

Lab 7 – OJ

Divide and Conquer

CS208 Algorithm Design and Analysis
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Q1: K-th element

Description

You are given two **non-decreasing** arrays A, B . Their length are both n . Now please output the kth element after combining the two subarray $A[l...r]$ and $B[l...r]$ and sorting the combined array in ascending order.

Sample Input 1

of queries
3
5

Length of arrays, n
5 5 2

1 3 5 7 9

2 3 4 5 6

1 5 6

1 5 7

5 5 2

Sample Output 1

9

$A = [1, 3, 5, 7, 9] \Rightarrow A_{5...5} = [9]$

$B = [2, 3, 4, 5, 6] \Rightarrow B_{5...5} = [6]$

Sorting and combining $A_{5...5}$ and $B_{5...5}$
 $\Rightarrow [6, 9]$

$K = 2 \Rightarrow \text{output } 9$

2

Q1: K-th element

Sample Input 1

```
3 5
1 3 5 7 9
2 3 4 5 6
5 5 2
1 5 6
1 5 7
```

Sample Output 1

```
9
5
5
```

$A = [1, 3, 5, 7, 9] \Rightarrow A_{1 \dots 5} = A$

$B = [2, 3, 4, 5, 6] \Rightarrow B_{1 \dots 5} = B$

Sorting and combining $A_{1 \dots 5}$ and $B_{1 \dots 5}$
 $\Rightarrow [1, 2, 3, 3, 4, 5, 5, 6, 7, 9]$

$K = 6 \Rightarrow \text{output } 5$

Q2: Range sum

Description

You are given an array A and two integers L and R .

Let's define $S(l, r) = \sum_{i=l}^r A_i$ ($l \leq r$).

Please calculate the numbers of pair (l, r) satisfying $L \leq S(l, r) \leq R$ and $l \leq r$.

Input Format

The first line contains three integers n, L, R , denoting the length of array and the two integers L, R .

The second line contains n integers A_i ($-10^4 \leq A_i \leq 10^4$), denoting the elements of array A .

Output Format

One line, one integer indicating the answer.

Sample Input 1

```
7 -11 9
-3 9 -11 20 -4 -7 6
```

Sample Output 1

```
19
```

Q2: Range sum

Sample Input 1

```
7 -11 9
-3 9 -11 20 -4 -7 6
```

Sample Output 1

```
19
```

$n = 7, L = -11, R = 9$

$A = [-3, 9, -11, 20, -4, -7, 6]$

$\text{Sum}(1, 1) = -3$

$\text{Sum}(1, 2) = -3 + 9 = 6$

...

$\text{Sum}(6, 7) = -7 + 6 = -1$

$\text{Sum}(7, 7) = 6$

19 pairs satisfying $-11 \leq \text{Sum}(l, r) \leq 9$