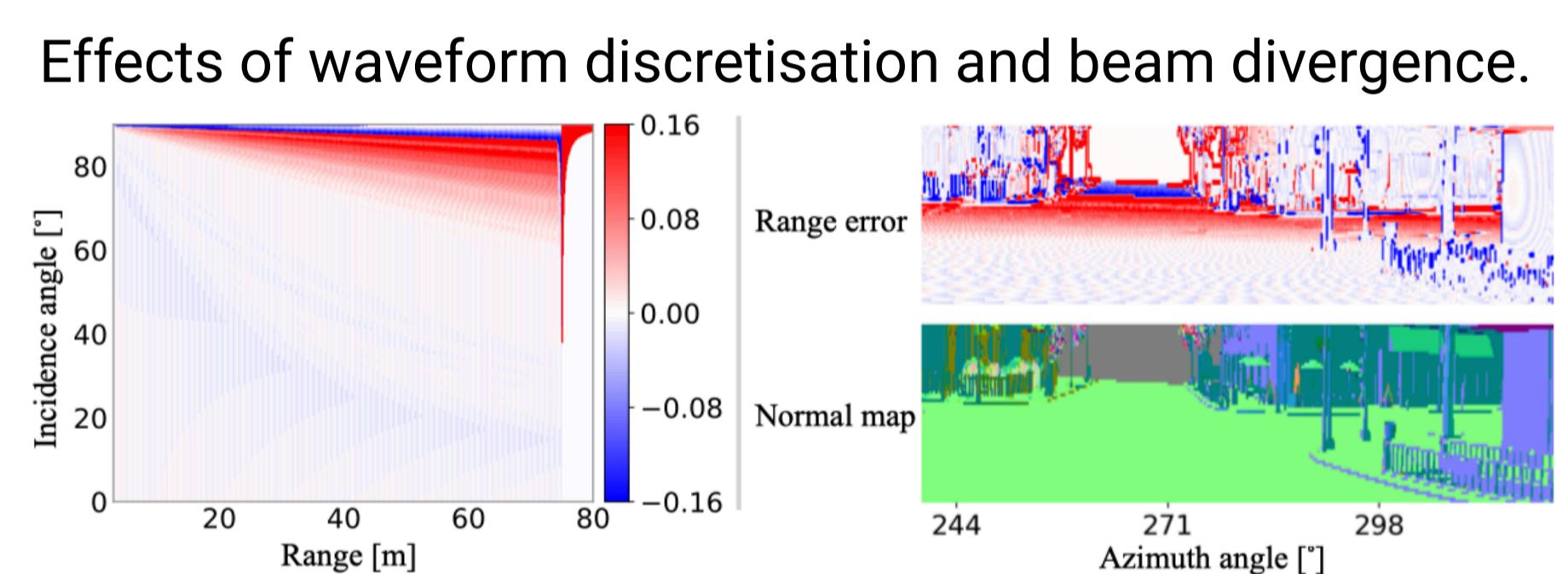


- Evaluation of synthesised novel views via proxy task. In this example, the geometry inaccuracy (-100 cm) leads to erroneous semantic segmentation.



### Our contribution

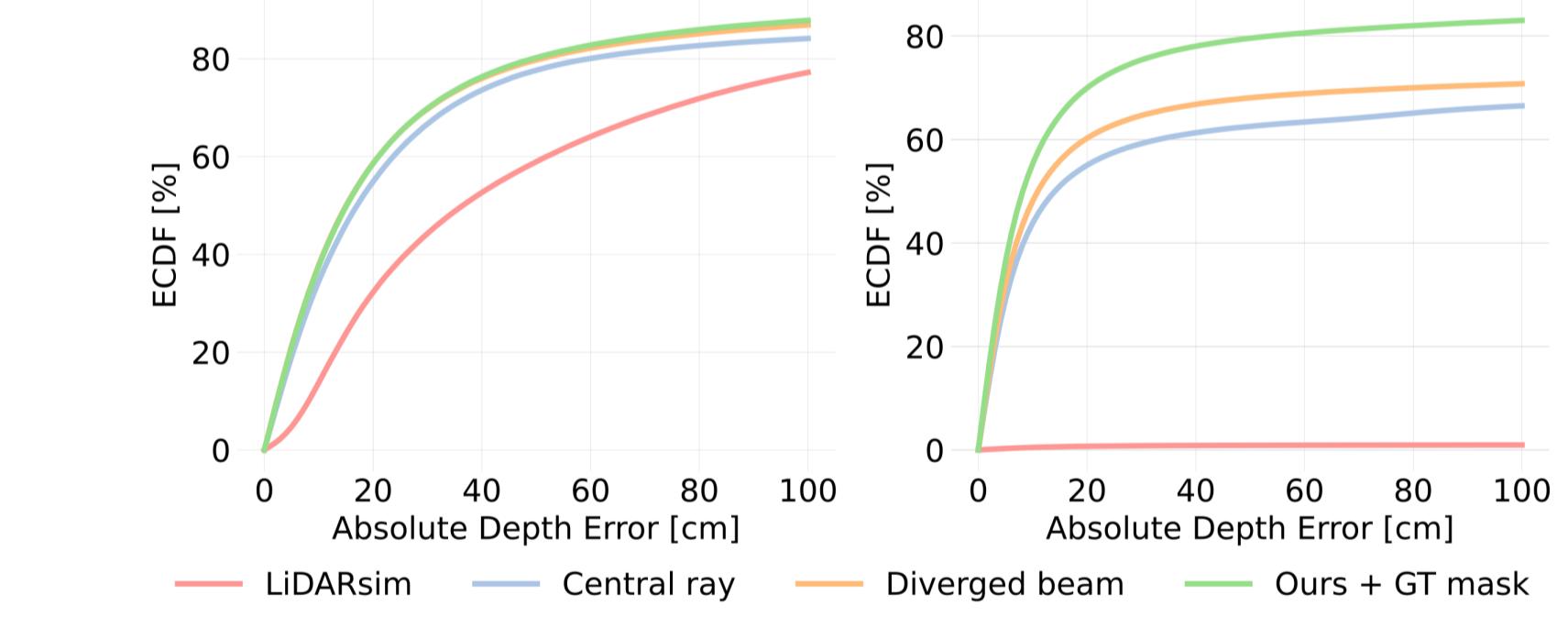
- Devised the volume rendering scheme for active sensors;
- Proposed a neural field model grounded on the physical LiDAR sensing process;
- Proposed a closed-loop evaluation protocol to evaluate NVS performance;
- Developed a LiDAR simulator that supports *diverging beam profile*.



- Effectiveness of volume rendering for active sensing.

Method	TownClean			Waymo Interp.		
	MAE ↓	MedAE ↓	CD ↓	MAE ↓	MedAE ↓	CD ↓
i-NGP	41.0 (-1.2)	4.1 (0.0)	17.6 (0.2)	25.3 (-1.1)	4.5 (-1.0)	10.5 (-1.1)
DS-NeRF	37.4 (-4.2)	3.0 (-0.9)	14.4 (-2.2)	27.4 (-0.8)	5.4 (-1.0)	13.6 (-0.9)
URF	46.4 (3.0)	4.5 (0.3)	18.4 (1.6)	28.3 (0.1)	5.3 (-0.1)	13.1 (0.2)
Ours	32.0 (-2.1)	2.3 (-2.5)	9.0 (-3.9)	30.8 (-2.1)	5.1 (-2.0)	12.1 (-2.3)

- Benefits of diverging beam profile.



- Results on Waymo NVS dataset by varying the displacement.

	Numbers are reported as MedAE/CD [cm].				
	i-NGP	DS-NeRF	URF	LiDARsim	Ours
(0.5, 0.5, 0.5)	7.0 / 14.4	7.0 / 16.0	9.0 / 19.6	16.1 / 33.1	<b>5.4 / 13.0</b>
(1.5, 1.5, 1.0)	8.4 / 17.6	7.8 / 18.5	11.0 / 27.5	16.5 / 37.9	<b>5.8 / 14.3</b>
(2.5, 2.5, 1.5)	11.6 / 28.0	9.3 / 22.8	13.9 / 35.5	17.2 / 46.3	<b>6.4 / 18.4</b>

### Future work

- Extend to handle dynamic scenes;
- Additionally handle scattering and attenuation effects in adverse weather;
- Recover “true” geometry from biased measurements.