

Lab 8 – Practice

Divide and Conquer (p2)

CS208 Algorithm Design and Analysis
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Question: Bank account detection

- Suppose you're consulting for a bank that's concerned about fraud detection, and they come to you with the following problem. They have a collection of n bank cards that they've confiscated, suspecting them of being used in fraud. Each bank card corresponds to a unique account in the bank. Each account can have many bank cards corresponding to it, and we'll say that two bank cards are **equivalent** if they correspond to the same account.
- It's very difficult to read the account number off a bank card directly, but the bank has a high-tech "equivalence tester" that takes two bank cards and, after performing some computations, determines whether they are equivalent.

Question: Bank account detection

- Their question is the following: among the collection of n cards, is there a set of more than $n/2$ of them that are all equivalent to one another? Assume that the only feasible operations you can do with the cards are to pick two of them and plug them in to the equivalence tester. Show how to decide the answer to their question with only $O(n \log n)$ invocations of the equivalence tester (or even better).

Grading

- Explain your solution with pseudo code and explain the time complexity. To be graded at Week 11.
- Total point: 1