

## Q1

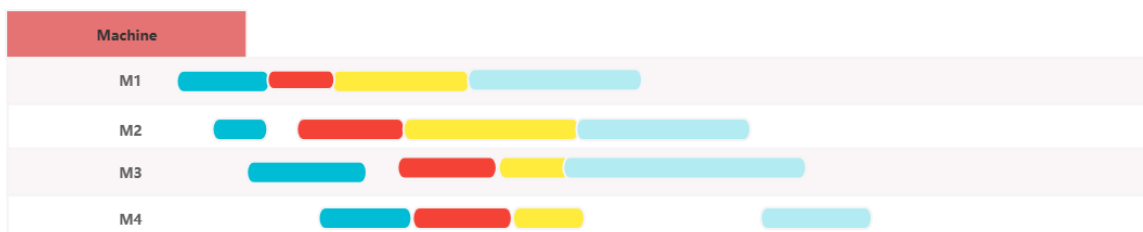
depth1						
1	2{5.38}	3{7.30}	4{8.69}	5{7.10}	6{4.54}	7{6.48}
2	1{8.48}	3{7.30}	4{10.48}	5{8.54}	6{5.10}	7{6.68}
3	1{10.48}	2{7.38}	4{12.39}	5{10.38}	6{6.54}	7{7.30}
4	1{8.07}	2{6.76}	3{8.59}	5{7.32}	6{5.30}	7{7.30}
5	1{7.72}	2{6.07}	3{7.83}	4{8.56}	6{4.54}	7{6.55}
6	1{9.01}	2{6.48}	3{7.83}	4{10.34}	5{8.39}	7{6.41}
7	1{10.96}	2{8.06}	3{8.59}	4{12.39}	5{10.40}	6{6.41}

By using the greedy solution of tour length 10, there are 8 depth 2 nodes can be terminated.

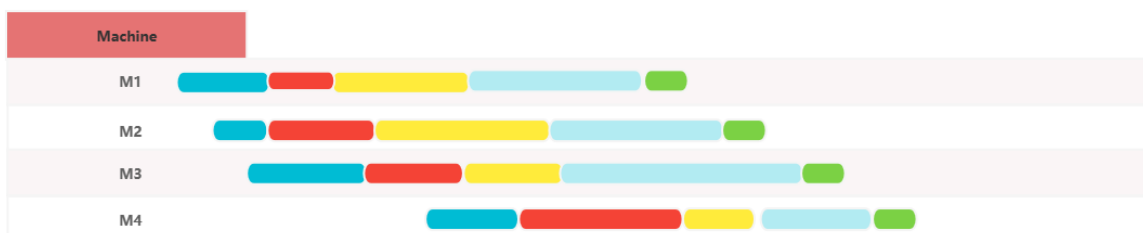
They are 0-2-4, 0-3-1, 0-3-4, 0-3-5, 0-6-4, 0-7-1, 0-7-4, 0-7-5.

## Q2

Suppose there are 4 jobs and 4 machines, then select "Blue lattice" as the first job. The schedule is shown in followings:



Then compress the wait time for all tasks except the first for all machines. And add a period which is the shortest time in the remains jobs of the last machine used by "Green lattice". Then select the maximum total time from all machines as for lower bound.



## Q3

For 10-machine  $n$ -job flowshop scheduling problems, in one hour, the size of the problem that can be solved depends on several factors, including computer performance, algorithm efficiency, and problem characteristics. Here's a simple estimate, assuming the use of a high-performance computer and an efficient branch and bound algorithm for solving.

Let's assume that our algorithm can process 1000 nodes per second (which is a relatively high speed, depending on the optimization level of the algorithm and actual hardware performance). Then, in one hour, the number of nodes the algorithm can process is:

$$1000 \text{ nodes/second} \times 3600 \text{ seconds/hour} = 3,600,000 \text{ nodes/hour}$$

Now we need to consider how much time each node takes to compute. Since we're dealing with a 10-machine flowshop scheduling problem, the number of nodes may exponentially increase with the number of jobs,  $n$ . Let's assume each node takes an average of 1 millisecond to compute (which is also a relatively fast estimate). Then, the size of the problem the algorithm can handle in one hour is:

$$3,600,000 \text{ nodes/hour} \times 0.001 \text{ seconds/node} = 3,600 \text{ nodes/hour}$$

This means that for a 10-machine flowshop scheduling problem, assuming each node takes an average of 1 millisecond to compute, the algorithm can roughly handle a problem size of 3600 in one hour. This is a very rough estimate, and the actual situation may vary depending on computer performance, algorithm efficiency, and problem characteristics.