

Section 2.1 (Continued)

Example: $\frac{dy}{dx} = y^2 - y^3$

$f(y)$
dependent variable y .

autonomous differential equation

$$0 = y^2 - y^3 = y^2(1 - y)$$

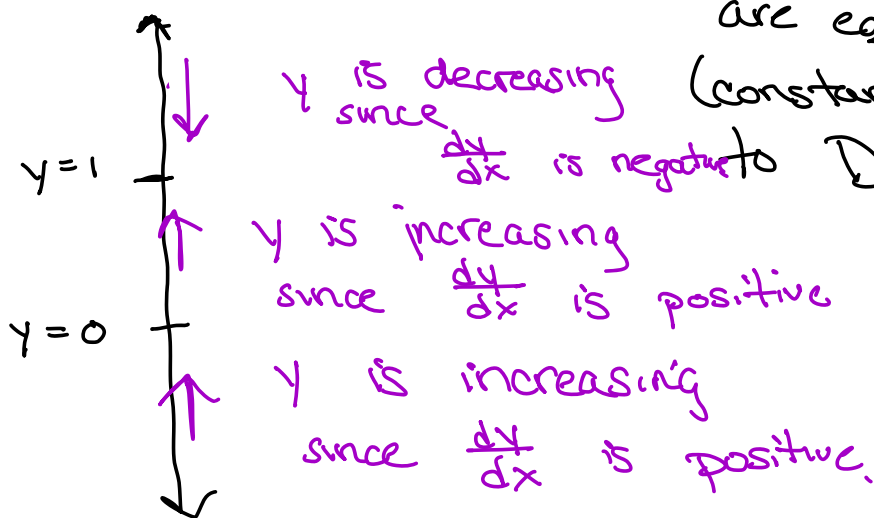
$$y = 0, y = 1$$

$$y(x) \equiv 0, y(x) \equiv 1$$

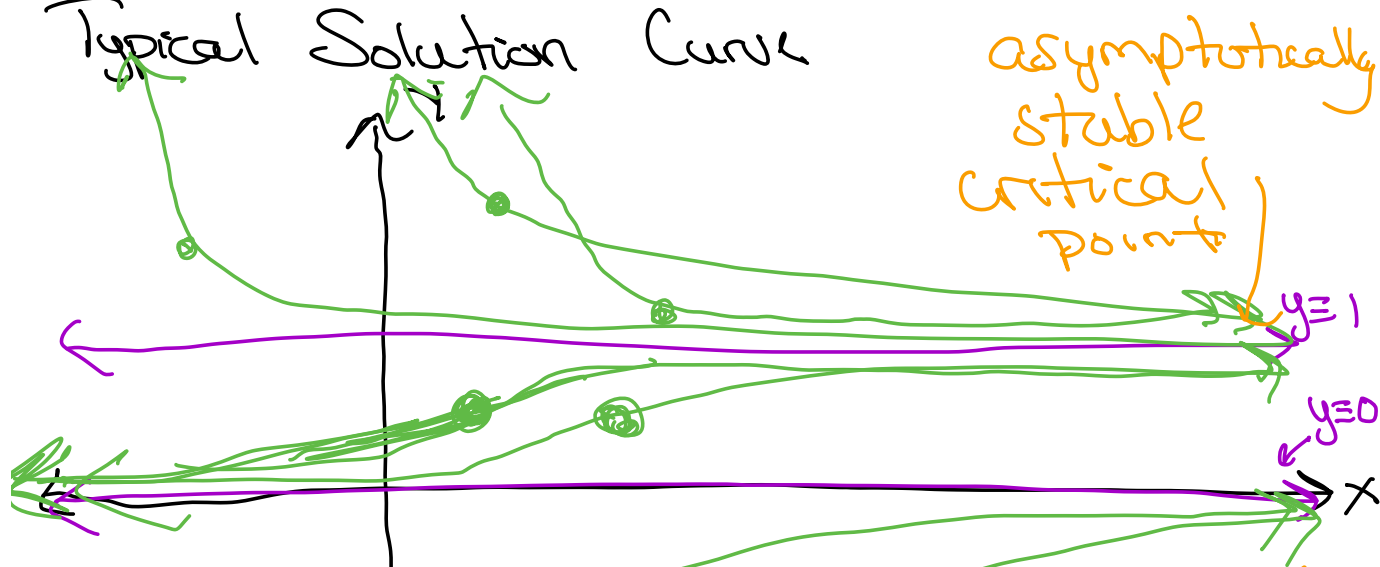
$$y \equiv 0 \text{ and } y \equiv 1$$

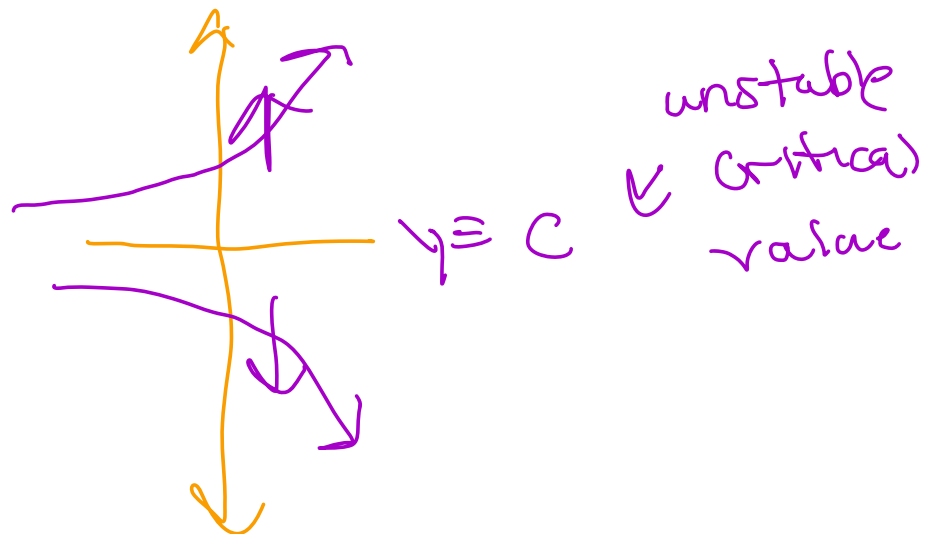
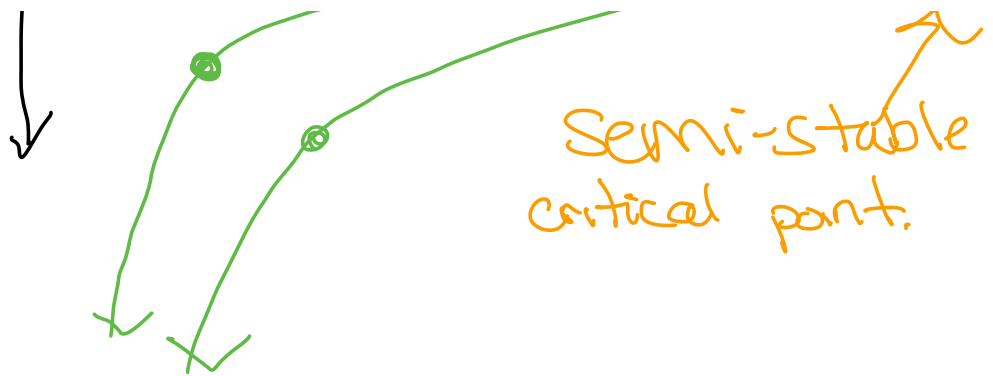
are equilibrium
(constant) solution

Phase Portrait



Typical Solution Curve





$$\frac{dy}{dx} = y^2 + 5y + 4 = (y + 4)(y + 1)$$

